

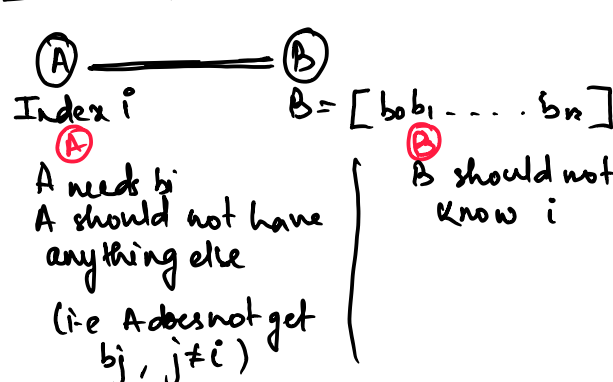
Using

- i) PPTM adversary.
- ii) Negligible Error Probability.

We achieved

- Symmetric Key Cipher Q) What can be achieved
- Data Integrity A) **Everything**
- Public Key Crypto
- Signatures

Oblivious Transfer.



**OT Protocol**

**Step 1:-** A chooses a random array

$r = [r_0, r_1, \dots, r_n]$   
 encrypts  $m_j$  ith bit with  $B$ 's PK  
 (Bit he wants to receive from  $B$ )  
 $r' = [r_0, r_1, \dots, \text{Enc}_{PK_B}(r_i), \dots, r_n]$   
 sends to B

**Step 2:-**

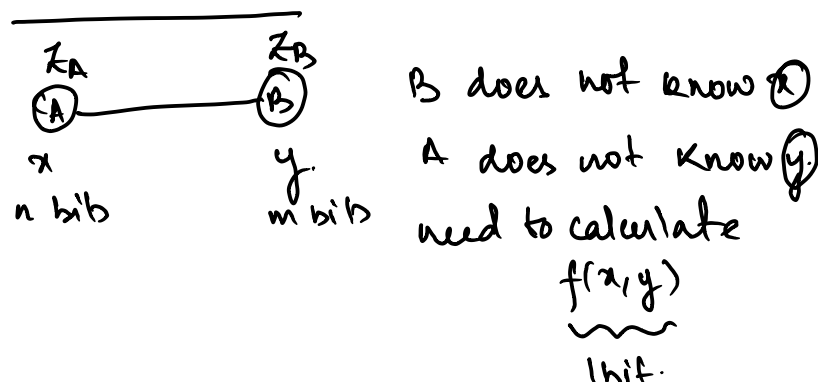
receives  $r'$   
 can't distinguish from completely random string.  
 does not know  $i$   
 Decrypts the entire string.  
 $\sigma = [\sigma_0, \sigma_1, \dots, \sigma_n]$   
 Note:  $\sigma_i = r_i$   
 And sends  $z$   
 $z = [\sigma_0 \oplus b_0, \sigma_1 \oplus b_1, \dots, \sigma_n \oplus b_n]$

**Step 3:-**

A receives  $z$  and retrieves  $b_i$  as  
 $b_i = z[i] \oplus \sigma_i$   
 $= \sigma_i \oplus b_i \oplus \sigma_i$   
 $= b_i //$

This is a **semi-honest** scheme, you rely on A to delete the array  $z$  after he calculates  $b_i$

**General Scheme.**



Say there are  $z_A \in Z_A$  generated by  $f: \{0,1\}^n \times \{0,1\}^m \rightarrow \{0,1\}^k$   
 $A \& B$  such that  $(z_A \oplus z_B = f)$

**Scheme**

- Step 1:- A chooses  $z_A$  from  $\{0,1\}^n$
- Step 2:-  $\forall y$ , A calculates  $f(x, y_i)$   
 sends  $f(x, y_i) \oplus z_A = z_{B_i}$   
 (size array  $2^m$ )
- Step 3:- B knows the correct  $y$ ,  
 $\therefore$  knows correct index  $i$ ,  
 $\therefore$  gets  $z_B$

Now, both can reveal  $z_A \& z_B$   
 and calculate  $z_A \oplus z_B = f(x, y)$   
 (without having to reveal  $x, y$ )

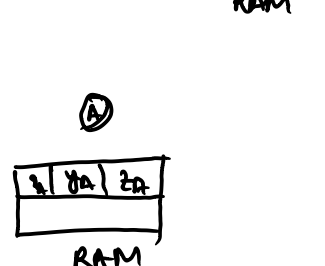
Issue is that we need to calculate  $f(x, y_i)$  for  $2^m$  diff.  $y_i$ 's  
 Even if  $f$  is polynomial size circuit we still need Exponential time

**Solution**

- Every polynomial size circuit can be simulated using
- i) AND gate.
- ii) XOR gate

Have a TDP (Trusted Third Party)

**Private 2 Party Computation**



$x = x_A \oplus x_B$   
 $y = y_A \oplus y_B$   
 $z = z_A \oplus z_B$

**Instruction Set Architecture.**

- i) Calculation XOR privately.  
 $z = x \oplus y$   
 $= (x_A \oplus x_B) \oplus (y_A \oplus y_B)$   
 $= (x_A \oplus y_A) \oplus (x_B \oplus y_B)$   
 $= z_A \oplus z_B$

$\therefore$  XOR is simple, just store  $x_A \oplus y_A$  individually &  $x_B \oplus y_B$

- ii) Calculating AND privately.

Need to use Oblivious Transfer.

$z_A \leftarrow \{0,1\}^k$  randomly.

→ A calculates an array of size 4

$[z_A \oplus (x_A y_A), z_A \oplus (x_A \bar{y}_A), z_A \oplus (\bar{x}_A y_A), z_A \oplus (\bar{x}_A \bar{y}_A)]$

$(x_A, y_A) \quad (0,0) \quad (0,1) \quad (1,0) \quad (1,1)$

→ B uses his values of  $(x_B, y_B)$  to obtain the correct index of the array. ( $z_B$ )

→ A & B store  $z_A \& z_B$  in some location, TDP gets  $z$  in that location.

Example.

$x_B, y_B = (1,0)$

$z = x \wedge y$

$= (x_A \oplus x_B) \wedge (y_A \oplus y_B)$

$= (x_A \oplus 1) \wedge (y_A \oplus 0)$

$= \bar{x}_A y_A$

B retrieves 3rd index from array.

$= z_A \oplus \bar{x}_A y_A$



Similar Schemes for n-party comm.

TDP =  $\bigoplus_{i=1}^n RAM_i$

used in Electronic voting schemes

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