

The forestecology R package for fitting and assessing neighborhood models of the effect of interspecific competition on the growth of trees

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Abstract

1. Neighborhood competition models are powerful tools to measure the effect of interspecific competition. Statistical methods to ease the application of these models are currently lacking.

2. We present the **forestecology** package providing methods to i) specify neighborhood competition models, ii) evaluate the effect of competitor species identity using permutation tests, and iii) measure model performance using spatial cross-validation. Following Allen & Kim (2020), we implement a Bayesian linear regression neighborhood competition model.

3. We demonstrate the package's functionality using data from the Smithsonian Conservation Biology Institute's large forest dynamics plot, part of the ForestGEO global network of research sites. Given ForestGEO's data collection protocols and data formatting standards, the package was designed with cross-site compatibility in mind. We highlight the importance of spatial cross-validation when interpreting model results.

4. The package features i) **tidyverse**-like structure whereby verb-named functions

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can be modularly “piped” in sequence, ii) functions with standardized inputs/outputs of simple features **sf** package class, and iii) an S3 object-oriented implementation of the Bayesian linear regression model. These three facts allow for clear articulation of all the steps in the sequence of analysis and easy wrangling and visualization of the geospatial data. Furthermore, while the package only has Bayesian linear regression implemented, the package was designed with extensibility to other methods in mind.

Keywords: forest ecology, interspecific competition, neighborhood competition, tree growth, R, ForestGEO, spatial cross-validation

1 Introduction

Repeat-censused forest plots offer excellent opportunities to test neighborhood models of the effect of competition on the growth of trees (Canham et al. 2004). Neighborhood models of competition have been used to: test whether the species identity of a competitor matters [Uriarte et al. (2004); measure species-specific competition coefficients (Das 2012, Tatsumi et al. (2016)); test competing models to see what structures competitive interactions, e.g. traits or phylogeny (Allen & Kim 2020, Uriarte et al. 2010); and inform selective logging practices (Canham et al. 2006). Although these are well-described methods, few methods are currently available for easy application.

We address this shortcoming with the `forestecology` R package providing methods and data for forest ecology model fitting and assessment, available on CRAN (<https://cran.r-project.org/package=forestecology>) and on GitHub (<https://github.com/rudeboybert/forestecology>). The package is written to model stem diameter growth between two censuses based on neighborhood competition, largely following the methods in Allen & Kim (2020).

Let $i = 1, \dots, n_j$ index all n_j trees of “focal” species j ; let $j = 1, \dots, J$ index all J focal species; and let $k = 1, \dots, K$ index all K “competitor” species. The average annual growth in diameter at breast height (DBH) y_{ij} (in centimeters/year) of the i^{th} tree of focal species j is modeled as

$$y_{ij} = \beta_{0,j} + \beta_{\text{dbh},j} \cdot \text{dbh}_{ij} + \sum_{k=1}^K \lambda_{jk} \cdot x_{ijk}^{\text{comp}} + \epsilon_{ij} \quad (1)$$

where $\beta_{0,j}$ is the diameter-independent growth rate of species j ; dbh_{ij} is the DBH of the focal tree at the earlier census and $\beta_{\text{dbh},j}$ the slope of that species’s diameter-growth relationship; x_{ijk}^{comp} is the sum of some numerical explanatory variable of all trees of competitor species k and λ_{jk} quantifies the corresponding change in growth for individuals of group j from these competitors; and ϵ_{ij} is a random error term distributed $\text{Normal}(0, \sigma^2)$.

Allen & Kim (2020) use the sum of the basal area of all trees of competitor species k as x_{ijk}^{comp} . Furthermore, they estimate all parameters via Bayesian linear regression, while exploiting Normal/Inverse Gamma conjugacy to derive closed-form solutions to all posterior distributions¹. These closed-form solutions are not as computationally expensive as approximations from Markov Chain Monte Carlo algorithms.

To evaluate whether competitor species identity matters, Allen & Kim (2020) run a permutation test where a null hypothesis of no species grouping-specific effects of competition is assumed, thus the species identity of all competitors can be permuted:

$$\begin{aligned} H_0 : \lambda_{jk} &= \lambda_j \text{ for all } k = 1, \dots, K \\ \text{vs. } H_A : &\text{at least one } \lambda_{jk} \text{ is different} \end{aligned} \tag{2}$$

Furthermore, to account for the spatial autocorrelation in their estimates of out-of-sample model error, Allen & Kim (2020) use spatial cross-validation. Estimates of model error that do not account for this dependence tend to underestimate the true model error (Roberts et al. 2017).

The package is designed with “tidy” design principles in mind (Wickham et al. 2019). Much like all **tidyverse** packages, **forestecology** has verb-named functions that can be modularly composed using the pipe `%>%` operator to sequentially complete all necessary analysis steps (Bache & Wickham 2020).

Furthermore, the inputs and outputs of most functions use the same “simple features for R” data structures for spatial data from the **sf** package (Pebesma 2018). Previously **sp** package classes were commonly used for storing spatial data and interfacing with geospatial libraries (Bivand et al. 2013); the **sf** package aims to improve on the **sp** package by:

¹See S1 Appendix of Allen & Kim (2020), available at <https://doi.org/10.1371/journal.pone.0229930.s004>

1. Using simple feature access as the base standard for representing and encoding spatial data, rather than shapefiles (Herring 2011).
2. Leveraging improvements in external libraries for reading and writing spatial data (GDAL) and for geometrical operations (GEOS) (Warmerdam 2008, Team (2017)).
3. Integrating closely with the popular `tidyverse` suite of packages for data science (Wickham et al. 2019).

By using the `sf` package classes to represent spatial data rather than the `sp` package, the implementation and use of the `forestecology` package’s spatial algorithms was greatly simplified.

Lastly, currently the package only implements the Bayesian linear regression model detailed in Equation 1. As we demonstrate in Section 2.4 however, the fitting of this model is self-contained in a single function `comp_bayes_lm()` which returns an object of S3 class type `comp_bayes_lm`. This class has generic methods implemented to print, make predictions, and plot all results. Therefore the package can be modularly extended to fit other models as long as they are coded similarly to `comp_bayes_lm()` and have equivalent generic methods implemented.

2 forestecology workflow: a case study

We present a case-study of `forestecology`’s functionality on data from the Smithsonian Conservation Biology Institute (SCBI) large forest dynamics plot in Front Royal, VA, USA, part of the ForestGEO global network of research sites (Bourg et al. 2013, Anderson-Teixeira et al. (2015)). The 25.6 ha (640 x 400 m) plot is located at the intersection of three of the major physiographic provinces of the eastern US—the Blue Ridge, Ridge and Valley, and Piedmont provinces—and is adjacent to the northern end of Shenandoah National Park.

The package has the following goals: to evaluate i) the effect of competitor species

identity using permutation tests and ii) model performance using spatial cross-validation.

We outline the four-step basic analysis sequence:

1. Compute the growth of stems based on two censuses.

2. Add spatial information:

1. Define a buffer region of trees.

2. Add spatial cross-validation block information.

3. Identify all focal trees and their competitors.

4. Apply model, which includes:

1. Fit model.

2. Compute predicted values.

3. Visualize posterior distributions.

We start by loading all packages.

```
library(tidyverse)
library(lubridate)
library(sf)
library(patchwork)
library(forestecology)
library(blockCV)

# Resolve conflicting functions
filter <- dplyr::filter
select <- dplyr::select
```

2.1 Step 1: Compute the growth of trees based on census data

We first compute the growth of trees using data from two censuses. `compute_growth()` computes the average annual growth based on census data that roughly follows ForestGEO standards. Despite such standards, minor variations will still exist between sites, thereby necessitating some data wrangling. For example, the SCBI site records all DBH values in millimeters (Bourg et al. 2013), whereas the Michigan Big Woods site used in Allen & Kim (2020) records them in centimeters (Allen et al. 2020).

We load both 2008 and 2014 SCBI census `.csv` files as they existed on GitHub on 2021/08/02 and perform minor data wrangling (Gonzalez-Akre, McGregor, Anderson-Teixeira, Dow, Herrmann, Terrell, Kim, Vinod & Helcoski 2020). We then only consider a 9 ha subsection of the 25.6 ha of the site to speed up computation for this example: `gx` from 0–300 instead of 0–400 and `gy` from 300–600 instead of 0–640.

```
census_2013_scbi <- read_csv("scbi.stem2.csv") %>%  
  select(stemID, sp, date = ExactDate, gx, gy, dbh, codes, status) %>%  
  mutate(  
    # Convert date from character to date  
    date = mdy(date),  
    # Convert dbh to be in cm  
    dbh = as.numeric(dbh)/10  
  ) %>%  
  filter(gx < 300, between(gy, 300, 600))  
  
census_2018_scbi <- read_csv("scbi.stem3.csv") %>%  
  select(stemID, sp, date = ExactDate, gx, gy, dbh, codes, status) %>%  
  mutate(  
    date = mdy(date),
```

```
    dbh = as.numeric(dbh)/10
  ) %>%
  filter(gx < 300, between(gy, 300, 600))
```

124 These two data frames are then used as inputs to `compute_growth()`, along with `id`
125 specifying the variable that uniquely identifies each tree-stem. We also discard all resprouts
126 with `code == R` in the later census, since we are only interested in the growth of surviving,
127 and not resprouted, stems.

```
growth_scbi <- compute_growth(census_1 = census_2013_scbi, census_2 = census_2018_scbi %>%
  filter(!str_detect(codes, "R")), id = "stemID")
growth_scbi %>%
  select(stemID, sp, dbh1, dbh2, growth, geometry)
## Simple feature collection with 7954 features and 5 fields
## Geometry type: POINT
## Dimension: XY
## Bounding box: xmin: 0.2 ymin: 300 xmax: 300 ymax: 600
## CRS: NA
## # A tibble: 7,954 x 6
##   stemID sp      dbh1 dbh2 growth geometry
##   <dbl> <fct> <dbl> <dbl> <dbl> <POINT>
## 1      4 nysy  13.6  14.2  0.103 (14.2 428)
## 2      5 havi   8.8   9.6  0.150 (9.4 436)
## 3      6 havi   3.25  4    0.140 (1.3 434)
## 4     77 qual  65.2  66   0.141 (34.7 307)
## 5     79 tiam  47.7  46.8 -0.161 (40 381)
## # ... with 7,949 more rows
```

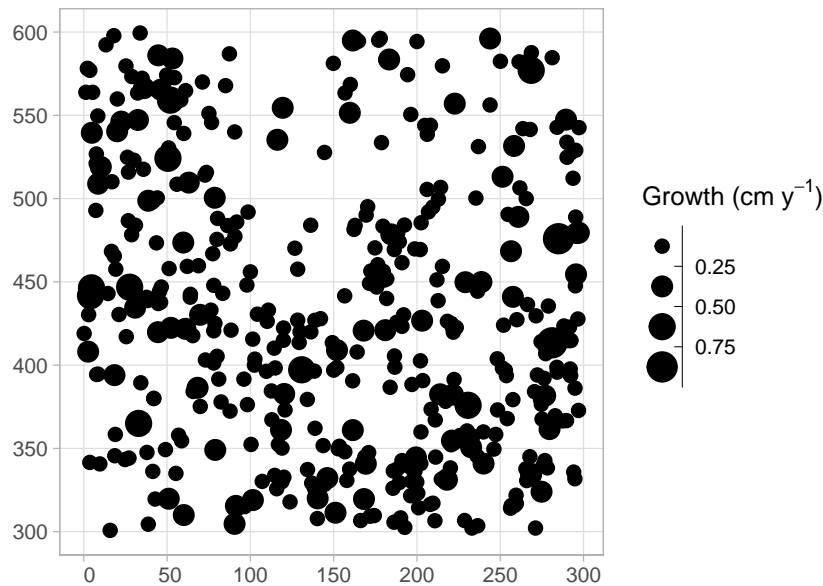



Figure 1: Step 1 - Compute growth of trees based on census data. A map of the growth of a random sample of 500 trees from a 9 ha subsection of the Smithsonian Conservation Biology Institute (SCBI) forest plot.

The output `growth_scbi` is a data frame of class `sf` that includes among other variables the species variable `sp` converted to a factor, the average annual `growth` in DBH ($\text{cm} \cdot \text{y}^{-1}$) for all stems that were alive at both time points, and the `sf` package's encoding of geolocations of geometry type `<POINT>`. Given that `growth_scbi` is of class `sf`, it can be easily plotted in `ggplot2` using `geom_sf()` as seen in Figure 1.

```
ggplot() + geom_sf(data = growth_scbi %>%
  sample_n(500), aes(size = growth)) + scale_size_binned(limits = c(0.1,
  1)) + labs(size = expression(paste(Growth, " (cm ", y^{
  -1
  }, " )"))))
```

We also load species information as it existed on GitHub on 2021/08/02, which includes family, genus, and species information; as well as classifications of the canopy position (canopy, canopy emergent, understory, shrub layer) and drought tolerance (intolerant, resistant) of the species.

```

sp_info <- read_csv("SCBI_ForestGEO_sp_ecology.csv") %>%
  select(sp = spcode, family, genus, species, canopy_position, drought_tolerance) %>%
  mutate()
sp_info
## # A tibble: 65 x 6
##   sp      family      genus      species      canopy_position drought_toleran~
##   <chr> <chr>      <chr>      <chr>      <chr>          <chr>
## 1 acne  Sapindaceae  Acer       negundo     understory     drought-resista~
## 2 acpl  Sapindaceae  Acer       platanoides canopy         drought-resista~
## 3 acru  Sapindaceae  Acer       rubrum      canopy         drought-resista~
## 4 aial  Simaroubaceae Ailanthus  altissima  canopy         drought-resista~
## 5 amar  Rosaceae     Amelanchier arborea  understory     drought-resista~
## # ... with 60 more rows

```

137 We join this species information to our `growth_scbi` data frame.

```

growth_scbi <- growth_scbi %>%
  left_join(sp_info, by = "sp") %>%
  # TODO:
  mutate(sp = as.factor(sp))

```

138 Furthermore, we compute two potential competitor explanatory variables x_{ijk}^{comp} from
 139 Equation 1. First, the basal area of each tree as a function of its DBH in the earlier
 140 census. Second, the above ground biomass as estimated by allometric equations encoded
 141 in the `get_biomass()` function from the `allodb` package (Gonzalez-Akre, Piponiot, Lepore
 142 & Anderson-Teixeira 2020); this function has DBH, species, and geographic coordinates as
 143 arguments.

```
# Install development version of allodb using:
# remotes::install_github("forestgeo/allodb")
library(allodb)
growth_scbi <- growth_scbi %>%
  mutate(
    # Compute basal area:
    basal_area = 0.0001 * pi * (dbh1 / 2)^2,
    # Compute above ground biomass:
    agb = get_biomass(
      dbh = dbh1,
      genus = genus,
      species = species,
      coords = c(-78.2, 38.9)
    )
  )
```

2.2 Step 2: Add spatial information

We then add spatial information to `growth_scbi`. We first add a “buffer region” to the periphery of the study region. Since some of our model’s explanatory variables are cumulative, we must ensure that all trees being modeled are not biased to have different neighbor structures. This is of concern for trees at the boundary of the study region who will not have all their neighbors included in the census stems. To account for such edge effects, only trees that are not part of this buffer region, i.e. are part of the interior of the study region, will have their growth modeled (Waller & Gotway 2004).

Our model of interspecific competition relies on a spatial definition of who competitor trees are: all trees within a distance `comp_dist` of a focal tree. Here we set `comp_dist` to

154 7.5m, a value informed by other studies (Canham et al. 2004, Uriarte et al. (2004), Canham
155 et al. (2006)), but the package could also be used to compare multiple distances and see
156 which is best supported (see Appendix 2 9). We use `comp_dist` and a manually constructed
157 `sf` representation of the study region's boundary as inputs to `add_buffer_variable()` to
158 add a `buffer` boolean variable to `growth_scbi`. All trees with `buffer` equal to `FALSE` will
159 be our focal trees whose growth will be modeled, whereas those with `TRUE` will only act as
160 competitor trees.

```
# Define competitive distance range
comp_dist <- 7.5

# Manually construct study region boundary
study_region_scbi <- tibble(x = c(0, 300, 300, 0, 0), y = c(300, 300, 600,
  600, 300)) %>%
  sf_polygon()

growth_scbi <- growth_scbi %>%
  add_buffer_variable(size = comp_dist, region = study_region_scbi)
```

161 The second element of spatial information we add are blocks corresponding to folds
162 of a spatial cross-validation algorithm. Conventional cross-validation algorithms assign
163 individual observations to folds by randomly resampling them all while assuming they are
164 statistically independent. In the case of forest census data however, observations exhibit
165 spatial autocorrelation. We therefore incorporate this dependence into the cross-validation
166 algorithm by resampling spatial blocks of trees (Roberts et al. 2017, Pohjankukka et al.
167 (2017)).

168 We first manually define an `sf` object defining four folds that partition the study region.
169 We then use the output of the `spatialBlock()` function from the `blockCV` package to

170 associate each tree in `growth_scbi` to the correct `foldID` (Valavi et al. 2019). This `foldID`
171 variable will be used in Section 2.6.

172 Figure 2 illustrates the net effect of adding these two elements of spatial information to
173 `growth_scbi`.

```
# Manually define spatial blocks to act as folds

n_fold <- 4

fold1 <- cbind(c(0, 150, 150, 0), c(300, 300, 450, 450))
fold2 <- cbind(c(150, 300, 300, 150), c(300, 300, 450, 450))
fold3 <- cbind(c(0, 150, 150, 0), c(450, 450, 600, 600))
fold4 <- cbind(c(150, 300, 300, 150), c(450, 450, 600, 600))

blocks_scbi <- bind_rows(sf_polygon(fold1), sf_polygon(fold2), sf_polygon(fold3),
  sf_polygon(fold4)) %>%
  mutate(folds = c(1:n_fold) %>%
    factor())

# Associate each observation to a fold

spatial_block_scbi <- spatialBlock(speciesData = growth_scbi, k = n_fold,
  selection = "systematic", blocks = blocks_scbi, showBlocks = FALSE, verbose = FALSE)

growth_scbi <- growth_scbi %>%
  mutate(foldID = spatial_block_scbi$foldID %>%
    factor())

ggplot() + geom_sf(data = blocks_scbi, fill = "transparent", linetype = "dashed") +
  geom_sf_text(data = growth_scbi %>%
    sample_n(1000), aes(label = foldID, col = buffer))
```

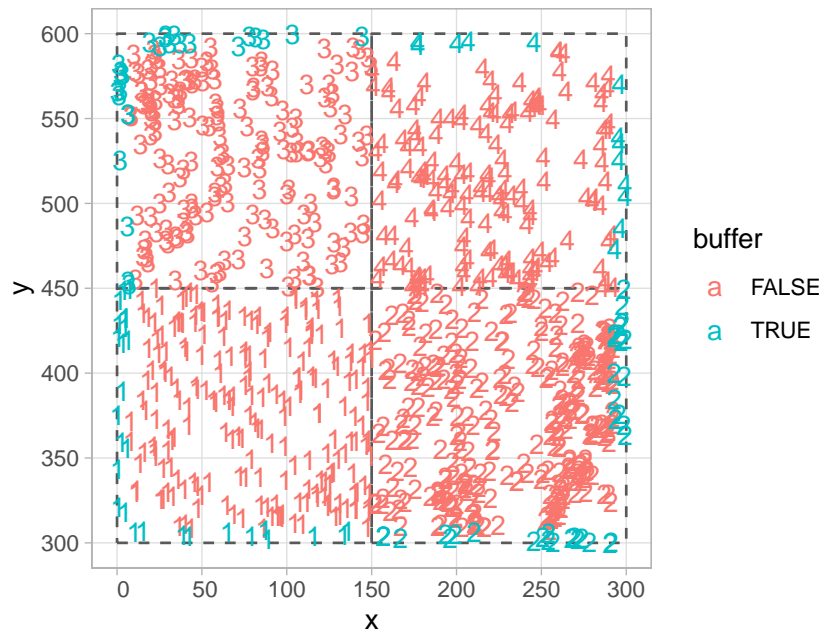


Figure 2: Step 2 - Add spatial information. A buffer region and spatial cross-validation blocks 1 through 4. The location of each tree is marked with its fold number where the folds are delineated with solid lines. The color of each digit indicates whether the tree is part of the buffer region (thus will only be considered as a competitor tree) or is part of the interior of the study region (thus is a focal tree whose growth is of modeled interest).

2.3 Step 3: Identify all focal and corresponding competitor trees

We then identify all focal trees and their corresponding competitor trees. More specifically, identify all trees that are not part of the buffer region, have a valid `growth` measurement, and have at least one neighbor within 7.5m. We do this using `create_focal_vs_comp()`, which takes the previously detailed `comp_dist` and `id` arguments as well as the `sf` representation of the spatial cross-validation blocks and returns a new data frame `focal_vs_comp_scbi`.

```
# TODO:

growth_scbi <- growth_scbi %>%
  mutate(comp_x_var = basal_area)

focal_vs_comp_scbi <- growth_scbi %>%
```

```

    create_focal_vs_comp(comp_dist, blocks = blocks_scbi, id = "stemID")
focal_vs_comp_scbi %>%
  select(focal_ID, focal_sp, geometry, growth, comp)
## # A tibble: 6,296 x 5
##   focal_ID focal_sp   geometry growth comp
##   <dbl> <fct>       <POINT> <dbl> <list>
## 1      4 nysy     (14.2 428)  0.103 <tibble [20 x 4]>
## 2      5 havi     (9.4 436)  0.150 <tibble [32 x 4]>
## 3     79 tiam     (40 381) -0.161 <tibble [20 x 4]>
## 4     80 caca    (38.7 422)  0.253 <tibble [12 x 4]>
## 5     96 libe    (60 310)  0.262 <tibble [14 x 4]>
## # ... with 6,291 more rows

```

180 The resulting `focal_vs_comp_scbi` has 6296 rows, representing the subset of the 7954
 181 trees in `growth_scbi` that will be considered as focal trees. The variables `focal_ID` and
 182 `focal_sp` relate to tree-stem identification and species information. Most notably however
 183 is the variable `comp`, which contains information on all competitor trees saved in `tidyr`
 184 package list-column format (Wickham 2020). To inspect this information, we flatten the
 185 `comp` list-column for the tree with `focal_ID` 4 in the first row, here a `tibble [20 × 4]`,
 186 into regular columns using `unnest()` from the `tidyr` package.

```

focal_vs_comp_scbi %>%
  filter(focal_ID == 4) %>%
  select(focal_ID, dbh, comp) %>%
  unnest(cols = "comp")
## # A tibble: 20 x 6
##   focal_ID dbh comp_ID dist comp_sp comp_x_var
##   <dbl> <dbl> <dbl> <dbl> <fct>      <dbl>

```

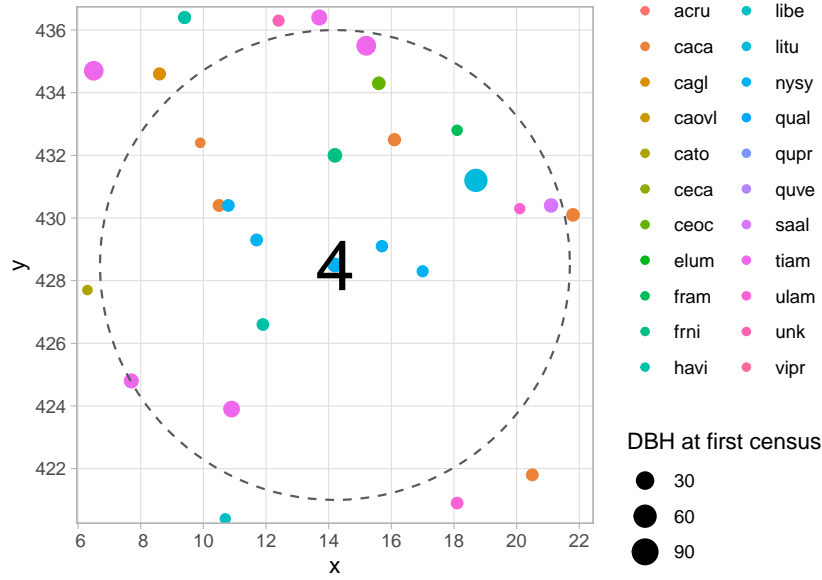


Figure 3: Step 3 - Identify all focal and corresponding competitor trees. The dashed circle extends 7.5m away from the focal tree 4 while all 20 competitor trees are within this circle.

```
## 1      4  13.6    1836  7.48 tiam    0.0176
## 2      4  13.6    1847  2.81 nysy    0.00332
## 3      4  13.6    1848  1.62 nysy    0.00396
## 4      4  13.6    1849  2.62 nysy    0.00535
## 5      4  13.6    1850  2.98 havi    0.00472
## # ... with 15 more rows
```

We observe 4 variables describing 20 competitor trees: the unique tree-stem ID, the distance to the focal tree (all ≤ 7.5 m), the species, and the basal area (in m^2) calculated as $\frac{\pi \times (\text{DBH}/2)^2}{10000}$ for the DBH in cm from the earlier census. Saving competitor information in list-column format minimizes redundancy since we do not need to repeat information on the focal tree 20 times. We visualize the spatial distribution of these trees in Figure 3.

2.4 Step 4: Fit model

Lastly, we fit the competition Bayesian linear regression model for tree growth outlined in Equation 1 using `comp_bayes_lm()`. This function has an option to specify prior distribu-

195 tions of all parameters, chosen here to be the defaults detailed in `?comp_bayes_lm`.

```
comp_bayes_lm_scbi <- focal_vs_comp_scbi %>%  
  comp_bayes_lm(prior_param = NULL)
```

196 The resulting `comp_bayes_lm_scbi` is an object of S3 class type `comp_bayes_lm` contain-
197 ing the posterior values of all parameters. Furthermore, this class includes generics for
198 three methods. First, the generic for `print()` displays the names of all prior and posterior
199 parameters and the model formula:

```
comp_bayes_lm_scbi  
  
## Bayesian linear regression model parameters with a multivariate Normal  
## likelihood. See ?comp_bayes_lm for details:  
##  
##   parameter_type      prior posterior  
## 1 Inverse-Gamma on sigma^2 a_0    a_star  
## 2 Inverse-Gamma on sigma^2 b_0    b_star  
## 3 Multivariate t on beta  mu_0    mu_star  
## 4 Multivariate t on beta  V_0     V_star  
##  
## Model formula:  
## growth ~ sp + dbh + dbh * sp + acne * sp + acru * sp + amar * sp + astr  
## * sp + caca * sp + caco * sp + cade * sp + cagl * sp + caovl * sp + cato  
## * sp + ceca * sp + ceoc * sp + chvi * sp + cofl * sp + crpr * sp + crsp  
## * sp + divi * sp + elum * sp + fagr * sp + fram * sp + frni * sp + frpe  
## * sp + havi * sp + ilve * sp + juci * sp + juni * sp + libe * sp + litu  
## * sp + nysy * sp + pist * sp + pivi * sp + ploc * sp + prav * sp + prse  
## * sp + qual * sp + quco * sp + qufa * sp + qumi * sp + qupr * sp + quru
```

```
## * sp + quve * sp + rops * sp + saal * sp + saca * sp + tiam * sp + ulam
## * sp + ulru * sp + unk * sp + vipr * sp
```

200 Next, the generic for `predict()` takes the posterior parameter values in `comp_bayes_lm_scbi`
 201 and a `newdata` data frame, and outputs a vector `growth_hat` of predicted DBH values \widehat{y}_{ij}
 202 computed from the posterior predictive distribution.

```
focal_vs_comp_scbi <- focal_vs_comp_scbi %>%
  mutate(growth_hat = predict(comp_bayes_lm_scbi, newdata = focal_vs_comp_scbi))
```

```
focal_vs_comp_scbi %>%
  select(focal_ID, focal_sp, dbh, growth, growth_hat)
## # A tibble: 6,296 x 5
##   focal_ID focal_sp   dbh growth growth_hat
##   <dbl> <fct>   <dbl> <dbl>    <dbl>
## 1      4 nysy    13.6  0.103   0.0809
## 2      5 havi     8.8  0.150   0.112
## 3     79 tiam    47.7 -0.161   0.229
## 4     80 caca     5.15  0.253   0.121
## 5     96 libe     2.3  0.262   0.142
## # ... with 6,291 more rows
```

203 We can now compare the observed and predicted growths to compute the root mean
 204 squared error (RMSE) of our model:

```
model_rmse <- focal_vs_comp_scbi %>%
  rmse(truth = growth, estimate = growth_hat) %>%
  pull(.estimate)
```

```
model_rmse
## [1] 0.128
```

205 Lastly, the generic for `ggplot2::autoplot()` allows us to visualize all posterior dis-
206 tributions, as seen in Figure 4. Setting `type` to `"intercepts"` and `"dbh_slopes"` returns
207 species-specific posterior distributions for $\beta_{0,j}$ and $\beta_{dbh,j}$ respectively, while setting `type =`
208 `"competition"` returns competition coefficients $\lambda_{j,k}$.

```
# Plot posteriors for only a subset of species
sp_to_plot <- c("litu", "quru", "cagl")

plot1 <- autoplot(comp_bayes_lm_scbi, type = "intercepts", sp_to_plot = sp_to_plot)
plot2 <- autoplot(comp_bayes_lm_scbi, type = "dbh_slopes", sp_to_plot = sp_to_plot)
plot3 <- autoplot(comp_bayes_lm_scbi, type = "competition", sp_to_plot = sp_to_plot)

# Combine plots using the patchwork package
(plot1 | plot2)/plot3
```

209 For many users the visualizations of $\lambda_{j,k}$ will be of particular interest as they provide
210 insight into species-specific competitive interactions, where negative values indicate a com-
211 petitor species which slows the growth of a focal species. Here, for example, we see that
212 tulip poplars (litu) have a strong negative effect on the growth of conspecifics but relatively
213 lesser effect on pignut hickory (cagl) and red oak (quru) neighbors.

214 Currently the `forestecology` package can only fit the competition Bayesian linear
215 regression model in Equation 1. However, it can be extended to any model as long as it is
216 implemented in a function similar to `comp_bayes_lm()`.

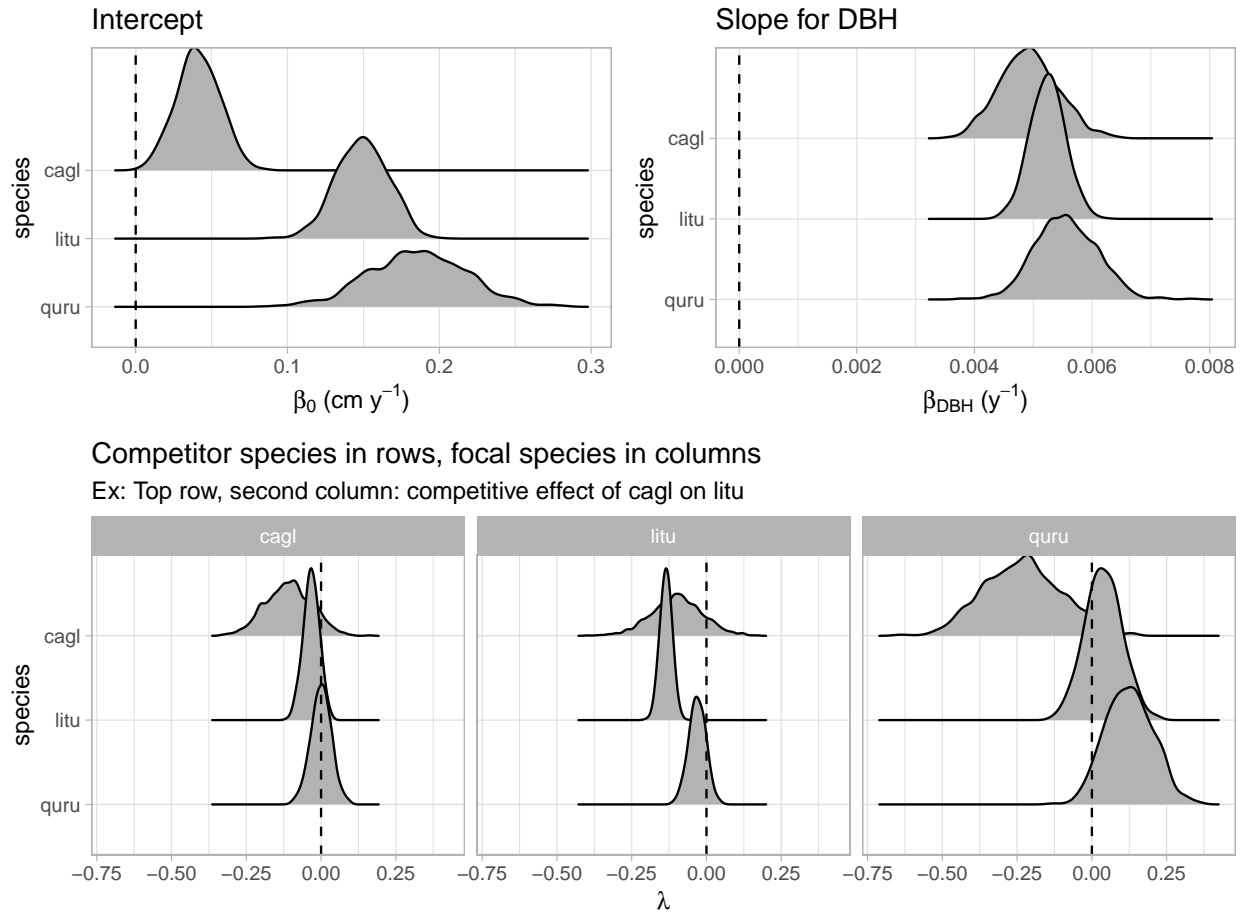


Figure 4: Step 4 - Fit model. Posterior distributions of all parameters. For compactness we include only three species.

2.5 Evaluate the effect of competitor species identity using permutation tests

To evaluate the effect of competitor species identity, we use the above four steps along with the permutation test in Equation 2. Under a null hypothesis where competitor species identity does not matter, we can permute the competitor species identities within each focal tree, compute the RMSE test statistic, repeat this process several times to construct a null distribution, and compare it to the observed RMSE to assess significance. Going back to our example in Section 2.3 of focal tree with `focal_ID` 4 and its 20 competitors, the permutation test only randomly resamples the `comp_sp` variable without replacement, leaving all other variables intact. This resampling is nested within each focal tree in order to preserve neighborhood structure. We perform this permutation test once again using `comp_bayes_lm()` but by setting `run_shuffle = TRUE`.

```
comp_bayes_lm_scbi_shuffle <- focal_vs_comp_scbi %>%  
  comp_bayes_lm(prior_param = NULL, run_shuffle = TRUE)  
  
focal_vs_comp_scbi <- focal_vs_comp_scbi %>%  
  mutate(growth_hat_shuffle = predict(comp_bayes_lm_scbi_shuffle, newdata = focal_vs_c  
  
model_rmse_shuffle <- focal_vs_comp_scbi %>%  
  rmse(truth = growth, estimate = growth_hat_shuffle) %>%  
  pull(.estimate)  
model_rmse_shuffle  
## [1] 0.131
```

The resulting permutation test RMSE of 0.131 is larger than the earlier RMSE of 0.128, suggesting that models that do incorporate competitor species identity better fit the data.

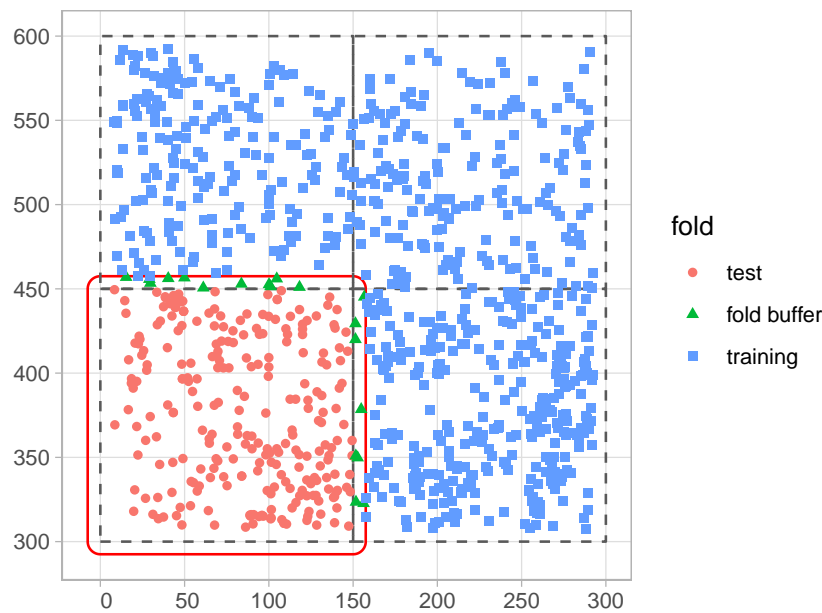


Figure 5: Schematic of spatial cross-validation. Using the $k = 1$ fold (bottom-left) as the test set, $k = 2$ through 4 as the training set, along with a "fold buffer" extending outwards from the test set to maintain spatial independence between it and the training set.

2.6 Evaluate model performance using spatial cross-validation

To evaluate model performance, we use spatial cross-validation. The model fit in Section 2.4 uses the same data to both fit and assess model performance. Given the spatial-autocorrelation of our data, this can potentially lead to overfit models (Roberts et al. 2017). To mitigate this risk, we use the spatial cross-validation blocking scheme encoded in the `foldID` variable from Section 2.2 and visualized in Figure 2.

At each iteration of the cross-validation, one fold acts as the test set and the remaining three act as the training set. We fit the model to all focal trees in the training set, apply the model to all focal trees in the test set, compute predicted values, and compute the RMSE. Furthermore, to maintain spatial independence between the test and training sets, a "fold buffer" that extends 7.5m outwards from the boundary of the test set is considered; all trees within this "fold buffer" are excluded from the training set (see Figure 5).

This process is repeated for each of the four folds acting as the test set, then the four RMSE's are averaged to provide a single estimate of model error. This algorithm is

implemented in `run_cv()`, which acts as a wrapper function to both `comp_bayes_lm()` that fits the model and `predict()` that returns predicted values.

```
focal_vs_comp_scbi <- focal_vs_comp_scbi %>%  
  run_cv(comp_dist = comp_dist, blocks = blocks_scbi)
```

```
model_rmse_cv <- focal_vs_comp_scbi %>%  
  rmse(truth = growth, estimate = growth_hat) %>%  
  pull(.estimate)  
model_rmse_cv  
## [1] 0.14
```

The resulting RMSE of 0.14 computed using cross-validation is larger than the earlier RMSE of 0.128, suggesting that models that do not account for spatial autocorrelation generate model error estimates that are overly optimistic, i.e. RMSE values that are too low.

3 Importance of spatial cross-validation

`run_cv()` also accepts the `run_shuffle` argument in order to permute competitor species identity as described in Section 2.5. Figure 6 compares model performance for 49 permutations of competitor species and RMSE calculations, both with and without cross-validation. Without cross-validation, competitor species identity does matter as the observed RMSE was significantly lower than the permutation null distribution of RMSE. However, once we incorporate spatial cross-validation, this improvement disappears. These results suggest that in this 9 ha subplot of the SCBI plot, competitive interactions do not depend on the identity of the competitor, which is the opposite of what has been observed in other locations (Allen & Kim 2020, Uriarte et al. (2004)). This provides a striking example of the

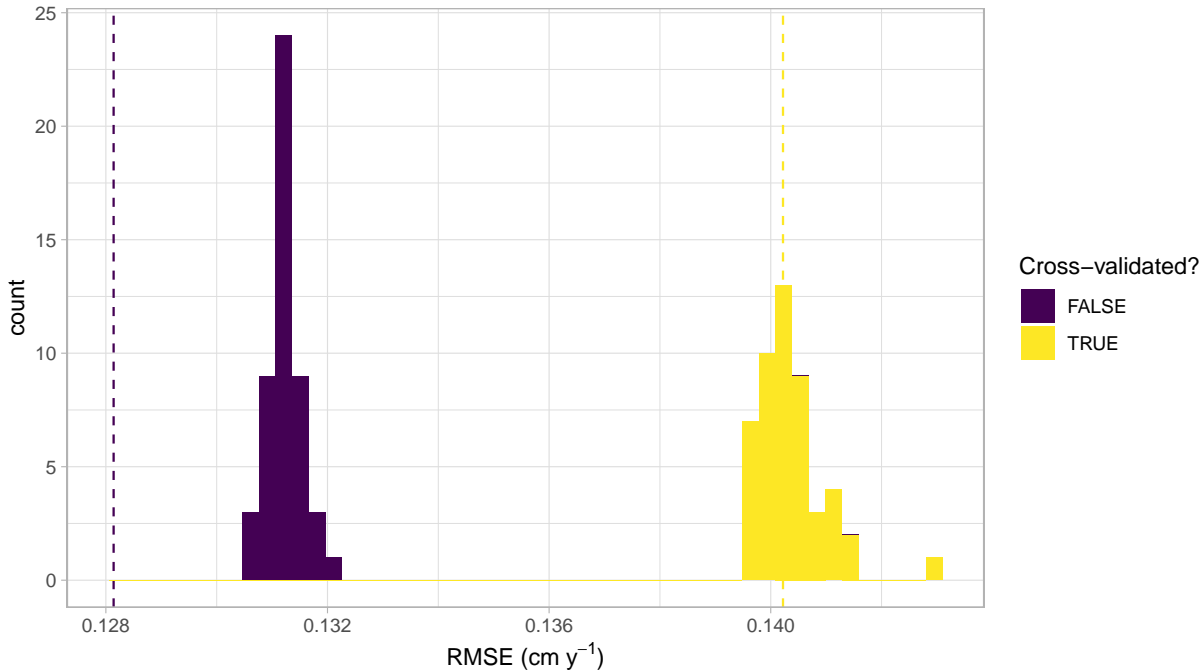


Figure 6: Comparison of root mean squared error of models for standard, permuted, and spatially cross-validated error estimates. The dotted lines show observed RMSE while the histograms show the null distribution of RMSE for 49 permutations under the null hypothesis of no competitor species identity effects. The colors indicate whether spatial cross-validation was used or not.

importance of cross-validation, as without it the over-fit model gives rise to an incorrect conclusion.

4 Conclusion and future work

The `forestecology` package provides an accessible way to fit and test models of neighborhood competition. The package follows the `tidy` data design principles, leverages the `sf` package for spatial data, and S3 open-oriented model implementation structure (Pebesma 2018). We hope that the package will increase the use of neighborhood competition models to better understand what structures plant competition.

While the package is designed with ForestGEO plot data in mind, we envision that it can be modified to work on any single large, mapped forest plot in which at least two mea-

surements of each individual have been taken. Furthermore, we hope that future versions of the package will be flexible to other plot layouts, for example inventory plot-structure with many spatially separated plots like the US Forest Service Forest Inventory and Analysis plots (Smith 2002).

We also hope to extend the `forestecology` package’s functionality to account for a larger variety of models for tree growth. One clear future direction would be to allow competition based on species trait values rather than species identity. There is evidence that traits predict competitive outcomes (Kunstler et al. 2012, Lasky et al. (2014), Uriarte et al. (2010)). Thus an extension of the model would allow λ values from Equation 1 to be a function of the traits of competing species.

Lastly, the `forestecology` current uses the `blockCV` package behind the scenes to create the spatial blocks acting as folds for our spatial cross-validation algorithm detailed in Sections 2.2 and 2.6 (Valavi et al. 2019). This back-end functionality could be substituted with the `spatialsample` package for spatial resampling infrastructure; a `tidymodels` package under active development as of 2021 (Silge 2021, Kuhn & Wickham (2020)).

5 Acknowledgments

We thank Sophie Li for their feedback on the package interface. The authors declare no conflicts of interest.

6 Author’s contributions

AYK and DNA conceived the ideas and coded a draft of the package. AYK wrote an initial manuscript draft. SPC rewrote much of the package’s code to align with R and “tidy” best practices (Wickham et al. 2019). All authors contributed to subsequent drafts and gave final approval for manuscript.

7 Data accessibility

We intend to archive all data and source code for this manuscript on GitHub at <https://github.com/rudeboybert/forestecology> and on Zenodo upon acceptance. The example Smithsonian Conservation Biology Institute census data are available on GitHub at https://github.com/SCBI-ForestGEO/SCBI-ForestGEO-Data/tree/master/tree_main_census/data/census-csv-files and are archived on Zenodo at <https://doi.org/10.5281/zenodo.2649301> (Gonzalez-Akre, McGregor, Anderson-Teixeira, Dow, Herrmann, Terrell, Kim, Vinod & Helcoski 2020).

8 Appendix 1: Replicate RMSE comparison

This code replicates Figure 6: A comparison of root mean squared error of models for standard, permuted, and spatial cross-validated error estimates.

```
library(tidyverse)
library(lubridate)
library(here)
library(sf)
library(viridis)
library(forestecology)
library(blockCV)
library(tictoc)

# Compute growth of trees based on census data
# -----
census_2013_scbi <- here("paper/scbi.stem2.csv") %>%
```

```
read_csv() %>%
  select(stemID, sp, date = ExactDate, gx, gy, dbh, codes, status) %>%
  mutate(date = mdy(date), dbh = as.numeric(dbh)/10) %>%
  filter(gx < 300, between(gy, 300, 600))

census_2018_scbi <- here("paper/scbi.stem3.csv") %>%
  read_csv() %>%
  select(stemID, sp, date = ExactDate, gx, gy, dbh, codes, status) %>%
  mutate(date = mdy(date), dbh = as.numeric(dbh)/10) %>%
  filter(gx < 300, between(gy, 300, 600))

growth_scbi <- compute_growth(census_1 = census_2013_scbi, census_2 = census_2018_scbi %>%
  filter(!str_detect(codes, "R")), id = "stemID")

# Add spatial information
# ----- Define buffer region
# using competitive distance range
comp_dist <- 7.5

study_region_scbi <- tibble(x = c(0, 300, 300, 0, 0), y = c(300, 300, 600,
  600, 300)) %>%
  sf_polygon()

growth_scbi <- growth_scbi %>%
  add_buffer_variable(size = comp_dist, region = study_region_scbi)
```

```
# Manually define spatial blocks to act as folds
fold1 <- rbind(c(0, 300), c(150, 300), c(150, 450), c(0, 450))
fold2 <- rbind(c(150, 300), c(300, 300), c(300, 450), c(150, 450))
fold3 <- rbind(c(0, 450), c(150, 450), c(150, 600), c(0, 600))
fold4 <- rbind(c(150, 450), c(300, 450), c(300, 600), c(150, 600))
n_fold <- 4

blocks_scbi <- bind_rows(sf_polygon(fold1), sf_polygon(fold2), sf_polygon(fold3),
  sf_polygon(fold4)) %>%
  mutate(folds = c(1:n_fold) %>%
    factor())

# Associate each observation to a fold
SpatialBlock_scbi <- spatialBlock(speciesData = growth_scbi, k = n_fold,
  selection = "systematic", blocks = blocks_scbi, showBlocks = FALSE, verbose = FALSE)

growth_scbi <- growth_scbi %>%
  mutate(foldID = SpatialBlock_scbi$foldID %>%
    factor())

# Compute focal versus competitor tree information
# -----
focal_vs_comp_scbi <- growth_scbi %>%
  create_focal_vs_comp(comp_dist, blocks = blocks_scbi, id = "stemID")
```

```
# Fit model and make predictions

# ----- Number of permutation

# shuffles:
num_shuffle <- 49

# Save results here

run_time <- 0
observed_RMSE <- 0
observed_RMSE_CV <- 0
shuffle_RMSE <- vector("list", 1)
shuffle_RMSE_CV <- vector("list", 1)
filename <- here("paper/simulation_results/") %>%
  str_c("2021-03-03_scbi_", num_shuffle, "_shuffles")

# Run all simulations 0. Setup simulation for this species type ----

# Start clock
tic()

# 1. Compute observed test statistic: RMSE with no cross-validation
# ---- Fit model (compute posterior parameters)
comp_bayes_lm_scbi <- focal_vs_comp_scbi %>%
  comp_bayes_lm(prior_param = NULL, run_shuffle = FALSE)

# Make predictions and compute RMSE
observed_RMSE <- focal_vs_comp_scbi %>%
  mutate(growth_hat = predict(comp_bayes_lm_scbi, focal_vs_comp_scbi)) %>%
```

```
rmse(truth = growth, estimate = growth_hat) %>%
pull(.estimate)

# 2. Compute observed test statistic: RMSE with cross-validation
# -----
observed_RMSE_CV <- focal_vs_comp_scbi %>%
  run_cv(comp_dist = comp_dist, blocks = blocks_scbi) %>%
  rmse(truth = growth, estimate = growth_hat) %>%
  pull(.estimate)

# 3. Permutation distribution: RMSE with no cross-validation
# ----- Compute num_shuffle permutation test statistics
shuffle_RMSE <- numeric(length = num_shuffle)
for (j in 1:num_shuffle) {
  # Fit model (compute posterior parameters) with shuffling
  comp_bayes_lm_scbi <- focal_vs_comp_scbi %>%
    comp_bayes_lm(prior_param = NULL, run_shuffle = TRUE)

  # Make predictions and compute RMSE
  shuffle_RMSE[j] <- focal_vs_comp_scbi %>%
    mutate(growth_hat = predict(comp_bayes_lm_scbi, focal_vs_comp_scbi)) %>%
    rmse(truth = growth, estimate = growth_hat) %>%
    pull(.estimate)
}

# 4. Permutation distribution: RMSE with cross-validation
```

```
# ----- Compute num_shuffle permutation test statistics
shuffle_RMSE_CV <- numeric(length = num_shuffle)

# Compute num_shuffle permutation test statistics
for (j in 1:num_shuffle) {
  # Compute and save RMSE
  shuffle_RMSE_CV[j] <- focal_vs_comp_scbi %>%
    run_cv(comp_dist = comp_dist, blocks = blocks_scbi, run_shuffle = TRUE) %>%
    rmse(truth = growth, estimate = growth_hat) %>%
    pull(.estimate)

  # Status update
  str_c("Shuffle with permutation ", j, " at ", Sys.time()) %>%
    print()
}

# 5. Save results ----
clock <- toc(quiet = TRUE)
run_time <- clock$toc - clock$tic

model_comp_tbl <- tibble(run_time = run_time, observed_RMSE = observed_RMSE,
  observed_RMSE_CV = observed_RMSE_CV, shuffle_RMSE = shuffle_RMSE, shuffle_RMSE_CV =
  )
save(model_comp_tbl, file = filename %>%
  str_c(".RData"))
```

```
# Visualize results
# -----

model_comp <- bind_rows(model_comp_tbl %>%
  select(run_time, observed = observed_RMSE, shuffle = shuffle_RMSE) %>%
  mutate(CV = FALSE), model_comp_tbl %>%
  select(run_time, observed = observed_RMSE_CV, shuffle = shuffle_RMSE_CV) %>%
  mutate(CV = TRUE)) %>%
  gather(type, RMSE, -c(run_time, CV))

model_comp_observed <- model_comp %>%
  filter(type == "observed") %>%
  unnest(cols = c(RMSE))

model_comp_shuffle <- model_comp %>%
  filter(type == "shuffle") %>%
  unnest(cols = c(RMSE))

cv_plot <- ggplot() + geom_vline(data = model_comp_observed, aes(xintercept = RMSE,
  col = CV), linetype = "dashed", show.legend = F) + geom_histogram(data = model_comp_observed,
  aes(x = RMSE, fill = CV), bins = 50) + labs(fill = "Cross-validated?",
  x = expression(paste("RMSE (cm ", y^{
    -1
  }, ")")))) + scale_color_viridis(discrete = TRUE, option = "D") + scale_fill_viridis(option = "D")
theme_light()

cv_plot

filename %>%
```



```
str_c(".pdf") %>%  
ggsave(plot = cv_plot, width = 16/2, height = 9/2)
```

9 Appendix 2: Compare different competitive distances

For all the above analyses we took the cut off distance (`comp_dist`) for two stems to compete as 7.5 m. This distance has been estimated in previous neighborhood competition studies in forests (Canham et al. 2004, Uriarte et al. (2004), Canham et al. (2006)). We used 7.5 m in Allen & Kim (2020) as an average of the values estimated in other studies. But our package can be used to find which distance is best supported by the data. Here we provide an example using another section of the SCBI plot to provide an additional example of the CV block layout. To speed computation we do not consider species differences in competitive effects and treat all species as the same.

```
census_2013_scbi <- read_csv("scbi.stem2.csv") %>%  
  select(stemID, sp, date = ExactDate, gx, gy, dbh, codes, status) %>%  
  mutate(date = mdy(date), dbh = as.numeric(dbh)/10) %>%  
  filter(gx < 400, gy < 400)  
  
census_2018_scbi <- read_csv("scbi.stem3.csv") %>%  
  select(stemID, sp, date = ExactDate, gx, gy, dbh, codes, status) %>%  
  mutate(date = mdy(date), dbh = as.numeric(dbh)/10) %>%  
  filter(gx < 400, gy < 400)  
  
growth_scbi <- compute_growth(census_1 = census_2013_scbi, census_2 = census_2018_scbi %>%  
  filter(!str_detect(codes, "R")), id = "stemID") %>%
```

```
# make all species the same, needs to be factor with at least two
# levels
mutate(sp = factor("A", levels = c("A", "B")))

study_region_scbi <- tibble(x = c(0, 400, 400, 0, 0), y = c(0, 0, 400, 400,
0)) %>%
  sf_polygon()

n_fold <- 4

fold1 <- cbind(c(0, 200, 200, 0), c(0, 0, 200, 200))
fold2 <- cbind(c(200, 400, 400, 200), c(0, 0, 200, 200))
fold3 <- cbind(c(0, 200, 200, 0), c(200, 200, 400, 400))
fold4 <- cbind(c(200, 400, 400, 200), c(200, 200, 400, 400))

blocks_scbi <- bind_rows(sf_polygon(fold1), sf_polygon(fold2), sf_polygon(fold3),
  sf_polygon(fold4)) %>%
  mutate(folds = c(1:n_fold) %>%
    factor())

# Associate each observation to a fold
spatial_block_scbi <- spatialBlock(speciesData = growth_scbi, k = n_fold,
  selection = "systematic", blocks = blocks_scbi, showBlocks = FALSE, verbose = FALSE)

growth_scbi <- growth_scbi %>%
  mutate(foldID = spatial_block_scbi$foldID %>%
    factor())
```

```

mult_dist_comp <- tibble(dist = c(5, 6.25, 7.5, 8.75, 10), rmse = 0)

for (i in 1:length(mult_dist_comp$dist)) {
  comp_dist <- mult_dist_comp$dist[i]

  growth_scbi <- growth_scbi %>%
    add_buffer_variable(size = comp_dist, region = study_region_scbi)

  focal_vs_comp_scbi <- growth_scbi %>%
    create_focal_vs_comp(comp_dist = comp_dist, blocks = blocks_scbi,
      id = "stemID") %>%
    run_cv(comp_dist = comp_dist, blocks = blocks_scbi)

  mult_dist_comp$rmse[i] <- focal_vs_comp_scbi %>%
    rmse(truth = growth, estimate = growth_hat) %>%
    pull(.estimate)
}

mult_dist_comp %>%
  ggplot(aes(dist, rmse)) + geom_point() + xlab("Distance (m)") + ylab("RMSE (cm)")

```

315 Here we see that a cut off distance of approximately 6 m minimizes RMSE.

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