

Space Group Encoding

This file contains the conversion tables for a compact space group encoding scheme. Table 1 lists the point symmetry parts of the 14 basic matrices, and Table 2 lists the conversions for the components of translation vectors. The remaining tables contain the generator strings for all 230 space groups. These tables should be used along with the information in section 10.7 (page 252) of the text book.¹

Table 1: Explicit point symmetry matrices for the 14 matrices used to encode the space group generators.

$a = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$	$b = \begin{pmatrix} -1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$	$c = \begin{pmatrix} -1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -1 \end{pmatrix}$
$d = \begin{pmatrix} 0 & 0 & 1 \\ 1 & 0 & 0 \\ 0 & 1 & 0 \end{pmatrix}$	$e = \begin{pmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & -1 \end{pmatrix}$	$f = \begin{pmatrix} 0 & -1 & 0 \\ -1 & 0 & 0 \\ 0 & 0 & -1 \end{pmatrix}$
$g = \begin{pmatrix} 0 & -1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 1 \end{pmatrix}$	$h = \begin{pmatrix} -1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & -1 \end{pmatrix}$	$i = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -1 \end{pmatrix}$
$j = \begin{pmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$	$k = \begin{pmatrix} 0 & -1 & 0 \\ -1 & 0 & 0 \\ 0 & 0 & 1 \end{pmatrix}$	$l = \begin{pmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 1 \end{pmatrix}$
$m = \begin{pmatrix} 0 & 1 & 0 \\ -1 & 0 & 0 \\ 0 & 0 & -1 \end{pmatrix}$	$n = \begin{pmatrix} 0 & -1 & 0 \\ 1 & -1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$	

Table 2: Conversions for the components of translation vectors in the space group encoding scheme.

$A = \frac{1}{6}$	$B = \frac{1}{4}$	$C = \frac{1}{3}$	$D = \frac{1}{2}$	$E = \frac{2}{3}$	$F = \frac{3}{4}$
$G = \frac{5}{6}$	$O = 0$	$X = -\frac{3}{8}$	$Y = -\frac{1}{4}$	$Z = -\frac{1}{8}$	

¹Four errors in the generator strings (for space groups 90, 107, 108, and 214) were pointed out by Matthew G. O'Brien and were corrected in this document on 9/25/2011.

Table 3: Generator strings for the 230 space groups.

Space Group	Generators	Space Group	Generators
1- P1 (C_1^1)	000	2- P1 (C_1^1)	100
3- P2 (C_2^1)	$01c0000$	4- P2₁ (C_2^2)	$01c0D00$
5- C2 (C_2^3)	$02aDDOc0000$	6- Pm (C_s^1)	$01j0000$
7- Pc (C_s^2)	$01j0OD0$	8- Cm (C_s^3)	$02aDDOj0000$
9- Cc (C_s^4)	$02aDDOjOOD0$	10- P2/m (C_{2h}^1)	$11c0000$
11- P2₁/m (C_{2h}^2)	$11cOD00$	12- C2/m (C_{2h}^3)	$12aDDOc0000$
13- P2/c (C_{2h}^4)	$11cOOD0$	14- P2₁/c (C_{2h}^5)	$11cODD0$
15- C2/c (C_{2h}^6)	$12aDDOcOOD0$	16- P222 (D_2^1)	$02b000c0000$
17- P222₁ (D_2^2)	$02bOODcOOD0$	18- P2₁2₁2 (D_2^3)	$02b000cDD00$
19- P2₁2₁2₁ (D_2^4)	$02bDODcODD0$	20- C222₁ (D_2^5)	$03aDDObOODcOOD0$
21- C222 (D_2^6)	$03aDDOb000c0000$	22- F222 (D_2^7)	$04aODDaDODb000c0000$
23- I222 (D_2^8)	$03aDDDOb000c0000$	24- I2₁2₁2₁ (D_2^9)	$03aDDDbDODcODD0$
25- Pmm2 (C_{2v}^1)	$02b000j0000$	26- Pmc2₁ (C_{2v}^2)	$02bOODjOOD0$
27- Pcc2 (C_{2v}^3)	$02b000jOOD0$	28- Pma2 (C_{2v}^4)	$02b000jD000$
29- Pca2₁ (C_{2v}^5)	$02bOODjD000$	30- Pnc2 (C_{2v}^6)	$02b000jODD0$
31- Pmn2₁ (C_{2v}^7)	$02bDODjDOD0$	32- Pba2 (C_{2v}^8)	$02b000jDD00$
33- Pna2₁ (C_{2v}^9)	$02bOODjDD00$	34- Pnn2 (C_{2v}^{10})	$02b000jDDD0$
35- Cmm2 (C_{2v}^{11})	$03aDDOb000j0000$	36- Cmc2₁ (C_{2v}^{12})	$03aDDObOODjOOD0$
37- Ccc2 (C_{2v}^{13})	$03aDDOb000jOOD0$	38- Amm2 (C_{2v}^{14})	$03aODDb000j0000$
39- Abm2 (C_{2v}^{15})	$03aODDb000cODD0$	40- Ama2 (C_{2v}^{16})	$03aODDb000jD000$
41- Aba2 (C_{2v}^{17})	$03aODDb000jD000$	42- Fmm2 (C_{2v}^{18})	$04aODDaDODb000j0000$
43- Fdd2 (C_{2v}^{19})	$04aODDaDODb000jBBB0$	44- Imm2 (C_{2v}^{20})	$03aDDDOb000j0000$
45- Iba2 (C_{2v}^{21})	$03aDDDOb000jD000$	46- Ima2 (C_{2v}^{22})	$03aDDDOb000jD000$
47- Pmmm (D_{2h}^1)	$12b000c0000$	48- Pnnn (D_{2h}^2)	$03b000c000hDDD1BBB$
49- Pccm (D_{2h}^3)	$12b000cODD0$	50- Pban (D_{2h}^4)	$03b000c000hDDO1BBO$
51- Pmma (D_{2h}^5)	$12bD00c0000$	52- Pnna (D_{2h}^6)	$12bD00cDDD0$
53- Pmna (D_{2h}^7)	$12bDODcDOD0$	54- Pcca (D_{2h}^8)	$12bD00cOOD0$
55- Pbam (D_{2h}^9)	$12b000cDDO0$	56- Pccn (D_{2h}^{10})	$12bDDOcODD0$
57- Pbcm (D_{2h}^{11})	$12bOODcODD0$	58- Pnnm (D_{2h}^{12})	$12b000cDDD0$
59- Pmmn (D_{2h}^{13})	$03b000cDDOhDDO1BBO$	60- Pbcn (D_{2h}^{14})	$12bDDDcOOD0$
61- Pbca (D_{2h}^{15})	$12bDODcODD0$	62- Pnma (D_{2h}^{16})	$12bDODcODD0$
63- Cmcm (D_{2h}^{17})	$13aDDObOODcODD0$	64- Cmca (D_{2h}^{18})	$13aDDObODDcODD0$
65- Cmmm (D_{2h}^{19})	$13aDDOb000c0000$	66- Cccm (D_{2h}^{20})	$13aDDOb000cOOD0$
67- Cmma (D_{2h}^{21})	$13aDDObODOcODD0$	68- Ccca (D_{2h}^{22})	$04aDDObDDOc000hODD1OBB$
69- Fmmm (D_{2h}^{23})	$14aODDaDODb000c0000$	70- Fddd (D_{2h}^{24})	$05aODDaDODb000c000hBBB1ZZZ$
71- Immm (D_{2h}^{25})	$13aDDDOb000c0000$	72- Ibam (D_{2h}^{26})	$13aDDDOb000cDDO0$
73- Ibca (D_{2h}^{27})	$13aDDDObDODcODD0$	74- Imma (D_{2h}^{28})	$13aDDDObDODcODD0$
75- P4 (C_4^1)	$02b000g0000$	76- P4₁ (C_4^2)	$02bOODgOOB0$
77- P4₂ (C_4^3)	$02b000gOOD0$	78- P4₃ (C_4^4)	$02bOODgOOF0$
79- I4 (C_4^5)	$03aDDDOb000g0000$	80- I4₁ (C_4^6)	$03aDDDObDDgODB0$

Table 3: Generator strings for the 230 space groups (continued).

Space Group	Generators	Space Group	Generators
81– P4 (S_4^1)	$02bOOOmOOO0$	82– I4 (S_4^2)	$03aDDDbOOOmOOO0$
83– P4/m (C_{4h}^1)	$12bOOOgOOO0$	84– P4₂/m (C_{4h}^2)	$12bOOOgOOD0$
85– P4/n (C_{4h}^3)	$03bOOOgDDOhDDO1YBO$	86– P4₂/n (C_{4h}^4)	$03bOOOgDDDbDDDD1YYY$
87– I4/m (C_{4h}^5)	$13aDDDbOOOgOOO0$	88– I4₁/a (C_{4h}^6)	$04aDDDbDDDbODDbODD1OYZ$
89– P4₂₂ (D_4^1)	$03bOOOgOOOcOOO0$	90– P4₂₁₂ (D_4^2)	$03bOOOgDDOcDDO0$
91– P4₁₂₂ (D_4^3)	$03bOODgOOBcOOO0$	92– P4₁₂₁₂ (D_4^4)	$03bOODgDDBcDDB0$
93– P4₂₂₂ (D_2^5)	$03bOOOgOODcOOO0$	94– P4₂₂₁₂ (D_2^6)	$03bOOOgDDDbDDO0$
95– P4₃₂₂ (D_4^7)	$03bOODgOOFcOOO0$	96– P4₃₂₁₂ (D_4^8)	$03bOODgDDFcDDF0$
97– I4₂₂ (D_4^9)	$04aDDDbOOOgOOOcOOO0$	98– I4₁₂₂ (D_4^{10})	$04aDDDbDDDbODDbODD0$
99– P4mm (C_{4v}^1)	$03bOOOgOOOjOOO0$	100– P4bm (C_{4v}^2)	$03bOOOgOOOjDDO0$
101– P4₂cm (C_{4v}^3)	$03bOOOgOODjOOD0$	102– P4₂nm (C_{4v}^4)	$03bOOOgDDDbDDO0$
103– P4cc (C_{4v}^5)	$03bOOOgOOOjOOD0$	104– P4nc (C_{4v}^6)	$03bOOOgOOOjDDO0$
105– P4₂mc (C_{4v}^7)	$03bOOOgOODjOOO0$	106– P4₂bc (C_{4v}^8)	$03bOOOgOODjDDO0$
107– I4mm (C_{4v}^9)	$04aDDDbOOOgOOOjOOO0$	108– I4cm (C_{4v}^{10})	$04aDDDbOOOgOOOjOOD0$
109– I4₁md (C_{4v}^{11})	$04aDDDbDDDbODDbjOOO0$	110– I4₁cd (C_{4v}^{12})	$04aDDDbDDDbODDbjOOD0$
111– P4₂m (D_{2d}^1)	$03bOOOmOOOcOOO0$	112– P4₂c (D_{2d}^2)	$03bOOOmOOOcOOD0$
113– P4₂₁m (D_{2d}^3)	$03bOOOmOOOcDDO0$	114– P4₂₁c (D_{2d}^5)	$03bOOOmOOOcDDD0$
115– P4₂m (D_{2d}^5)	$03bOOOmOOOjOOO0$	116– P4₂c (D_{2d}^6)	$03bOOOmOOOjOOD0$
117– P4₂b (D_{2d}^7)	$03bOOOmOOOjDDO0$	118– P4₂n (D_{2d}^8)	$03bOOOmOOOjDDD0$
119– I4₂m (D_{2d}^9)	$04aDDDbOOOmOOOjOOO0$	120– I4₂c (D_{2d}^{10})	$04aDDDbOOOmOOOjOOD0$
121– I4₂m (D_{2d}^{11})	$04aDDDbOOOmOOOcOOO0$	122– I4₂d (D_{2d}^{12})	$04aDDDbOOOmOOOcDOF0$
123– P4/mmm (D_{4h}^1)	$13bOOOgOOOcOOO0$	124– P4/mcc (D_{4h}^2)	$13bOOOgOOOcOOD0$
125– P4/nbm (D_{4h}^3)	$04bOOOgOOOcOOOhDDO1YYO$	126– P4/nnc (D_{4h}^4)	$04bOOOgOOOcOOOhDDDD1YYY$
127– P4/mbm (D_{4h}^5)	$13bOOOgOOOcDDO0$	128– P4/mnc (D_{4h}^6)	$13bOOOgOOOcDDD0$
129– P4/nmm (D_{4h}^7)	$04bOOOgDDOcDDOhDDO1YBO$	130– P4/ncc (D_{4h}^8)	$04bOOOgDDOcDDDbDDO1YBO$
131– P4₂/mmc (D_{4h}^9)	$13bDDOgDDOcODD0$	132– P4₂/mcm (D_{4h}^{10})	$13bOOOgODDcOOD0$
133– P4₂/nbc (D_{4h}^{11})	$04bOOOgDDDbODDhDDDD1YBY$	134– P4₂/nnm (D_{4h}^{12})	$04bOOOgDDDbOOOhDDDD1YBY$
135– P4₂/mbc (D_{4h}^{13})	$13bOOOgODDcDDO0$	136– P4₂/mnm (D_{4h}^{14})	$13bOOOgDDDbDDD0$
137– P4₂/nmc (D_{4h}^{15})	$04bOOOgDDDbDDDbDDDD1YBY$	138– P4₂/ncm (D_{4h}^{16})	$04bOOOgDDDbDDOhDDDD1YBY$
139– I4/mmm (D_{4h}^{17})	$14aDDDbOOOgOOOcOOO0$	140– I4/mcm (D_{4h}^{18})	$14aDDDbOOOgOOOcOOD0$
141– I4₁/amd (D_{4h}^{19})	$05aDDDbDDDbODDbDOFhODD1OBZ$	142– I4₁/acd (D_{4h}^{20})	$05aDDDbDDDbODDbDOBhODD1OBZ$
143– P3 (C_3^1)	$01nOOO0$	144– P3₁ (C_3^2)	$01nOOC0$
145– P3₂ (C_3^3)	$01nOOE0$	146– R3 (C_3^4)	$02aECCnOOO0$
147– P3 (C_{3i}^1)	$11nOOO0$	148– R3 (C_{3i}^2)	$12aECCnOOO0$
149– P3₁₂ (D_3^1)	$02nOOOfOOO0$	150– P3₂₁ (D_3^2)	$02nOOOcOOO0$
151– P3₁₁₂ (D_3^3)	$02nOOCfOOE0$	152– P3₁₂₁ (D_3^4)	$02nOOCeOOO0$
153– P3₂₁₂ (D_3^5)	$02nOOEfOOC0$	154– P3₂₂₁ (D_3^6)	$02nOOEeOOO0$
155– R3₂ (D_3^7)	$03aECCnOOOcOOO0$	156– P3m1 (C_{3v}^1)	$02nOOOkOOO0$
157– P3₁m (C_{3v}^2)	$02nOOOlOOO0$	158– P3c1 (C_{3v}^3)	$02nOOOkOOD0$
159– P3₁c (C_{3v}^4)	$02nOOOlOOD0$	160– R3m (C_{3v}^5)	$03aECCnOOOkOOO0$

Table 3: Generator strings for the 230 space groups (continued).

Space Group	Generators	Space Group	Generators
161– R3c (C_{3v}^6)	$03aECCnOOOkOOD0$	162– P31m (D_{3d}^1)	$12nOOOfOOO0$
163– P31c (D_{3d}^2)	$12nOOOfOOD0$	164– P3m1 (D_{3d}^3)	$12nOOOeOOO0$
165– P3c1 (D_{3d}^4)	$12nOOOeOOD0$	166– R3m (D_{3d}^5)	$13aECCnOOOeOOO0$
167– R3c (D_{3d}^6)	$13aECCnOOOeOOD0$	168– P6 (C_6^1)	$02nOOObOOO0$
169– P6₁ (C_6^2)	$02nOOCbOOD0$	170– P6₅ (C_6^3)	$02nOOEbOOD0$
171– P6₂ (C_6^4)	$02nOOEbOOO0$	172– P6₄ (C_6^5)	$02nOOCbOOO0$
173– P6₃ (C_6^6)	$02nOOObOOD0$	174– P6 (C_{3h}^1)	$02nOOOiOOO0$
175– P6/m (C_{6h}^1)	$12nOOObOOO0$	176– P6₃/m (C_{6h}^2)	$12nOOObOOD0$
177– P622 (D_6^1)	$03nOOObOOOeOOO0$	178– P6₁22 (D_6^2)	$03nOOCbOODeOOC0$
179– P6₅22 (D_6^3)	$03nOOEbOODeOEE0$	180– P6₂22 (D_6^4)	$03nOOEbOOOeOEE0$
181– P6₄22 (D_6^5)	$03nOOCbOOOeOOC0$	182– P6₃22 (D_6^6)	$03nOOObOODeOOO0$
183– P6mm (C_{6v}^1)	$03nOOObOOOkOOO0$	184– P6cc (C_{6v}^2)	$03nOOObOOOkOOD0$
185– P6₃cm (C_{6v}^3)	$03nOOObOODkOOD0$	186– P6₃mc (C_{6v}^4)	$03nOOObOODkOOO0$
187– P6m2 (D_{3h}^1)	$03nOOOiOOOkOOO0$	188– P6c2 (D_{3h}^2)	$03nOOOiOODkOOD0$
189– P62m (D_{3h}^3)	$03nOOOiOOOeOOO0$	190– P62c (D_{3h}^4)	$03nOOOiOODeOOO0$
191– P6/mmm (D_{6h}^1)	$13nOOObOOOeOOO0$	192– P6/mcc (D_{6h}^2)	$13nOOObOOOeOOD0$
193– P6₃/mcm (D_{6h}^3)	$13nOOObOODeOOD0$	194– P6₃/mmc (D_{6h}^4)	$13nOOObOODeOOO0$
195– P23 (T^1)	$03bOOOcOOOdOOO0$	196– F23 (T^2)	$05aODDaDODbOOOcOOOdOOO0$
197– I23 (T^3)	$04aDDDbOOOcOOOdOOO0$	198– P2₁3 (T^4)	$03bDODcODDdOOO0$
199– I2₁3 (T^5)	$04aDDDbDODcODDdOOO0$	200– Pm3 (T_h^1)	$13bOOOcOOOdOOO0$
201– Pn3 (T_h^2)	$04bOOOcOOOdOOOhDDD1YYY$	202– Fm3 (T_h^3)	$15aODDaDODbOOOcOOOdOOO0$
203– Fd3 (T_h^4)	$06aODDaDODbOOOcOOOdOOOhBBB1ZZZ$	204– Im3 (T_h^5)	$14aDDDbOOOcOOOdOOO0$
205– Pa3 (T_h^6)	$13bDODcODDdOOO0$	206– Ia3 (T_h^7)	$14aDDDbDODcODDdOOO0$
207– P432 (O^1)	$04bOOOcOOOdOOOeOOO0$	208– P4₂32 (O^2)	$04bOOOcOOOdOOOeDDD0$
209– F432 (O^3)	$06aODDaDODbOOOcOOOdOOOeOOO0$	210– F4₁32 (O^4)	$06aODDaDODbODDcDDOdOOOeFBF0$
211– I432 (O^5)	$05aDDDbOOOcOOOdOOOeOOO0$	212– P4₃32 (O^6)	$04bDODcODDdOOOeBFF0$
213– P4₁32 (O^7)	$04bDODcODDdOOOeFBB0$	214– I4₁32 (O^8)	$05aDDDbDODcODDdOOOeFBB0$
215– P43m (T_d^1)	$04bOOOcOOOdOOOlOOO0$	216– F43m (T_d^2)	$06aODDaDODbOOOcOOOdOOOlOOO0$
217– I43m (T_d^3)	$05aDDDbOOOcOOOdOOOlOOO0$	218– P43n (T_d^4)	$04bOOOcOOOdOOOlDDD0$
219– F43c (T_d^5)	$06aODDaDODbOOOcOOOdOOOlDDD0$	220– I43d (T_d^6)	$05aDDDbDODcODDdOOOlBBB0$
221– Pm3m (O_h^1)	$14bOOOcOOOdOOOeOOO0$	222– Pn3n (O_h^2)	$14bDDOcDODdOOOeOOD1YYY$
223– Pm3n (O_h^3)	$14bOOOcOOOdOOOeDDD0$	224– Pn3m (O_h^4)	$05bOOOcOOOdOOOeDDDbDDD1YYY$
225– Fm3m (O_h^5)	$16aODDaDODbOOOcOOOdOOOeOOO0$	226– Fm3c (O_h^6)	$16aODDaDODbOOOcOOOdOOOeDDD0$
227– Fd3m (O_h^7)	$07aODDaDODbODDcDDOdOOOeFBFhBBB1ZZZ$	228– Fd3c (O_h^8)	$07aODDaDODbODDcDDOdOOOeFBFhFFF1XXX$
229– Im3m (O_h^9)	$15aDDDbOOOcOOOdOOOeOOO0$	230– Ia3d (O_h^{10})	$15aDDDbDODcODDdOOOeFBB0$