

Last time?

- Point and segment Clipping
- Planes as homogenous vectors (duality)
- In homogeneous coordinates before division
- · Outcodes for efficient rejection
- Notion of convexity
- · Polygon clipping via walking
- Line rasterization, incremental computation

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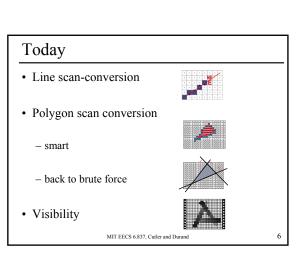
High-level concepts for 6.837

- · Linearity
- · Homogeneous coordinates
- · Convexity
- · Discrete vs. continuous
- Incremental computation
- Trying things on simple examples

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Scan Conversion (Rasterization) Modeling Transformations Illumination (Shading) Viewing Transformation (Perspective / Orthographic) Clipping Projection (to Screen Space) Scan Conversion (Rasterization) Visibility / Display MIT EECS 6.837, Cutler and Durand

Visibility / Display Modeling Transformations Illumination (Shading) Viewing Transformation (Perspective / Orthographic) Clipping Projection (to Screen Space) Scan Conversion (Rasterization) Vissibility / Display Projection (to Screen Space) Scan Conversion (Rasterization) Vissibility / Display * Almost every step in the graphics pipeline involves a change of coordinate system. Transformations are central to understanding 3D computer graphics. MIT EECS 6.837, Cutler and Durand * Almost every step in the graphics pipeline involves a change of coordinate system. Transformations are central to understanding 3D computer graphics.



Scan Converting 2D Line Segments

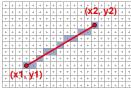
- Given:
 - Segment endpoints (integers x1, y1; x2, y2)
- Identify:
 - Set of pixels (x, y) to display for segment



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Line Rasterization Requirements

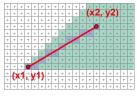
- Transform **continuous** primitive into **discrete** samples
- Uniform thickness & brightness
- · Continuous appearance
- No gaps
- Accuracy
- · Speed



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Algorithm Design Choices

- Assume:
 - -m = dy/dx, 0 < m < 1
- · Exactly one pixel per column
 - fewer \rightarrow disconnected, more \rightarrow too thick



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Naive Line Rasterization Algorithm

- Simply compute y as a function of x
 - Conceptually: move vertical scan line from x1 to x2

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- What is the expression of y as function of x?
- Set pixel (x, round (y(x)))



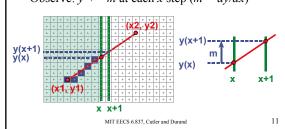
 $y = y1 + \frac{x - x1}{x2 - x1}(y2 - y1)$

y =(..

 $m = \frac{dy}{dx}$

Efficiency

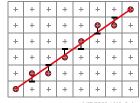
- Computing y value is expensive y = y1 + m(x x1)
- Observe: y += m at each x step (m = dy/dx)



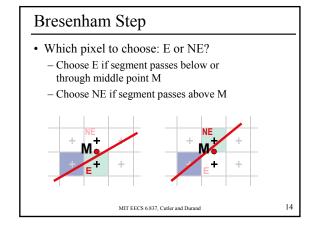
Bresenham's Algorithm (DDA)

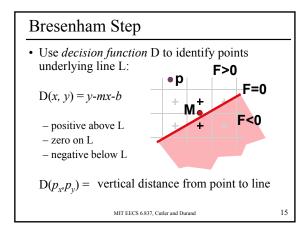
- Select pixel vertically closest to line segment

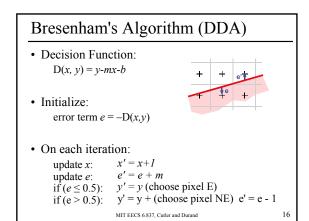
 intuitive, efficient,
 pixel center always within 0.5 vertically
- · Same answer as naive approach

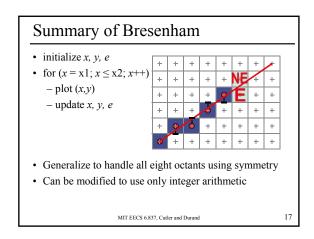


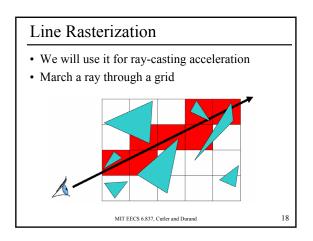
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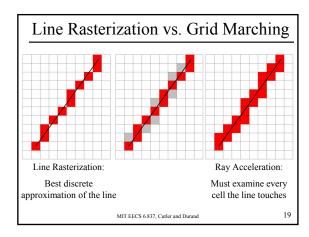


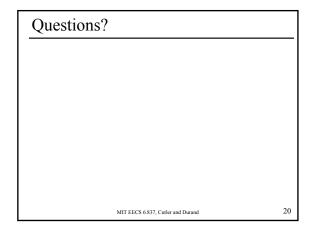




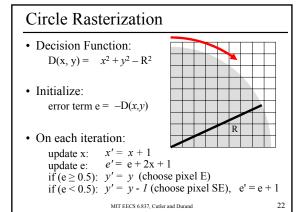








Circle Rasterization • Generate pixels for 2nd octant only • Slope progresses from 0 → −1 • Analog of Bresenham Segment Algorithm MIT EECS 6.837, Cutler and Durand 21



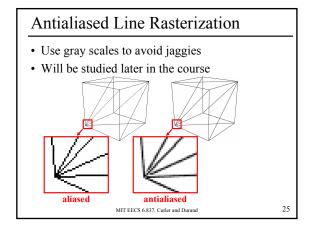
Philosophically Discrete differential analyzer (DDA): • Perform incremental computation • Work on derivative rather than function • Gain one order for polynomial – Line becomes constant derivative – Circle becomes linear derivative

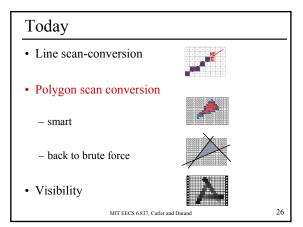
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Questions?

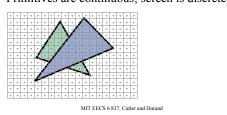
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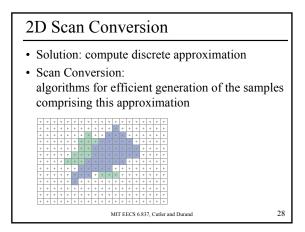


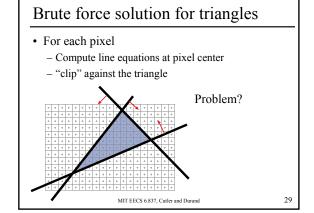
Geometric primitive – 2D: point, line, polygon, circle... – 3D: point, line, polyhedron, sphere... Primitives are continuous; screen is discrete

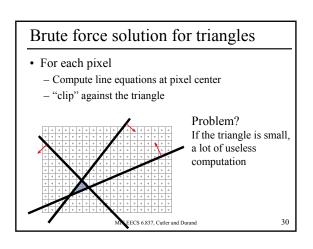
2D Scan Conversion

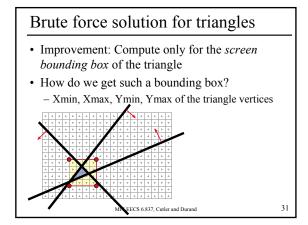


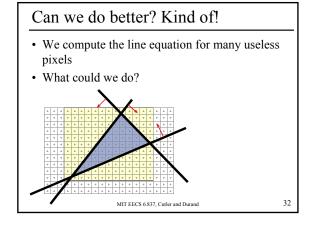
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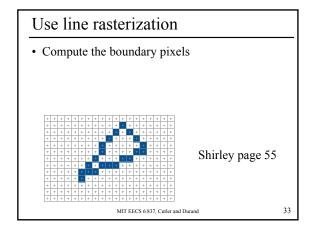


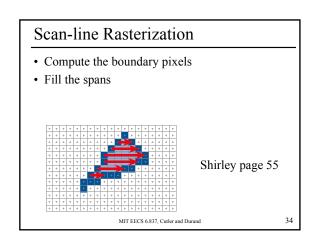


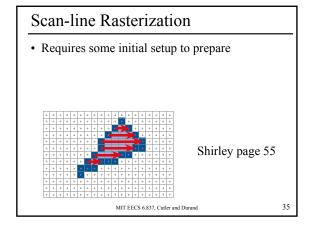


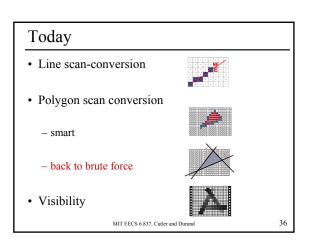






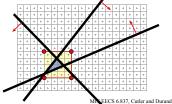






For modern graphics cards

- Triangles are usually very small
- · Setup cost are becoming more troublesome
- Clipping is annoying
- · Brute force is tractable

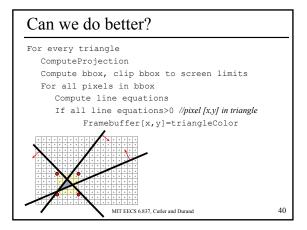


Modern rasterization For every triangle ComputeProjection Compute bbox, clip bbox to screen limits For all pixels in bbox Compute line equations If all line equations If all line equations>0 //pixel [x,y] in triangle Framebuffer[x,y]=triangleColor

Modern rasterization For every triangle ComputeProjection Compute bbox, clip bbox to screen limits For all pixels in bbox Compute line equations If all line equations/pixelfxy/in triangle FrameDuffer(x,y)**rriangleColor • Note that Bbox clipping is trivial

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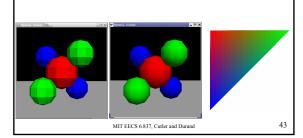
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Can we do better? For every triangle Compute Projection Compute bbox, clip bbox to screen limits Setup line eq compute a_idx, b_idy for the 3 lines Initialize line eq, values for bbox corner L_=a_ix0+b_iy+c_i For all scanline y in bbox For 3 lines, update Li For all x in bbox Increment line equations: Li+=adx If all Li>0 //pixel [x,y] in triangle Framebuffer [x,y]=triangleColor • We save one multiplication per pixel

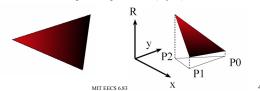


- Interpolate colors of the 3 vertices
- · Linear interpolation



Adding Gouraud shading

- Interpolate colors of the 3 vertices
- Linear interpolation, e.g. for R channel:
 - $-R=a_Rx+b_Ry+c_R$
 - Such that R[x0,y0]=R0; R[x1, y1]=R1; R[x2,y2]=R2
 - Same as a plane equation in (x,y,R)



Adding Gouraud shading

Interpolate colors For every triangle ComputeProjection Compute bbox, clip bbox to screen limits Setup line eq

Setup color equation For all pixels in bbox

Increment line equations

Increment color equation

If all Li>0 //pixel [x,y] in triangle

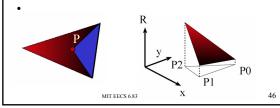
Framebuffer[x,y]=interpolatedColor

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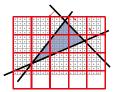
Adding Gouraud shading

- Interpolate colors of the 3 vertices
- Other solution: use barycentric coordinates
- $R=\alpha R_0 + \beta R_1 + \gamma R_2$
- Such that $P = \alpha P_0 + \beta P_1 + \gamma P_2$



In the modern hardware

- Edge eq. in homogeneous coordinates [x, y, w]
- · Tiles to add a mid-level granularity
 - Early rejection of tiles
 - Memory access coherence



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Ref

- Henry Fuchs, Jack Goldfeather, Jeff Hultquist, Susan Spach, John Austin, Frederick Brooks, Jr., John Eyles and John Poulton, "Fast Spheres, Shadows, Textures, Transparencies, and Image Enhancements in Pixel-Planes", Proceedings of SIGGRAPH '85 (San Francisco, CA, July 22–26, 1985). In *Computer Graphics*, v19n3 (July 1985), ACM SIGGRAPH, New York, NY, 1985.
- Juan Pineda, "A Parallel Algorithm for Polygon Rasterization" Proceedings of SIGGRAPH '88 (Atlanta, GA, August 1-5, 1988). In Computer Graphics, v22n4 (August 1988), ACM SIGGRAPH, New York, NY, 1988. Figure 7: Image from the spinning teapot performance test.
- Triangle Scan Conversion using 2D Homogeneous Coordinates, Marc Olano Trey Greer

http://www.cs.unc.edu/~olano/papers/2dh-tri/2dh-tri.pdf

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Take-home message

- The appropriate algorithm depends on
 - Balance between various resources (CPU, memory, bandwidth)
 - The input (size of triangles, etc.)
- Smart algorithms often have initial preprocess
 - Assess whether it is worth it
- To save time, identify redundant computation
 - Put outside the loop and interpolate if needed

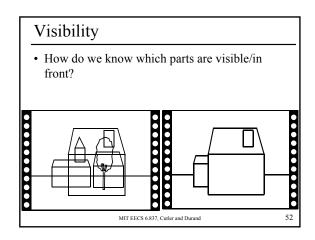
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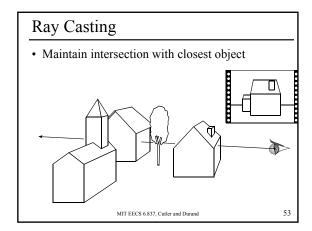
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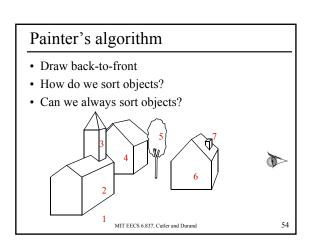
Questions?

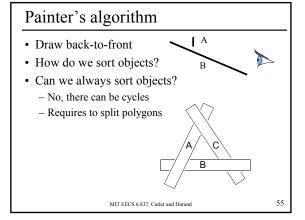
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Today • Line scan-conversion • Polygon scan conversion - smart - back to brute force • Visibility MIT EECS 6.837, Cutler and Durand 51









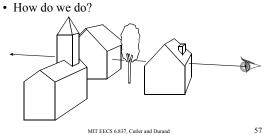
Painter's algorithm

- Old solution for hidden-surface removal
 - Good because ordering is useful for other operations (transparency, antialiasing)
- But
 - Ordering is tough
 - Cycles
 - Must be done by CPU
- · Hardly used now
- But some sort of partial ordering is sometimes useful
 - Usuall front-to-back
 - To make sure foreground is rendered first
 - For transparency

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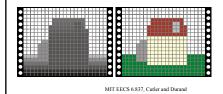
Visibility

- In ray casting, use intersection with closest t
- Now we have swapped the loops (pixel, object)



Z buffer

- In addition to frame buffer (R, G, B)
- Store distance to camera (z-buffer)
- Pixel is updated only if new z is closer than z-buffer value



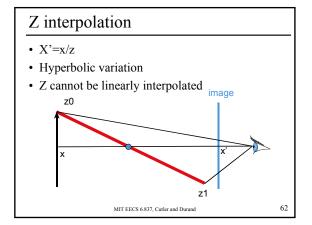
Z-buffer pseudo code

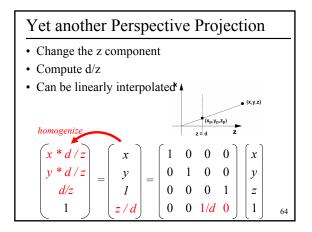
For every triangle Compute Projection, color at vertices Setup line equations Compute bbox, clip bbox to screen limits For all pixels in bbox Increment line equations Compute curentZ Increment currentColor If all line equations>0 //pixel [x,y] in triangle If currentZ<zBuffer[x,y] //pixel is visible</pre> Framebuffer[x,y]=currentColor zBuffer[x,y]=currentZ

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Works for hard cases! MIT EECS 6.837, Cutler and Durand

What exactly do we store • Floating point distance • Can we interpolate z in screen space? - i.e. does z vary linearly in screen space? z0 x MIT EECS 6.837, Cutler and Durand 61





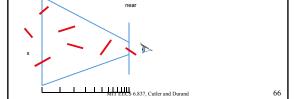
Advantages of 1/z

- Can be interpolated linearly in screen space
- Puts more precision for close objects
- Useful when using integers
 - more precision where perceptible

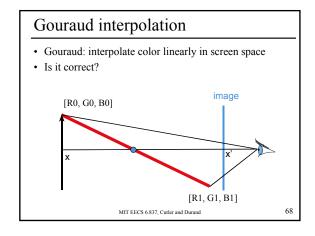
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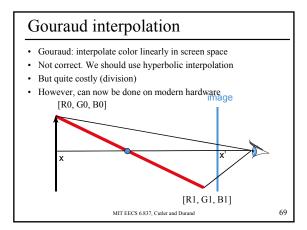
Integer z-buffer

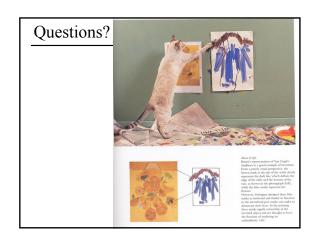
- Use 1/z to have more precision in the foreground
- Set a near and far plane
 - 1/z values linearly encoded between 1/near and 1/far
- · Careful, test direction is reversed



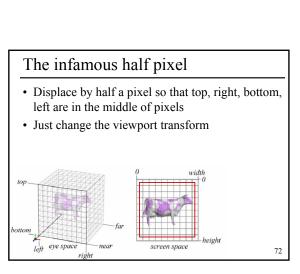
Integer Z-buffer pseudo code For every triangle Compute Projection, color at vertices Setup line equations, depth equation Compute bbox, clip bbox to screen limits For all pixels in bbox Increment line equations Increment curent_lovZ Increment currentColor If all line equations>0 //pixel [x,y] in triangle If current_lovZ>lovzBuffer[x,y]/pixel is visible Framebuffer[x,y]=currentColor lovzBuffer[x,y]=currentLovZ

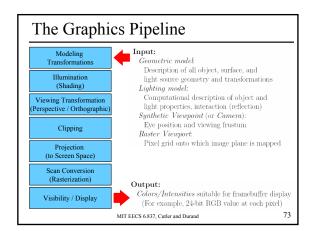


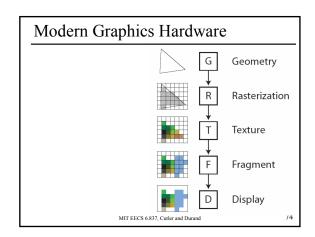


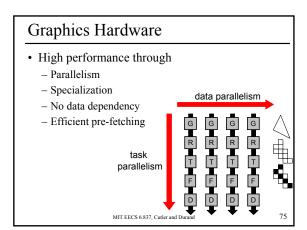


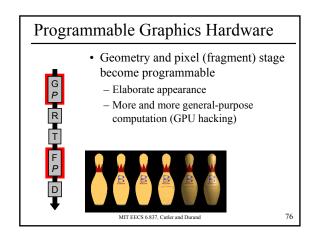
The infamous half pixel • I refuse to teach it, but it's an annoying issue you should know about • Do a line drawing of a rectangle from [top, right] to [bottom,left] • Do we actually draw the columns/rows of pixels?











Modern Graphics Hardware

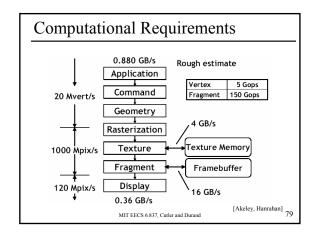
- About 4-6 geometry units
- · About 16 fragment units
- Deep pipeline (~800 stages)
- Tiling (about 4x4)
 - Early z-rejection if entire tile is occluded
- Pixels rasterized by quads (2x2 pixels)
 - Allows for derivatives
- Very efficient texture pre-fetching
 - And smart memory layout

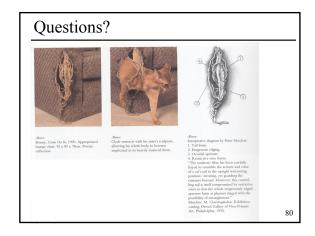
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Current GPUs

- · Programmable geometry and fragment stages
- 600 million vertices/second, 6 billion texels/second
- · In the range of tera operations/second
- Floating point operations only
- · Very little cache

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Next Week: Ray Casting Acceleration

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