Exercise 01

Given is a cluster of n machines, each having a probability p of failing.

a) The probability of one machine to not fail is $1 - p$.
The probability of ALL machines not failing is n times $1 - p$ which is $(1 - p)^n$.
The probability of at least one machine failing is the opposite event and thus $1 - (1 - p)^n$.

b) The probability p_k of exactly k machines failing can be described using the binomial distribution. The binomial distribution describes the discrete probabilities of the number of successes in a sequence of independent experiments. As we have independent machines in the cluster with the number of successes corresponding to a machine failing we can write:

$$p(k|p,n) = \binom{n}{k} p^k (1-p)^{n-k}$$

p^k is the probablity that k machines fail which has to be multiplied to the probability that the other $n - k$ machines do not fail. The binomial coefficient is the combinatoric element and describes in which way k elements can be chosen from n elements.

c) Zz.: $p_1 + p_2 + ... + p_n = 1 - (1 - p)^n$
We have $p_1 = p_2 = ... = p_n = p = \binom{n}{k} p^k (1-p)^{n-k}$

$$p_1 + p_2 + ... + p_n = \sum_{k=1}^{n} \binom{n}{k} p^k (1-p)^{n-k}$$

We can use the binomial theorem: $\sum_{k=0}^{n} \binom{n}{k} y^k x^{n-k} = (x + y)^n$ but have to subtract p_0 again

$$\begin{aligned}
&= \sum_{k=0}^{n} \binom{n}{k} p^k (1-p)^{n-k} - \binom{n}{0} p^0 (1-p)^n \\
&= ((1-p) + p)^n - (1-p)^n \\
&= 1^n - (1-p)^n \\
&= 1 - (1-p)^n
\end{aligned}$$

Exercise 02

a1) -join() - TRANSFORMATION

Input: otherDataset, [numTasks]

Output: Returns a dataset with "Key/(V1,V2)" pairs.

Code Example rdd1 = sc.parallelize([("foo", 1), ("bar", 2), ("baz", 3)])
rdd2 = sc.parallelize([("foo", 4), ("bar", 5), ("bar", 6)])
rdd1.join(rdd2)

a2) -sort() - TRANSFORMATION - Could not find sort() in reference used sortByKey() instead -https://spark.apache.org/docs/2.2.0/rdd-programming-guide.html

Input: [ascending], [numTasks

Output: When called on a dataset of (K, V) pairs where K implements Ordered, returns a dataset of (K, V) pairs sorted by keys in ascending or descending order, as specified in the boolean ascending argument.

Code Example: $names = sc.textFile(sys.argv[1])$
$filtered_rows = names.filter(lambdaline : "Count" notinline).map(lambdaline : line.split(","))$
$filtered_rows.map(lambdan : (str(n[1]), int(n[4]))).sortByKey().collect()$

a2) -groupby() - TRANSFORMATION - Could not find groupby() in reference used groupByKey() instead -https://spark.apache.org/docs/2.2.0/rdd-programming-guide.html

Input: [ascending], [numTasks]

Output: Returns a dataset with "Key/Value" Pairs sorted ascending or descending.

Code Example: lines = spark.read.text(sys.argv[1]).rdd.map(lambda r: r[0])
words = lines.flatMap(lambda x: x.split(' '))
words.reduceByKey(lambda x, y: x + y, 5)
words.groupByKey(5)

b1) -NOTE All the tested source code is in $U1_Ex2.py$

-INTERSECTION

Input: [RDD]

Output: Returns a RDD with the intersecting elements of two datasets.

Code example: intersectRDD1 = sc.parallelize(range(1, 10))
intersectRDD2 = sc.parallelize(range(5, 15))
intersect = intersectRDD1.intersection(intersectRDD2).collect()
print(intersect)

exampleOutput: [8, 9, 5, 6, 7]

b2) -DISTINCT

Input: [numTasks]

Output: Return a new dataset that contains the distinct elements of the source dataset.

example Code: distinctRDD1 = sc.parallelize(range(1, 12))
distinctRDD2 = sc.parallelize(range(8, 20))
distinct = distinctRDD1.union(distinctRDD2).distinct().collect()
print(distinct)

exampleOutput: [8, 16, 1, 9, 17, 2, 10, 18, 3, 11, 19, 4, 12, 5, 13, 6, 14, 7, 15]

b3) -UNION

Input: [RDD]

Output: Return a new dataset that contains the union of the elements in the source dataset and the argument.

example Code: unionRDD1 = sc.parallelize(range(1, 7))
unionRDD2 = sc.parallelize(range(3, 10))
union = unionRDD1.union(unionRDD2).collect()
print(union)

exampleOutput: [1, 2, 3, 4, 5, 6, 3, 4, 5, 6, 7, 8, 9]

b4) -COLLECT

Input: NONE is called as a function on an RDD

Output: Return all the elements of the dataset as an array at the driver program.

example Code: collection = sc.parallelize([1, 2, 3, 4, 5]).flatMap(lambda x: [x, x, x]).collect()
print(collection)

exampleOutput: [1, 1, 1, 2, 2, 2, 3, 3, 3, 4, 4, 4, 5, 5, 5]

b5) -COUNT

Input: NONE is called as a function on an RDD

Output: Return all the number of elements of the dataset as an array at the driver program.

example Code: names1RDD = sc.parallelize(["Daniela", "Marvin", "Rudolf", "Kevin", "Jaqueline"])
counts = names1RDD.count()
print(counts)

exampleOutput: 5

b6) -FIRST

Input: NONE is called as a function on an RDD

Output: Return all the first element of the dataset as an array at the driver program.

example Code: names2RDD = sc.parallelize(["Daniela", "Marvin", "Rudolf"])
first = names2RDD.first()
print(first)

exampleOutput: Daniela