

ECE 3030

Physical Foundations of Computer Engineering

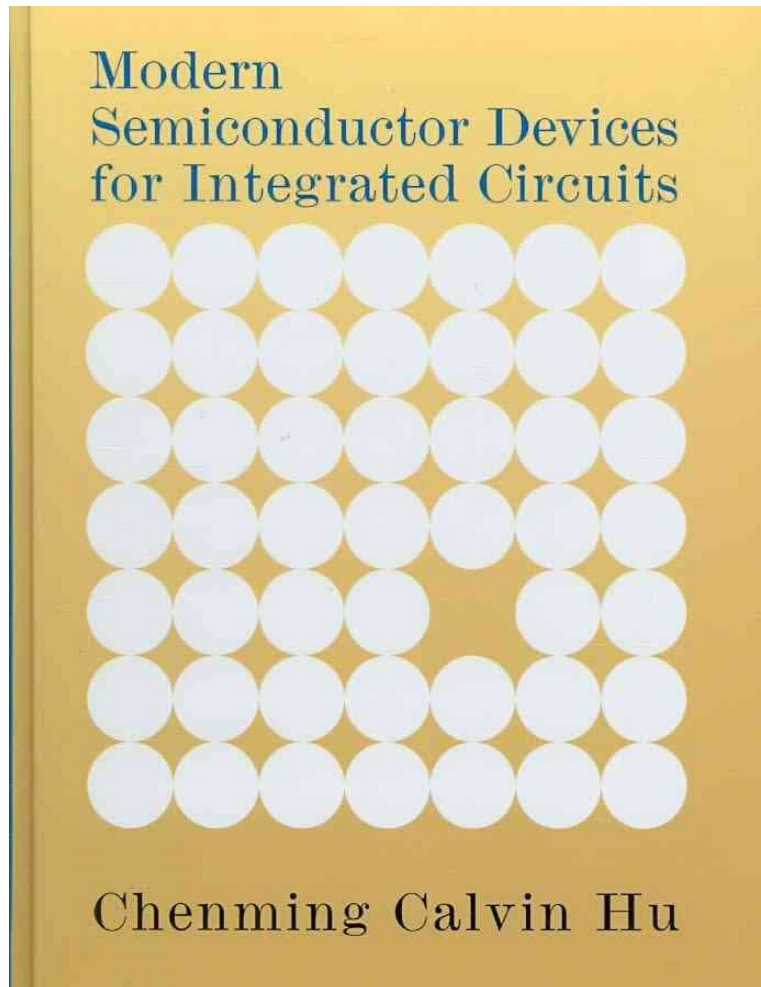
MOS Electrostatics-II

Asif Khan

*Department of Electrical and Computer Engineering
Georgia Institute of Technology*



Reference



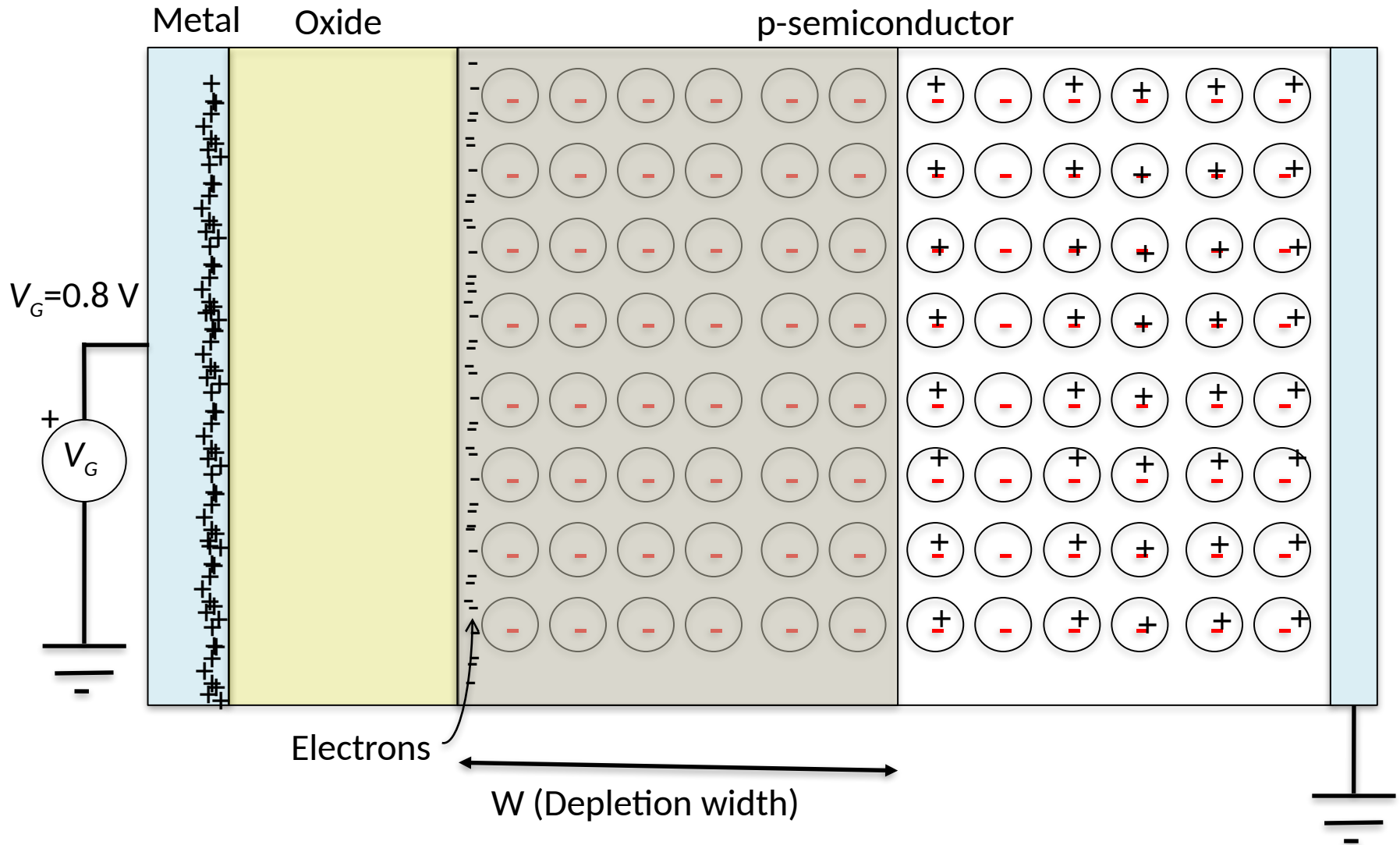
Modern Semiconductor Devices for Integrated Circuits

Chapter 5: Section 5.3, 5.4, 5.5

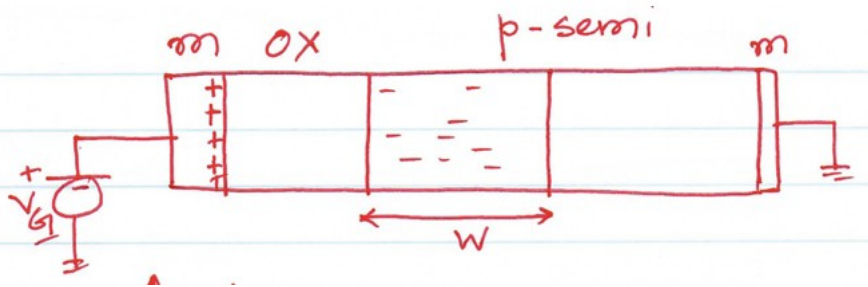
Resources

Recorded lecture available at <https://youtu.be/gU85ggnOCIU>

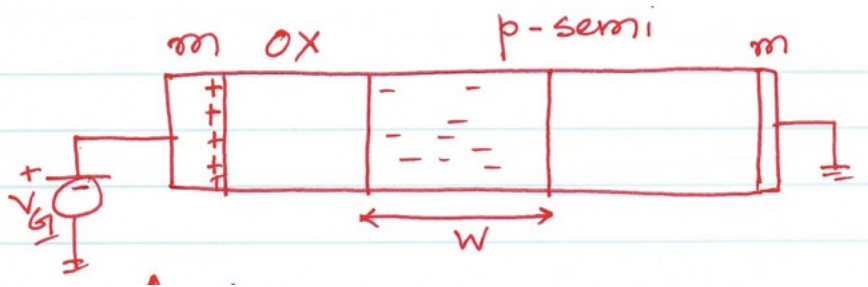
What happens when you apply $V_G > \text{Threshold}$?



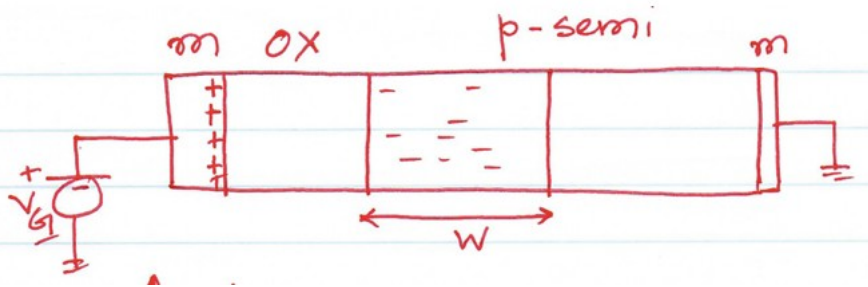
Electrostatics of MOS Capacitors



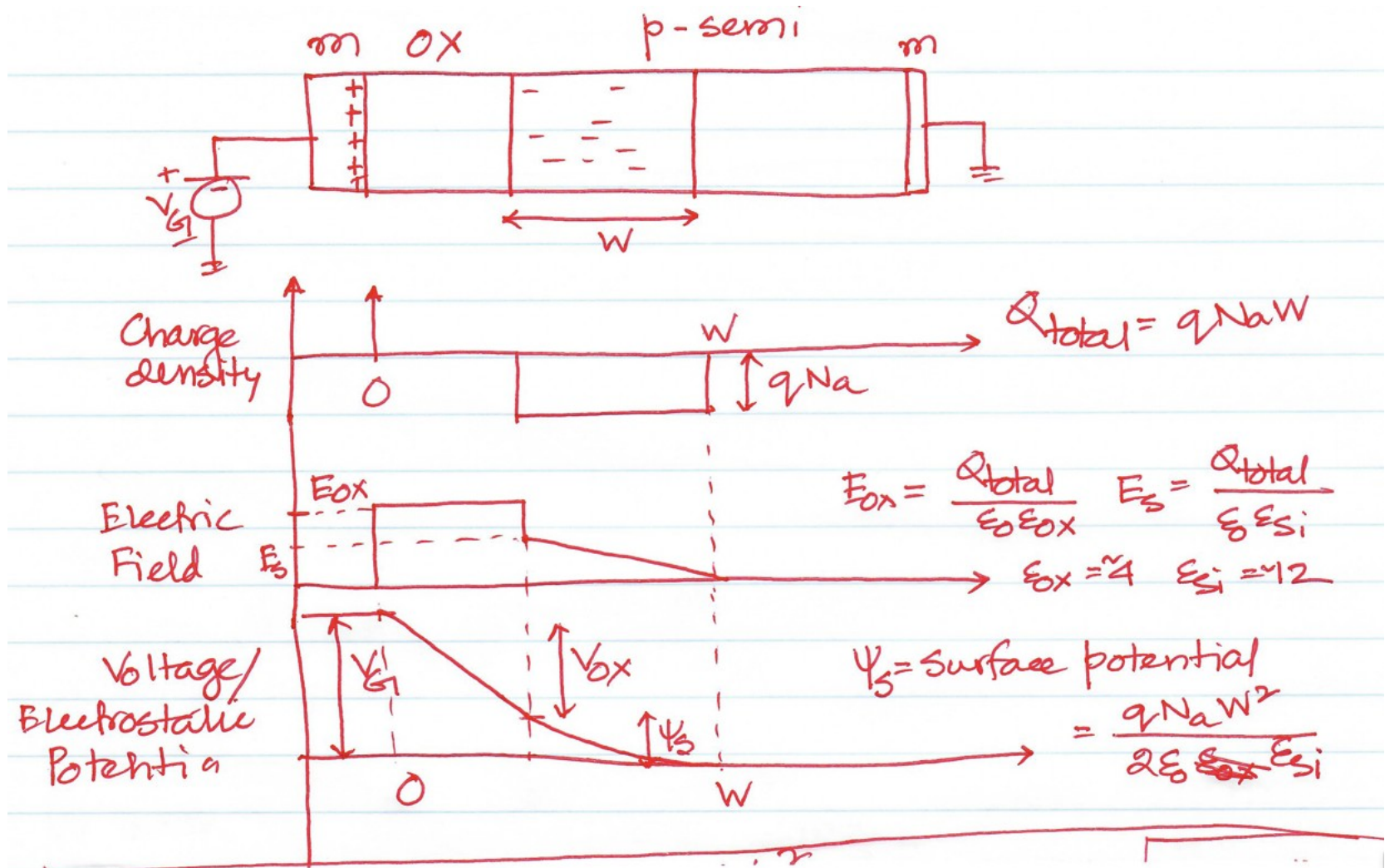
Electrostatics of MOS Capacitors



Electrostatics of MOS Capacitors



Electrostatics of MOS Capacitors



Electrostatics of MOS Capacitors


$$\psi_s = \frac{qNaW^2}{2\epsilon_0\epsilon_{Si}} \quad W = \sqrt{\frac{2\epsilon_0\epsilon_{Si}\psi_s}{qNa}}$$

$$V_G = V_{ox} + \psi_s = \frac{qNaW}{C_{ox}} + \psi_s = \frac{\sqrt{2\epsilon_0\epsilon_{Si}qNa\psi_s}}{C_{ox}} + \psi_s$$

\downarrow
 $\frac{Q_{total}}{C_{ox}}$

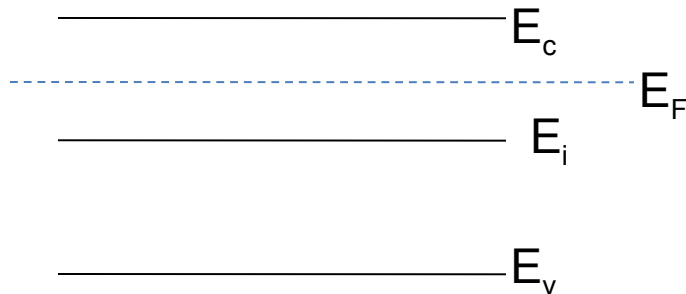
At threshold, $\psi_s = 2\psi_B \Rightarrow$

$$V_t = V_G(\psi_s = 2\psi_B)$$
$$= \frac{\sqrt{4\epsilon_0\epsilon_{Si}qNa\psi_B}}{C_{ox}} + 2\psi_B$$



How to create inversion?

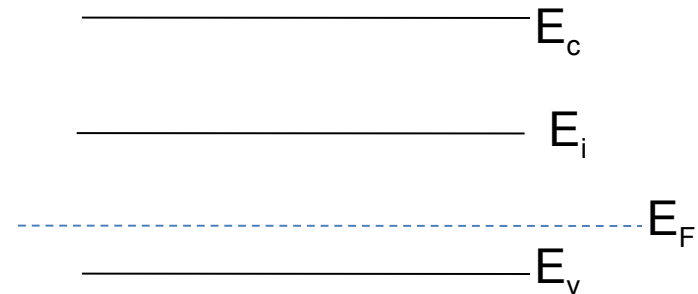
n-type



$$n = N_c e^{(E_F - E_C)/kT}$$

The closer the Fermi level is to the conduction band, the larger is the number of electrons

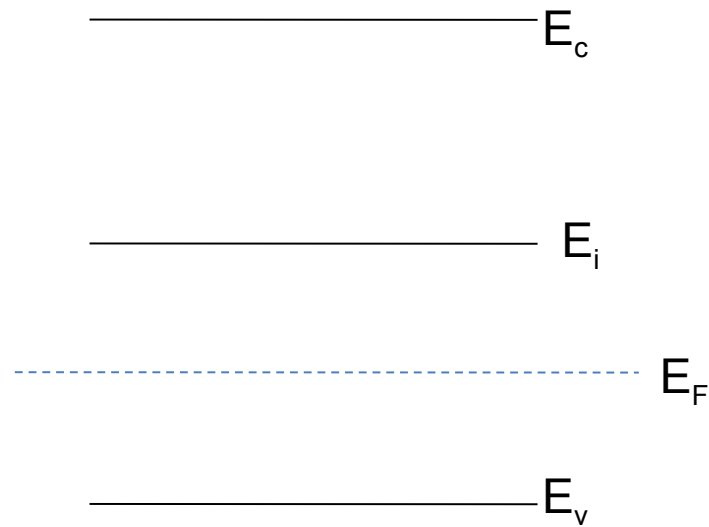
p-type



$$p = N_v e^{(E_V - E_F)/kT}$$

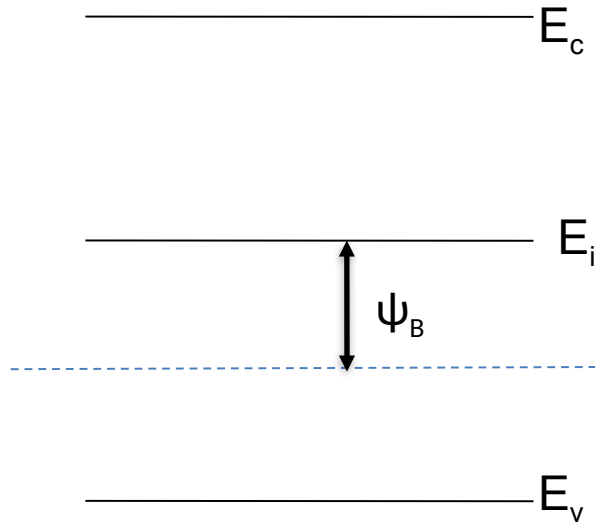
The closer the Fermi level is to the valence band, the larger is the number of holes

How to create inversion?

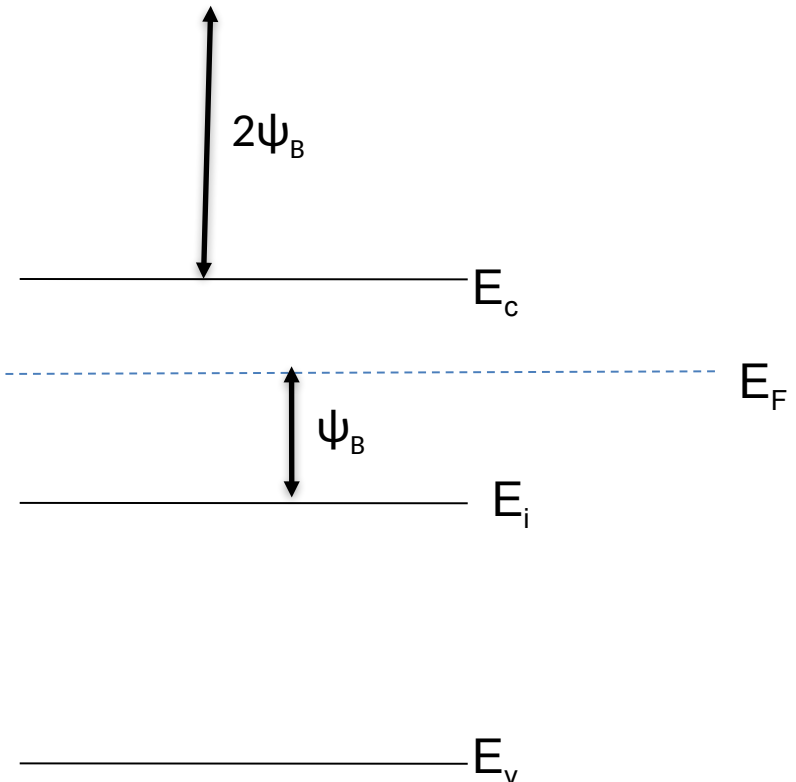


How to create inversion?

Before

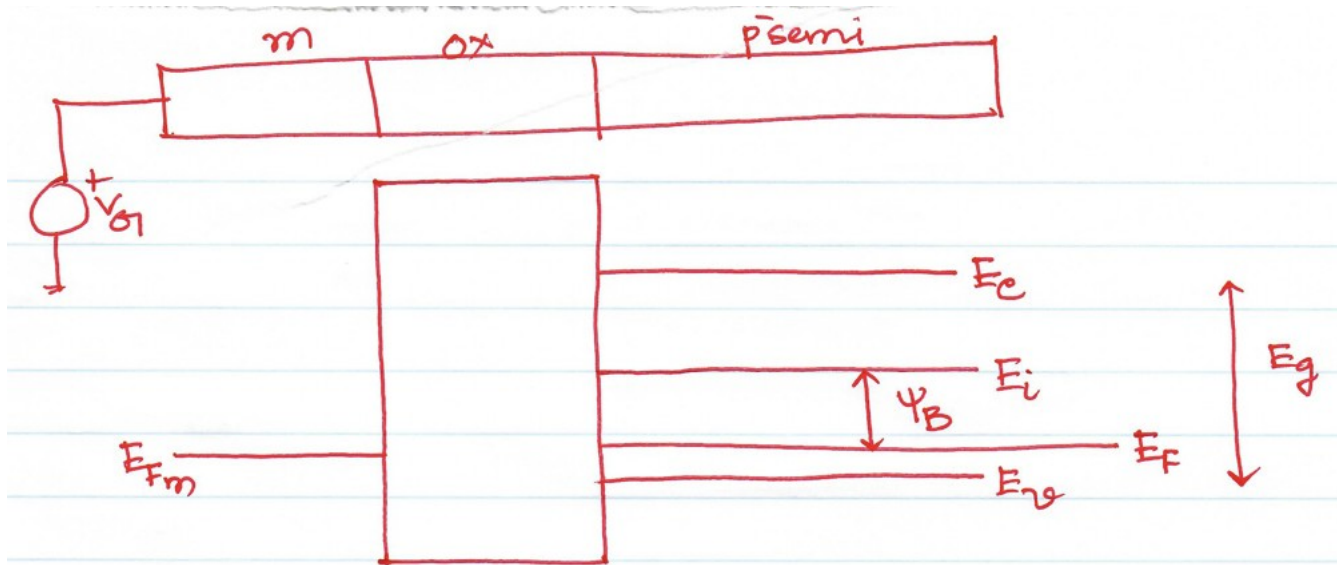


At Threshold

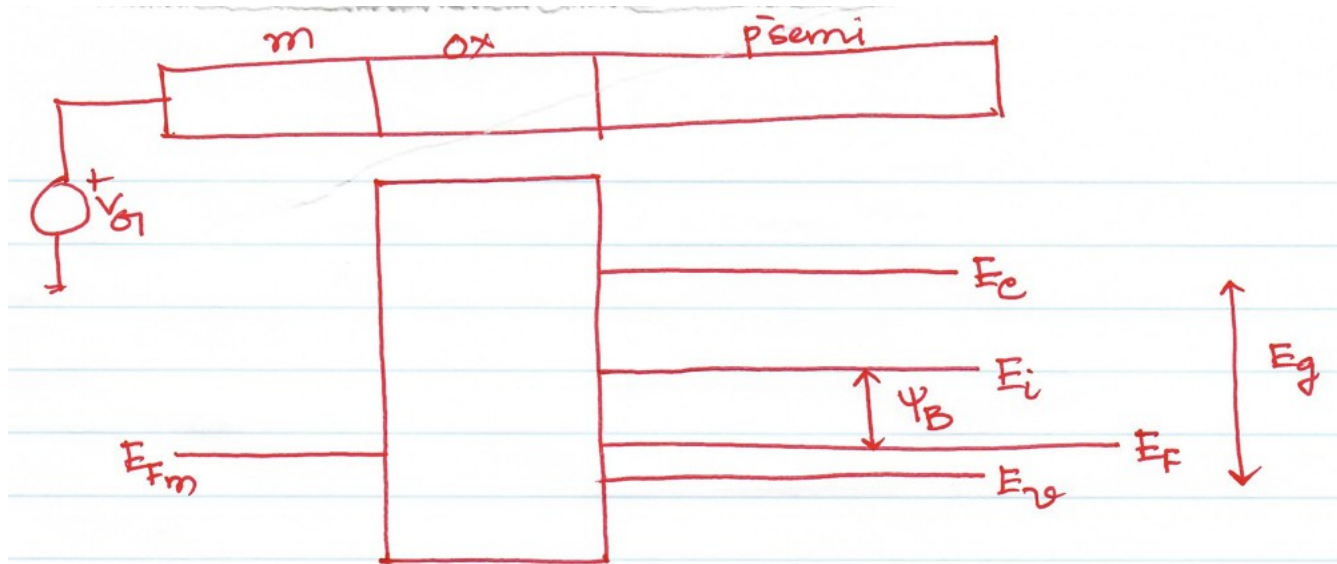


The semiconductor needs to a voltage/electrostatic potential= $2\psi_B$ for carrier inversion

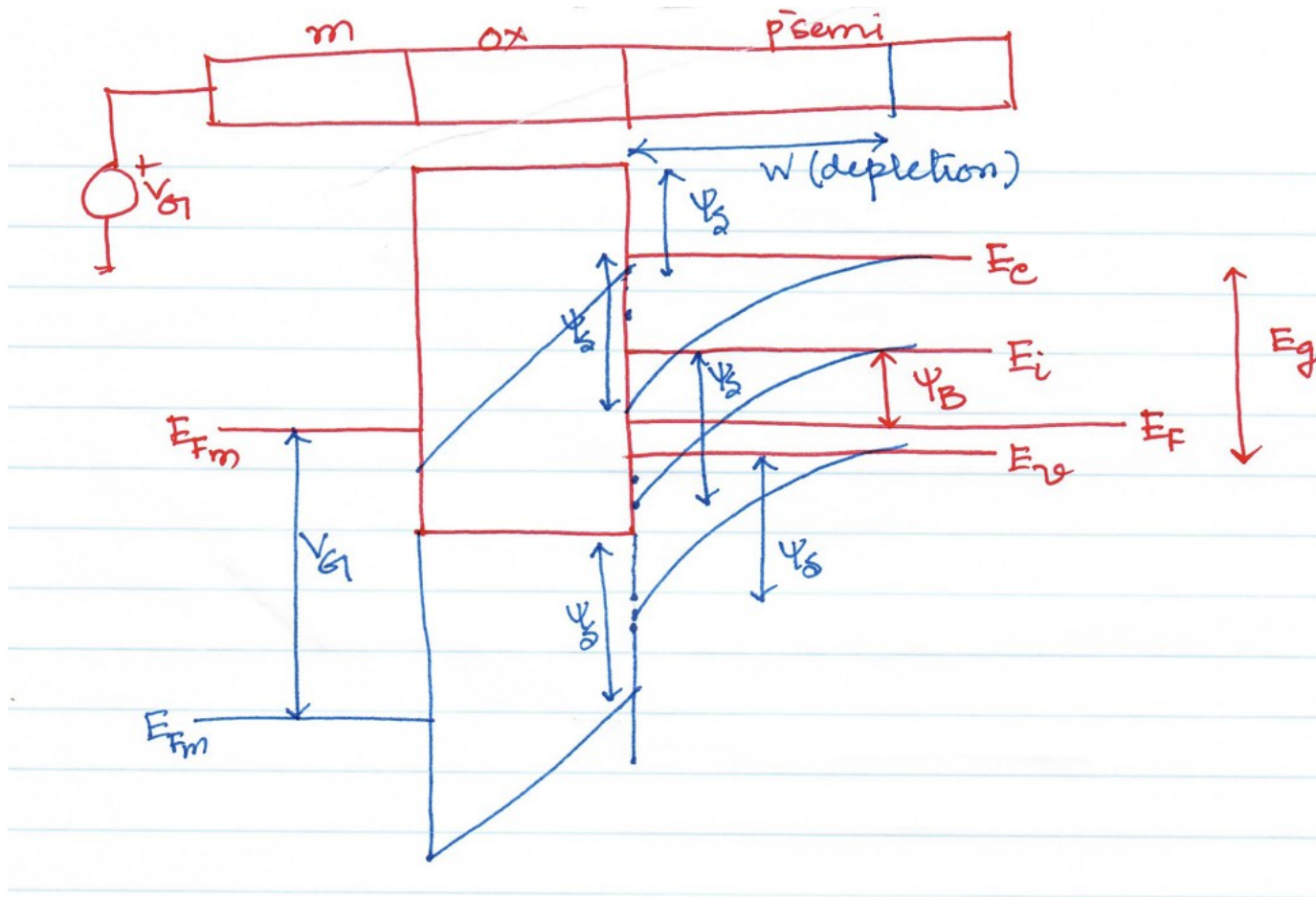
Band Diagram with $V_G=0$

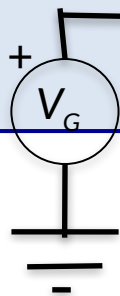


Band Diagram with $V_G > 0$



Band Diagram with an applied VG

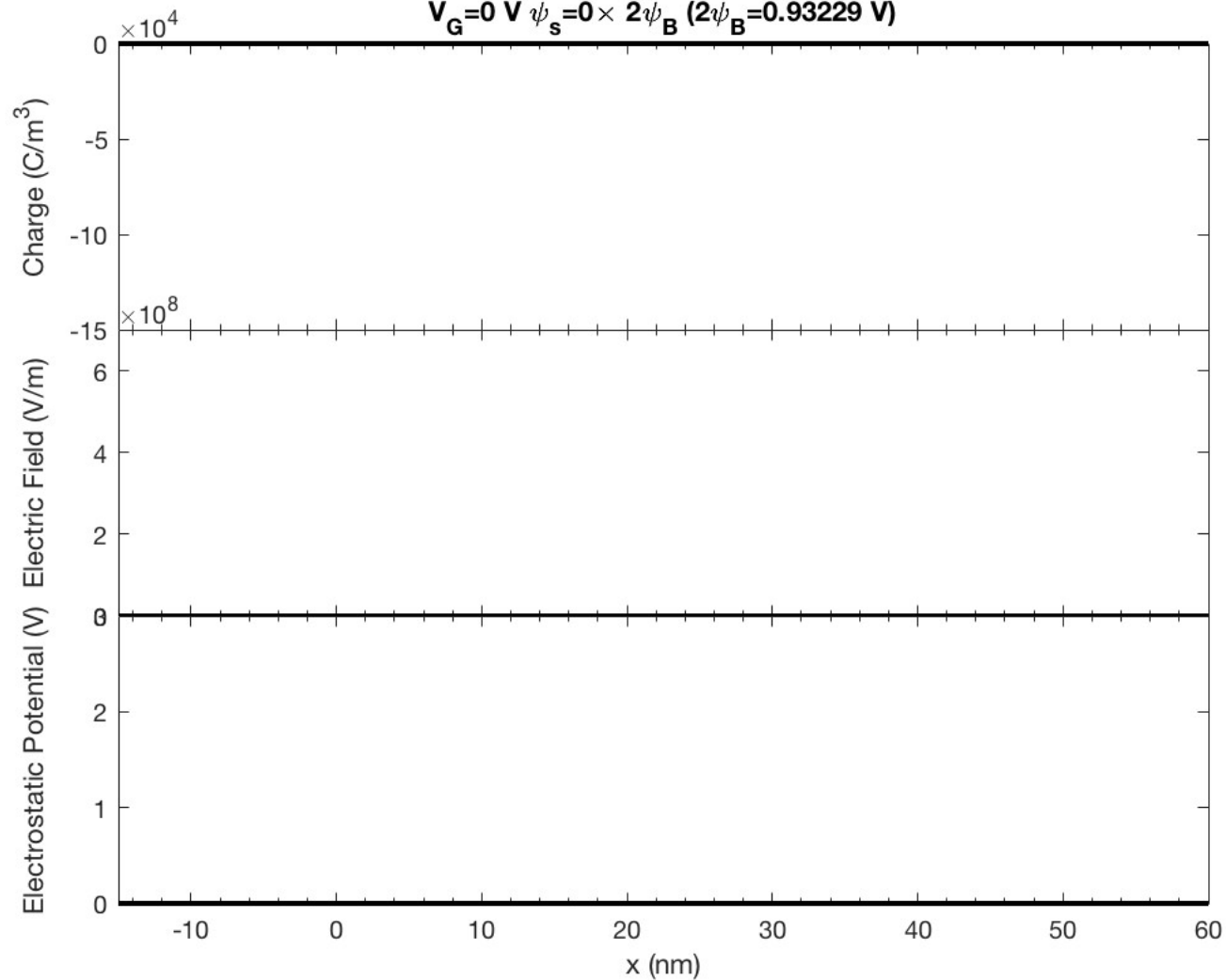




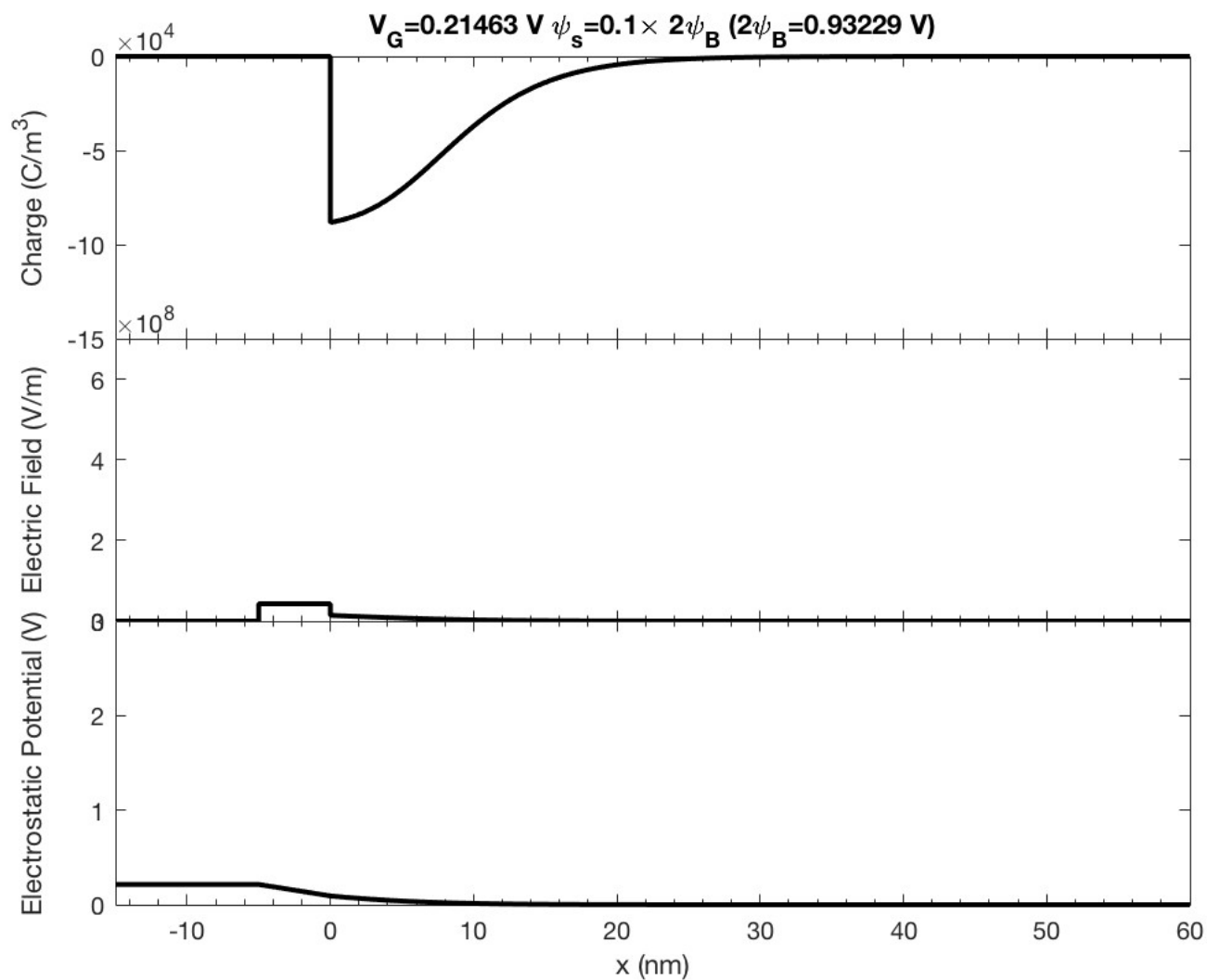
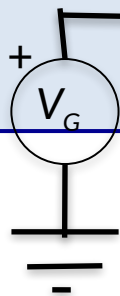
metal ox

p-semi

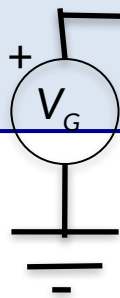
$$V_G = 0 \text{ V } \psi_s = 0 \times 2\psi_B \text{ (} 2\psi_B = 0.93229 \text{ V)}$$



$$N_A = 1\text{e}24 \text{ /m}^3$$

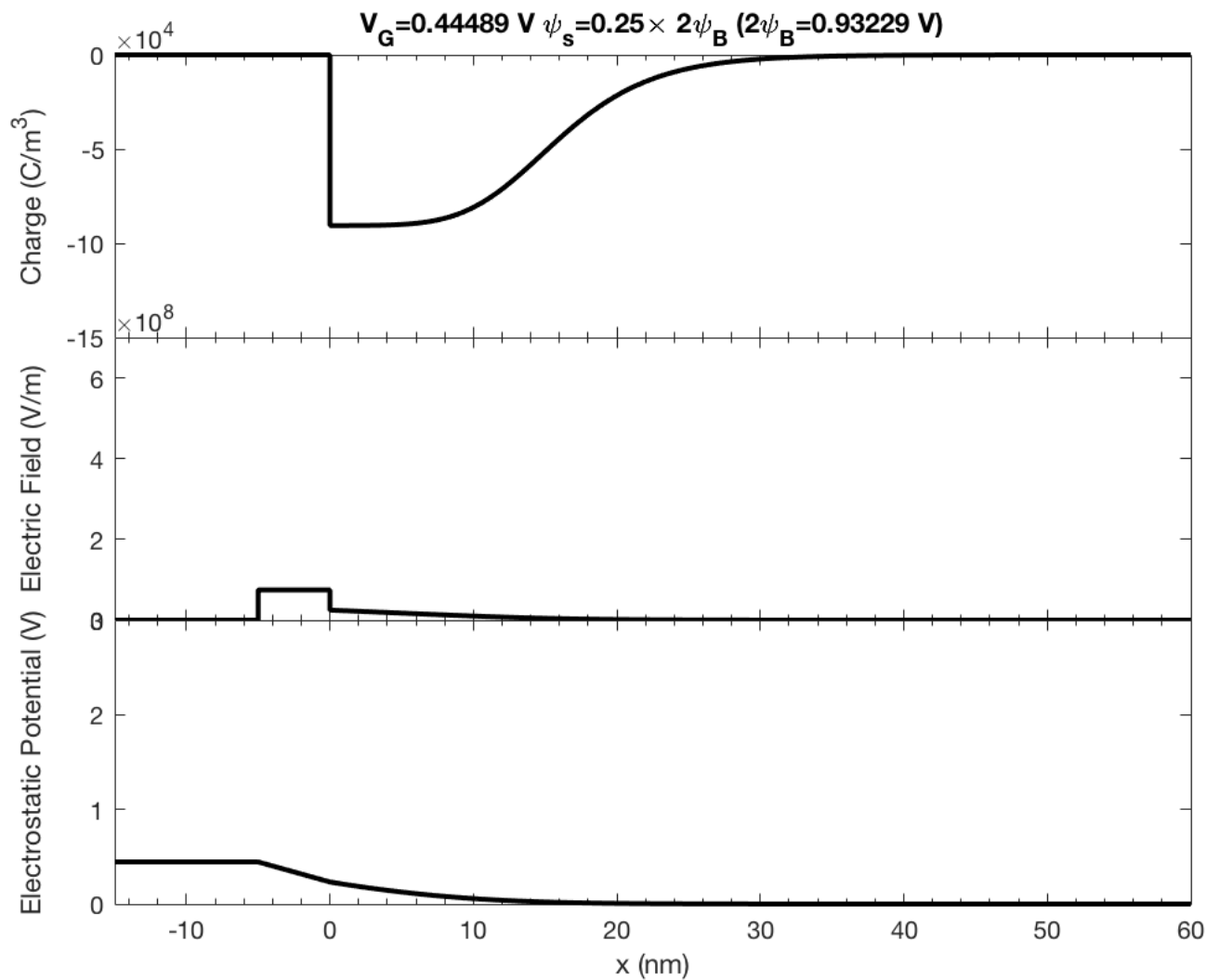


$$N_A = 1 \times 10^{24} / \text{m}^3$$

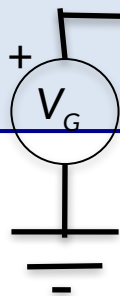


metal ox

p-semi

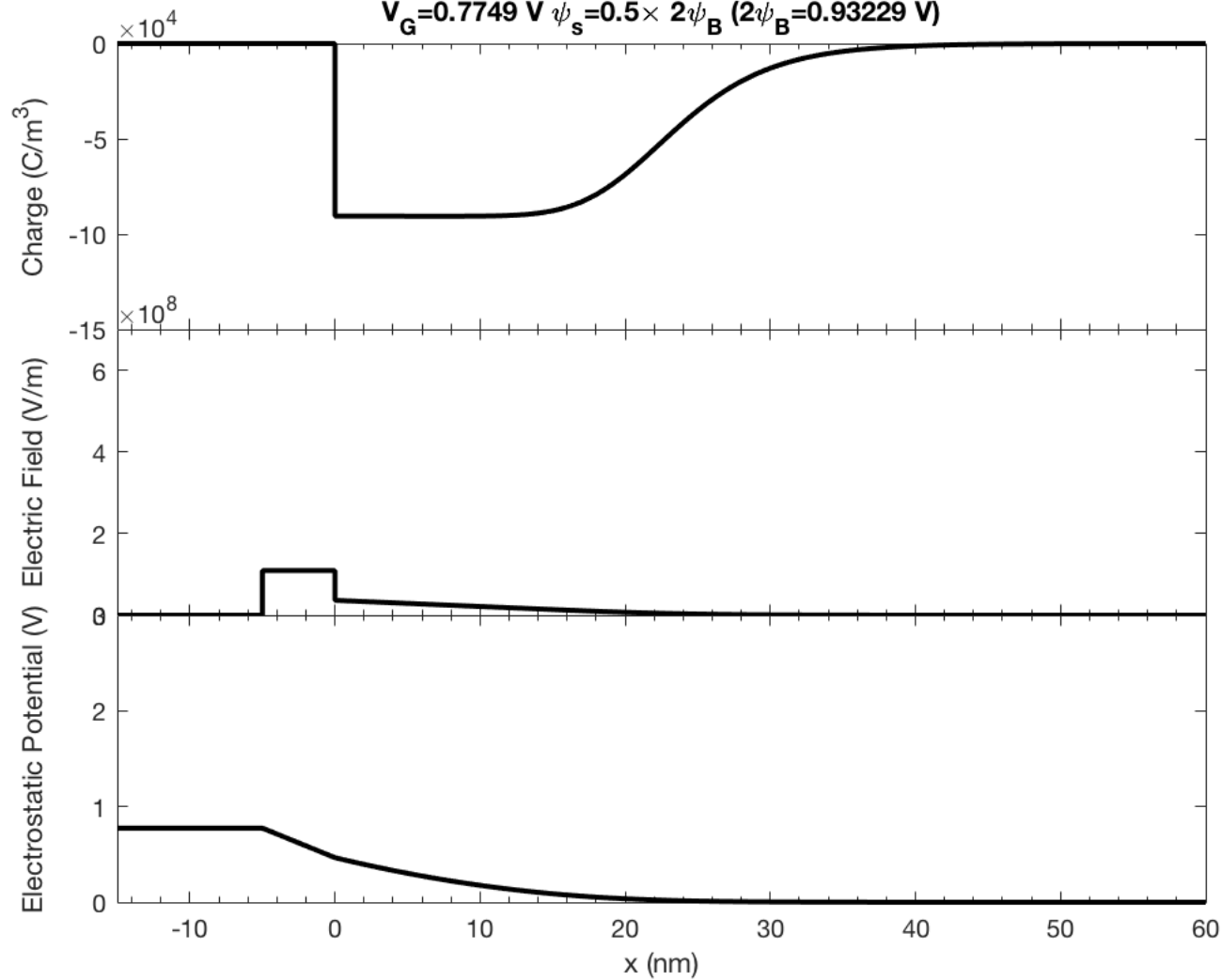


$$N_A = 1e24 / \text{m}^3$$

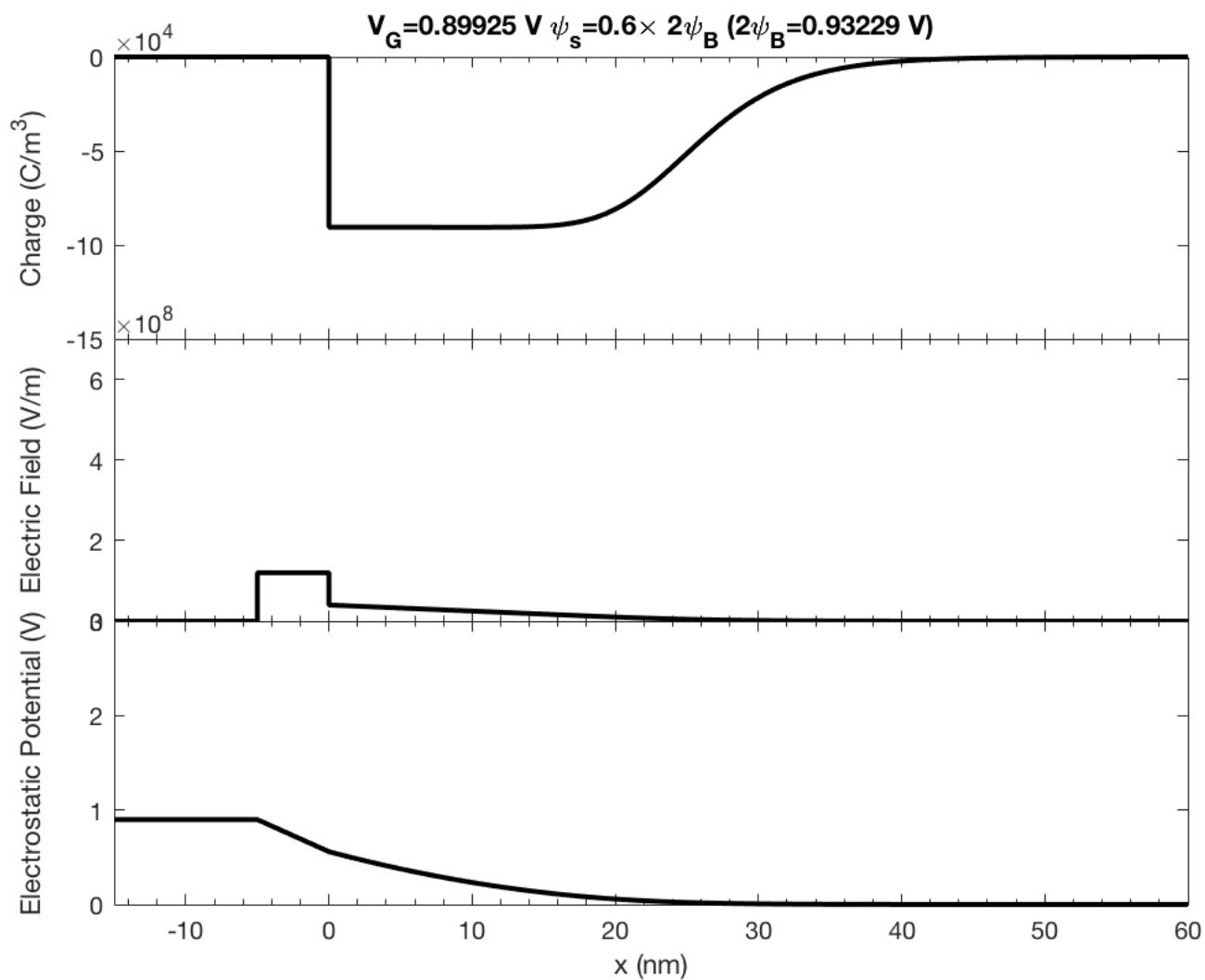
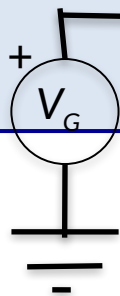


metal ox p-semi

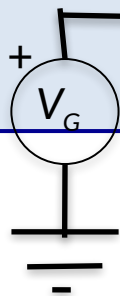
$$V_G = 0.7749 \text{ V } \psi_s = 0.5 \times 2\psi_B \text{ (} 2\psi_B = 0.93229 \text{ V)}$$



$$N_A = 1e24 / \text{m}^3$$

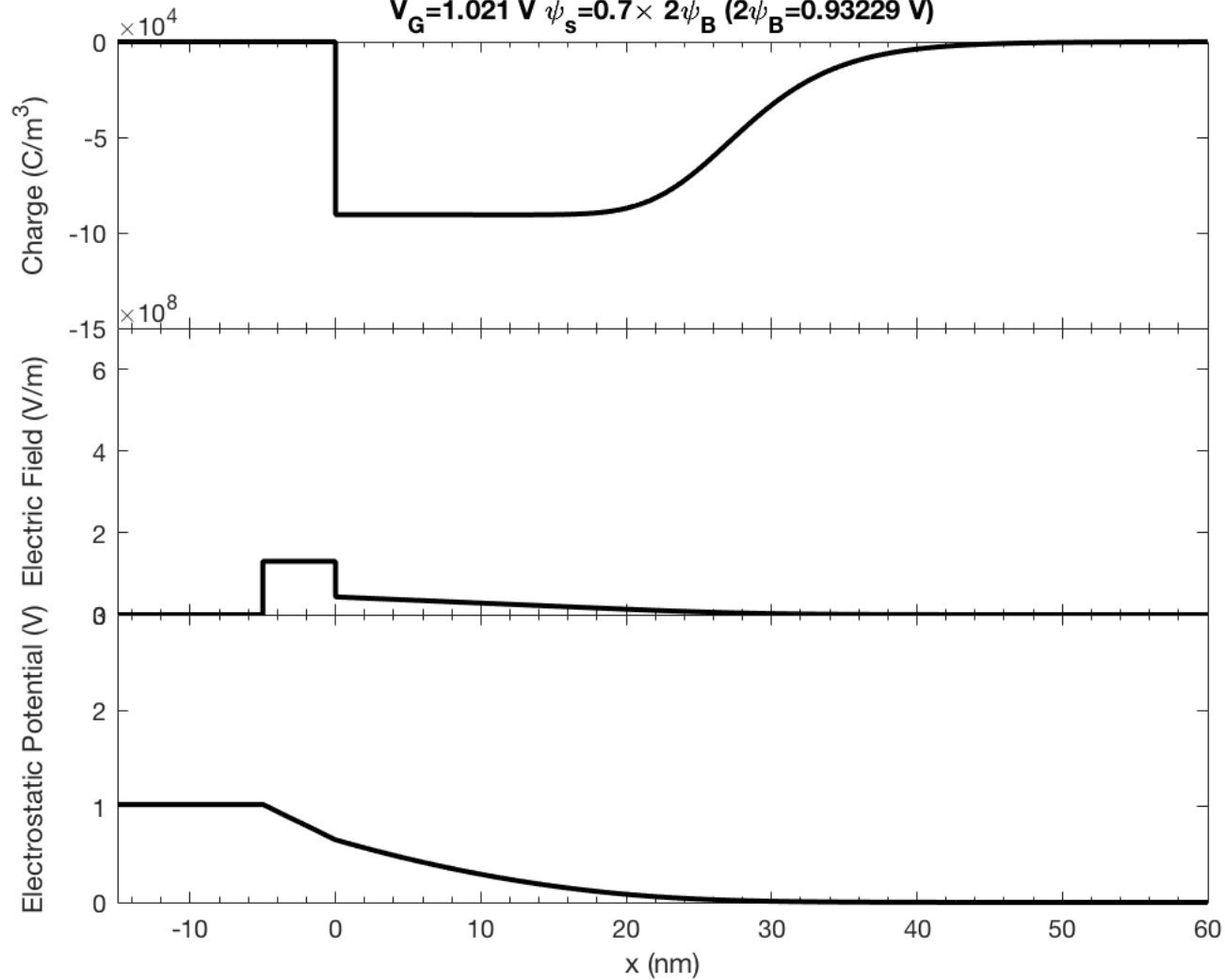


$$N_A = 1\text{e}24 / \text{m}^3$$

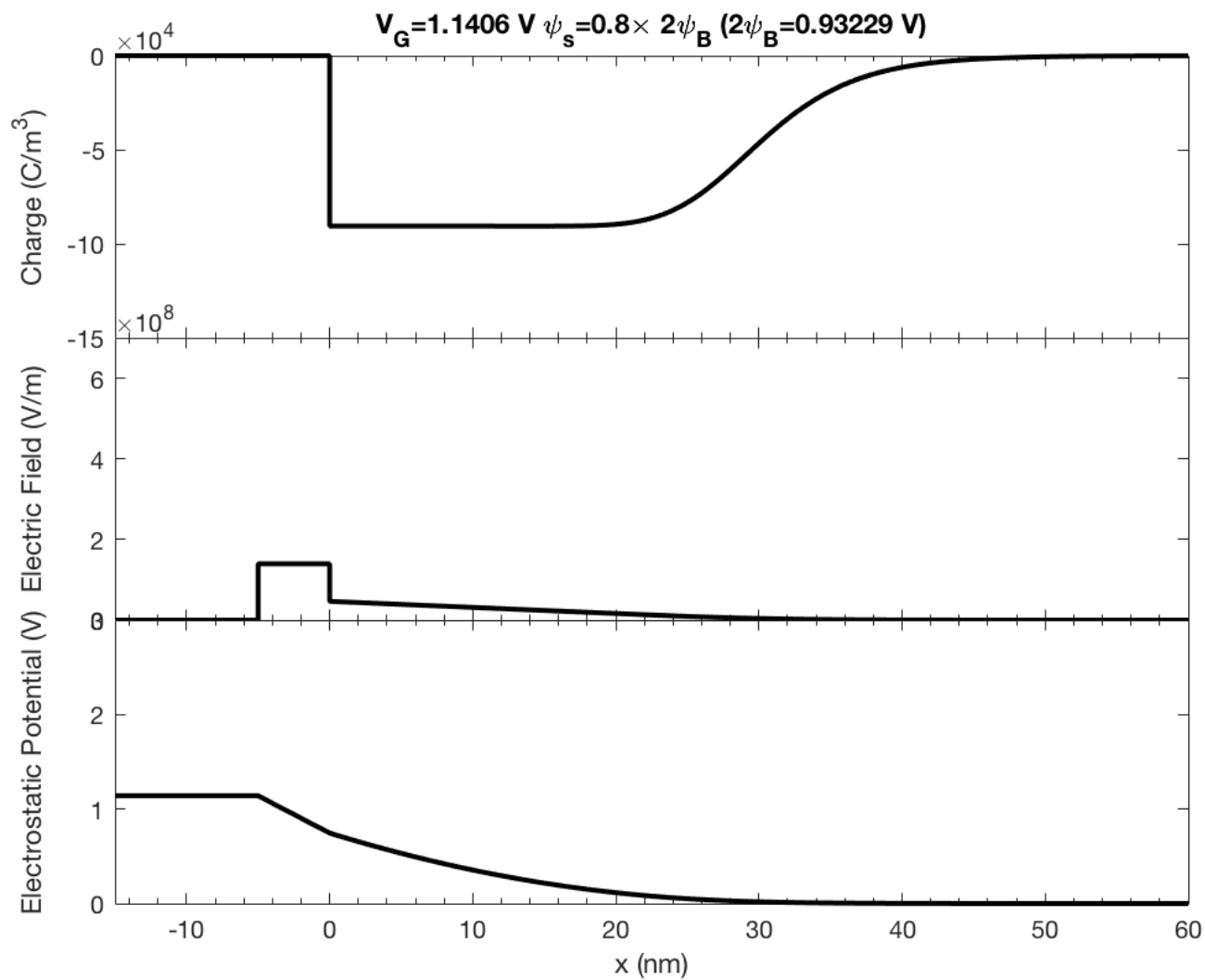
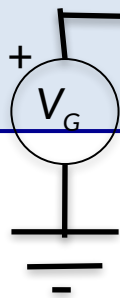


metal ox p-semi

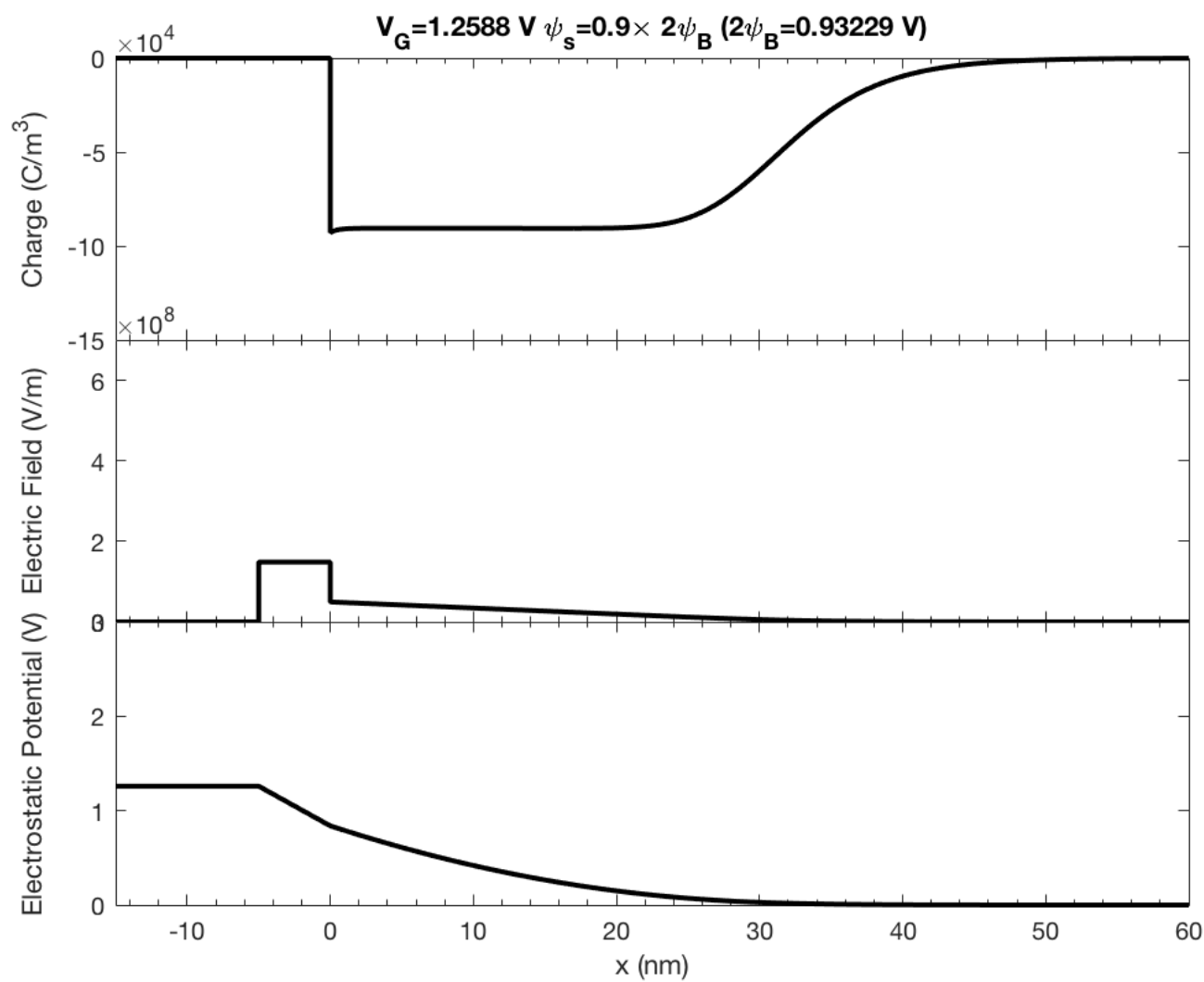
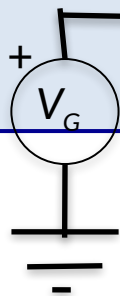
$$V_G = 1.021 \text{ V } \psi_s = 0.7 \times 2\psi_B \text{ (} 2\psi_B = 0.93229 \text{ V)}$$



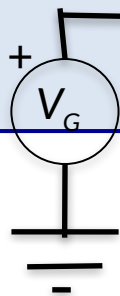
$$N_A = 1 \times 10^{24} \text{ /m}^3$$



$$N_A = 1 \times 10^{24} / \text{m}^3$$

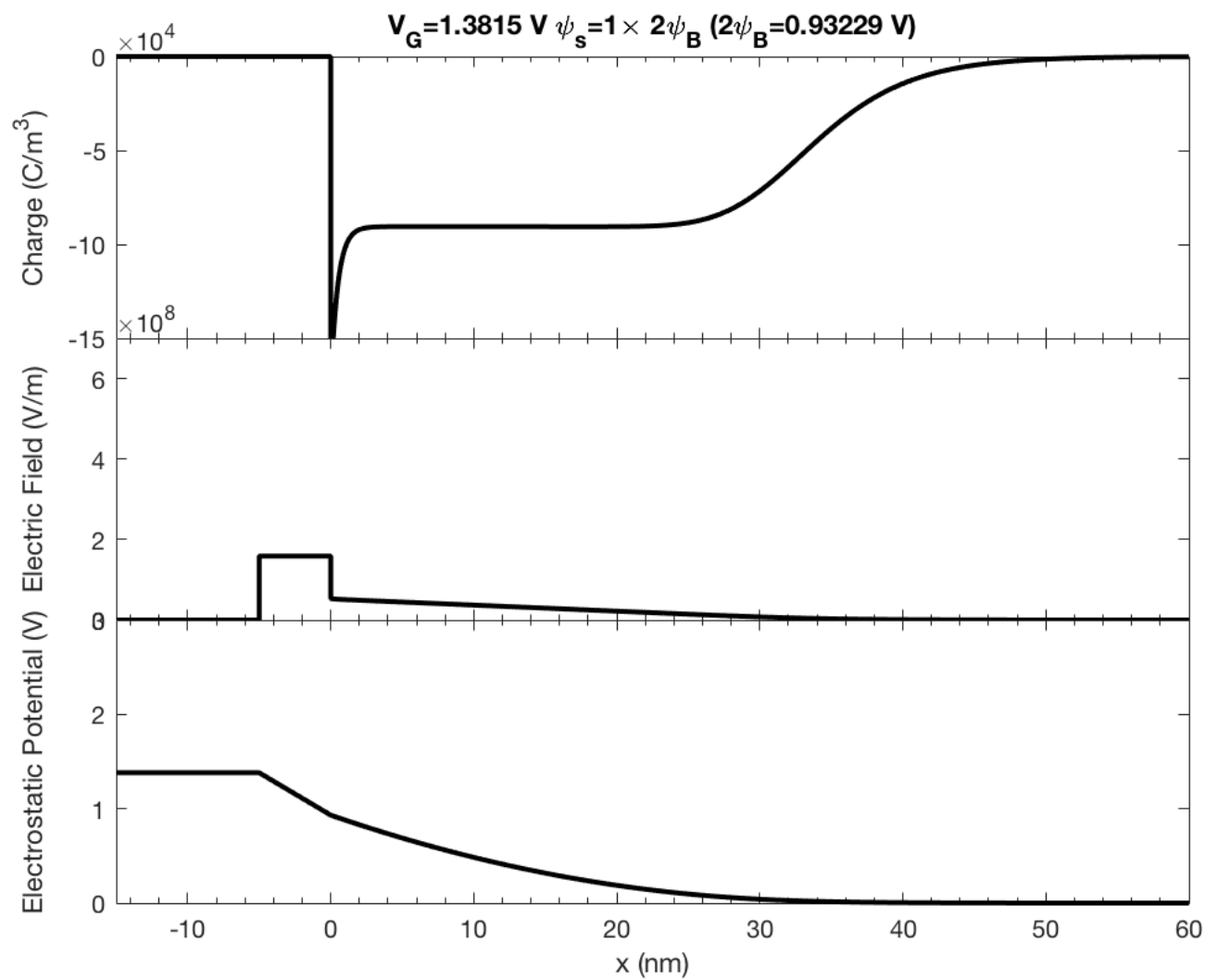


$$N_A = 1 \times 10^{24} / \text{m}^3$$

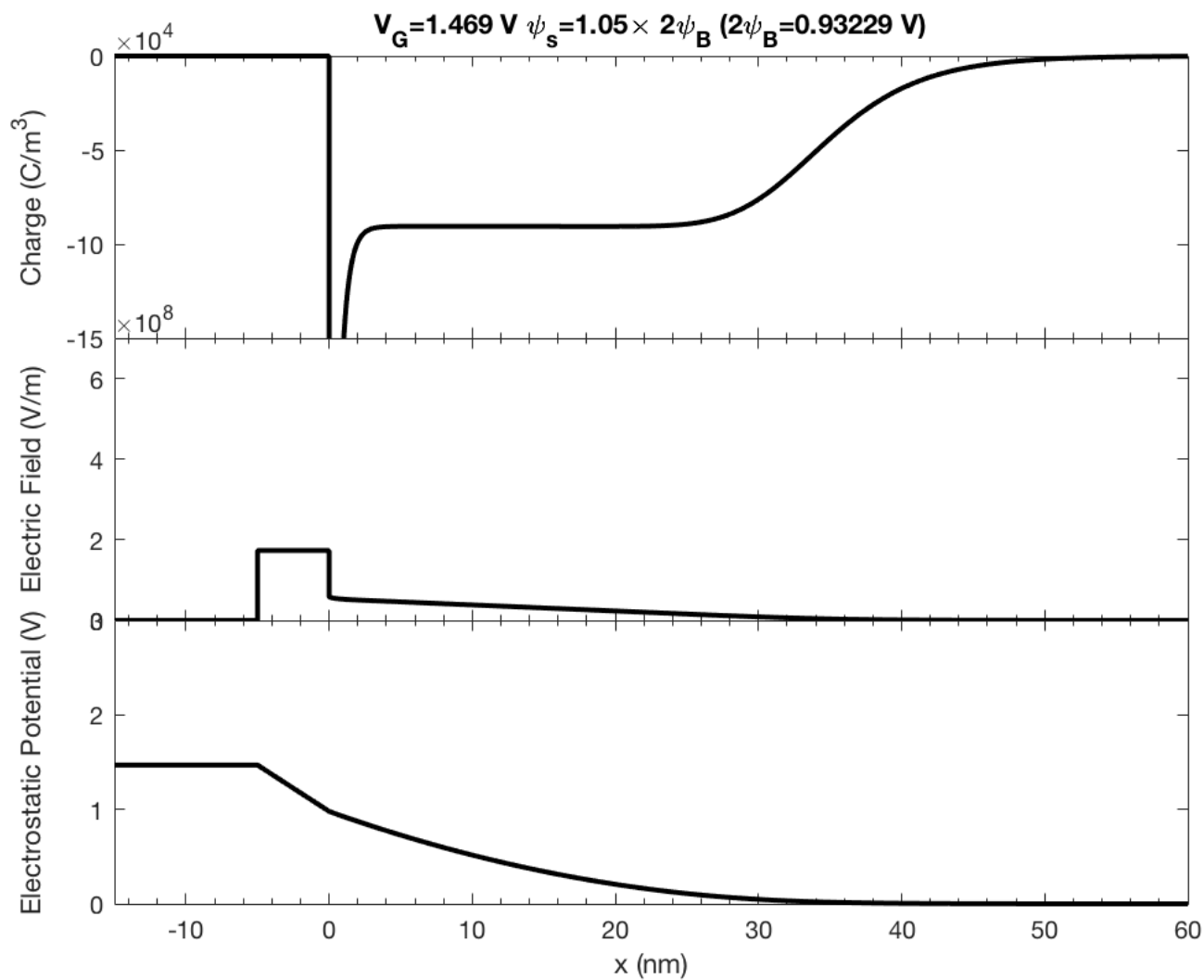
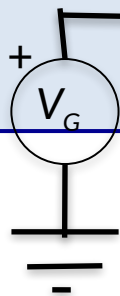


metal ox

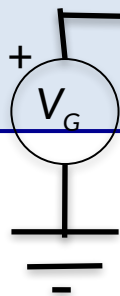
p-semi



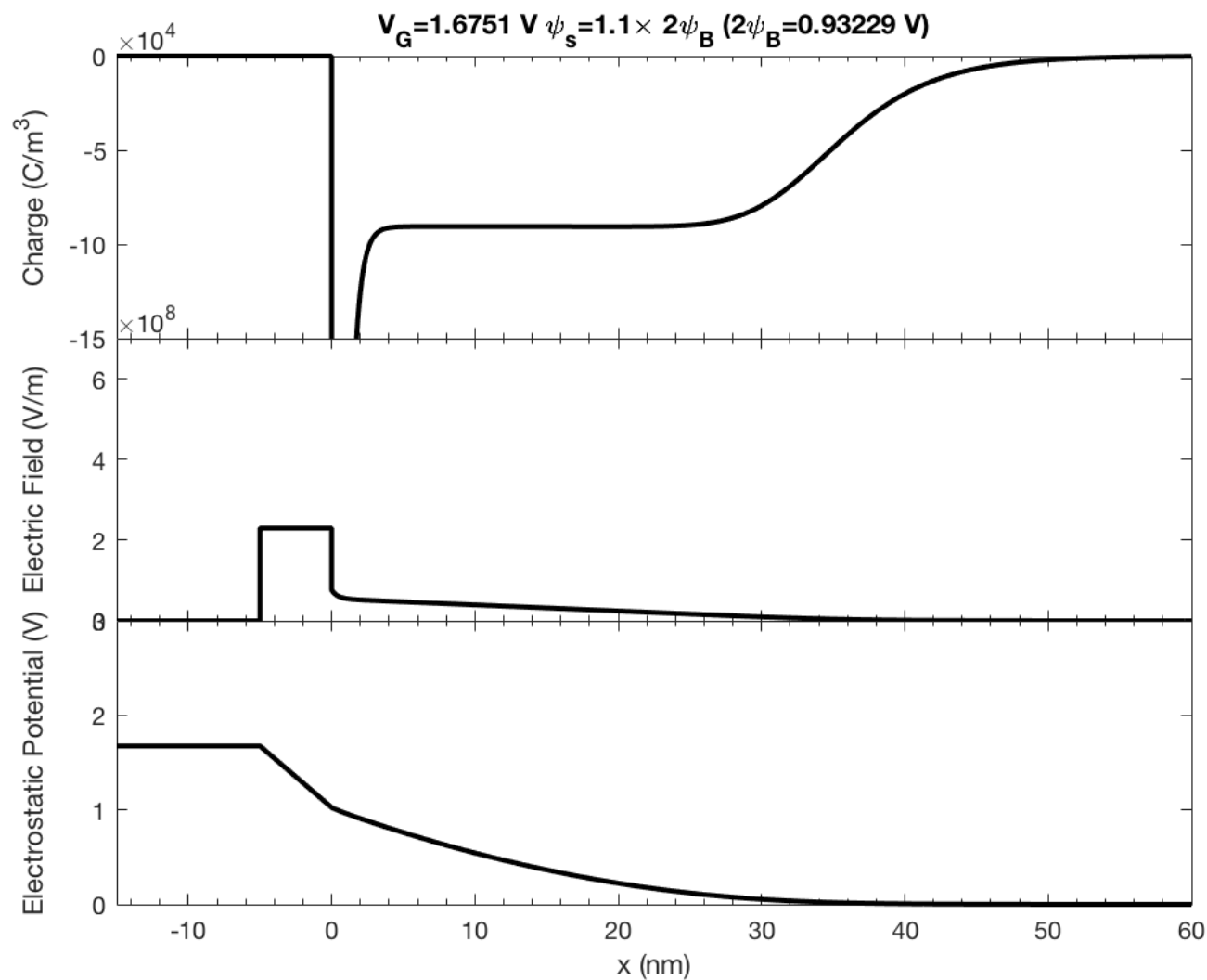
$$N_A = 1e24 / \text{m}^3$$



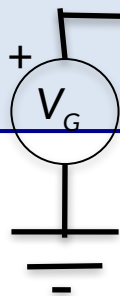
$$N_A = 1 \times 10^{24} / \text{m}^3$$



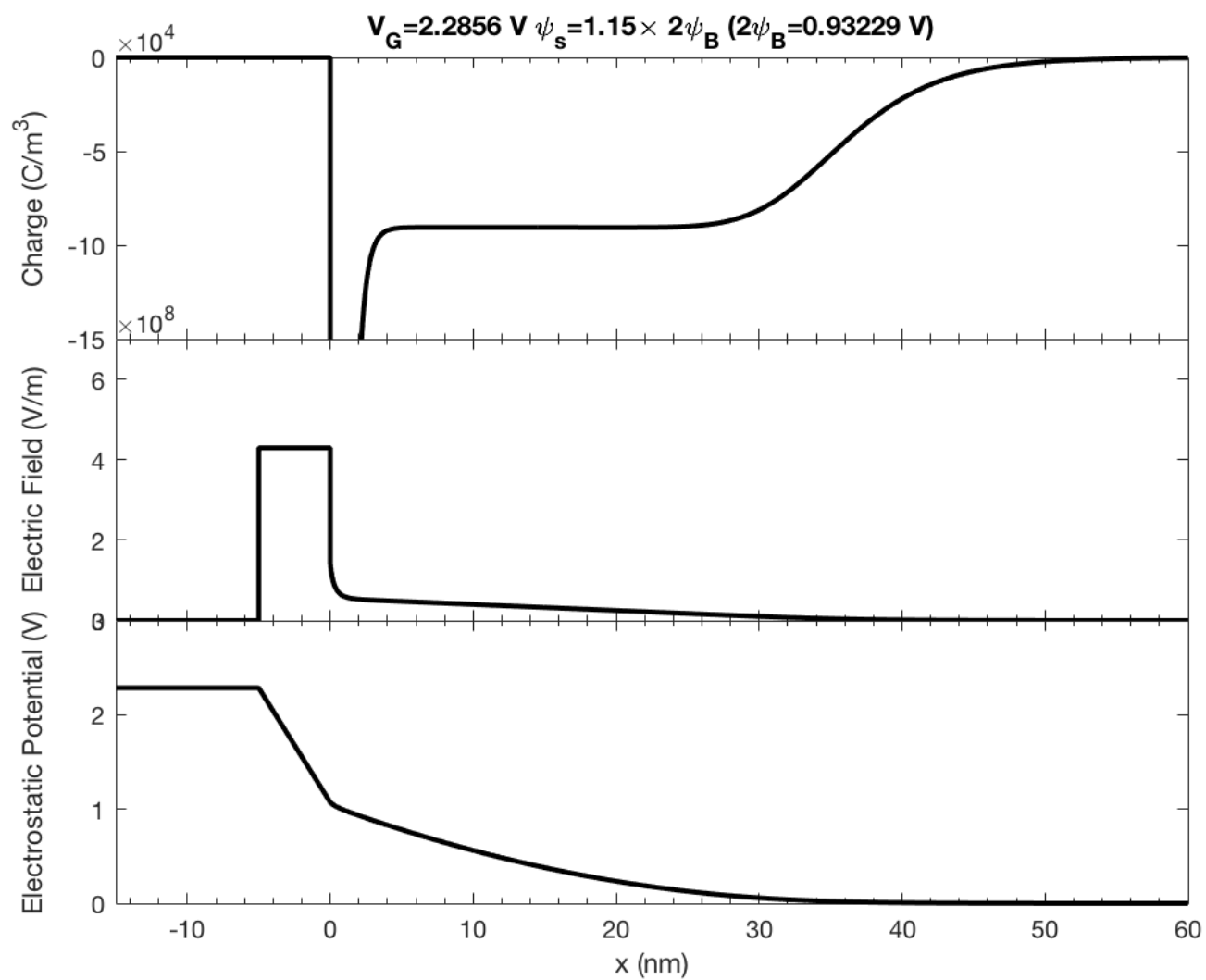
metal ox p-semi



$$N_A = 1e24 / \text{m}^3$$

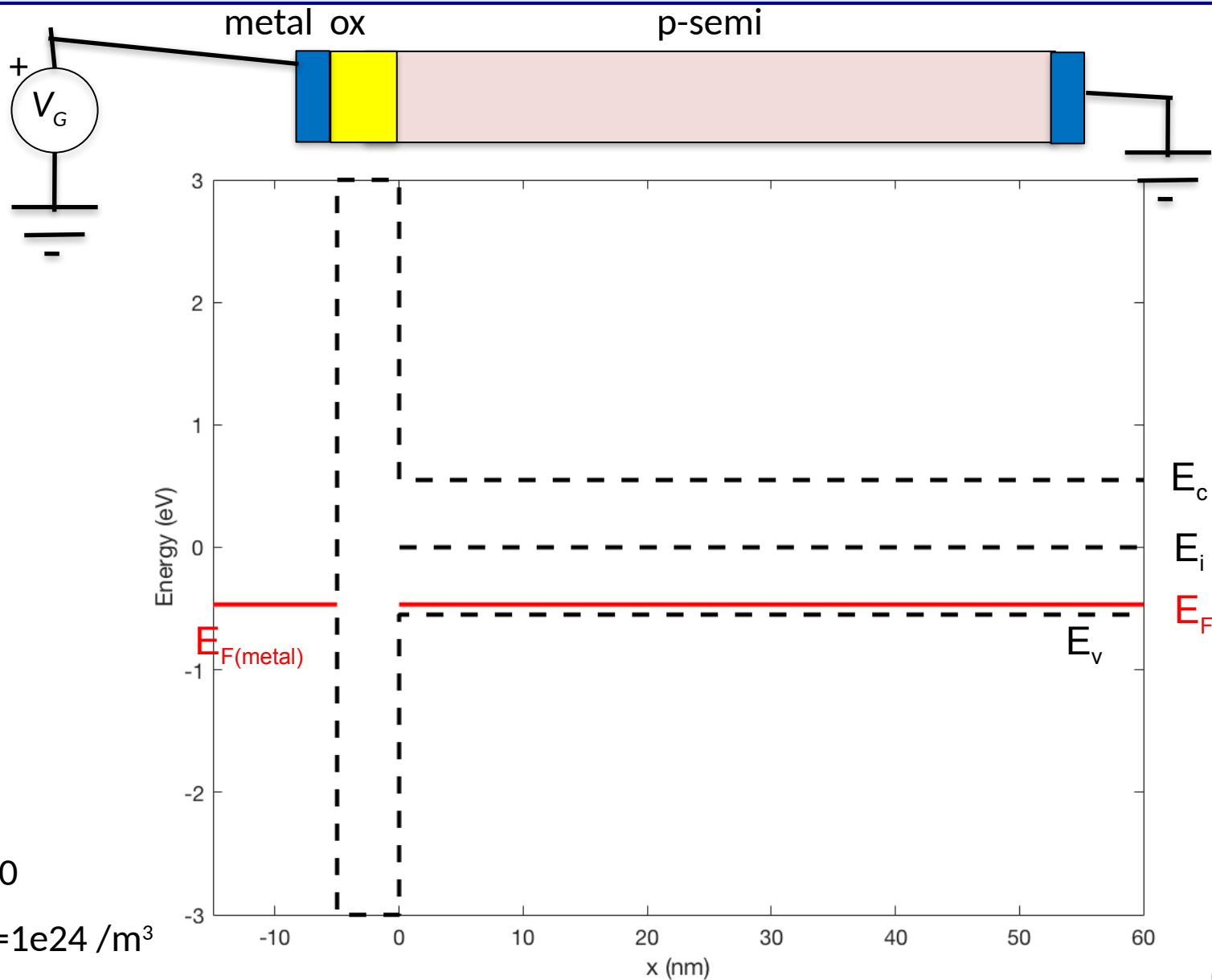


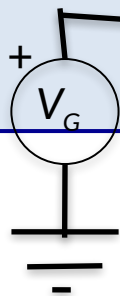
metal ox p-semi



$$N_A = 1e24 / \text{m}^3$$

Band Diagram of MOS Capacitors

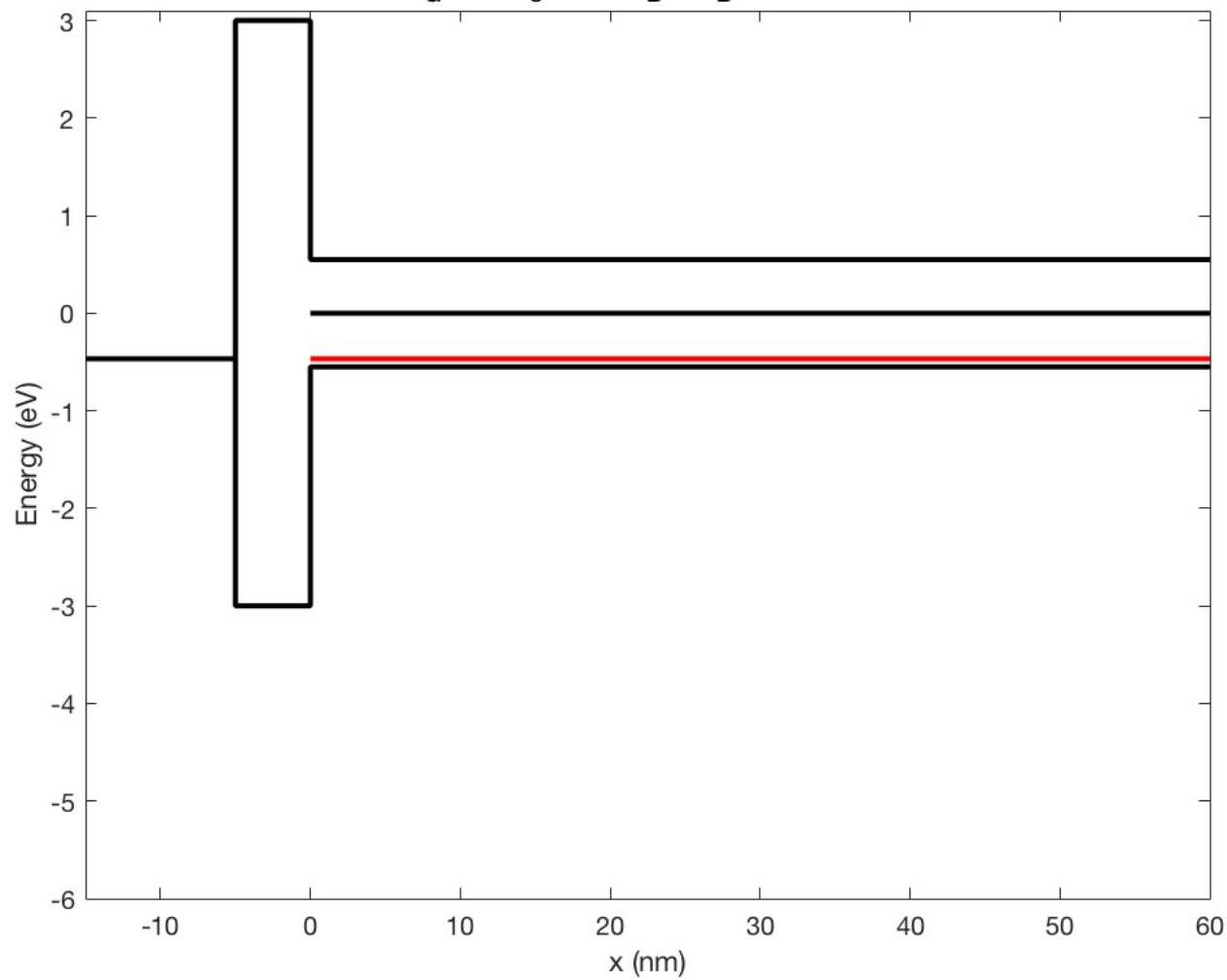




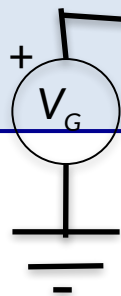
metal ox

p-semi

$$V_G = 0 \text{ V } \psi_s = 0 \times 2\psi_B \text{ (} 2\psi_B = 0.93229 \text{ V)}$$



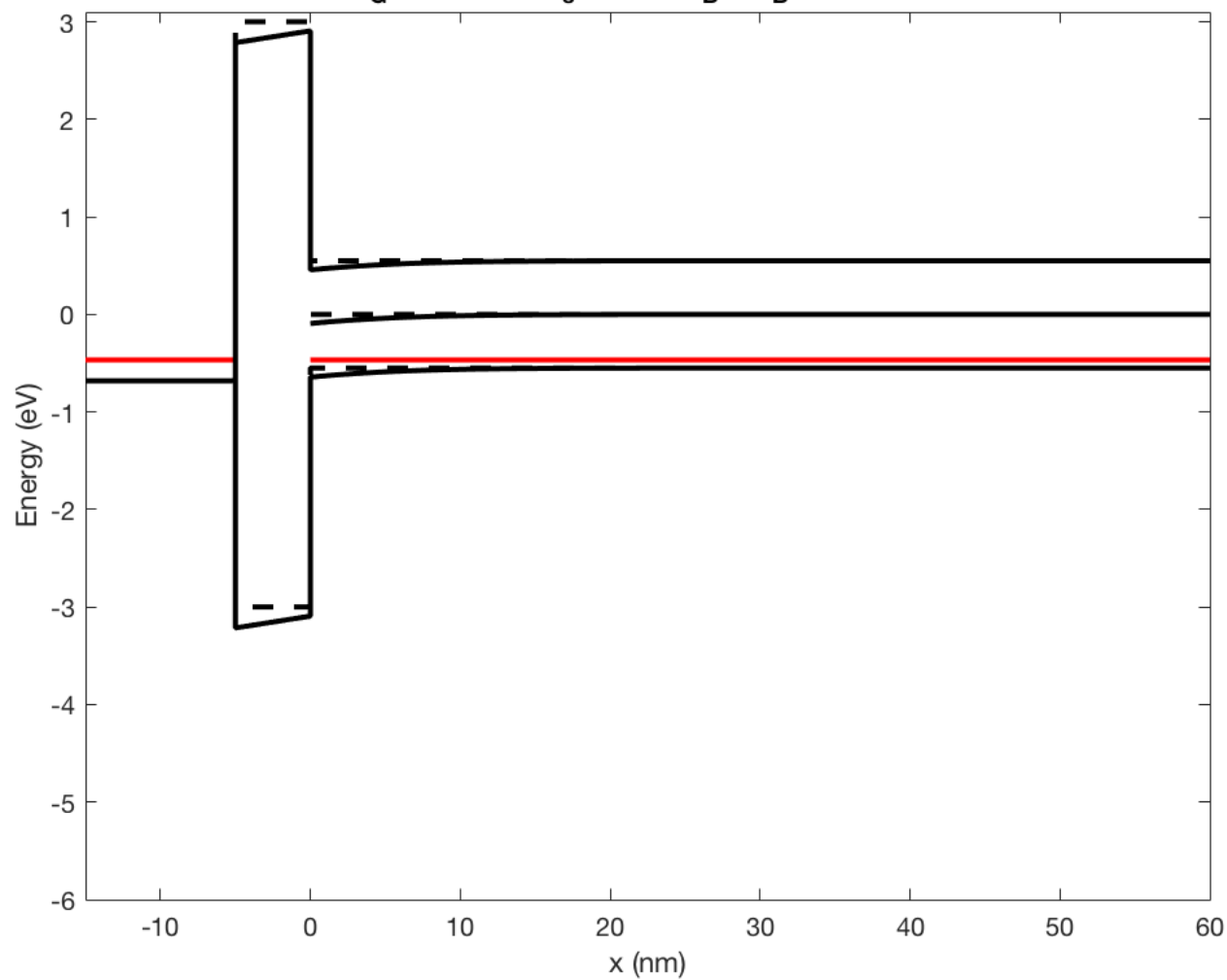
$$N_A = 1e24 / \text{m}^3$$



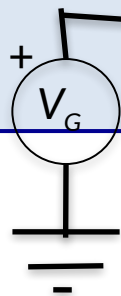
metal ox

p-semi

$$V_G = 0.21463 \text{ V } \psi_s = 0.1 \times 2\psi_B \text{ (} 2\psi_B = 0.93229 \text{ V)}$$



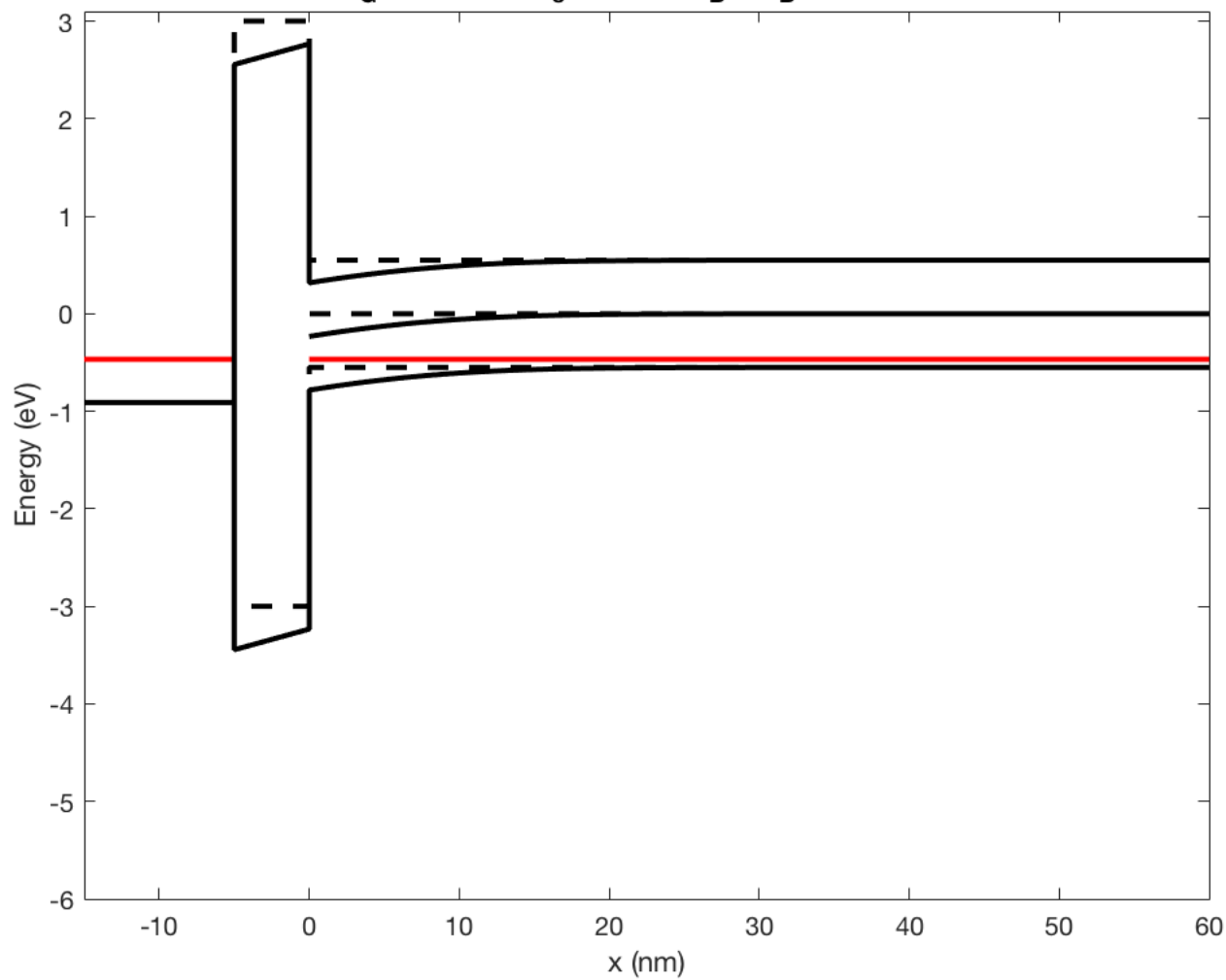
$$N_A = 1e24 / m^3$$



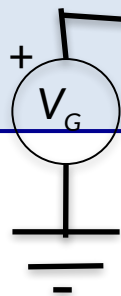
metal ox

p-semi

$$V_G = 0.44489 \text{ V} \quad \psi_s = 0.25 \times 2\psi_B \quad (2\psi_B = 0.93229 \text{ V})$$



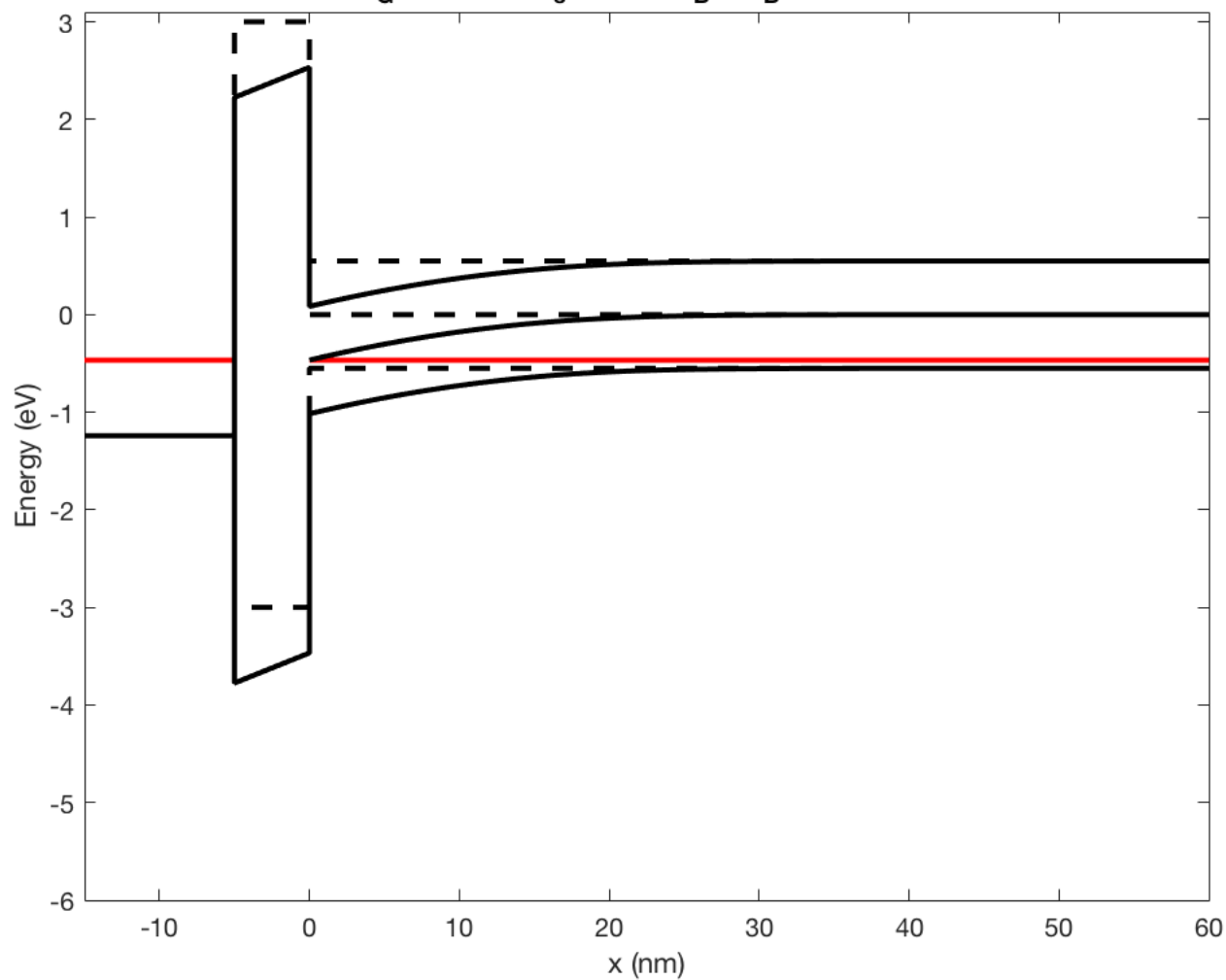
$$N_A = 1e24 / \text{m}^3$$



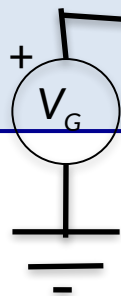
metal ox

p-semi

$$V_G = 0.7749 \text{ V } \psi_s = 0.5 \times 2\psi_B \text{ (} 2\psi_B = 0.93229 \text{ V)}$$



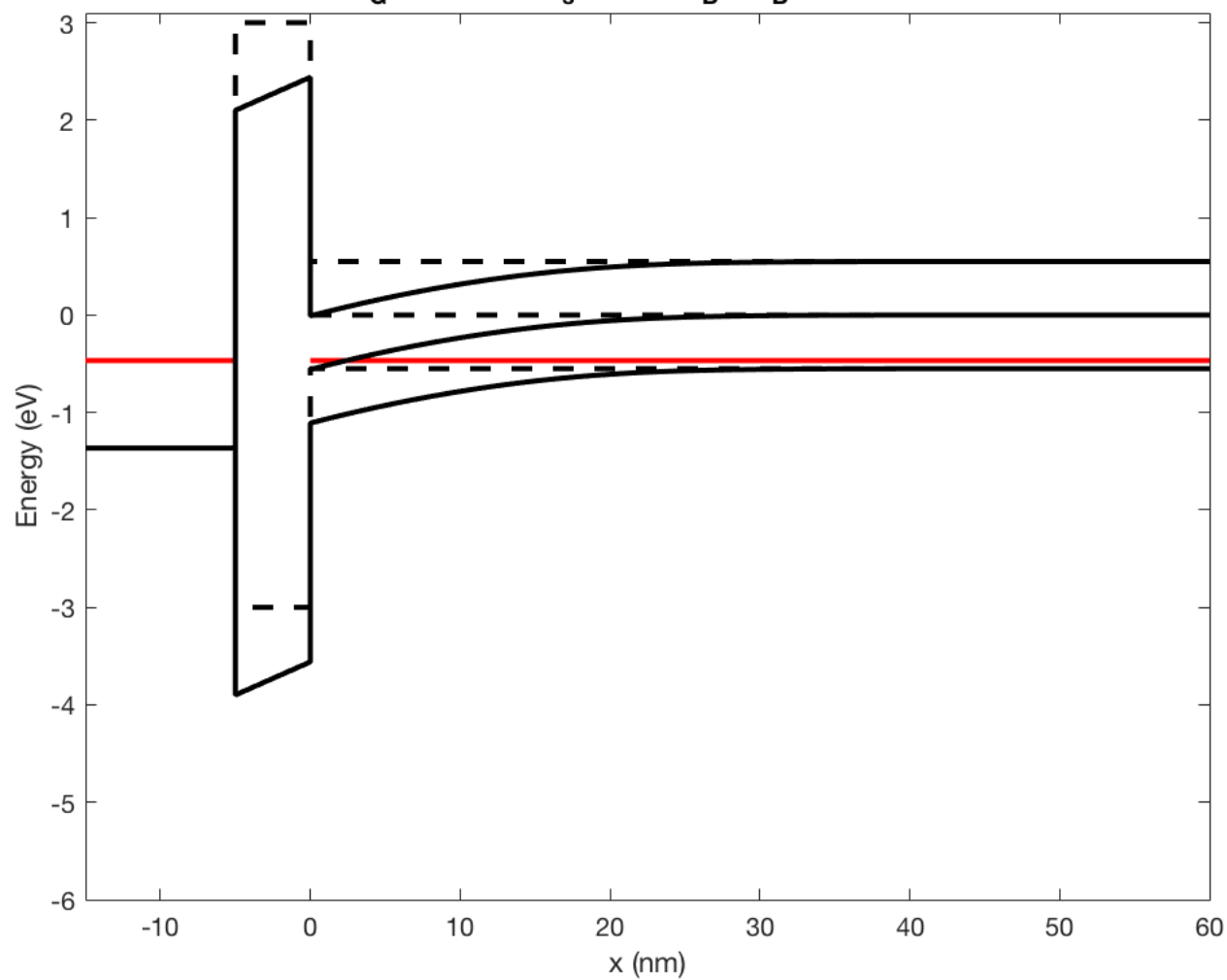
$$N_A = 1e24 / \text{m}^3$$



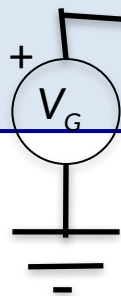
metal ox

p-semi

$$V_G = 0.89925 \text{ V } \psi_s = 0.6 \times 2\psi_B \text{ (} 2\psi_B = 0.93229 \text{ V)}$$



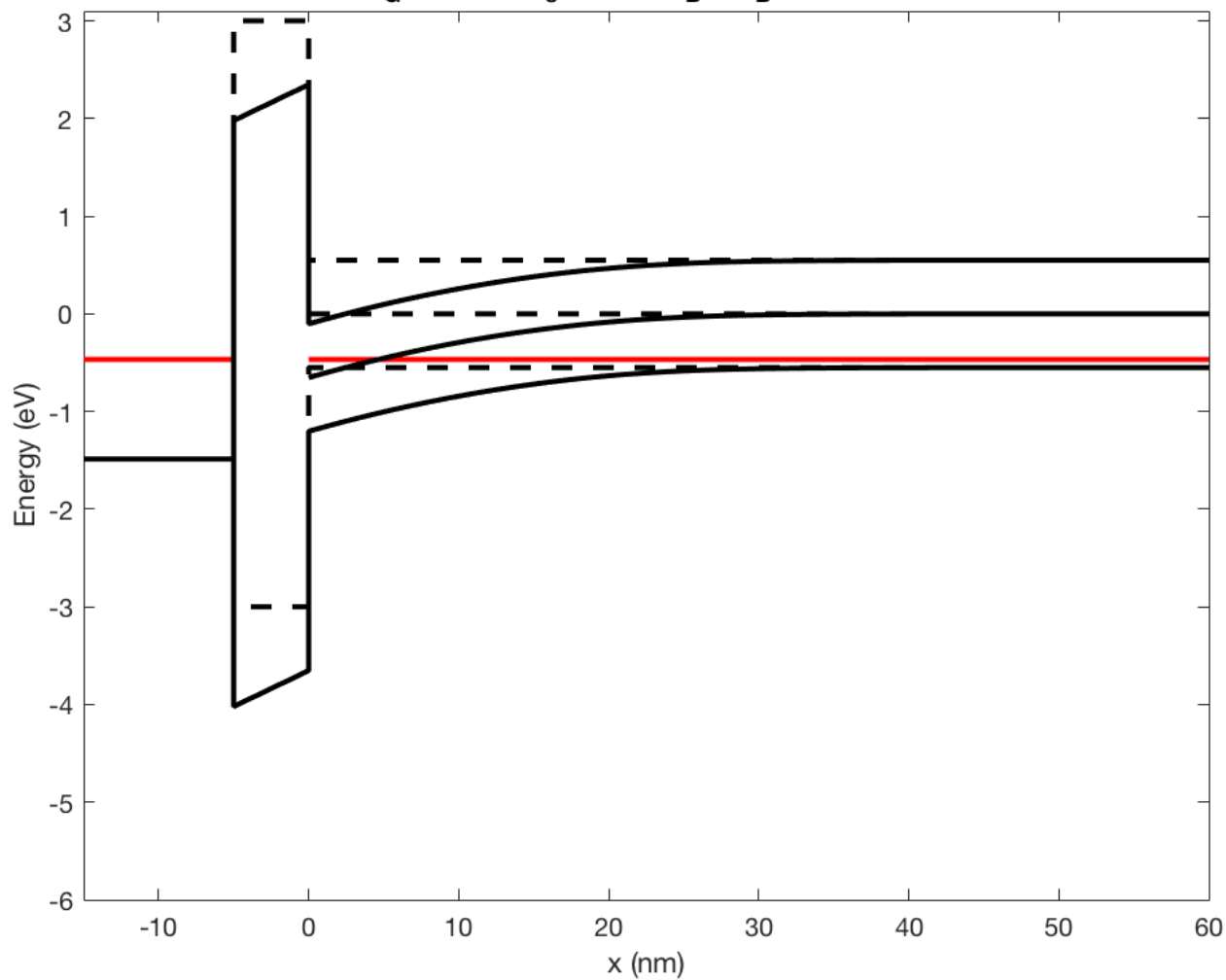
$$N_A = 1e24 / \text{m}^3$$



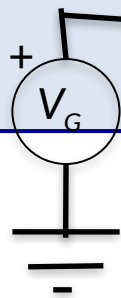
metal ox

p-semi

$$V_G = 1.021 \text{ V} \quad \psi_s = 0.7 \times 2\psi_B \quad (2\psi_B = 0.93229 \text{ V})$$



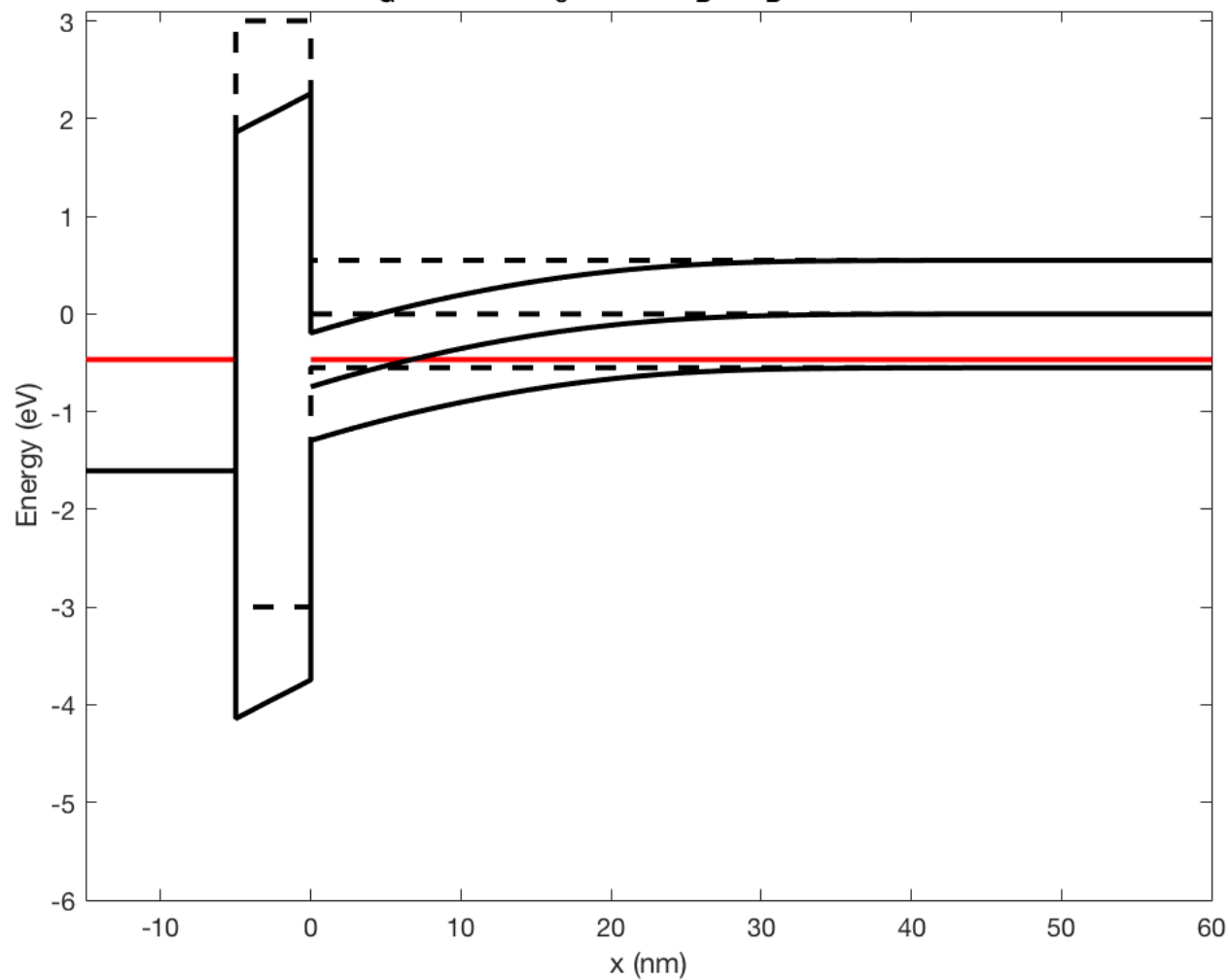
$$N_A = 1e24 /m^3$$



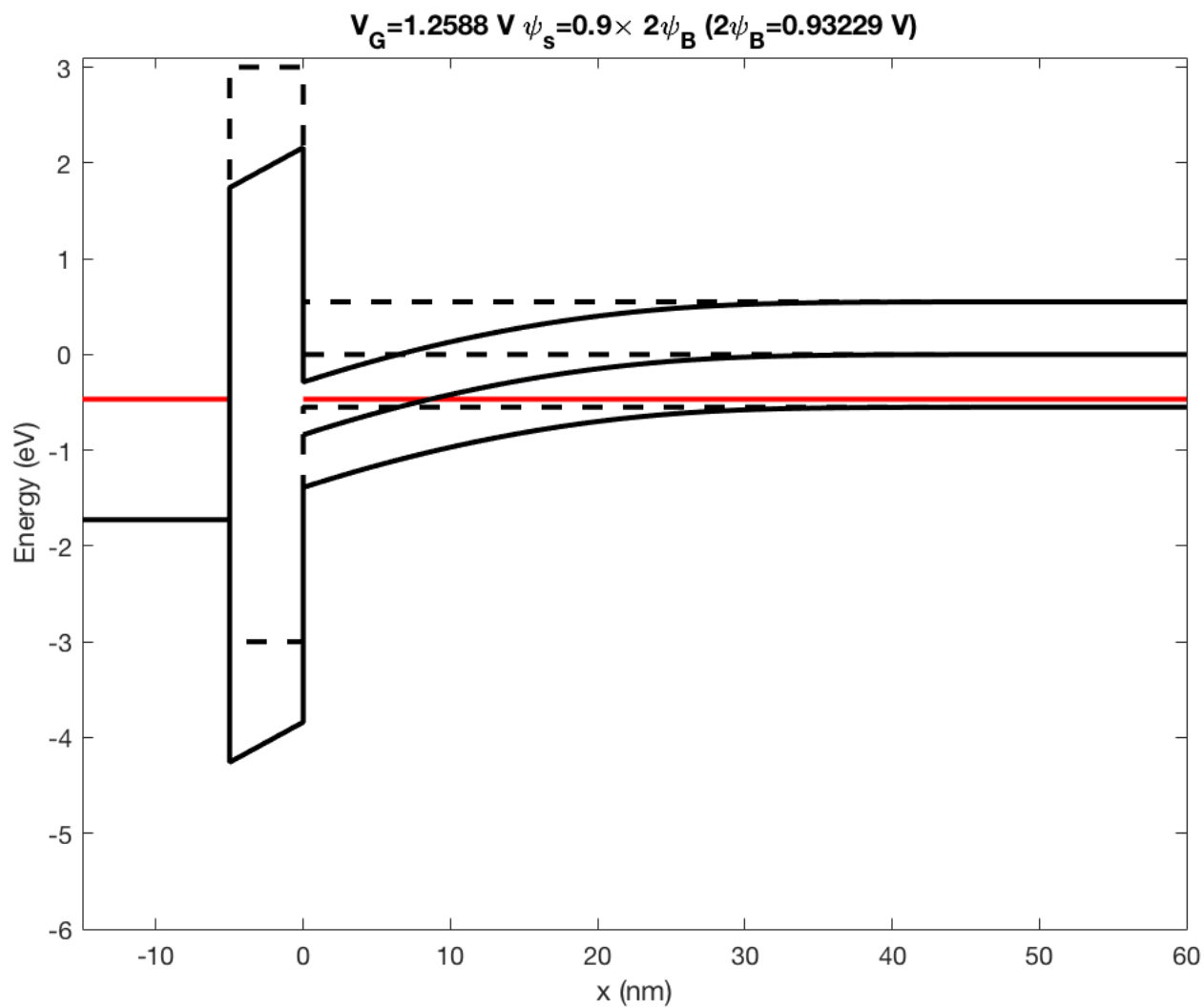
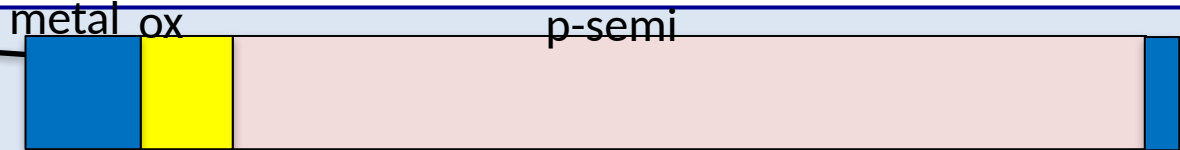
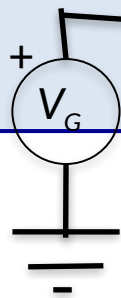
metal ox

p-semi

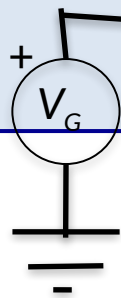
$$V_G = 1.1406 \text{ V } \psi_s = 0.8 \times 2\psi_B \text{ (} 2\psi_B = 0.93229 \text{ V)}$$



$$N_A = 1e24 / \text{m}^3$$



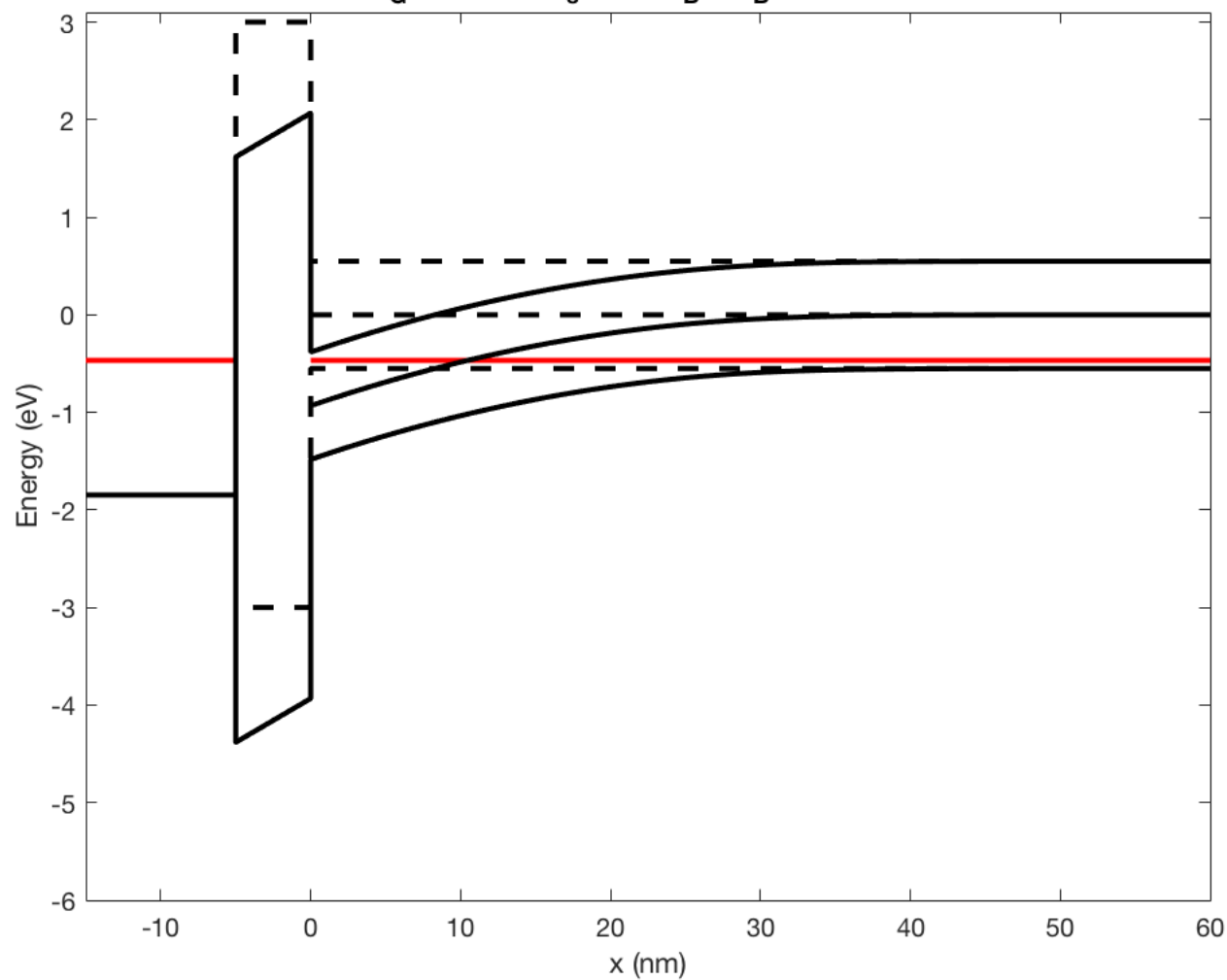
$$N_A = 1e24 / \text{m}^3$$



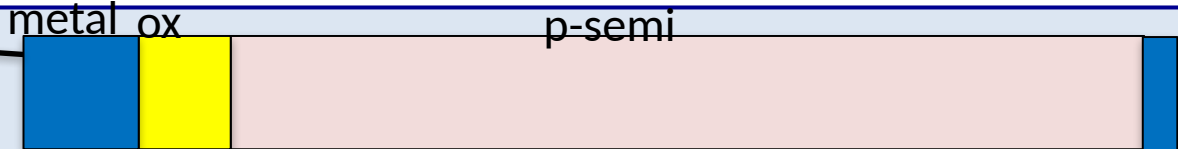
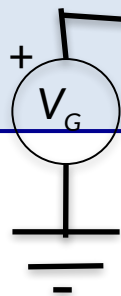
metal ox

p-semi

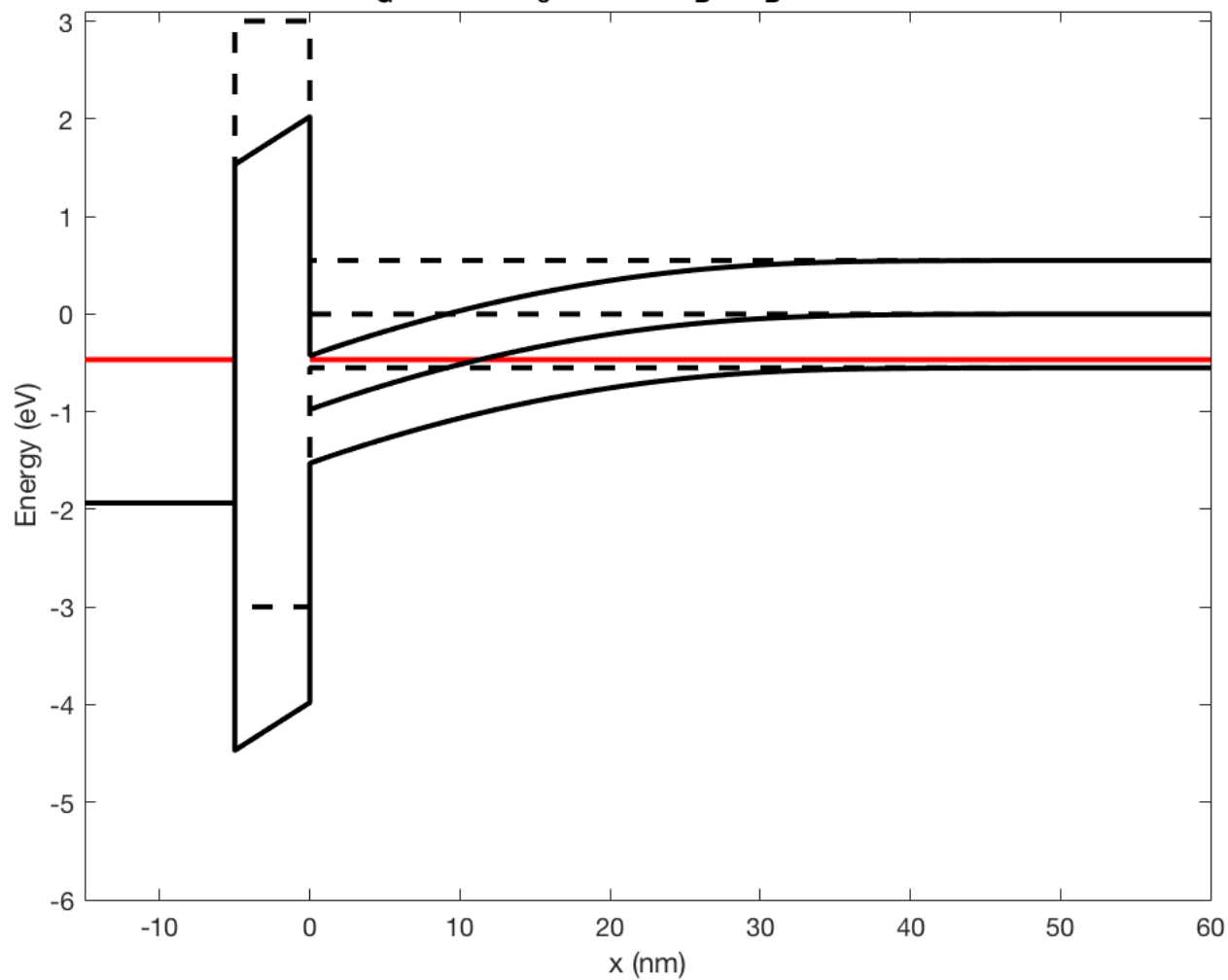
$$V_G = 1.3815 \text{ V } \psi_s = 1 \times 2\psi_B \text{ (} 2\psi_B = 0.93229 \text{ V)}$$



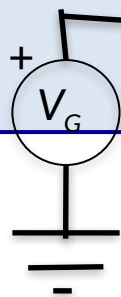
$$N_A = 1e24 / \text{m}^3$$



$$V_G = 1.469 \text{ V} \quad \psi_s = 1.05 \times 2\psi_B \quad (2\psi_B = 0.93229 \text{ V})$$

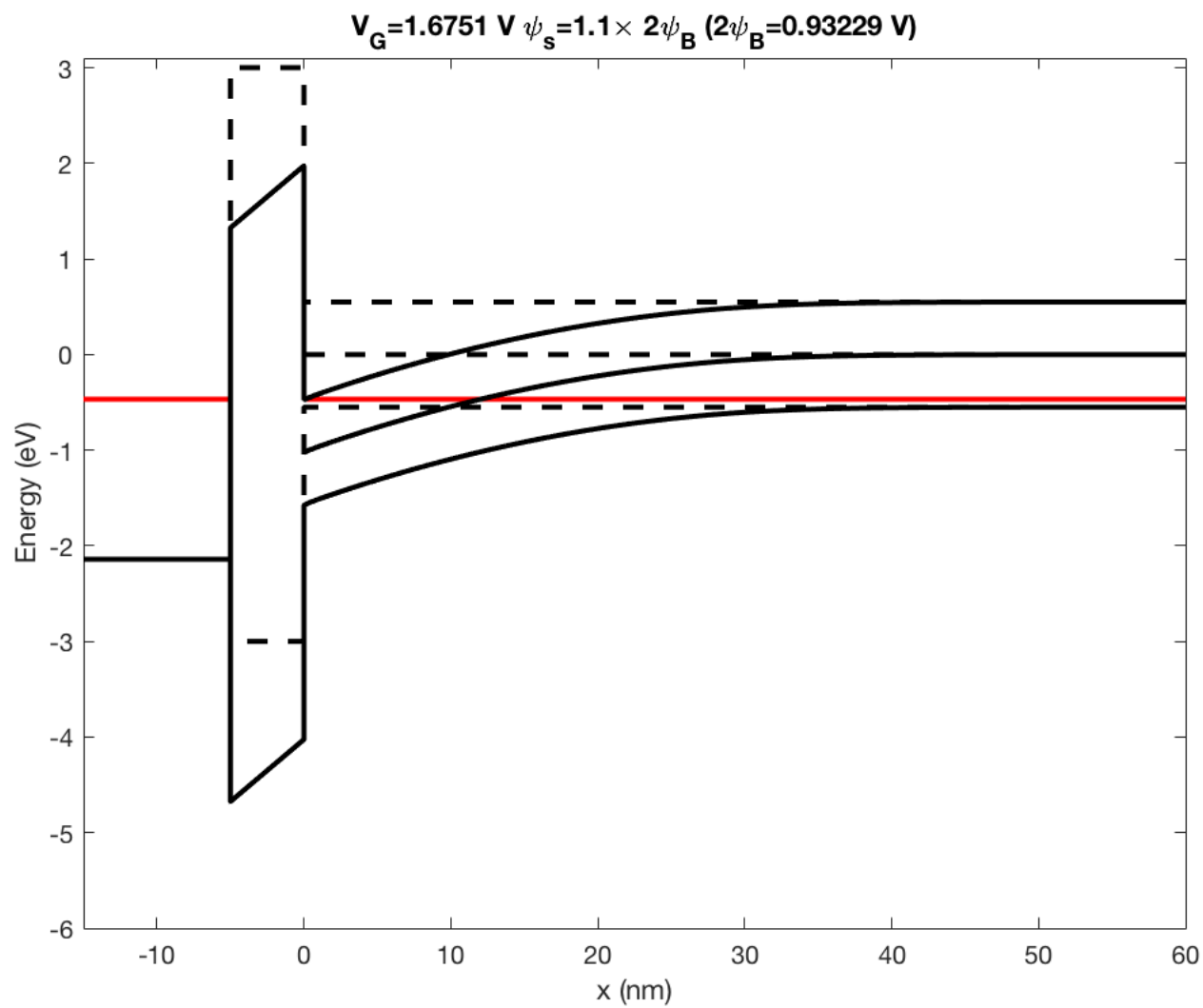


$$N_A = 1e24 / m^3$$

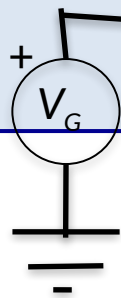


metal ox

p-semi



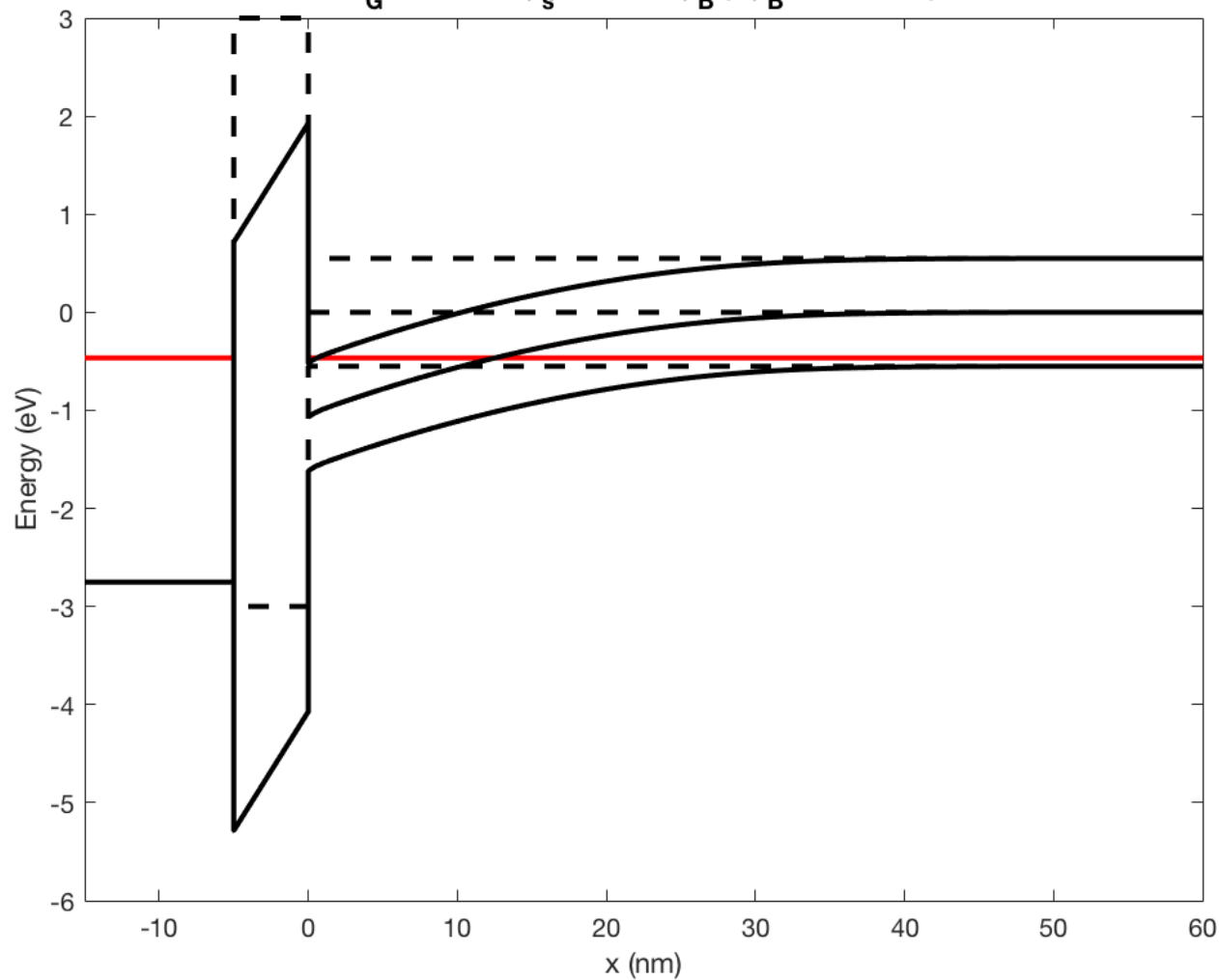
$$N_A = 1e24 / \text{m}^3$$



metal ox

p-semi

$$V_G = 2.2856 \text{ V} \quad \psi_s = 1.15 \times 2\psi_B \quad (2\psi_B = 0.93229 \text{ V})$$



$$N_A = 1e24 / \text{m}^3$$