Simulation.rewrite.rst

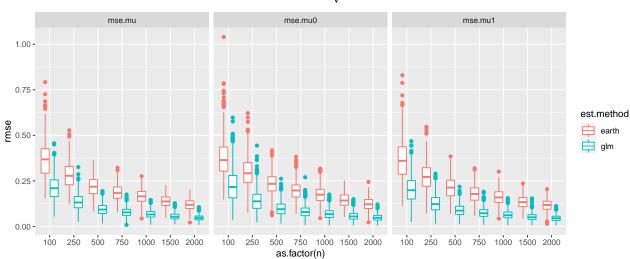
1 Scenario 1

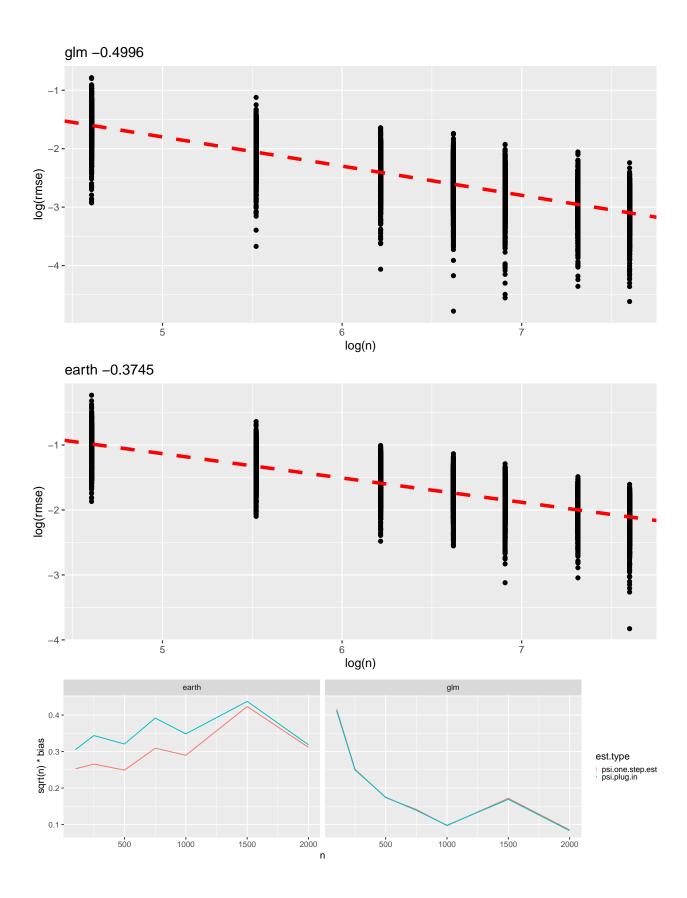
- W_1 , W_2 and W_3 are all continuous random variables
- no interaction term in $Y \sim A + W$, i.e., $\tau(W)$ is a constant

$$\begin{split} W_1 \sim Unif(-1,1) \\ W_2 \sim Unif(-1,1) \\ W_3 \sim Unif(-1,1) \\ A \sim Bernoulli(\pi_0) \ where \ \pi_0 = expit(0.5 + \frac{1}{3}W_1) \\ Y \sim N(\mu_0,1) \\ \mu_0(A,W) = 0.1 + 0.2 * A + 0.5 * W_1 - 0.3 * W_2 + 0.1 * W_3 \\ \mu_0(1,W) = 0.3 + 0.5 * W_1 - 0.3 * W_2 + 0.1 * W_3 \\ \mu_0(0,W) = 0.1 + 0.5 * W_1 - 0.3 * W_2 + 0.1 * W_3 \\ \tau(W) = 0.2 \\ \psi_0 = 0.04 \\ \theta_0 = 0 \end{split}$$

$glm: glm(Y \sim ., data=AW, family='gaussian')$ # earth: SL.library = c("SL.earth")

$$rmse = \frac{\sqrt{\sum (\hat{\mu} - \mu_0)^2}}{\sqrt{n}}$$





3 Scenario 3

$$\begin{split} W_1 \sim Unif(-1,1) \\ W_2 \sim Unif(-1,1) \\ W_3 \sim Bernoulli(0.5) \\ A \sim Bernoulli(\pi_0) \ where \ \pi_0 = expit(0.5 + \frac{1}{3}W_1) \\ Y \sim N(\mu_0,1) \ where \ \mu_0 = 0.1 + 0.25 * A + 0.75A(W_1^2 + W_3) + W_1 + W_2^2 \\ \tau(W) = 0.25 + 0.75 * (W_1^2 + W_3) \\ \psi_0 = 0.956 \\ \theta_0 = 0.191 \end{split}$$

```
# gam.correct: gam.model <- as.formula("Y ~ W1 + I(W2^2) + I(W1^2):A + A*W3") # earth: SL.library = c("SL.earth") # gam.mgcv: gam.model <- as.formula("Y ~ s(W1) + s(W2) + s(W1, by=A) + s(W2, by=A) + A*W3") # mu.reg <- mgcv:: gam(gam.model, data = AW, method = "REML")
```

