Concepts (Principles) of Object-Oriented Programming Study Guide

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Object-oriented programming is an exceptionally bad idea which could only have originated in California.

Edsger Dijkstra

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1 Introduction

This study guide takes its information from the Concepts of Object-Oriented Programming course website.

Objects have:

- State
- Location in memory
- Behavior

Core concepts:

- Object model
- Interfaces and encapsulation
- Classification and Polymorphism

Language concepts:

- Classes
- Inheritance
- Subtyping
- Dynamic binding

Methods are invoked on a receiver object:

Example 1.1 (receivers). Imagine there is a dog class and a human class. Here the dog instance is the receiver.

```
Dog dog = new Dog();
Human human = new Human();
dog.peeOn(human);
```

2 Typing

2.1 Types

Q: Why bother doing proofs about programming languages? They are almost always boring if the definitions are right.

A: The definitions are almost always wrong.

Benjamin C. Pierce

Definition 2.1 (Nominal Types). Type equivalence based on the type's name.

Definition 2.2 (Structural Types). Type equivalence based on availability of methods and fields.

Definition 2.3 (Static Typing). Types are determined at compile time, may be inferred or declared explicitly.

Definition 2.4 (Dynamic Typing). Types are determined at run time.

Sometimes run time checks are needed even in so-called "Static" languages.

Example 2.1 (Downcasts). Downcasts could fail so they need a run time check.

```
String foo(Object o){
   String s = (String) o;
   return s;
}
```

2.2 Syntactic Subtyping

Definition 2.5 (Substitution Principle). Subtype objects may be used wherever supertype objects are expected.

Definition 2.6 (Syntactic Subtyping). Subtype receivers S understand the messages of supertype receivers T.

$$values(S) \subseteq values(T)$$
 (1)

S has a wider interface than T.

$$interface(T) \subseteq interface(S)$$
 (2)

We then say that S <: T.

Definition 2.7 (Nominal Subtyping). S <: T when S explicitly declares T as a supertype.

Definition 2.8 (Structural Subtyping). S <: T when S has the same available methods and fields as T.

For S <: T, then any field or method in S that overrides one in T must have at least the same visibility.

Example 2.2 (Java Visibility).

Definition 2.9 (Function Subtyping). Recall from lambda calculi with subtyping that parameter types should be *contravariant* and that return types should be *covariant*:

$$\frac{T_1 <: S_1 \qquad S_2 <: T_2}{S_1 \to S_2 <: T_1 \to T_2}$$

In OO this applies to methods.

Example 2.3 (Why contravariant parameters?). Consider the following:

```
class Animal {}

class Cat <: Animal {
    public void squish() { ... }
}

class Human {
    public void pet(Animal a) {}
}

class CatLover <: Human {
    public void pet(Cat c) {
        c.squish();
    }
}

We could have client code:

void client(Human h) {
    h.pet(new Animal())
}

That is called as:
client(new CatLover());</pre>
```

This would invoke CatLover's pet method, which will call squish on an Animal. However we don't know if Animal in general may be squished? This message will not be understood.

In pretty-much all OO languages that anyone cares about return types are covariant but parameter types are invariant because this would make *overloading* more troublesome.

Definition 2.10 (Reference Subtyping). Recall from lambda calculi with subtyping that mutable reference types must be invariant:

$$\frac{S <: T \qquad T <: S}{\text{ref } S <: \text{ref } T}$$

In OO this applies to class's mutable fields.

Example 2.4 (Why invariant fields?). We can think of a mutable field has having a read and a write method.

```
class Super {
    T field;

    T read() {
        return this.field;
    }

    void write(T t) {
        this.field = t;
    }
}

class Sub <: Super {
    S field;

    S read() {
        return this.field;
    }

    void write(S s) {
        this.field;
    }
}</pre>
```

From doing function subtyping on read we get that S <: T. From doing function subtyping on write we get that T <: S.

Arrays in java are covariant because Java is stupid. So writes to arrays require a run time check.

Example 2.5 (covariant arrays in Java). Consider the following:

```
1 String[] strs = {"hello", "world"};
2 Object[] objs = strs;
3 for (Object obj : objs) {
4     System.out.println(obj);
5 }
6 System.out.println()
7 objs[0] = new Object();
This fails at line 7. There is a run time check that throws a java.lang.ArrayStoreException for array writes.
```

Example 2.6 (contravariant arrays?). What if Java had contravariant arrays? Consider:

```
1 Object[] objs = [new Object(), new Object()];
2 String strs = objs;
3 strs[0] = "hello";
4 for (String str : strs) {
5     System.out.println("bro" + str);
6 }
```

Here this would require a run time check at line 5 when we read from the array.

In general we want covariant for reads, or types in *positive* positions whereas we want contravariant for writes or types in *negative* positions. If what should be an invariant relation is treated as covariant, then we need a run time check for *writes*. If what should be an invariant relation is treated a contravariant, then we need a run time check for *reads*.

2.3 Behavioral Subtyping

Definition 2.11 (Semantic Classification of Subtyping).

$$S <: T \to behaviors(T) \subseteq behaviors(S) \tag{4}$$

We would like to constrain how overriding method's pre- and postconditions may be logically related.

Definition 2.12 (Overriding Preconditions). Overriding methods may weaken preconditions.

$$S <: T \to \forall \ S_m \ override \ T_m \to pre(T_m) \to pre(S_m)$$
 (5)

Definition 2.13 (Overrding Postconditions). Overriding methods may *strengthen* postconditions.

$$S <: T \to \forall S_m \ override \ T_m \to post(S_m) \to post(T_m)$$
 (6)

We may allow a stronger result:

$$S <: T \to \forall S_m \ override \ T_m \to old(pre(T_m)) \to post(S_m) \to post(T_m)$$
 (7)

These rules for pre- and postconditions are reminiscent of the rule of consequence from Hoare Logic:

$$\frac{P \to P' \qquad \{P'\} \ c \ \{Q'\} \qquad Q' \to Q}{\{P\} \ c \ \{Q\}}$$

We may think of P as the precondition of the supertype, Q as the postcondition of the supertype, P' as the precondition of the subtype, and Q' as the postcondition of the subtype.

Definition 2.14 (Overriding Invariants). Subtypes may have stronger class invariants for fields:

$$S <: T \to inv(S) \to inv(T)$$
 (8)

Definition 2.15 (History Constraints). Properties of class fields that describe how objects evolve over time. Such a relation on a class's field must be *reflexive* and *transitive*.

$$constraint(T_f) := old(T_f) \sqsubseteq T_f$$
 (9)

where \sqsubseteq is reflexive and transitive. Relations in history constraints may be represented as pure boolean functions.

Example 2.7 (History Constraint). Consider a stopwatch class that has the time.

```
class Stopwatch {
    // constraint: old(time) <= time
    int time;

    void tick() {
        this.time++;
    }
}</pre>
```

public void set (int val) {

Definition 2.16 (Overriding History Constraints). Subtypes may *strengthen* history constraints for fields.

```
S <: T \to \forall \ S_f \ override \ T_f \to constraint(S_f) \to constraint(T_f) (10)
```

3 Inheritance

Inheritance is not a core concept [of OOP].

Peter Müller

Specifically, programming without inheritance is distinctly not object-oriented; that would merely be programming with abstract data types.

Grady Booch

Subtyping expresses *classification*, whereas inheritance is a means of *code reuse*. Subclassing is both subtyping and inheritance. In inheritance there is only 1 super object at run time The sub object is an instance of the super object. In aggregation an object has another object as a field, and delegates to that object. It's possible to simulate subclassing with subtyping and delegation.

Example 3.1 (Immutable and Mutable Types). Consider the following java code for an immutable cell:

```
class ImmutableCell {
    // constraint: old(val) = val
    private int val;

    public ImmutableCell (int val) {
        this.val = val;
    }

    public int get () {
        return this.val;
    }
}

We could want to write a mutable cell. How should it be related to
ImmutableCell? Ideally a MutableCell could inherit all of ImmutableCell's functionality and add a setter:
class MutableCell extends ImmutableCell {
        public MutableCell (int val) {
            super(val);
        }
}
```

```
this.val = val;
}
```

However MutableCell breaks the history constraint on val, so it cannot be a Behavioral subtype! In Java it would be best to use aggregation:

```
class MutableCell {
    ImmutableCell cell;

    public MutableCell (int val) {
        this.cell = new ImmutableCell(val);
    }

    public int get () {
        this.cell.get();
    }

    public void set (int val) {
        this.cell = new ImmutableCell(val);
    }
}
```

Admittedly this is stupid: it could just have an int field and do away with the overhead of storing another object.

Example 3.2 (Private Inheritance). In C++ it's possible for a class to inherit *privately* from another class. This achieves code reuse without introducing a subtyping relation. Now we can implement the immutable and mutable cell example as we wanted to before.

```
class ImmutableCell {
    private:
        // constraint: old(val) = val
        int val;
    public:
        ImmutableCell (int v) {
            val = v;
        int get () {
            return val;
};
class MutableCell : private ImmutableCell {
    public:
        MutableCell (int v) : ImmutableCell(v) {}
        ImmutableCell::get
        void set (int v) {
            val = v;
}
```

3.1 Dynamic Method Binding

The object-oriented model makes it easy to build up programs by accretion. What this often means, in practice, is that it provides a structured way to write spaghetti code.

Paul Graham

Definition 3.1 (Static binding). At compile time a method is selected based on the *Static* type of the receiver's *Syntactic* expression.

Definition 3.2 (Dynamic binding). At run time a method is selected based on the *Dynamic* type of the receiver object's *value*.

Java and Scala have Dynamic binding by default, whereas C++ and C# have Static binding by default.

Definition 3.3 (Two-step Method). Given a method call on some receiver, to determine what method will be called given an OO program do:

- 1. Find the best-matching method based on the Static type of the receiver and arguments.
- 2. Based on the *Dynamic* type of receiver see if this method is overriden.

This is different in each language. In Java for step 1 any method in the Static class and any of its superclass's are equally valid options. In C++ and C# it starts at the Static and goes up the class hierarchy until a suitable method is found. This is each languages overloading resolution.

Definition 3.4 (Fragile Base-class Scenario). In general any potentially overriden methods may cause problems. A subclass's behavior may be affected by changes to the superclass, and the way a subclass overrides a superclass may break the superclass's behavior. In particular:

- A superclass should not change calls to Dynamically bound methods.
- subclass's should override any method that would otherwise break an invariant.
- A superclass should never call a Dynamically bound method in a constructor.
- Adding an overloading method to a superclass may affect the subclass (particularly in Java).

In general a superclass does *not* know what method may be invoked at run time for any overridable method.

In C++ and C# a superclass may declare a method as virtual if a subclass may override it. In C# a subclass may specify a method with override if a superclass declares it with virutal. In C# a subclass may specify a method with new if it wants to specify that the method doesn't have anything to do with the superclass's method; it does not override and it has different behavior.

3.1.1 Binary Methods and the Visitor Pattern

A Binary method takes the receiver and one parameter (usually of the same type or one related in a subtype hierarchy). We want behavior to depend on the *Dynamic* types of both. However simple overriding is not sound because parameter types should be contravariant.

Example 3.3 (Equals). Consider that when we want to invoke an equals method we would like to have the most specialized version invoked.

```
class Animal {
    public boolean equals (Animal a) { ... }
}
class Cat extends Animal {
    public boolean equals (Cat c) { ... }
}
```

Cat's equals does not override Animal's. Cat's equals overloads Animal's. Consider:

```
Cat c1 = new Cat();
Cat c2 = new Cat();
Animal a1 = c1;
Animal a2 = c2;
a1.equals(a2);
```

Here Animal's equals method is called even though Cat's would be safe and what we want. If we allowed an override than the following unsafe code would be accepted:

```
Cat c = new Cat();
Animal a = new Animal();
c.equals(a);
```

Since method resolution is determined by the Dynamic type of the receiver c, Cat's equals could be called which makes bad assumptions about its parameter in this case. What we would like is resolution to be determined by both the Dynamic type of the receiver and that of its argument.

In languages such as Java, C++, and C# how does one specialize behavior based on the Dynamic type of both the receiver and that of its argument?

Example 3.4 (Type tests). We can check the type of the parameter:

```
class Cat extends Animal {
    public boolean equals (Animal a) {
        if (a instanceof Cat) {
            Cat c = (Cat) a;
            ...
        } else {
            return super.equals(a);
        }
    }
}
```

Example 3.5 (Double invocation). Both the super and subclass may have appropriate methods to dispatch to depending on the parameter types. Consider the following:

```
class Animal {
    public boolean equals (Animal a) {
        // Give up
        return a.equalsAnimal(this);
    }

    // Terminal method
    public boolean equalsAnimal(Animal a) {
        // General for all Animals, Gives up
        ...
    }

    public boolean equalsBirb(Birb b) {
        // Give up
        return this.equalsAnimal(b);
    }

    public boolean equalsCat(Cat c) {
        // Give up
        return this.equalsAnimal(c);
}
```

```
class Birb extends Animal {
    public boolean equals (Animal a) {
        return a.equalsBirb(this);
    }

    public boolean equals (Birb b) {
        // Specific code for Birbs
        ...
    }
}

class Cat extends Animal {
    public boolean equals (Animal a) {
        return a.equalsCat(this);
    }

    public boolean equalsCat(Cat c) {
        // Specific code for Cats
        ...
    }
}
```

In general if we want to specialize a binary method $m: receiver \times T \to A$ where there is a super class T and subclasses S_i , $\forall i, S_i <: T$, we need the following:

- $m \in T \land \forall i, m \in S_i$.
- $\forall i, m_i : receiver \times S_i \to A \land m_i \in T \land m_i \in S_i$
- $m_{general} : receiver \times T \rightarrow A \wedge m_{general} \in T$

Where \in is used to denote a method is explicitly implemented in a particular class. In Java $m_{general}$ is inherited by the S_i . $m \in T$ and each $m_i \in T$ will dispatch to $m_{general}$. m in each S_i will dispatch to m_i flipping the arguments.

Example 3.6 (Dynamic resolution in C#). C# allows one to Dynamically resolve the calling method:

```
class Animal {
    boolean equals (Animal a) {
        // General code for Animals
    }
}

class Cat : Animal {
    boolean equals (Cat c) {
        // Specific code for Cats
    }
}

static boolean equals (Animal a1, Animal a2) {
    return (a1 as dynamic).equals(a2 as dynamic);
}
```

Cat's equals overloads Animal's. Which method is called depends on the run time type of each argument. This requires run time checks.

Example 3.7 (Multiple Dispatch). Some (experimental) languages support multiple dispatch.

```
class Animal {
    boolean equals (Animal a) {
        // General code for Animals
    }
}
class Cat : Animal {
    boolean equals (Animal@Cat c) {
        // Specific code for Cats
    }
}
```

In a call to equals the method is determined by the Dynamic type of the argument as well. In Cat's equals, the parameter c has Static type Animal and dispatch type Cat. Every call needs to have a unique best method, or else typechecking fails.

3.2 Multiple Inheritance

I made up the term "object-oriented," and I can tell you I did not have C++ in mind.

Alan Kay

C makes it easy to shoot yourself in the foot. In C++ it's harder, but when you do, you blow off your whole leg.

Bjarne Stroustrup

A type may have several subtypes and (direct) supertypes. For instance, it makes sense to say Tabby <: Cat and Tiger <: Cat, as well as Cat <: Animal and that Cat <: Furball, where Animal and Furball are not necessarily related. Sometimes we would like to reuse code from several superclasses as well. In OOP, why not combine both into multiple inheritance?

Remark. Java and C# only support single inheritance but using aggregation may simulate single inheritance and interfaces.

Multiple inheritance is just bad. Here's why.

3.2.1 Ambiguities

A subclass S may inherit directly from both T_1 and T_2 , and T_1 and T_2 may both have a field f or method m. When an instance of S is the receiver for m or f how does it choose which one? The client may need to explicitly refer to which field or method. Sometimes methods may be combined into one overriding method in the subclass.

3.2.2 Repeated Inheritance

Sometimes a subclass S inherits directly from both T_1 and T_2 , where T_1 and T_2 both inherit directly from Top. Top may have some field f. How many copies of f should S have? This is the infamous diamond problem.

By default C++ has non-virtual inheritance, where two copies of each Top class exist in memory. The constructor for Top is called twice, once for T_1 , and once for T_2 .

In C++ one may also inherit *virtually*, where only one copy of Top exists in memory and its constructor is just called once. In this case, the smallest subclass S must call the constructor for Top directly. If there is a constructor for Top without arguments, this will be called first by default. Constructors should not realy upon the virtual superclass constructors they call to maintain invariants.

3.3 Linearization

Scala has *mixins* or *traits* that may help specialize classes. Traits extend exactly one superclass and some number of traits. When mixing in a trait in a class declaration the class *must* be a subclass of the direct superclass of each trait.

Remark.

for all classes C, traits T s.t. T extends C, T <: C

The dynamic dispatch order is determined by *linerization*.

Definition 3.5 (Linearization). L determines the dispatch order.

$$L(C \ extends \ C' \ with \ T_1... \ with \ T_n) = C, L(T_n) \bullet ... \bullet L(T_1) \bullet L(C')$$

$$\tag{11}$$

$$\varepsilon \bullet B = B \tag{12}$$

$$(a,A) \bullet B = \begin{cases} A \bullet B & a \in B \\ a, A \bullet B & a \notin B \end{cases}$$
 (13)

The initialization order is the opposite.

A subclass only has one copy of a superclass in memory. In initialization each constructor is called exactly once, where arguments to a superclass constructor are provided by the immediately preceding class in the linearization order.

Behavioral subtyping can only be checked when a trait is mixed in. Traits are difficult to reason about because:

- Like in C++ virutal inheritance they don't know how their superclasses get initialized.
- Traits do not know which methods they override.
- Traits do not know Statically which class super calls will go to.

4 More Typing

If Sun were to hand the management of Java over to a committee of monkeys, would it be more successful?

Eric Sink

4.1 Bytecode Verification

The Java Virtual Machine (JVM) runs *java bytecode*. In order to make some guarantees about some arbitrary bytecode loaded by a program, the bytecode must be typechecked.

Definition 4.1 (Java Virutal Machine). JVM is a stack-based language that consists of the following:

- A stack (duh). Operations push elements onto the stack and pop them off.
- A (potentially finite) set of registers. The first stores this, then method parameters, then local variables.
- A heap where objects are stored in memory. The stack and regiters may have pointers to the heap.

A sample of the JVM instruction set is provided in 1.

JVM instructions are typechecked. There's a max stack size MS, input type list for the stack S, input type list for registers R, and output type list for the stack S', and an output type list for the registers R'. Some of the basic rules are given in 2.

```
\begin{array}{lll} instr & ::= & \mathsf{iconst}\ z & & \mathsf{push}\ \mathsf{int}\ z \ \mathsf{onto}\ \mathsf{the}\ \mathsf{stack} \\ & & & & & \mathsf{load}_\tau\ r & & \mathsf{push}\ \mathsf{value}\ \mathsf{in}\ \mathsf{register}\ r \ \mathsf{onto}\ \mathsf{the}\ \mathsf{stack} \\ & & & & \mathsf{store}_\tau\ r & & \mathsf{pop}\ \mathsf{top}\ \mathsf{value}\ \mathsf{from}\ \mathsf{stack}\ \mathsf{into}\ \mathsf{register}\ r \\ & & & & \mathsf{pop}\ \mathsf{top}\ \mathsf{value}\ \mathsf{store}_\tau\ r \\ & & & & \mathsf{pop}\ \mathsf{top}\ \mathsf{value}\ \mathsf{stack}\ \mathsf{into}\ \mathsf{register}\ r \\ & & & & \mathsf{pop}\ \mathsf{top}\ \mathsf{value}\ \mathsf{stack}\ \mathsf{into}\ \mathsf{register}\ r \\ & & & \mathsf{pop}\ \mathsf{top}\ \mathsf{value}\ \mathsf{stack}\ \mathsf{and}\ \mathsf{push}\ v_1 \otimes v_2 \\ & & & & \mathsf{pop}\ \mathsf{top}\ \mathsf{value}\ \mathsf{stack}\ \mathsf{and}\ \mathsf{push}\ v_1 \otimes v_2 \\ & & & \mathsf{pop}\ \mathsf{top}\ \mathsf{value}\ \mathsf{stack}\ \mathsf{and}\ \mathsf{push}\ \mathsf{v}_1 \otimes v_2 \\ & & & \mathsf{pop}\ \mathsf{top}\ \mathsf{value}\ \mathsf{stack}\ \mathsf{and}\ \mathsf{push}\ \mathsf{v}_1 \otimes v_2 \\ & & & \mathsf{pop}\ \mathsf{args}\ v_n, ..., v_1\ \mathsf{receiver}\ v\ \mathsf{then}\ \mathsf{push}\ \mathsf{C.m.v}(v_1, ..., v_n) \\ & & \mathsf{pop}\ v\ \mathsf{and}\ \mathsf{method}\ \mathsf{return}\ v \\ & & \mathsf{pop}\ \mathsf{value}\ \mathsf{log}\ \mathsf{log}\
```

Figure 1: JVM instructions

Figure 2: JVM instruction typing

Remark. Note that the rule for stores does not check that the previous type in the register is related. Thus bytecode typing allows strong updates, something not allowed in java source code.

Instructions may have several predecessors because of jumps. Thus the *smallest common supertype*, or $join \sqcup needs$ to be selected.

Remark. With multiple subtyping (such as with interfaces in Java) it may not be possible to calculate the join. A run time check is necessary for interface method invocation.

(Old) Java needed to perform type inference on bytecode. Because joins need to be computed, a worklist algorithm is necessary. In this dataflow analysis, for each instruction instr(p) at a program point (line) p, we have in(p) for the types of the stack and registers before the instruction, and out(p) for the types of the stack and registers after the instruction. Thus we have:

$$instr(p): in(p) \to out(p)$$
 (14)

The dataflow equation we solve for is:

$$in(p) = | \{out(q) \mid q \text{ predeces } p\}$$
 (15)

We want to take all of the precedessor instructions of p, take the joins of their types in their stacks and registers. This join is exactly what we want to compute for in(p).

To start out we want the stack to be empty, and the registers to contain the known parameter types P_i and \top for the local variables. The algorithm is given in 1. Note that \sqcup fails for different stack sizes.

```
Algorithm 1 JVM Type Inference
```

```
in(0) \leftarrow (\varepsilon, [P_1, ..., P_n, \top, ..., \top])
worklist \leftarrow \{p \mid instr(p) \text{ in method}\}
while \ worklist \neq \emptyset \ do
p \leftarrow \min \ worklist
worklist \leftarrow worklist \setminus \{p\}
instr(p) : in(p) \rightarrow out(p)
for \ all \ q \ succeeding \ p \ do
in(q) \leftarrow in(q) \sqcup out(p)
if \ in(q) \ has \ changed \ then
worklist \leftarrow worklist \cup \{q\}
end \ if
end \ for
end \ while
```

Read this to learn more about java bytecode verification.

4.2 Parametric Polymorphism

Classes and methods may be parameterized with types (yay!). In OOP this is called *generic types*. It is possible to specify upper bounds on these type parameters. Upper bounds via subtyping on type parameters is the lame OOP way of accomplishing ad-hoc polymorphism, like typeclasses in Haskell or traits in Rust. If S <: T, how should we relate G(S) and G(T)?

Example 4.1 (Covariant Generics). Suppose:

$$\frac{S <: T}{G \langle S \rangle <: G \langle T \rangle}$$

In Java we could define a class for lists:

```
class List <A> {
    void add (A a) { ... }
    A head () { ... }
}
Suppose we had client code:
List <String > ls = new List <String > ();
List <Object > lo = ls;
ls.add("Hello there");
Object o = lo.head();
lo.add(new Object);
```

Everything works fine until we add a Object to the String list. recall the principle that covariant types work for reads but not for writes! Thus in general covariant generics are not sound. If we allowed covariant generics than we would need a run time check for writes.

Example 4.2 (Contravariant Generics). Suppose:

$$\frac{S <: T}{G \langle T \rangle <: G \langle S \rangle}$$

Consider the previous List class. Now we could write client code:

```
List <Object > lo = new List <Object >();
List <String > ls = lo;
lo.add(new Object);
ls.add("General_Kenobi");
String s = ls.head();
```

This time everything works until we try to get the head from the list as a String, because it is an Object. The recall the principle that contravariant types work for writes but not for reads! Thus in general contravariant generics are unsound. If we allowed contravariant generics than we would need a run time check for reads.

Java has chosen to only allow *invariant* generics. By contrast Scala only has invariant generics by default, allowing one to specify if a type parameter is covariant or contravariant. Scala allows contravariant type parameters when they only occur in a positive position, are only read from. Scala allows contravariant type parameters when they only occur in a negative positive, i.e. are only written to.

Example 4.3 (Scala covariant parameter). Consider an immutable cell in Scala:

```
class ImmutableCell[+A] (val : A) {
    def get() : A { val }
}
```

Here A is only used as a return type, i.e. a positive position.

Question: what about constructor?

Example 4.4 (Scala contravariant parameter). Consider a comparison interface:

```
\begin{array}{c} \text{interface } \operatorname{Comparison}[-A] \ \{\\ \text{int } \operatorname{compare}\left(A\right);\\ \} \end{array}
```

Here A is only used as a method parameter to be written to, i.e. a negative positive.

When we are stuck with *invariant* generics how do we write code that works with different instantiations of a type parameter?

In OOP (especially Java) this is an issue when what you want is ad-hoc polymorphic functionality for a supertype that works on subtypes, but since you don't have ad-hoc polymorphism you need to create another interface and class(es) that have their own subtype relations. Also you cannot pass functions as arguments in these languages in general so ... here's a convoluted example to motivate a kind of problem one may encounter.

Example 4.5 (Additional type parameters). Here we are going to try to demonstrate that Java forces one to twist themselves into a prezle if they just want to use standard type parameters. Suppose there's some Comparator interface and generic TreeSet class that represents a set implemented in a tree data structure. In order to search for elements it needs to compare elements in binary nodes of the tree. Thus it needs some way to have a compare function for its elements. Because we are in Java we cannot pass functions as arguments.

```
interface Comparator<T> {
    int compare(T x, T y);
class TreeSet<E extends Comparator<E>>> {
    TreeSet () \{ \}
    void add (E elem) { ... }
    boolean member (E elem) { ... }
    void remove (E elem) { ... }
}
Suppose that we would like to create a TreeSet<Student> where Students are a Person, and Person has a
general comparison operation for people.
class Person implements Comparator<Person> {
    int compare (Person x, Person y) { ... }
}
class Student extends Person {
Where we would like to have client code:
TreeSet < Student > ts = new TreeSet < Student > ();
Well too bad. Java gets angry because Student is "not within the bounds of the type variable (of TreeSet)."
That is, we don't know Student <: Comparator (Student). If we try to have Student directly implement
the Comparator interface Java still isn't satisfied:
class Student extends Person implements Comparator<Student> {
    int compare(Student x, Student y) { ... }
Java complains that "Comparator cannot be inherited with different arguments: Student and Person." If
Person does not implement Comparator then Java is satisfied, but we would like it to. If we would like to
have our cake and eat it too we need to modify our TreeSet class as follows:
class TreeSet<E extends F, F extends Comparator<F>>> {
    TreeSet () {}
    void add (E elem) { ... }
    boolean member (E elem) { ... }
    void remove (E elem) { ... }
And then out client code would need to look like:
TreeSet<Person, Student> ts = new TreeSet<Person, Student>();
```

Here we needed to make explicit in TreeSet's type parameters that the element type does not necessarily need to have its own Comparator, but that it has a supertype that implements Comparator. As shown this is very tedious.

How can we avoid addition type parameters and constraints?

4.2.1 Wildcards

Definition 4.2 (Wildcards). Java has so called *wildcards* that represent *existential types*.

$$G\langle ? \rangle \triangleq \exists A, G\langle A \rangle$$
 (16)

In Java there is no way to explicitly instantiate these existential types. Java's type system does this automatically. The type argument to the instance of an existential type is abstract to clients.

Example 4.6 (Wildcard identity). Java accepts the following identity function:

```
static List <?> id (List <?> 1) {
    return 1;
}
```

In the body of id the Java compiler is able to show $\exists E, List\langle E \rangle$, where 1 is a *proof* of $\exists E, List\langle E \rangle$. However it does not know that the parameter type and return type are the same.

```
List < String > 1 = id (new ArrayList < String > );
```

The above fails because java only knows that the result of id(new ArrayList<List>) is $\exists E, List\langle E \rangle$. Java does not remember that the E in question is a String. The best we can do is:

```
List <?> l = id(new ArrayList < String > );
```

Java does not even allow:

```
List < Object > l = id (new ArrayList < String > );
```

Since Java generics are invariant in general $\exists E, G \langle E \rangle \not <: G \langle Object \rangle$.

Example 4.7 (Reading from and writing to wildcards). Java rejects the following:

```
static void merge (Collection <?> x, Collection <?> y) {
    x.addAll(y);
}
```

We have the following types:

```
\begin{split} \mathbf{x}:\exists A, Collection \langle A \rangle \\ \mathbf{y}:\exists B, Collection \langle B \rangle \\ \mathbf{addAll}: \forall C, Collection \langle C \rangle \times (\exists D, Collection \langle D \rangle \wedge D <: C) \rightarrow () \end{split}
```

When x is the receiver of addAll, its universal type C is instantiated with some unknown parameter type. Java is implicitly unpacking x's type as some unknown A.

```
\mathtt{addAdll}\langle A \rangle : Collection\langle A \rangle \times (\exists D, Collection\langle D \rangle \wedge D <: A) \rightarrow ()
```

When y is passed as an argument to x.addAll y's type is implicitly unpacked with some unknown type parameter B. Java will not be able to satisfy the type bounds of

```
addAdll\langle A \rangle : Collection\langle A \rangle \times (genericCollectionB \wedge B <: A) \rightarrow ()
```

Since there's no relationship between A and B. Even if we try:

```
static void merge (Collection <?> x, Collection <?> y) {
    for (Object elem : y) {
        x.add(elem);
    }
}
```

Java will still be unconvinced. We have:

```
\operatorname{add}: \forall C, Collection \langle C \rangle \times C \to () \operatorname{add} \langle A \rangle : Collection \langle A \rangle \times A \to ()
```

Which is even more strict. Of course A <: Object and B <: Object. However in order to pass elem into x.add, we need that Object <: A.

We would like to be able to constrain wildcards in some way.

Definition 4.3 (Bounding wildcards). Java offers the following:

$$G\langle ? \text{ extends } T \rangle \triangleq \exists A, G\langle A \rangle \land A <: T$$

 $G\langle ? \text{ super } T \rangle \triangleq \exists A, G\langle A \rangle \land T <: A$

Example 4.8 (Reading from and writing to wildcards revisited). We may now constrain the existential type parameters in our merge example:

```
static <E> void merge (Collection <? super E> x, Collection <? extends E> y) {
    x.addAll(y);
    for (A elem : y) {
        x.add(elem);
    }
}
```

Everything works now because we have the following:

```
\begin{split} \mathbf{x}: \exists A, Collection \langle A \rangle \wedge E <: A \\ \mathbf{y}: \exists B, Collection \langle B \rangle \wedge B <: E \\ \mathbf{add}: \forall C, Collection \langle C \rangle \times C \rightarrow () \\ \mathbf{addAll}: \forall C, Collection \langle C \rangle \times (\exists D, Collection \langle D \rangle \wedge D <: C) \rightarrow () \end{split}
```

When x's type gets implicitly unpacked we get some type A and the knowledge that E <: A. Similarly when y's type is unpacked we get some type B and the knowledge that B <: E. When x is the receiver of add and addAll we get:

```
\verb"add" \langle A \rangle : Collection" \langle A \rangle \times A \to () \verb"addAll" \langle A \rangle : Collection" \langle A \rangle \times (\exists D, Collection" \langle D \rangle \wedge D <: A) \to ()
```

Thus when we pass elem into x.add we need to show that B <: A. This is true by transitivity of subtyping. The same evidence is used when we pass y into x.addAll.

In java, given some generic class G, we can use wildcards to make certain instances of G covariant or contravariant. This is called *use-site variance*.

Example 4.9 (Use-site variance). Suppose we have some cell class:

```
class Cell <E> {
    private E elem;
    Cell (E elem) { this.elem = elem; }
    E get () { return this.elem; }
    void set (E elem) { this.elem = elem; }
}
```

Say we have that Student extends Person. We can create a covariant Cell that only allows us to perform reads:

```
1  Cell <? extends Person > readOnly = new Cell < Student > (new Student());
2  Object o = readOnly.get();  // good
3  Person p = readOnly.get();  // good
4  Student s = readOnly.get();  // bad
5  readOnly.set(new Object());  // bad
6  readOnly.set(new Person());  // bad
7  readOnly.set(new Student());  // bad
```

Both of the final set calls fail, as Java is unable to correctly constrain the type parameters. We have the type information:

```
\label{eq:condition} \begin{split} \texttt{readOnly}:\exists E, Cell\langle E \rangle \land E <: Person \\ \texttt{readOnly.get}:() \rightarrow E \land E <: Person \\ \texttt{readOnly.set}: E \land E <: Person \rightarrow () \end{split}
```

Where for readOnly.get and readOnly.set E is some unpacked type whose only constraint is that E <: Person. Let's take this line by line.

- 1. Declare a covariant-use-site Cell with an upper bound Person.
- 2. Typechecks because the result E of readOnly.get is bounded above by Person, so it is acceptable to assign it to an Object.
- 3. Typechecks because the result E of readOnly.get is bounded above by Person, so it is acceptable to assign it to a Person.
- 4. Reading as a Student fails because we need to somehow show that E <: Student, but all we have is that E <: Person. In principle E could be a Person, which does not work as a Student in general.
- 5. Setting the cell to \mathtt{Object} fails because we would need to show that Object <: E and Object <: Person, which does not hold.
- 6. Attempting to set the cell to a Person fails because we do not know that Person <: E.
- 7. Setting the cell to a Student fails because of the same principle.

Intuitively writing to read0nly fails because we have information about the lower bound of E.

We may also create a contravariant cell that only allows us to perform writes. Suppose that there is also some class MasterStudent extends Student.

```
1 Cell<? super Student> writeonly = new Cell<Person>(new Person());
2 writeonly.set(new MasterStudent()); // good
3 writeonly.set(new Student());
                                     // good
                                     // bad
4 writeonly.set(new Person());
                                     // bad
5 writeonly.set(new Object());
                                     // bad
  MasterStudent m = writeonly.get();
                                     // bad
7
  Student s = writeonly.get();
                                     // bad
8 Person p
                 = writeonly.get();
  Object o
                 = writeonly.get();
                                     // good
```

We have the type information:

```
\begin{split} \texttt{readOnly}: \exists E, Cell \langle E \rangle \land Person <: E \\ \texttt{readOnly.get}: () \rightarrow E \land Person <: E \\ \texttt{readOnly.set}: E \land Person <: E \rightarrow () \end{split}
```

Where for readOnly.get and readOnly.set E is some unpacked type whose only constraint is that Person <: E. Let's take this line by line.

- 1. Declares a contravariant-use-site Cell with a lower bound Student.
- 2. Typechecks because we have that MasterStudent <: E from MasterStudent <: Student and Student <: E.
- 3. Typechecks because we have that Student <: E.
- 4. Fails because Person <: E does not hold.
- 5. Fails because Object <: E does not hold.
- 6. Fails because E <: MasterStudent does not hold in general.
- 7. Fails because E <: Student does not hold in general.
- 8. Fails because E <: Person does not hold in general.
- 9. Typechecks because $E <: Objects \ always \ holds.$

In principle it is possible to downcast to a more specific type.

Example 4.10 (TreeSet revisited). We may now only have a single type parameter for TreeSet via wild-cards.

```
class TreeSet<E extends Comparator<?>>> {
    ...
    TreeSet () {}
    void add (E elem) { ... }
    boolean member (E elem) { ... }
    void remove (E elem) { ... }
}
```

We may now define client code:

TreeSet<Student> ts = **new** TreeSet<Student>();

In general wildcards allow more flexibility than vanilla type parameters.

- Java does not allow lower bounds super for normal type parameters.
- Instantiation of a wildcard $G\langle ? \rangle$ may change over time: it may be reassigned an instance with a different type argument. However when reassigning a normal generic instance of $G\langle T \rangle$ it must always have a type argument of exactly T.

For some generic type G, we may define the set of instance types given some type argument. TODO: define this better or remove.

$$[\![G\langle T\rangle]\!] = \{H\langle T\rangle \mid \forall H, H <: G\} \tag{17}$$

$$\llbracket G\langle ? \rangle \rrbracket = \{ H\langle T \rangle \mid \forall H, T, H <: G \} \tag{18}$$

$$\llbracket G\langle ? <: T \rangle \rrbracket = \{ H\langle S \rangle \mid \forall H, S, H <: G \land S <: T \}$$
(19)

$$\llbracket G\langle S <:? \rangle \rrbracket = \{ H\langle T \rangle \mid \forall H, T, H <: G \land S <: T \}$$
(20)

Definition 4.4 (Subtyping generics). Given generic types H and G, we say that:

$$H\langle \mathcal{I}\rangle <: G\langle \mathcal{I}\rangle \equiv \llbracket H\langle \mathcal{I}\rangle \rrbracket \subseteq \llbracket G\langle \mathcal{I}\rangle \rrbracket$$

where \mathcal{I} is either a type parameter or a wildcard bound.

Remark. Subtyping in Java is undecidable do to wildcards.

4.2.2 Type Erasure

For backwards compatibility, Sun did not want to change the JVM after generics were introduced. So generic type information is erased by the compiler. $G\langle T\rangle$ becomes just G in java bytecode. Occaisionally the compiler needs to insert casts to the class used for the type argument for instances of generic types. Because of this, Java disallows the following:

- Performing instanceOf on a generic instance type $G\langle T \rangle$.
- .class of a generic instance type.
- arrays of generic types $G\langle T\rangle$ [].

C# allows the above.

Example 4.11 (Erasure and overloading). Java disallows the following because there is a name clash between each foo as a result of type erasure.

```
class Erasure<S, T> {
    void foo (S p) {}
    void foo (T p) {}
}
```

However C# does allow this in general. If one chooses to instantiate Erausre with the same types any call to foo will be ambiguous and cause a typechecking error.

```
Erasure < Object , Object > erasure = new Erasure < Object , Object > ();
erasure.foo(new Object()); // ambiquous!
```

In Java one can resolve the issue by giving the type parameters different upper bounds.

In Java static fields are shared by all instantiations of a generic class, but not in C#.

4.2.3 C++ Templates

In C++ one provides type parameters to classes and methods via *templates*. As you will see, intuitively templates are glorified macros.

Every time a template is instantiated the C++ generates an instantiated version of the code for the class or method for the given type arguments. This causes *code bloat*. Furthermore C++ templates are not typechecked. Only the parts of instance classes that get used after the class is instantiated get typechecked. In principle one could make all kinds of assumptions about the type parameter in a template class (about what methods and fields it has) and C++ will not complain unless its instantiation doesn't provide suitable type arguments.

C++ later added *concepts*. Concepts provide a way to specify constraints about a template's type parameter. These constraints are checked upon instantiation. To read more about concepts look here.

5 Information Hiding and Encapsulation

The problem with object-oriented languages is they've got all this implicit environment that they carry around with them. You wanted a banana but what you got was a gorilla holding the banana and the entire jungle.

Joe Armstrong

5.1 Information Hiding

Definition 5.1 (Information Hiding). A technique to *reduce* dependencies between modules. A module only provides clients with the fields and methods such that no invariants can be broken by clients. This is a *Static* concept.

Ideally class interfaces are thin and hide implementation details. To understand a single class hopefully one just has to understand the interfaces of any dependencies without looking at their implementations.

To use a class a client should only need to know:

- The class name.
- The type parameters and their bounds.
- The signatures and pre and postconditions of exposed methods.
- The types, invariants, and constraints of exposed fields.
- The above for any superclass or superinterface.

Example 5.1 (Subclass interface). We for some class S we can consider the interface it has to its superclass T. This includes any protected fields and methods of the superclass.

Example 5.2 (Friend (package) interface). Classes defined in the same package have access to each others default and protected fields and methods. They may be mutually defined.

Java offers the following access modifiers:

- private: Only the implementing class has access to these methods and fields. They can not even be overriden by subclasses. The most restrictive.
- default: Only classes defined in the same package has access to these fields and methods. In general they cannot be overriden by subclasses, unless the subclass is defined in the same package. Available in the friend interface.
- protected: These fields and methods are available to classes in the same package and any potential subclasses. Thus they may be overriden. Available in the subclass and friend interface.
- public: Everyone and their mother has access to these fields and methods. Of course may be overriden.

Question: how do access modifiers interact with overloading?

Recall 3.4. In principle any non-private field or method, anything that can be overriden may cause problems. Thus when changing a base class, any *observable* behavior, i.e. **not** private must be preserved.

Definition 5.2 (JLS1 Java method selection). When some receiver o invokes a method m, Statically/at compile time:

- 1. Find the static declaration of m.
- 2. Determine if m is accessible at the call site.
- 3. Determine if m is virtual (may be overriden) or non-virtual.

Then at run time

- 1. Compute the receiver's value.
- 2. Based on the Dynamic type of the receiver locate the method m to invoke.

Definition 5.3 (The Access rule). The access modifier of an overriding method must be at least as open as that of the overriden method.

Definition 5.4 (Rules for overriding). If S <: T, S.m overrides T.m only if T.m is accessible in S.m.

Example 5.3 (Default access methods). Consider the class Super defined in package A.

```
package A;
class Super {
    void foo() {
        System.out.println("A");
    }
}
And the class Sub in package B.
package B;
class Sub extends A.Super {
    public void foo() {
        System.out.println("B");
    }
}
```

Suppose we have the following client code that invokes foo in package A.

```
Super soup = new Sub(); soup.foo();
```

Since Super.foo() is not accessible in Sub.foo(), we would expect "A" to be printed. This is because Super.foo is default, thus is not available in Sub, and thus cannot be overriden by Sub.foo. However we would be wrong under the rules in 5.2. Under these rules Sub.foo will be selected and "B" will be printed. Let's step through the rules. First, at compile time:

- 1. We find the Static declaration of foo in Super.
- 2. We find that Super.foo is accessible at the call site.
- 3. The invocation is virtual.

Then at run time:

- 1. We find the Dynamic type of the receiver soup is Sub.
- 2. We locate Sub.foo since it is public and in the class Sub of the receiver soup.

Definition 5.5 (JLS2 Java method selection). Java fixed their broken 5.2 by ensuring that the Dynamically selected method is able to override the Statically determined method. When some receiver o invokes a method m, Statically/at compile time:

- 1. Find the static declaration of m.
- 2. Determine if m is accessible at the call site.
- 3. Determine if m is virtual (may be overriden) or non-virtual.

Then at run time

- 1. Compute the receiver's value.
- 2. Based on the Dynamic type of the receiver locate the method m to invoke that overrides the Statically determined method!

This is a refinement of 3.3 that more precisely considers access modifiers.

Example 5.4 (Don't always use protection). Let's consider the previous example, but now the modifiers are protected.

```
package A:
class Super {
    protected void foo() {
         System.out.println("A");
}
And the class Sub in package B.
package B;
class Sub extends A. Super {
    protected void foo() {
         System.out.println("B");
}
Suppose we have the following client code that invokes foo in package A.
package A;
class Client {
    void client() {
         Super soup = \mathbf{new} Sub();
         soup.foo();
    }
```

Again we would expect Super.foo to be invoked, printing "A", since Sub.foo is protected, and this unavailable to Client as Client is not a subclass of Sub nor is it in the same package. And again, even under the refined 5.5 we would be wrong. Let's go through the steps. At compile time:

- 1. We determine that the Static declaration is Super.foo.
- 2. Since Super.foo is protected and Client is in the same package as Super.
- 3. Super.foo may be overriden.

Then at run time:

- 1. The Dynamic value of soup is Sub.
- 2. Indeed Sub.foo overrides Super.foo, thus Sub.foo is called.

Thus Client was able to call a method that was not even available to it!.

5.2 Encapsulation

Ideally, any module behaves the same way, according to its specification, no matter what the calling context it. The client relies upon the **consistency of internal representations** of the invoked module. Furthermore the module should prevent clients from being able to violate its invariants. For instance, non-private fields are a way to set yourself up for failure, so stay outta trouble kids.

Definition 5.6 (Encapsulation). A technique to separate the memory state available to different *capsules*, so the memory states available to each capsule are disjoint. The boundaries delimiting memory are achieved via clear interfaces to these capsules so these capsules may guarantee invariants about their internal states. In this course encapsulation relates to the state of the program at run time, thus is a *Dynamic* concept.

Often the terms information hiding and encapsulation are used interchangeably, but here they are distinct. What is a capsule? It can be:

• An individual object.

- A structure composed of many objects.
- A class (with all of its objects).
- A package (with all of its classes and objects).

To provide encapsulation for a capsule we requires a precisely defined boundary and an interface for that boundary. The internal representation of a capsule is encapsulated if it can only be manipulated using its interface. To achieve internal consistency (invariants) of objects we should:

- 1. Apply information hiding.
- 2. Make consistency criteria explicit, via the use of contracts, i.e. with invariants, history constraints, pre- and postconditions.
- 3. Check that anything exposed by the interface, including those of possible subclasses, preserve consistency and prevent malicious clients from breaking consistency.

In practice this means that invariants should only refer to private fields, since anything else can be set by a client.

All this begs the question: what is an object structure?

6 Object Structures and Aliasing

I call it my billion-dollar mistake. It was the invention of the null reference in 1965.

Tony Hoare

Single objects are the atomic building blocks of OOP. From these we can build more complex objects or *object structures* when their classes have fields that are other objects.

Definition 6.1 (Object structure). A set of objects connected via references.

6.1 Aliasing

Definition 6.2 (Aliasing). We say that an object o is aliased by the aliases x and y if they both hold references to o. That is

$$x \mapsto o \land y \mapsto o \land x \neq y$$

An alias may be

- Local variables of methods, including this.
- Class fields (including static).
- Left expressions in general.

Definition 6.3 (Capturing). A form of unintended aliasing where a reference gets stored in a data structure. Often this occurs in constructors.

Aliases may be used to get around an object's boundary/interface.

Definition 6.4 (Leaking). Occurs when a data structure passes out or exposes a reference to some ostensibly internal object. This usually happens by mistake. Leaking can be exploited to bypass an object's boundary/interface.

6.2 Problems of Aliasing

The big lie of object-oriented programming is that objects provide encapsulation.

John Hogg.

Remark. If an interface has a method that accepts some object or object structure as an argument, and it captures that argument, its interface may be bypassed if the caller decides to mutate what was passed in. Just making fields private that represent the internal state of the callee does nothing.

Remark. If an interface has a method that returns an object, array, or reference part of its internal data structure this is leaking, and any client may modify this object and thus the internal state.

Here's a list of some other specific issues with aliasing:

- When performing explicit memory management one needs to be sure that when one is freeing a pointer that there are no other aliases. This is the so-called dangling pointer problem.
- Compilers should not inline objects that are aliased.

6.3 Unique References

7 Initialization

Object-oriented programming had boldly promised "to model the world." Well, the world is a scary place where bad things happen for no apparent reason, and in this narrow sense I concede that OO does model the world.

Dave Fancher

bang is property of local variable. committed is property of object local var points to.