

## ESE 546, FALL 2022

### HOMEWORK 1

RUI JIANG [RJIANG6@SEAS.UPENN.EDU]

**Solution 1** (Time spent: 1 hour).

**Part (a):** The slack variable formulation allows some data points to violate the margin constraint. To minimize these violations while still maximizing the margin, we add a penalty term to the objective function.

One common formulation is:

$$\begin{aligned} \text{minimize} \quad & \frac{1}{2} \|\theta\|^2 + \frac{1}{n} \sum_{i=1}^n \xi_i \\ \text{subject to} \quad & y_i(\theta^T x_i + \theta_0) \geq 1 - \xi_i, \quad \forall i = 1, \dots, n \\ & \xi_i \geq 0, \quad \forall i = 1, \dots, n \end{aligned}$$

where  $\frac{1}{n} \sum_{i=1}^n \xi_i$  is a normalized penalty by the number of samples.

**Solution 2** (Time spent: 1 hour). Your solution goes here.

**Solution 3** (Time spent: 1 hour). Your solution goes here.