

Understanding Attention Training via Output Relevance

Charlie Snell, Ruiqi Zhong, Jacob Steinhardt, Dan Klein



Outline

- Prior work on text classification:
 - Standardly trained attention \approx Explanations .
 - Can train models to attend to irrelevant words, same accuracy.
- Our work studies how the attention evolves at training time, for text classification and machine translation.



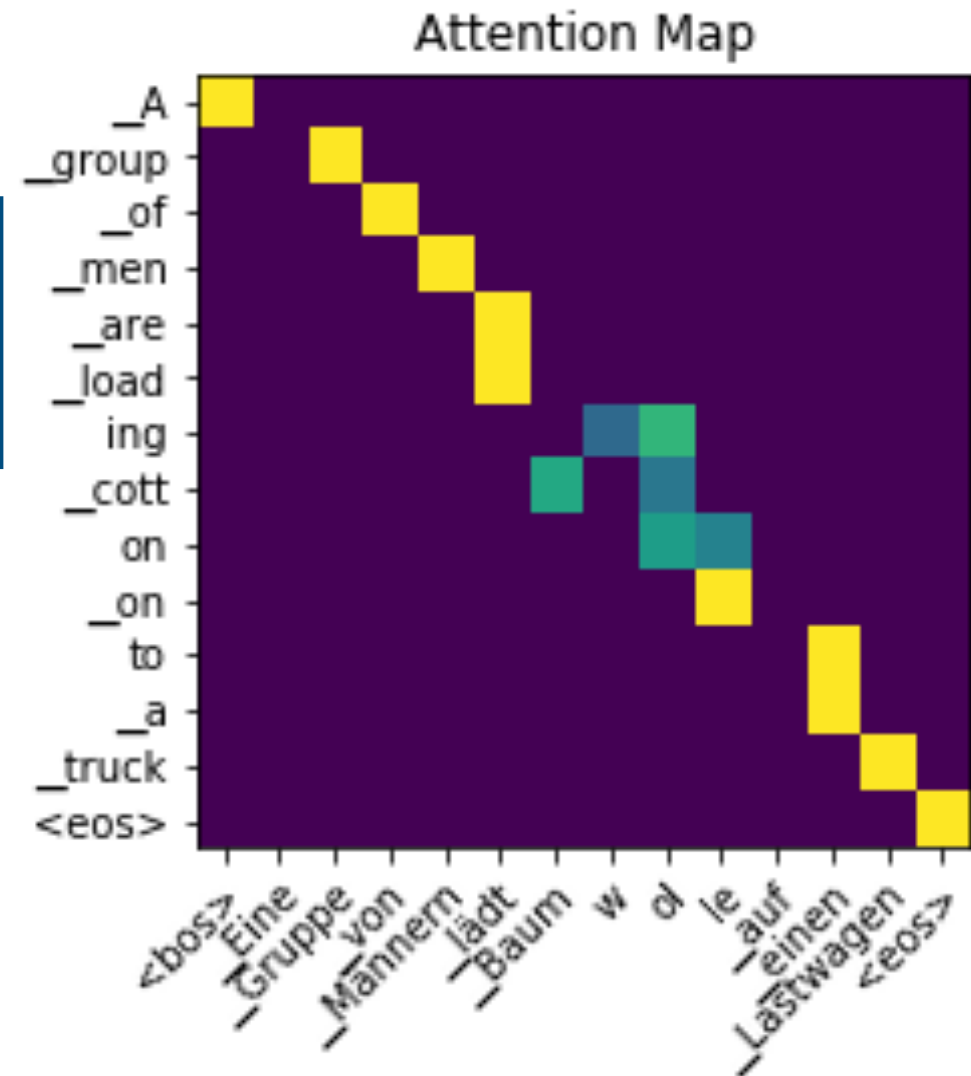
Attention Distribution over Inputs

Sentiment Classification

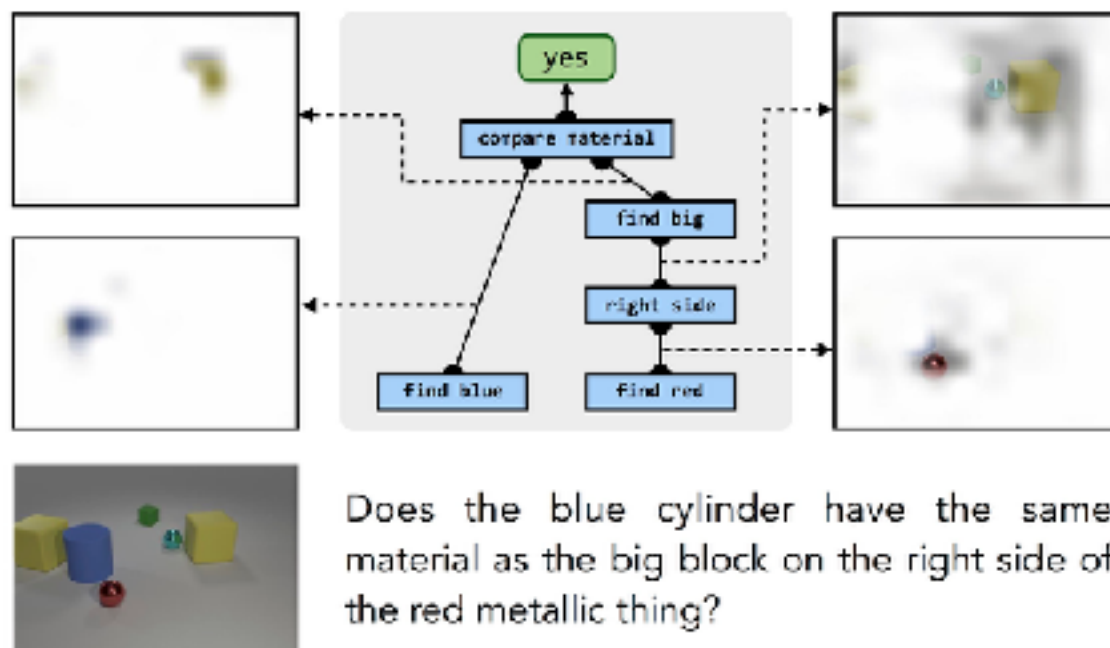
Negative

after 15 minutes watching the movie i was asking myself what to do leave the theater sleep or try to keep watching the movie to see if there was anything worth i finally watched the movie what a waste of time maybe i am not a 5 years old kid anymore

Seems to provide explanations !!



German -> English Translation



Visual Question Answering

Attention \approx Explanation?

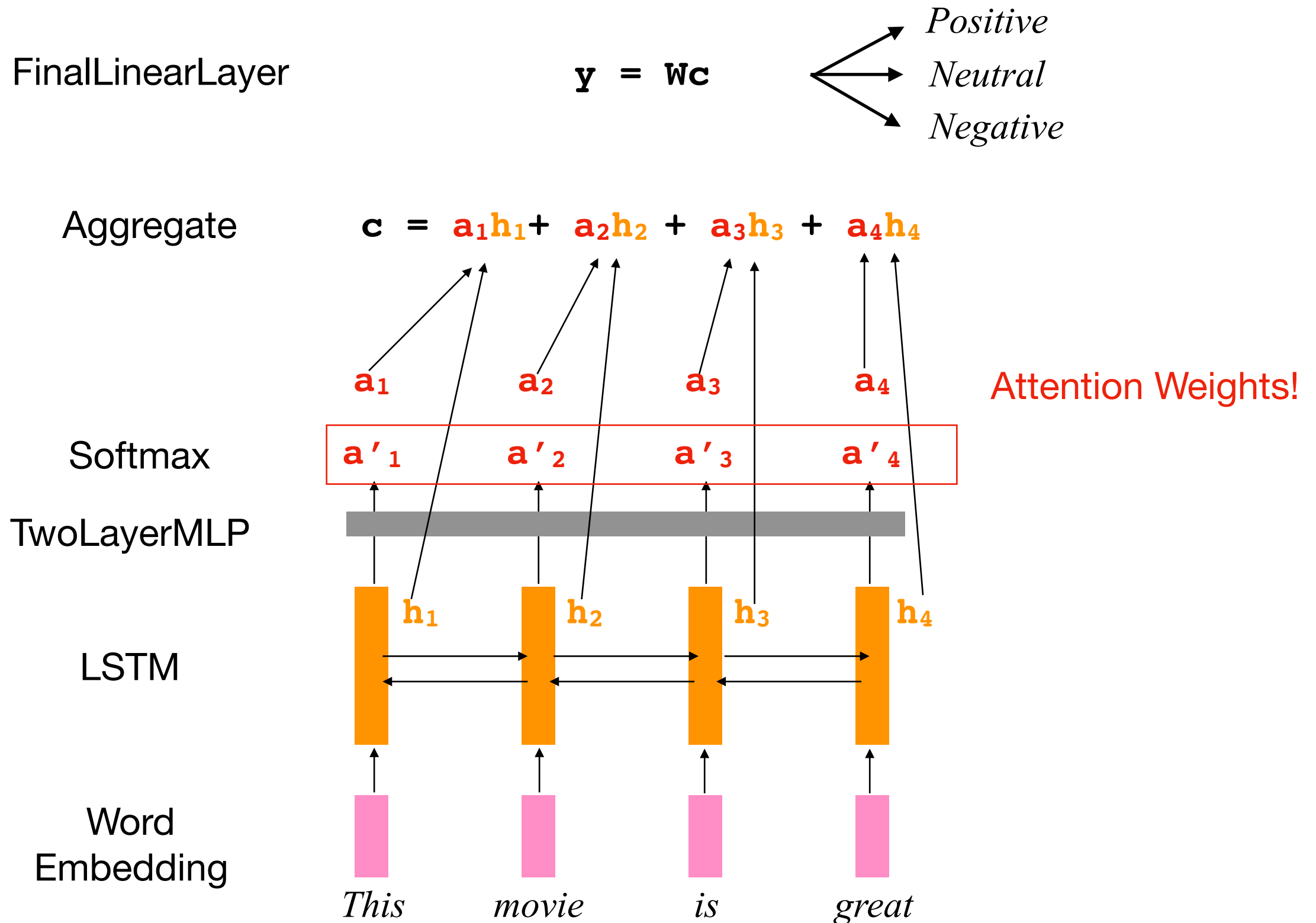
- Attention is not Explanation (Jain & Wallace 2019)
- Is Attention Interpretable? (Serrano & Smith 2019)
- Attention is not not Explanation (Wiegrefe & Pinter 2019)
- Attention Interpretability Across Tasks (Shikhar et al. 2019)
- Understanding Attention Training via Output Relevance (Snell et al. 2020)

A series of work trying to understand attention mechanism.

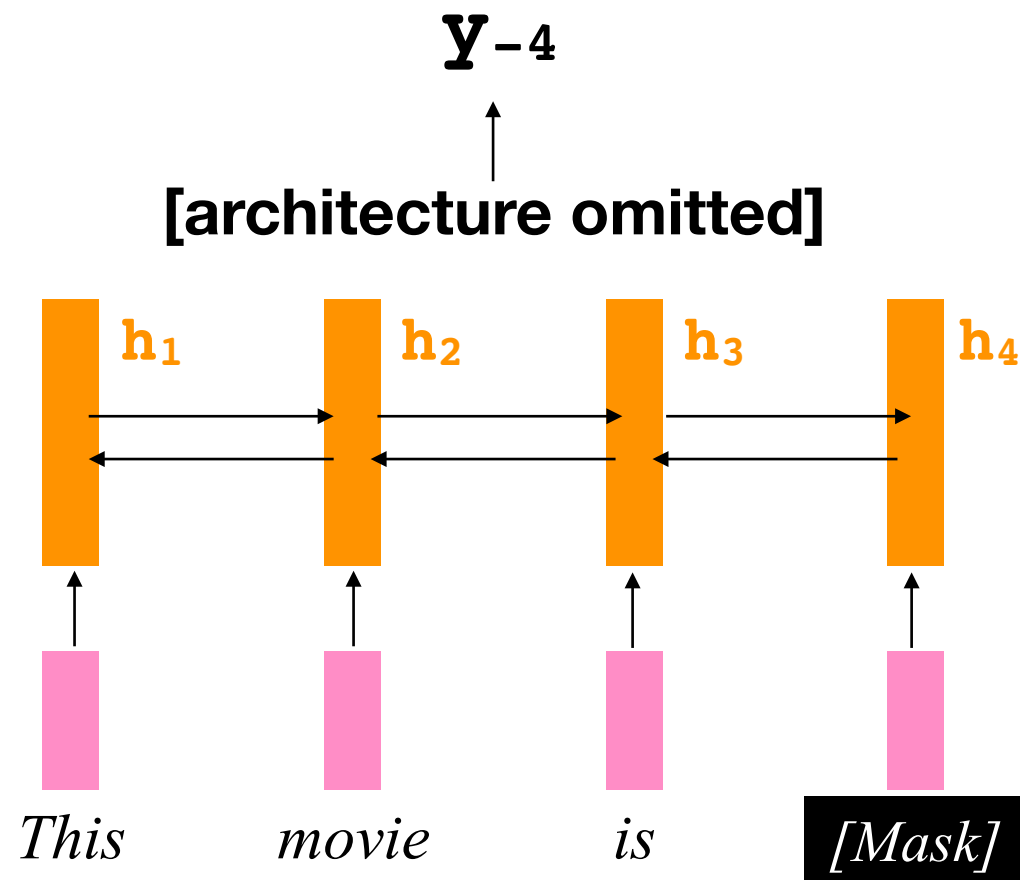
Prior Works on Classification

- If the model is trained in a standard way, attention weights correlate strongly with individual token influence.
- Uniform attention gives the same accuracy (attention does not matter) .
- Models can be trained to attend to irrelevant words, *without harming accuracy*.

Text Classification



Attention \approx Explanations



Leave-one-out influence:

$$\Delta_4 := y - y_{-4}$$

	<i>This</i>	<i>movie</i>	<i>is</i>	<i>great</i>	
Attention	\mathbf{a}_1	\mathbf{a}_2	\mathbf{a}_3	$\uparrow \mathbf{a}_4$	Strongly Correlates
Influence	Δ_1	Δ_2	Δ_3	$\uparrow \Delta_4$	

Train “Deceptive” Attention

Call a standard model P.
Now train the deceptive model Q.

$$\mathcal{L}(\mathcal{M}_P, \mathcal{M}_Q) = TVD(\hat{y}_P, \hat{y}_Q) - \lambda KL(\mathbf{a}_P || \mathbf{a}_Q)$$

Q makes similar
predictions as P.

Q attends
differently from P.

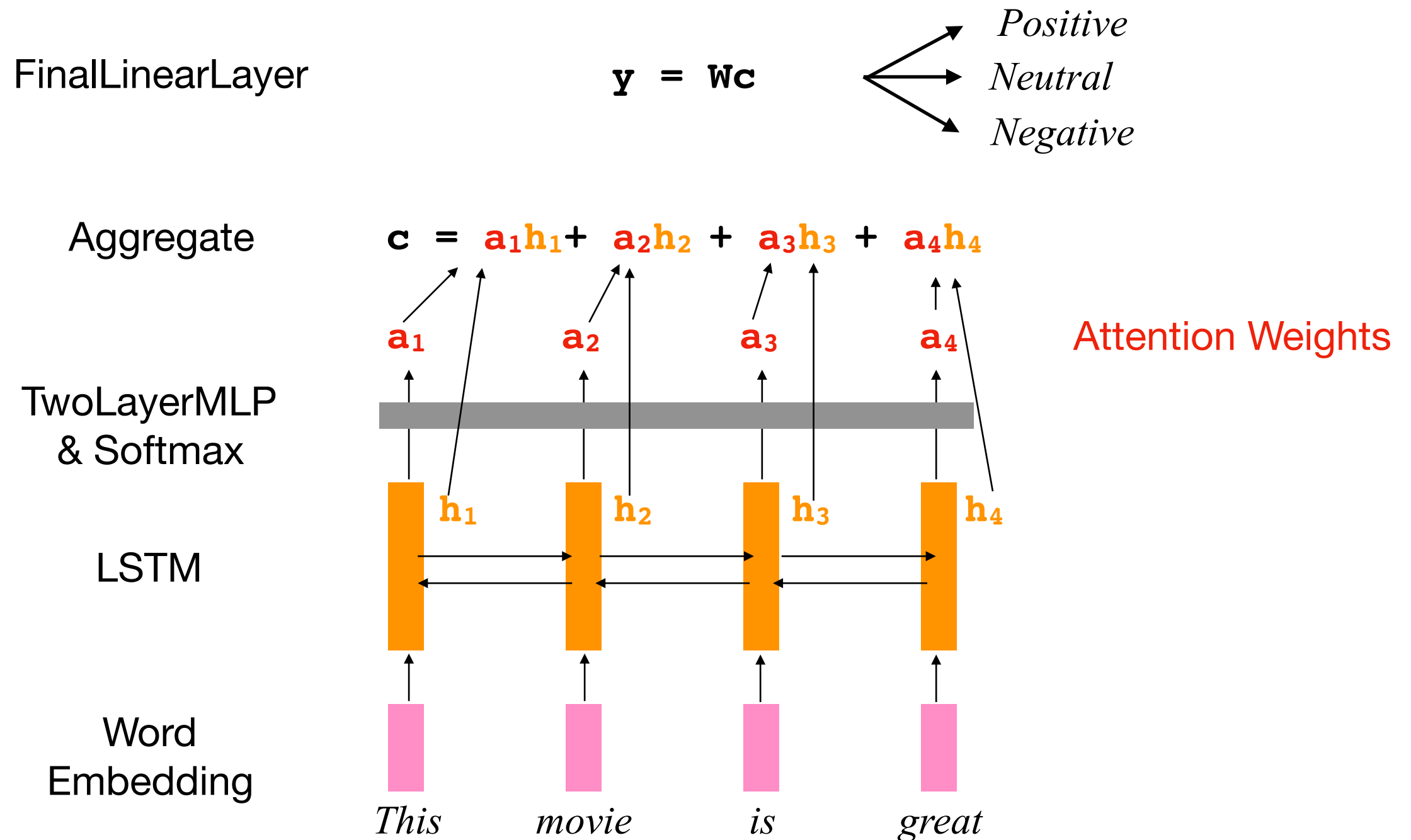
**Attention becomes anti-correlated
with explanations !**

Our Work:

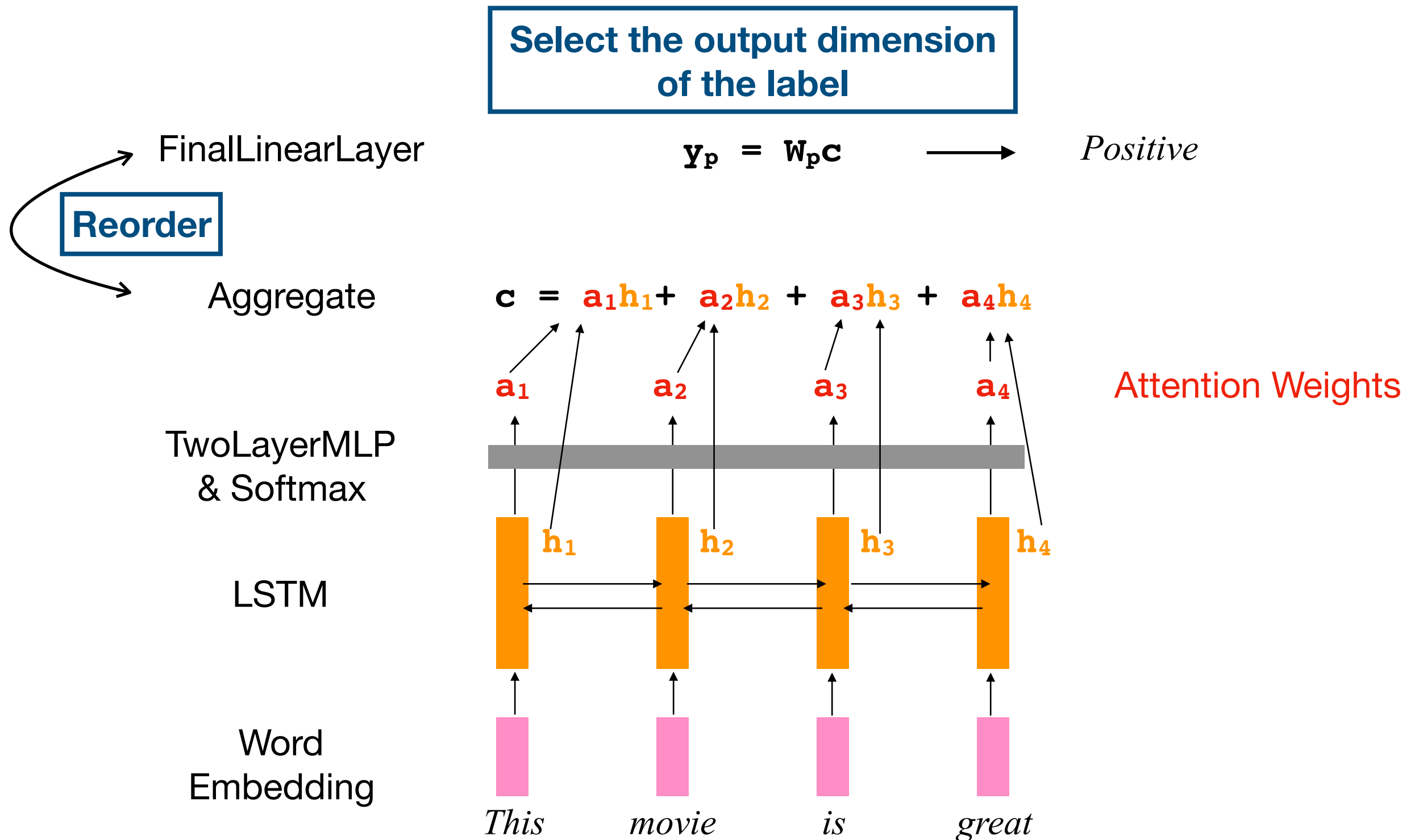
Understand Attention Training

- We can construct two models with the same loss but different attention weights.
- Need to open the black-box of standard training.

Defining Output Relevance



Defining Output Relevance



Defining Output Relevance

Training objective
optimizes y_p

Output Relevance r_4 :
how much does the model associate
 h_4 with the positive label

Aggregate

$$y_p = a_1 r_1 + a_2 r_2 + a_3 r_3 + a_4 r_4 \longrightarrow \text{Positive Logit}$$

FinalLinearLayer

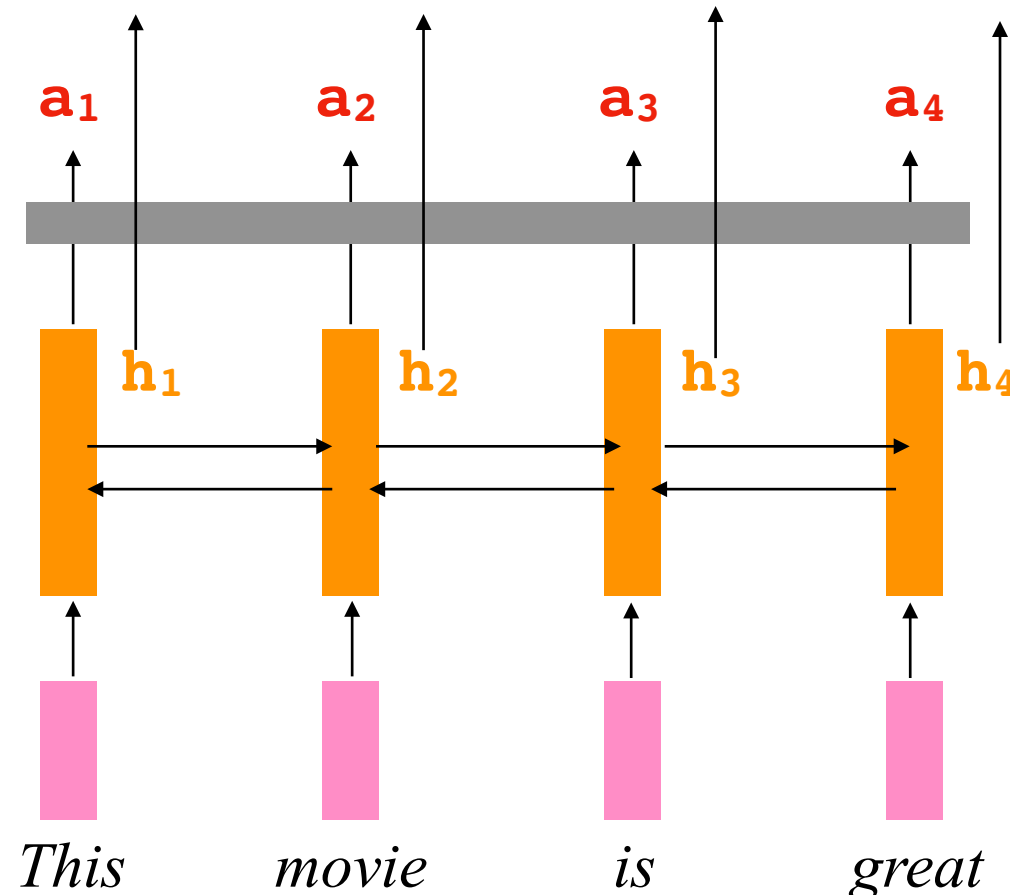
TwoLayerMLP
& Softmax

LSTM

Word
Embedding

$$r_1 = W_p h_1 \quad r_2 = W_p h_2 \quad r_3 = W_p h_3 \quad r_4 = W_p h_4$$

Attention Weights



Attention **a** and Output Relevance **r**

Training objective
maximizes y_p

Output Relevance **r**₄:
how much does the model associate
h₄ with the positive label

$$y_p = \mathbf{a}_1 \mathbf{r}_1 + \mathbf{a}_2 \mathbf{r}_2 + \mathbf{a}_3 \mathbf{r}_3 + \mathbf{a}_4 \mathbf{r}_4 \longrightarrow \text{Positive Logit}$$

- **a** attracted to larger **r**
- What is **a** and **r** when initialized? => both uniform
- How will **a** and **r** interact? Near the beginning, **a** remains uniform. Under uniform attention, **r** increases faster at "keyword" positions, then attracts **a**

Attention **a** and Output Relevance **r**

Training objective
maximizes y_p

Output Relevance **r**₄:
how much does the model associate
h₄ with the positive label

$$y_p = \mathbf{a}_1 \mathbf{r}_1 + \mathbf{a}_2 \mathbf{r}_2 + \mathbf{a}_3 \mathbf{r}_3 + \mathbf{a}_4 \mathbf{r}_4 \longrightarrow \text{Positive Logit}$$

- **a** attracted to larger **r**
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?

Intuition of Increasing r

Aggregate $\mathbf{y}_p = \mathbf{a}_1 \mathbf{r}_1 + \mathbf{a}_2 \mathbf{r}_2 + \mathbf{a}_3 \mathbf{r}_3 + \mathbf{a}_4 \mathbf{r}_4 \longrightarrow \text{Positive Logit}$

FinalLinearLayer

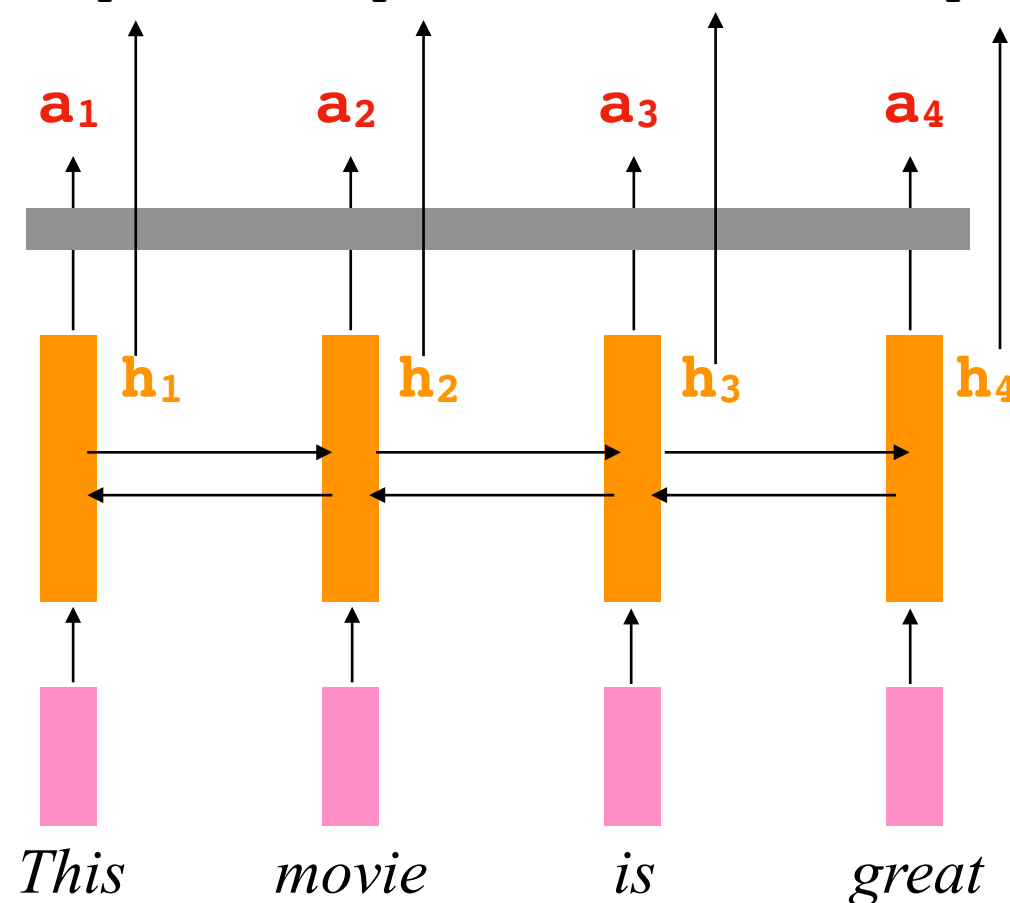
TwoLayerMLP
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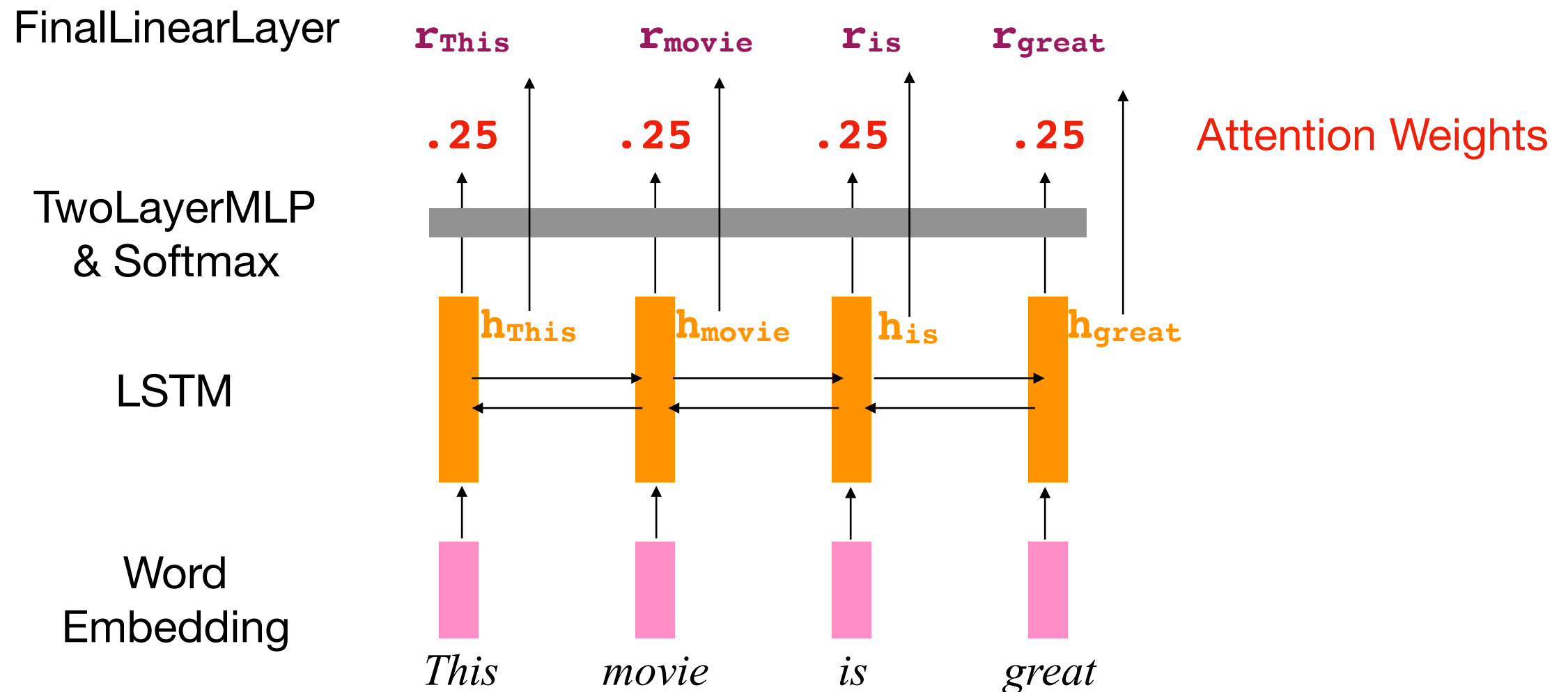
$$\mathbf{r}_1 = \mathbf{W}_p \mathbf{h}_1 \quad \mathbf{r}_2 = \mathbf{W}_p \mathbf{h}_2 \quad \mathbf{r}_3 = \mathbf{W}_p \mathbf{h}_3 \quad \mathbf{r}_4 = \mathbf{W}_p \mathbf{h}_4$$

Attention Weights



Intuition of Increasing r

Aggregate $\mathbf{y}_p = 0.25 (\mathbf{r}_{\text{This}} + \mathbf{r}_{\text{movie}} + \mathbf{r}_{\text{is}} + \mathbf{r}_{\text{great}}) \longrightarrow \text{Positive Logit}$



Intuition of Increasing r

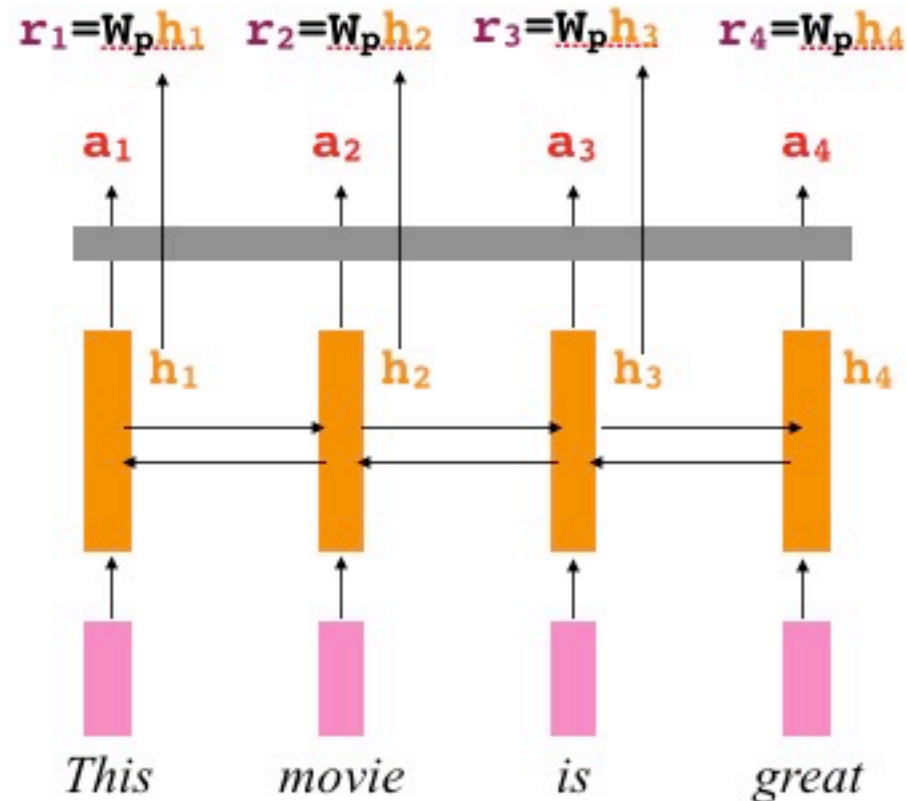
$$y_p = 0.25(r_{\text{This}} + r_{\text{movie}} + r_{\text{is}} + r_{\text{great}}) \longrightarrow \text{Positive Logit}$$

$$y_n = -0.25(r_{\text{This}} + r_{\text{movie}} + r_{\text{is}} + r_{\text{bad}}) \longrightarrow \text{Negative Logit}$$

- r_{This} , r_{movie} and r_{is} remains roughly unchanged (cancels out)
- r_{great} increases

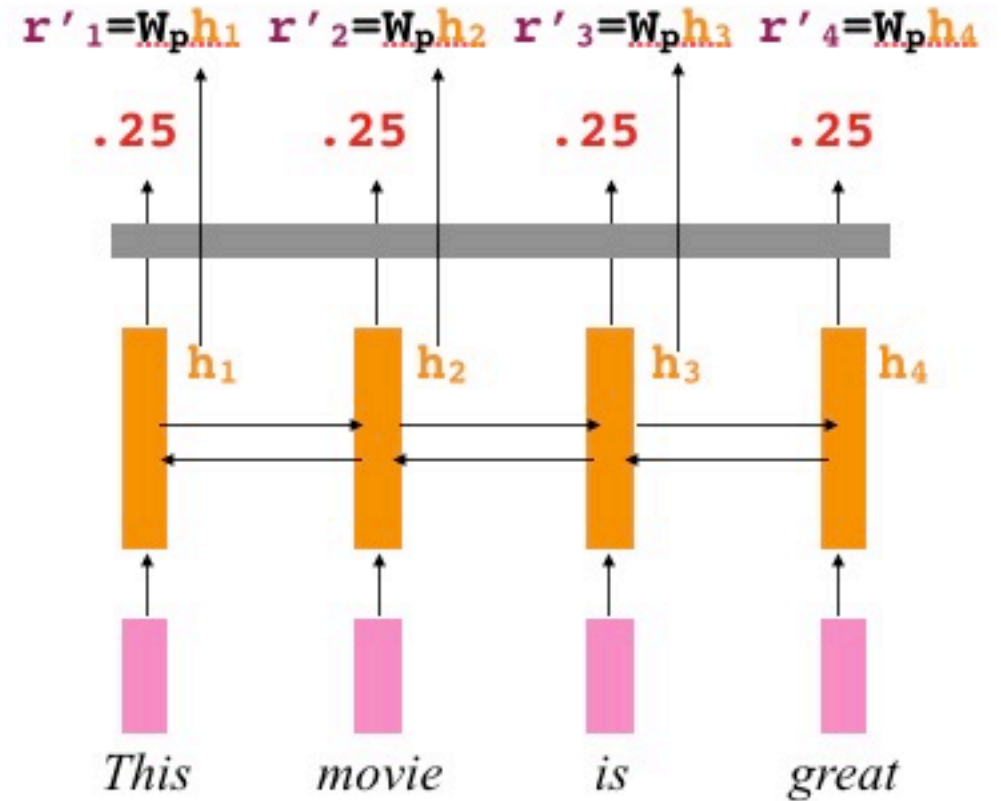
Increasing r Under Uniform Attention

$$\mathbf{y}_p = \mathbf{a}_1 \mathbf{r}_1 + \mathbf{a}_2 \mathbf{r}_2 + \mathbf{a}_3 \mathbf{r}_3 + \mathbf{a}_4 \mathbf{r}_4$$



standard training

$$\mathbf{y}_p = .25 (\mathbf{r}'_1 + \mathbf{r}'_2 + \mathbf{r}'_3 + \mathbf{r}'_4)$$

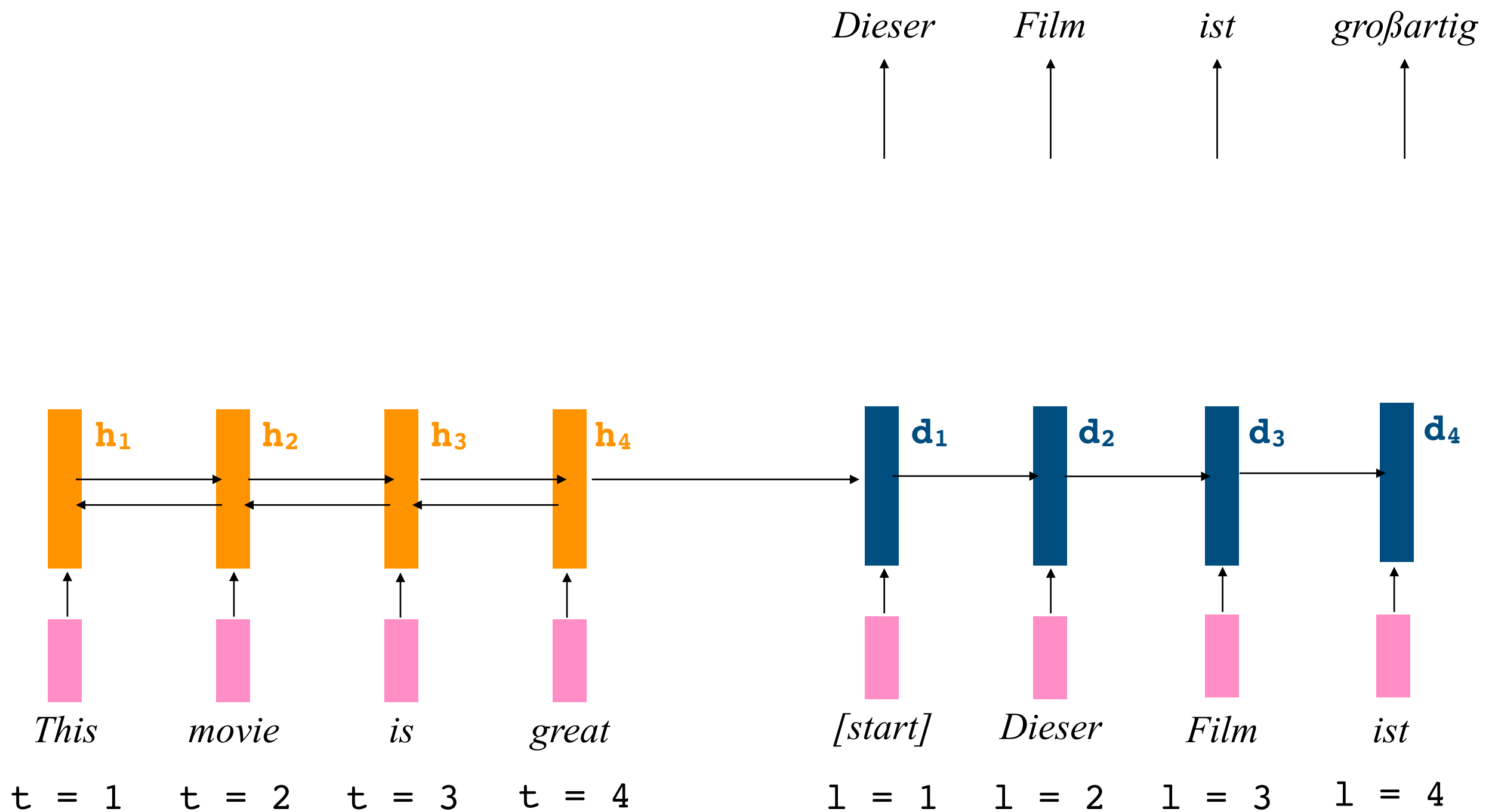


uniform attention training

- \mathbf{r}' still correlates with standard attention \mathbf{a}
- \mathbf{r}' correlates with individual token influence.

Seq2Seq Setup

(simplified)

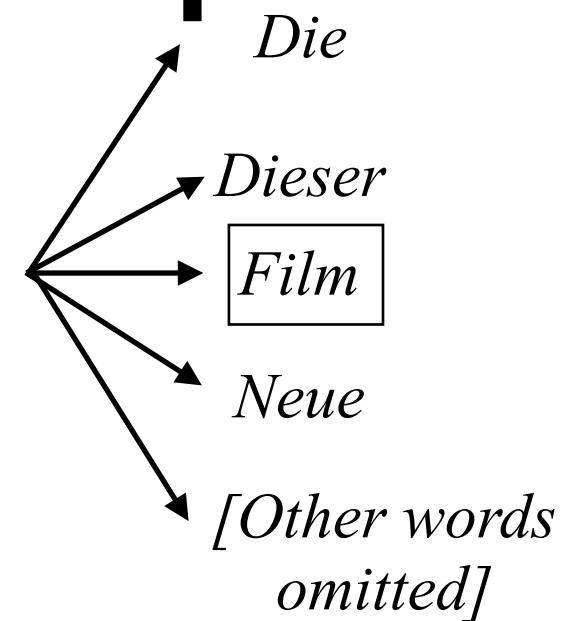


Seq2Seq Setup

(simplified)

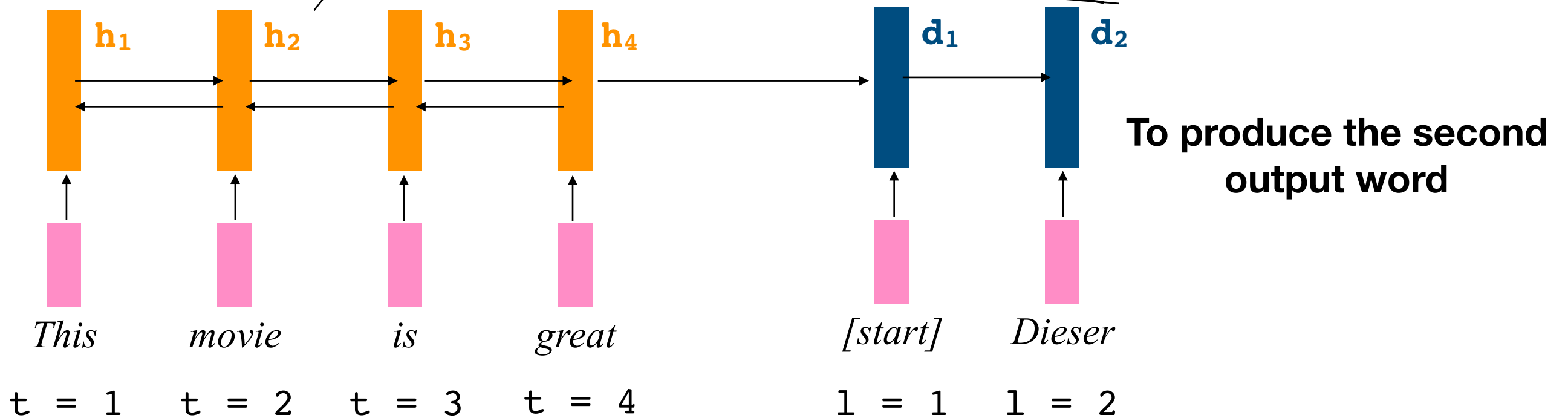
$$\mathbf{y}_2 = \mathbf{W}\mathbf{c}_2$$

$$\mathbf{c}_2 = \mathbf{a}_{21}\mathbf{h}_1 + \mathbf{a}_{22}\mathbf{h}_2 + \mathbf{a}_{23}\mathbf{h}_3 + \mathbf{a}_{24}\mathbf{h}_4$$



Reorder

$$\mathbf{a}'_{21} = \mathbf{h}_1\mathbf{d}_2 \quad \mathbf{a}'_{22} = \mathbf{h}_2\mathbf{d}_2 \quad \mathbf{a}'_{23} = \mathbf{h}_3\mathbf{d}_2 \quad \mathbf{a}'_{24} = \mathbf{h}_4\mathbf{d}_2$$



Seq2Seq Output Relevance

(simplified)

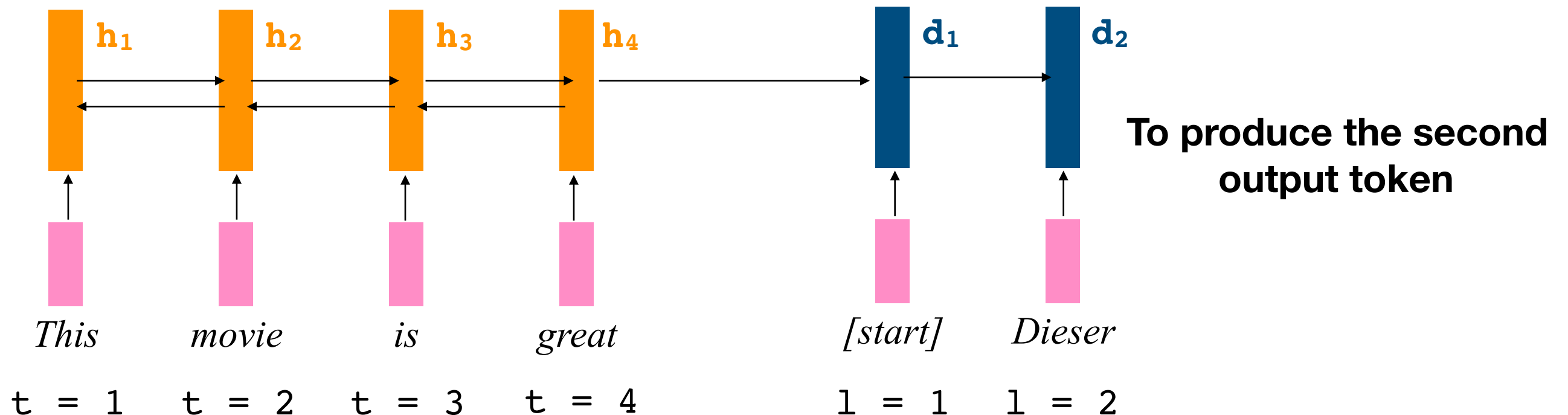
Training objective
optimizes $y_{2,\text{Film}}$

Output Relevance $r_{\text{Film},2}$:
how much does the model associate
 h_2 with the word “Film”

$$y_{2,\text{Film}} = a_{21}r_{\text{Film},1} + a_{22}r_{\text{Film},2} + a_{23}r_{\text{Film},3} + a_{24}r_{\text{Film},4}$$

$$r_{\text{Film},t} := W_{\text{Film}} h_t$$

$$a'_{21} = h_1 d_2 \quad a'_{22} = h_2 d_2 \quad a'_{23} = h_3 d_2 \quad a'_{24} = h_4 d_2$$



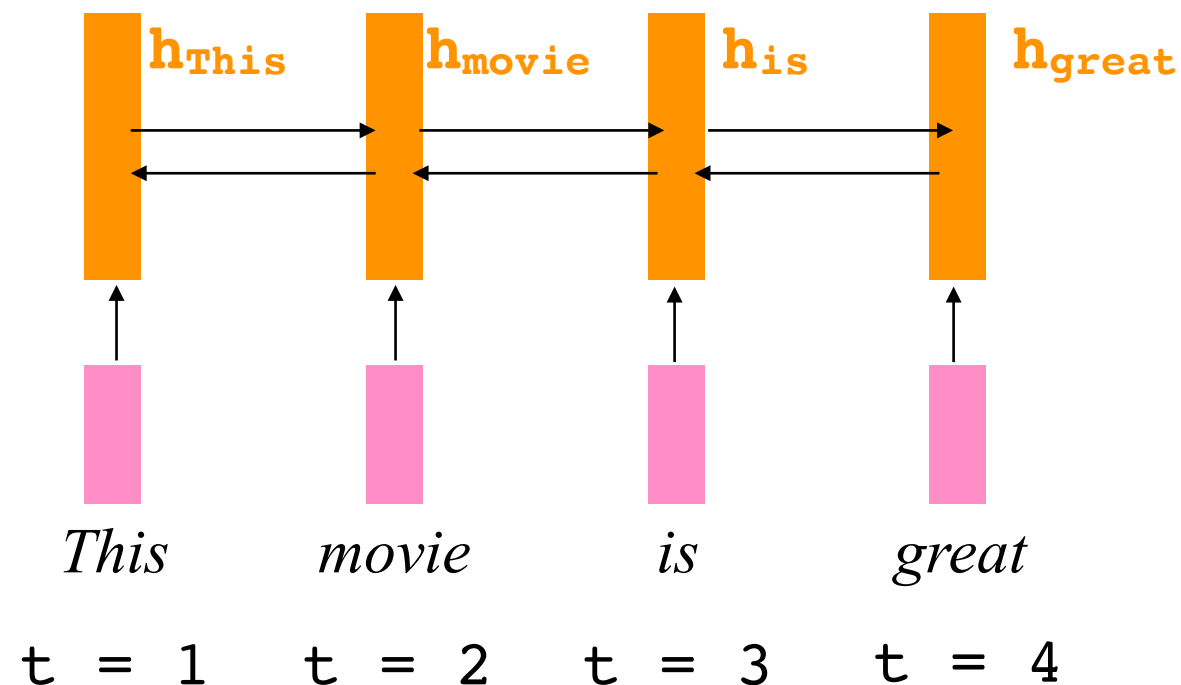
Intuition of Learning \mathbf{r} , “Dictionary”

Gradient update to maximize:

$$\text{Likelihood}(l = 2) = .25(\mathbf{r}_{\text{Film, This}} + \mathbf{r}_{\text{Film, movie}} + \mathbf{r}_{\text{Film, is}} + \mathbf{r}_{\text{Film, great}})$$

$\mathbf{r}_{\text{Film, This}}$ $\mathbf{r}_{\text{Film, movie}}$ $\mathbf{r}_{\text{Film, is}}$ $\mathbf{r}_{\text{Film, great}}$

.25 .25 .25 .25

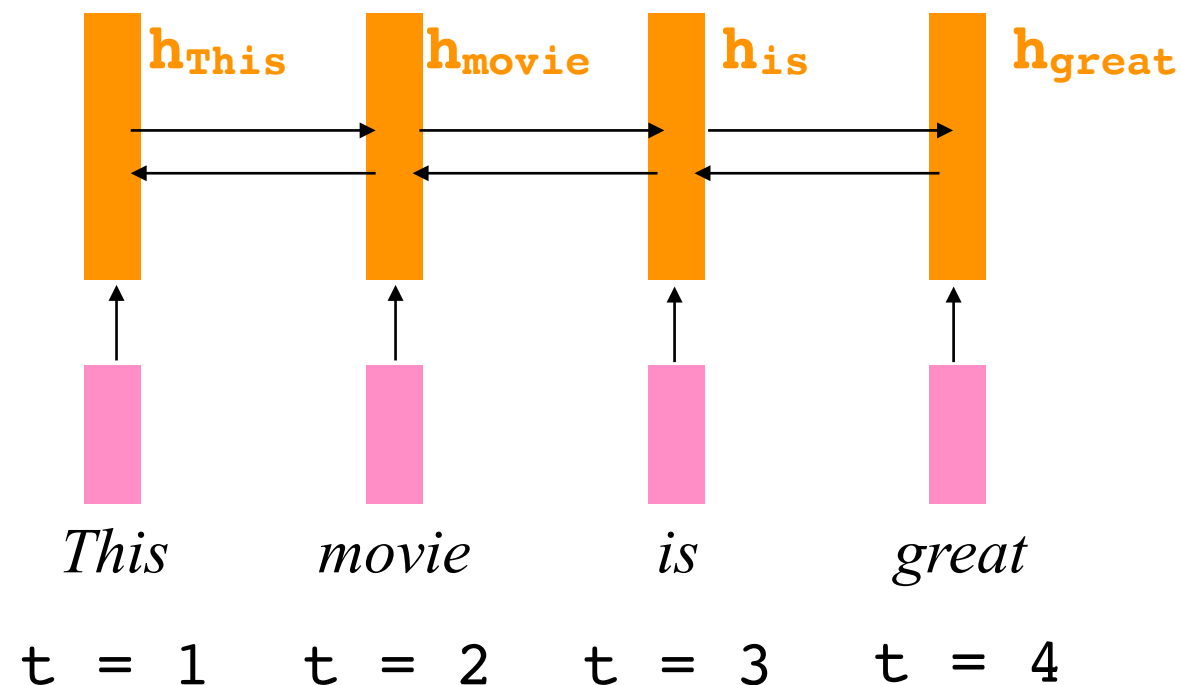


Intuition of Learning \mathbf{r} , “Dictionary”

Gradient update to maximize: $\text{Likelihood}(\mathbf{l} = 2) = \sum_t \mathbf{r}_{\text{Film},t}$
 $\mathbf{t} \in \{\text{This, movie, is, great}\}$

$\mathbf{r}_{\text{Film, This}}$ $\mathbf{r}_{\text{Film, movie}}$ $\mathbf{r}_{\text{Film, is}}$ $\mathbf{r}_{\text{Film, great}}$

.25 .25 .25 .25



Intuition of Learning \mathbf{r} , “Dictionary”

This movie is great
=> Dieser Film ist großartig


Gradient update to maximize:

Loss(sentence) $\sum_{\mathbf{l}} \sum_t \mathbf{r}_{\mathbf{l},t}$

$\mathbf{t} \in \{\text{This, movie, is, great}\}$

$\mathbf{l} \in \{\text{Dieser, Film, ist, großartig}\}$

How many times $\mathbf{r}_{\mathbf{l},t}$
appears in the sum.



\mathbf{r}	This	Movie	Is	Great
Dieser	1	1	1	1
Film	1	1	1	1
Ist	1	1	1	1
großartig	1	1	1	1

Looks like there is no reason
for the model to learn word-to-word correspondence

Intuition of Learning \mathbf{r} , “Dictionary”

This movie is great
=> Dieser Film ist großartig

Gradient update to maximize: $\sum_l \sum_t \mathbf{r}_{l,t}$

$\mathbf{t} \in \{\text{This, movie, is, great}\}$

$\mathbf{l} \in \{\text{Dieser, Film, ist, großartig}\}$

This movie is bad
=> Dieser Film ist schlecht

Gradient update to maximize: $\sum_l \sum_t \mathbf{r}_{l,t}$

$\mathbf{t} \in \{\text{This, movie, is, bad}\}$

$\mathbf{l} \in \{\text{Dieser, Film, ist, schlecht}\}$

add

\mathbf{r}	This	Movie	Is	Great	Bad
Dieser	2	2	2	1	1
Film	2	2	2	1	1
Ist	2	2	2	1	1
großartig	1	1	1	1	0
schlecht	1	1	1	0	1

Can recover \mathbf{r} (word-to-word correspondence) from “co-occurrence”.

Testing the “co-occurrence” Intuition

- Hypothesis: If we remove the co-occurrence statistics, **r** cannot be learned, and hence attention **a** fails to learn.
- Experiments on a “sequence copying task”.
 - Setting 1: the model learns the copying task from a distribution of permutations of [1, 40]. **~50% fails**
 - Setting 2: the model to learns from a distribution of length 40 array, each token is a uniform i.i.d. sample from [1, 40]. **Always successful**

```
input: 3 2 1 0 ; output: 3' 2' 1' 0'
input: 0 2 1 3 ; output: 0' 2' 1' 3'
input: 3 2 0 1 ; output: 3' 2' 0' 1'
input: 0 2 1 3 ; output: 0' 2' 1' 3'
input: 3 2 0 1 ; output: 3' 2' 0' 1'
```

```
input: 0 3 3 1 2 ; output: 2' 1' 1' 3' 0'
input: 1 2 2 3 3 ; output: 3' 0' 0' 1' 1'
input: 2 2 1 2 3 ; output: 0' 0' 3' 0' 1'
input: 3 2 1 0 0 ; output: 1' 0' 3' 2' 2'
input: 3 0 2 1 2 ; output: 1' 2' 0' 3' 0'
```

Takeaways ...

- Interpretable attention might not be necessary to achieve high accuracy (e.g. in text classification).
- Attention is shaped by training dynamics.
- Open the blackbox of training to understand neural networks.

References

- Jain, Sarthak, and Byron C. Wallace. "Attention is not explanation." *arXiv preprint arXiv:1902.10186* (2019).
- Wiegrefe, Sarah, and Yuval Pinter. "Attention is not not explanation." *arXiv preprint arXiv:1908.04626* (2019).
- Snell, Charlie, et al. "Understanding Attention Training via Output Relevance" *OpenReview Preprint* (2020)