

Lecture 8.1

Sorting and Searching

Sorting with Bubble Sort

- Compares two values next to each other and exchanges them if necessary to put them in the right order.
- Many variations on the order in which the pairs are examined.

Algorithm Analysis

- The BIG – O - Notation
- Some algorithms may take very little computer time to compute while others may take a considerable amount of time
- Example

```
c= 0;
sum = 0;
cin>>num;
while (num !=-1)
{sum+=num;c++;cin>>num;}
average=sum/count;
cout<<"Average is"<<average;
```

The BIG – O - Notation

- The algorithm
 - has 3 operations before the while loop
 - 4 operations within the while loop
 - 2 operations after the while loop
- In total (if loop executes 10 times)
 - $10*4 + 3+2$
- In total (if loop executes 100 times)
 - $100*4 + 3+2$
- We can generalize it to $4n+5$ (n = loops)
- For large values of n , the term $4n$ becomes the dominating term

The BIG – O - Notation

- Growth Rate of various functions
- Function grows as n (problem size grows)

n	$\log_2 n$	$n \log_2 n$	n^2	2^n
1	0	0	1	2
2	1	2	4	4
4	2	8	16	16
8	3	24	64	256
16	4	64	256	65,536

Growth Rate

n	$f(n)=n$	$f(n)=\log_2 n$	$f(n)=n \log_2 n$	$f(n)=n^2$	$f(n)=2^n$
10	0.01 μ s	0.03 μ s	0.033 μ s	0.1 μ s	1 μ s

- Time for $f(n)$ instructions on a computer that executes 1 billion instructions per second
- Definition – we say that $f(n)$ is **Big-O** of $g(n)$ written $f(n) = O(g(n))$ if there exists positive constants c and n_0 such that $f(n) \leq cg(n)$ for all $n \geq n_0$

Bubble Sort facts

- Efficient aspect of bubble sorts,
 - can quit early if the elements are almost sorted.
- Bubble sorts are $O(N^2)$ on the average,
- Can have an $O(N)$ best case.

$O(N^2)$

i	0	1	2	3	4	5	6	7	8	9	10
Pass 1	7	16	13	25	33	11	2	8	27	31	40
Pass 2	7	13	16	25	11	2	8	27	31	33	40

BS-fixed number of passes

```
void bubbleSort1 ( int x [ ] , int n )
{
    for (int pass=1; pass<n; pass++){ //count
        //how many times
        //This next loop becomes
        //shorter and shorter
        for ( int i=0; i < n - pass; i++ ) {
            if ( x [ i ] > x [ i+1 ] ) {
                //exchange elements
                int temp = x [ i ];
                x [ i ] = x [ i+1 ];
                x [ i+1 ] = temp;}}}
}
```

BS-fixed number of passes facts

- Fixed number of passes = length of the array - 1
- Each inner loop is one shorter than the previous one
- Disadvantage:
 - Always makes n-1 passes over the array,
 - Can't stop early if the array is already sorted.

BS-stop when no exchanges

```
void bubbleSort2 ( int x [ ] , int n ) {
    bool exchanges;
    int temp;
    do {
        exchanges = false; // assume no exchanges
        for ( int i=0; i < n-1; i++ ) {
            if ( x [ i ] > x [ i+1 ] ) {
                temp = x[ i ];
                x [ i ] = x[ i+1 ];
                x [ i+1 ] = temp;
                exchanges = true; }} // after
        //exchange,
        // must look again
    }while (exchanges);
}
```

BS—stop when no exchanges facts

- Continues making passes over the array as long as there were any exchanges.
- If the array already sorted, sort will stop after only one pass.
- Disadvantage:
 - Doesn't shorten the range each time by 1 as it could.

BS-stop when no exchanges, shorter each time

```
void bubbleSort3 ( int x [ ], int n ) {
    bool exchanges;
    int temp;
    do {
        n--; //make loop smaller each time
        exchanges = false; // assume this is last pass over array
        for ( int i=0; i < n; i++ ) {
            if ( x [ i ] > x [ i+1 ] ) {
                temp = x [ i ];
                x [ i ] = x [ i+1 ];
                x [ i+1 ] = temp;
                exchanges = true; // after exchange must look again
            }
        }
    } while (exchanges);
}
```

Linear Search

- Straightforward loop comparing every element in the array with the *key* (the item we are looking for).
- As soon as an equal value is found, it returns
- If loop finishes without finding a match, a -1 is returned.
- Good solution for small arrays

Linear Search code

```
int linearSearch ( int a [ ], int first, int last, int key)
{
    for ( int i = first; i <= last; i++) {
        if ( key == a [ i ] )
            return i;
    }
    return -1; // failed to find key
}
```

Binary Search

- Fastest way to search a sorted array.
- Look at the element in the middle.
 - If the key is equal to that, search is finished.
 - If the key is less than the middle element, do a binary search on first half.
 - If it's greater, do a binary search of the second half.

Binary Search (cont)

	3	5	8	9	11	13	26	27	31	33	40
i	0	1	2	3	4	5	6	7	8	9	10
	3	5	8	9	11	13	26	27	31	33	40
	3	5	8	9	11	13	26	27	31	33	40
i	0	1	2	3	4	5	6	7	8	9	10
	3	5	8	9	11	13	26	27	31	33	40

Binary search code

```
int binarySearch ( int sortedArray [ ] , int first, int last, int key ) {  
    while ( first <= last ) {  
        int mid =( first + last ) / 2; //compute mid point.  
        if ( key > sortedArray [ mid ] )  
            first = mid + 1; // repeat search in top half.  
        else if ( key < sortedArray [ mid ] )  
            last = mid - 1; // repeat search in bottom half.  
        else return mid; // found it. return position  
    }  
    return - ( first + 1 ); // failed to find key  
}
```