# Assignment\_2\_Ruixi Li

October 16, 2018

## 1 Assignment 2

1.0.1 MACS 30000, Dr. Evans

#### 1.0.2 Ruixi Li

Due Wednesday, Oct. 17 at 11:30 AM

```
In [1]: # Import packages
    import numpy as np
    import pandas as pd
    import statsmodels.api as sm
    # import matplotlib.pyplot as plt
    import matplotlib.pyplot as plt
    # plt.style.use('seaborn')
    import seaborn as sns

#Turn of Notebook Package Warnings
    import warnings
    warnings.filterwarnings('ignore')
```

## 1.0.3 1. Imputing age and gender

**(a) Proposed solution** For the age, I will use variables total income and weight in SurveyIncome.txt to fit a linear regression model. Then, I will use weight and the sum of labor income and capital income in BestIncome.txt to predict age into the BestIncome.txt.

For the gender, I will use variables total income and weight in SurveyIncome.txt to fit a logit model. Then, I will use weight and the sum of labor income and capital income in BestIncome.txt to predict age into the BestIncome.txt.

```
3 55128.180903 12692.670403 62.910559
                                                  149.218189
        4 44482.794867
                          9812.975746
                                       68.678295
                                                  152.726358
In [3]: # name my variables of BestIncome.txt
        BestIncome_cols = ['lab_inc','cap_inc','hgt','wgt']
        BestIncome.columns = BestIncome_cols
        BestIncome.head()
Out [3]:
                lab_inc
                              cap_inc
                                             hgt
                                                         wgt
        0
         52655.605507
                          9279.509829
                                       64.568138
                                                  152.920634
        1 70586.979225
                          9451.016902
                                       65.727648
                                                  159.534414
        2 53738.008339
                          8078.132315
                                       66.268796
                                                  152.502405
        3 55128.180903 12692.670403
                                       62.910559
                                                  149.218189
        4 44482.794867
                          9812.975746 68.678295
                                                  152.726358
In [4]: # run descriptive statistics of BestIncome.txt
        BestIncome.describe()
Out [4]:
                    lab_inc
                                  cap_inc
                                                    hgt
                                                                   wgt
               10000.000000 10000.000000
                                           10000.000000
                                                         10000.000000
        count
               57052.925133
                              9985.798563
                                              65.014021
                                                           150.006011
        mean
        std
                8036.544363
                              2010.123691
                                               1.999692
                                                             9.973001
        min
               22917.607900
                              1495.191896
                                              58.176154
                                                           114.510700
                                                           143.341979
        25%
               51624.339880
                              8611.756679
                                              63.652971
        50%
               56968.709935
                              9969.840117
                                              65.003557
                                                           149.947641
        75%
               62408.232277 11339.905773
                                              66.356915
                                                           156.724586
               90059.898537 19882.320069
                                              72.802277
                                                           185.408280
        max
In [5]: # read in my data of SurveyIncome.txt
        SurveyIncome = pd.read_csv("SurveyIncome.txt", header=None)
        SurveyIncome.head()
Out [5]:
                      0
                                                  3
         63642.513655
                                     46.610021
                                                1.0
                         134.998269
        1 49177.380692
                        134.392957
                                     48.791349
        2 67833.339128 126.482992
                                     48.429894
                                                1.0
        3 62962.266217 128.038121 41.543926
                                               1.0
        4 58716.952597 126.211980 41.201245
                                                1.0
In [6]: # name my variables of SurveyIncome.txt
        SurveyIncome_cols = ['tot_inc','wgt','age','female']
        SurveyIncome.columns = SurveyIncome_cols
        SurveyIncome.head()
Out[6]:
                tot_inc
                                           age
                                                female
                                wgt
                                                   1.0
        0
          63642.513655
                         134.998269
                                     46.610021
                        134.392957
        1 49177.380692
                                     48.791349
                                                   1.0
        2 67833.339128 126.482992
                                     48.429894
                                                   1.0
        3 62962.266217
                         128.038121
                                     41.543926
                                                   1.0
        4 58716.952597 126.211980 41.201245
                                                   1.0
```

```
Out[7]:
                   tot_inc
                                     wgt
                                                  age
                                                           female
        count
                1000.000000 1000.000000
                                         1000.000000
                                                      1000.00000
              64871.210860
                            149.542181
                                            44.839320
                                                          0.50000
       mean
        std
               9542.444214
                              22.028883
                                            5.939185
                                                          0.50025
              31816.281649
                              99.662468
                                            25.741333
                                                          0.00000
        min
        25%
              58349.862384
                              130.179235
                                           41.025231
                                                          0.00000
        50%
              65281.271149
                              149.758434
                                            44.955981
                                                          0.50000
        75%
              71749.038000
                              170.147337
                                            48.817644
                                                          1.00000
              92556.135462
                              196.503274
                                            66.534646
        max
                                                          1.00000
```

### (b) Here is where I'll use my proposed method from part (a) to impute age.

```
In [8]: # Define Outcome and Independent Variables
        outcome = 'age'
        features = ['tot_inc','wgt']
       X,y = SurveyIncome[features], SurveyIncome[outcome]
In [9]: X.head()
Out[9]:
                tot_inc
                                wgt
        0 63642.513655 134.998269
        1 49177.380692 134.392957
        2 67833.339128 126.482992
        3 62962.266217 128.038121
        4 58716.952597 126.211980
In [10]: y.head()
Out[10]: 0
              46.610021
              48.791349
         2
              48.429894
         3
              41.543926
              41.201245
         Name: age, dtype: float64
In [11]: # run regression
         X = sm.add_constant(X, prepend=False)
         m = sm.OLS(y, X)
         res = m.fit()
         print(res.summary())
```

#### OLS Regression Results

========									
Dep. Variab	Dep. Variable: age			R-squared:			0.001		
Model:			OLS	Adj.	R-squared:		-0.001		
Method:		Least Squ	ares	F-sta	atistic:		0.6326		
Date:		Tue, 16 Oct		Prob	(F-statist	ic):	0.531		
Time:		11:4	8:30	Log-I	Likelihood:		-3199.4		
No. Observa	tions:		1000	AIC:			6405.		
Df Residual	s:		997	BIC:			6419.		
Df Model:			2						
Covariance	Type:	nonro	bust						
========	========			=====					
	coef	std err		t	P> t	[0.025	0.975]		
tot_inc	2.52e-05	2.26e-05	 1	.114	0.266	-1.92e-05	6.96e-05		
wgt	-0.0067	0.010	-0	.686	0.493	-0.026	0.013		
const	44.2097	1.490	29	.666	0.000	41.285	47.134		
Omnibus:	=======	2	===== .460	Durb:	======= in-Watson:	========	1.921		
Prob(Omnibu	s):	0	.292	Jarqı	ıe-Bera (JB	):	2.322		
Skew:	-		.109	Prob		•	0.313		
Kurtosis:			.092	Cond			5.20e+05		

#### Warnings:

- [1] Standard Errors assume that the covariance matrix of the errors is correctly specified.
- [2] The condition number is large, 5.2e+05. This might indicate that there are strong multicollinearity or other numerical problems.

I obtained the following linear regression equation:

$$age = 44.2097 + 0.0000252totinc - 0.0067wgt$$

Then, I will predict age in BestIncome.txt:

In [13]: # predit age

X = BestIncome[features]

X = sm.add\_constant(X, prepend = False)

BestIncome['age'] = res.predict(X)

BestIncome.head()

Out[13]:		lab_inc	cap_inc	hgt	wgt	tot_inc	age
	0	52655.605507	9279.509829	64.568138	152.920634	61935.115336	44.742614
	1	70586.979225	9451.016902	65.727648	159.534414	80037.996127	45.154387
	2	53738 008339	8078 132315	66 268796	152 502405	61816 140654	44 742427

```
3 55128.180903 12692.670403 62.910559 149.218189 67820.851305 44.915836
4 44482.794867 9812.975746 68.678295 152.726358 54295.770612 44.551391
```

Here is where I'll use my proposed method from part (a) to impute gender.

```
In [14]: # Define Outcome and Independent Variables
        outcome = 'female'
        features = ['tot_inc','wgt']
        X,y = SurveyIncome[features], SurveyIncome[outcome]
In [15]: X.head()
Out[15]:
               tot_inc
                              wgt
        0 63642.513655 134.998269
        1 49177.380692 134.392957
        2 67833.339128 126.482992
        3 62962.266217 128.038121
        4 58716.952597 126.211980
In [16]: y.head()
Out[16]: 0
            1.0
        1
            1.0
        2
            1.0
        3
            1.0
             1.0
        Name: female, dtype: float64
In [17]: # run regression
        X = sm.add_constant(X, prepend=False)
        m = sm.Logit(y, X)
        res = m.fit()
        print(res.summary())
Optimization terminated successfully.
        Current function value: 0.036050
        Iterations 11
                        Logit Regression Results
______
Dep. Variable:
                                     No. Observations:
                                                                    1000
                            female
Model:
                                                                     997
                             Logit
                                     Df Residuals:
Method:
                               MLE Df Model:
Date:
                   Tue, 16 Oct 2018 Pseudo R-squ.:
                                                                  0.9480
                          11:48:31 Log-Likelihood:
Time:
                                                                 -36.050
                              True LL-Null:
                                                                 -693.15
converged:
```

LLR p-value:	4.232e-286
zzw p varac.	1.2020 200

=========									
	coef	std err	z	P> z	[0.025	0.975]			
tot_inc wgt const	-0.0002 -0.4460 76.7929	4.25e-05 0.062 10.569	-3.660 -7.219 7.266	0.000 0.000 0.000	-0.000 -0.567 56.078	-7.22e-05 -0.325 97.508			

Possibly complete quasi-separation: A fraction 0.55 of observations can be perfectly predicted. This might indicate that there is complete quasi-separation. In this case some parameters will not be identified.

I obtained the following logit regression equation:

$$logit(female) = 76.7929 - 0.0002 \times totinc - 0.4460 \times wgt$$

Then, I will predict gender in BestIncome.txt:

```
In [18]: # predict gender

X = BestIncome[features]

X = sm.add_constant(X, prepend = False)

BestIncome['gender'] = res.predict(X)
```

BestIncome['gender'] [BestIncome['gender'] >= 0.5] = 1
BestIncome['gender'] [BestIncome['gender'] < 0.5] = 0</pre>

BestIncome.head()

Out $[18]$ :		lab_inc	cap_inc	${ t hgt}$	wgt	${ tot\_inc}$	age	\
0	)	52655.605507	9279.509829	64.568138	152.920634	61935.115336	44.742614	
1	L	70586.979225	9451.016902	65.727648	159.534414	80037.996127	45.154387	
2	2	53738.008339	8078.132315	66.268796	152.502405	61816.140654	44.742427	
3	3	55128.180903	12692.670403	62.910559	149.218189	67820.851305	44.915836	
4	ŀ	44482.794867	9812.975746	68.678295	152.726358	54295.770612	44.551391	

gender

- 0.0
- 1 0.0
- 2 0.0
- 3 0.0
- 4 1.0

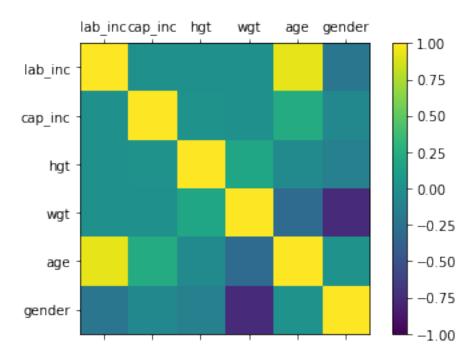
Out[19]:	lab_inc	cap_inc	hgt	wgt	age	gender
0	52655.605507	9279.509829	64.568138	152.920634	44.742614	0.0
1	70586.979225	9451.016902	65.727648	159.534414	45.154387	0.0
2	53738.008339	8078.132315	66.268796	152.502405	44.742427	0.0
3	55128.180903	12692.670403	62.910559	149.218189	44.915836	0.0
4	44482.794867	9812.975746	68.678295	152.726358	44.551391	1.0

(c) Here is where I'll report the descriptive statistics for my new imputed variables.

```
In [20]: # select age and gender from BestIncome.txt
         Imputed = BestIncome[['age', 'gender']]
         Imputed.head()
Out [20]:
                  age gender
        0 44.742614
                          0.0
                          0.0
         1 45.154387
        2 44.742427
                          0.0
        3 44.915836
                          0.0
        4 44.551391
                          1.0
In [21]: # descriptive statistics of imputed variables
         Imputed.describe()
Out [21]:
                                    gender
         count 10000.000000 10000.000000
        mean
                   44.890828
                                  0.454600
        std
                   0.219150
                                  0.497959
        min
                   43.976495
                                  0.000000
        25%
                   44.743776
                                  0.000000
        50%
                   44.886944
                                  0.000000
        75%
                   45.038991
                                  1.000000
                   45.703819
                                  1.000000
        max
```

#### (d) Correlation matrix for the now six variables

```
In [22]: # Correlation Matrix Plot
         def corr plot(df):
             names = df.columns
             N = len(names)
             correlations = df.corr()
             fig = plt.figure()
             ax = fig.add_subplot(111)
             cax = ax.matshow(correlations, vmin=-1, vmax=1)
             fig.colorbar(cax)
             ticks = np.arange(0,N,1)
             ax.set_xticks(ticks)
             ax.set_yticks(ticks)
             ax.set_xticklabels(names)
             ax.set_yticklabels(names)
             plt.show()
         corr_plot(BestIncome)
```



```
In [23]: # In Matrix Form
       corr = BestIncome.corr()
       corr.style.background_gradient()
       corr
Out[23]:
               lab_inc
                      cap_inc
                                  hgt
                                           wgt
                                                   age
                                                        gender
       lab_inc 1.000000 0.005325 0.002790 0.004507 0.924053 -0.215469
       cap_inc 0.005325 1.000000 0.021572 0.006299 0.234159 -0.062569
       hgt
              0.002790 \quad 0.021572 \quad 1.000000 \quad 0.172103 \quad -0.045083 \quad -0.127416
              wgt
              gender -0.215469 -0.062569 -0.127416 -0.763821 0.020059 1.000000
```

### 1.0.4 2. Stationarity and data drift

#### (a) Estimate by OLS and report coefficients

```
1
            2001.0 721.811673 67600.584142
       2
            2001.0 736.277908 58704.880589
       3
            2001.0 770.498485 64707.290345
            2001.0 735.002861 51737.324165
In [26]: # Run regression model
       outcome = 'salary_p4'
       features = ['gre_qnt']
       X, y = IncomeIntel[features], IncomeIntel[outcome]
In [27]: X.head()
         gre_qnt
Out [27]:
       0 739.737072
       1 721.811673
       2 736.277908
       3 770.498485
       4 735.002861
In [28]: y.head()
Out [28]: 0 67400.475185
       1 67600.584142
       2 58704.880589
       3 64707.290345
           51737.324165
       Name: salary_p4, dtype: float64
In [29]: X = sm.add_constant(X, prepend=False)
       m = sm.OLS(y, X)
       res = m.fit()
       print(res.summary())
                     OLS Regression Results
______
Dep. Variable:
                     salary_p4 R-squared:
                                                          0.263
Model:
                           OLS Adj. R-squared:
                                                         0.262
Method:
                 Least Squares F-statistic:
          Least Squares r-statistic.

Tue, 16 Oct 2018 Prob (F-statistic): 3.43e-68

11:48:32 Log-Likelihood: -10673.

1000 AIC: 2.135e+04
                                                          356.3
Date:
Time:
No. Observations:
                           998 BIC:
Df Residuals:
                                                       2.136e+04
Df Model:
                            1
Covariance Type: nonrobust
______
          coef std err t P>|t| [0.025 0.975]
-----
gre_qnt -25.7632 1.365 -18.875 0.000 -28.442 -23.085
```

const	8.954e+04	878.764	101	.895	0.000	8.78e+04	9.13e+04
Omnibus:		9.:	 118	Durbin-	-Watson:		1.424
Prob(Omni	bus):	0.0	010	Jarque-	-Bera (JB)	:	9.100
Skew:		0.2	230	Prob(JE	3):		0.0106
Kurtosis:		3.0	077	Cond. N	lo.		1.71e+03

#### Warnings:

- [1] Standard Errors assume that the covariance matrix of the errors is correctly specified.
- [2] The condition number is large, 1.71e+03. This might indicate that there are strong multicollinearity or other numerical problems.

Report coefficients and SE's

I obtained the following OLS regression equation:

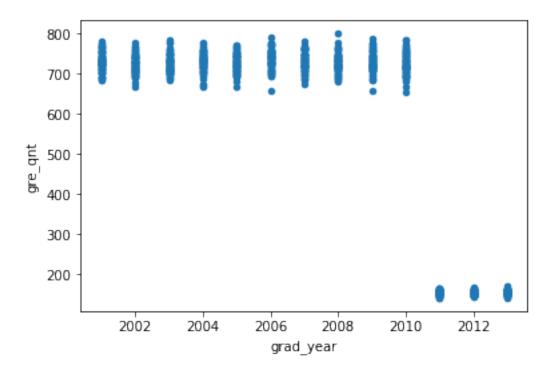
$$salaryp4 = 89540 - 25.7632 greqnt$$

and the estimated coefficients and standard errors are:

$$\beta_0 = 89540 \quad SE(\beta_0) = 878.764$$

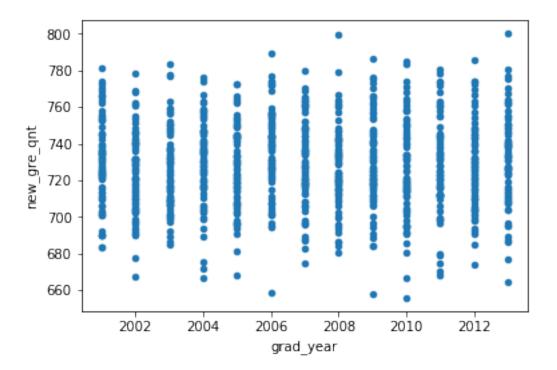
$$\beta_1 = -25.7632$$
  $SE(\beta_1) = 1.365$ 

## (b) Create a scatterplot of GRE score and graduation year.

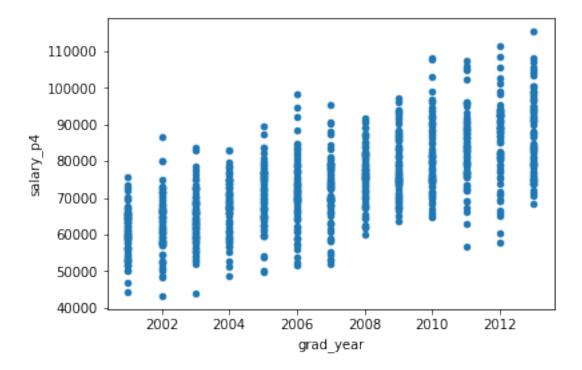


As we can see from the scatterplot above and the exercise, GRE quantitative scoring scale changed in 2011. My proposed solution is to convert two ways of scaling into one.

```
In [31]: # Implement the solution
         # Convert two scaling methods into one by zscore each gre gnt
         IncomeIntel['new_gre_qnt'] = IncomeIntel.apply(lambda x: x.gre_qnt/170*800
                                                         if x.grad_year>2010
                                                         else x.gre_qnt, axis=1)
         IncomeIntel.describe()
Out [31]:
                  grad_year
                                 gre_qnt
                                               salary_p4 new_gre_qnt
                             1000.000000
                                            1000.000000
                1000.000000
                                                          1000.000000
         count
                2006.994000
                                            74173.293777
                              596.510118
                                                           728.534611
         mean
         std
                   3.740582
                              242.361960
                                            12173.767372
                                                            23.619014
         min
                2001.000000
                              141.261398
                                            43179.183141
                                                           655.702537
         25%
                2004.000000
                              684.983551
                                            65778.240317
                                                           712.274822
         50%
                2007.000000
                              719.106878
                                            73674.204810
                                                           727.910127
         75%
                2010.000000
                              739.332537
                                            81838.874129
                                                           744.392487
                2013.000000
                              799.715533 115367.665815
                                                           800.000000
         max
In [32]: # Code and output of scatterplot
         grad_year = IncomeIntel['grad_year']
         gre_qnt = IncomeIntel['new_gre_qnt']
         IncomeIntel.plot(x='grad_year', y='new_gre_qnt', kind='scatter')
         plt.show()
```

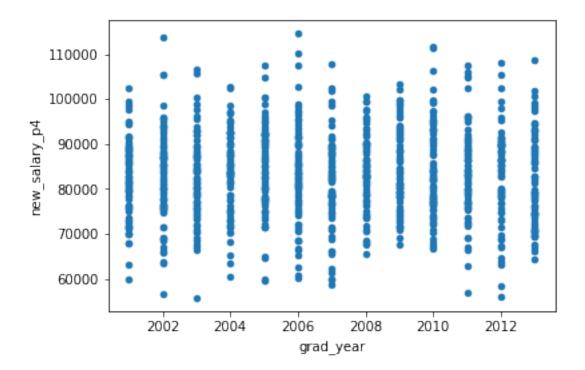


## (c) Create a scatterplot of income and graduation year



Because these data are not panel data, we cannot use differencing or log differencing methods to detrend them. So I will use the following method to modify the data.

```
In [34]: # Code to implement a solution
         avg_inc_by_year = IncomeIntel['salary_p4'].groupby(IncomeIntel\
                                                             ['grad_year']).mean().values
         avg_growth_rate = ((avg_inc_by_year[1:] - avg_inc_by_year[:-1]) \
                            / avg_inc_by_year[:-1]).mean()
         IncomeIntel['new_salary_p4'] = IncomeIntel.apply\
         (lambda x: x.salary_p4 / ((1 + avg_growth_rate) ** (x.grad_year - 2011)), axis=1)
         IncomeIntel.describe()
Out [34]:
                  grad_year
                                 gre_qnt
                                               salary_p4
                                                          new_gre_qnt
                                                                       new_salary_p4
         count
                1000.000000
                             1000.000000
                                             1000.000000
                                                          1000.000000
                                                                          1000.000000
                2006.994000
                              596.510118
                                            74173.293777
                                                                         83214.973802
         mean
                                                           728.534611
                   3.740582
                              242.361960
                                            12173.767372
                                                                         9667.722543
         std
                                                            23.619014
                2001.000000
                              141.261398
                                            43179.183141
                                                           655.702537
                                                                         55772.261434
         min
         25%
                2004.000000
                              684.983551
                                            65778.240317
                                                           712.274822
                                                                         76707.207282
         50%
                2007.000000
                              719.106878
                                            73674.204810
                                                           727.910127
                                                                         83279.745509
         75%
                                            81838.874129
                2010.000000
                              739.332537
                                                           744.392487
                                                                         89716.637333
         max
                2013.000000
                              799.715533
                                           115367.665815
                                                           800.000000
                                                                        114508.138911
In [35]: # Code and output of scatterplot
         grad_year = IncomeIntel['grad_year']
         new_salary_p4 = IncomeIntel['new_salary_p4']
         IncomeIntel.plot(x='grad_year', y='new_salary_p4', kind='scatter')
         plt.show()
```



## (d) Re-estimate coefficients with updated variables.

### OLS Regression Results

Dep. Variable:	new_salary_p4	R-squared:	0.001
Model:	OLS	Adj. R-squared:	-0.000
Method:	Least Squares	F-statistic:	0.6043
Date:	Tue, 16 Oct 2018	Prob (F-statistic):	0.437
Time:	11:48:33	Log-Likelihood:	-10595.
No. Observations:	1000	AIC:	2.119e+04
Df Residuals:	998	BIC:	2.120e+04
Df Model:	1		
Covariance Type:	nonrobust		

	coef	std err	t	P> t	[0.025	0.975]
new_gre_qnt const	-10.0695 9.055e+04	12.953 9441.560	-0.777 9.591	0.437 0.000	-35.487 7.2e+04	15.349 1.09e+05
Omnibus: Prob(Omnibus Skew: Kurtosis:	):	0.789 0.674 0.060 3.050		-		2.025 0.698 0.705 2.25e+04
=========	========		======	========	=======	=======

#### Warnings:

- [1] Standard Errors assume that the covariance matrix of the errors is correctly specified.
- [2] The condition number is large, 2.25e+04. This might indicate that there are strong multicollinearity or other numerical problems.

I obtained the following OLS regression equation:

$$newsalaryp4 = 9055 - 10.0695 new greant$$

and estimated coefficients and standard errors are:

$$\beta_0 = 9055 \quad SE(\beta_0) = 9441.560$$

$$\beta_1 = -10.0695$$
  $SE(\beta_1) = 12.953$ 

However, the GRE quantitative have a minimum score of 130, so it is over extrapolation of intercept estimator. Compared to the former result, this result is more reasonable after solving problems in both GRE quantitative and salary after 4 years. In the former interpretation of intercept estimator, a people with 0 GRE quantitative score can earn 89540 dollars per year. In the new model, If GRE quantitative score is 0, salary after 4 years is 9055 dollars, which is more realistic. However, the GRE quantitative have a minimum score of 130, so it is over extrapolation of intercept estimator. For the slope estimator, with each addition of GRE quantitative score, the salary after 4 years decrease 10.0695 dollars in the new model and decrease 25.7632 dollars in the previous model. The results in both model don't correspond to common sense that people with higher GRE quantitative score normally earns more salary, which contrast my hypothesis. But by solving the problem in the independent variables, the gap between empirical result and my hypothesis shortened.

#### 1.0.5 3. Assessment of Kossinets and Watts.

In this paper, the authors shortly present a literature review on homophily and then, bring out the research question which focuses on the origin of homophily: on what grounds do individuals selectively make or break some ties over others, and how do these choices shed light on the observation that similar people are more likely to become acquainted than dissimilar people?

To investigate more on this question, they using network data of a large uni- versity community which interactions, attributes, and affiliations are recorded. To construct the dataset, the authors merged three different databases: (1) the logs of e-mail interactions within the university

over one academic year, (2) a database of individual attributes (status, gender, age, department, number of years in the com- munity, etc.), and (3) records of course registration, in which courses were recorded separately for each semester. Dataset comprised 7,156,162 messages exchanged by 30,396 stable e-mail users during 270 days of observation. The available variables could be categorized into four groups: personal characteristics (age, gender, home state, formal status, years in school); organizational affiliations (primary department, school, campus, dormitory, academic field); course-related variables (courses taken, courses taught); and e-mail-related variables (days active, messages sent, messages received, in-degree, out-degree, reciprocated degree). A precise definitions of all vari- ables are provided in APPENDIX. A.

In the data cleaning process, from 43,553 individuals, the authors identified 34,574 users who were active throughout both semesters by the principle of sending and re- ceiving e-mail in both the first and the last months of the academic year. However, 43,553 individuals sent and received messages during the academic year. It is highly possible that they just didn't send or receive e-mail in both the first and the last months of the academic year. Simply dropped 8,979 individuals may result in a bi- ased model and diminish the authors' ability to answer the research question.

When match the data source to theoretical construct, the authors arbitrarily sup- pose that the university e-mail logs fully represents the social relationships of an individual. Nevertheless, it is not necessarily the case. Let's say a student seldom use e-mail to reach his friends. Instead, apps like Whatsup and Lines replaced e-mail with their convenience. This student is likely to be removed from the dataset in the context. Here is another example about the implicit closure. If there is a fraternity which never emails its member but has a fixed time and location for gathering, e-mail logs can't reflect the existence of this implicit foci. After two people from one class made friends in the gathering before they become friends through class, they may communicate with each other through e-mail. Then, the e-mail logs may indicates that they are friends with the explicit foci, which is that they are in the same class. Therefore, the dataset may fail to capture the real case.

In the chapter of origins of homophily, the authors proposed some problem on observed homophily. One might concerned that our measure of individual similarity acts, in effect, as an indicator variable for sharing a class, and that controlling for shared classes would effectively eliminate the potential for similarity to have any additional impact on tie formation, thereby artificially increasing the apparent importance of induced homophily vis-a-vis choice homophily. In order to address this potential sys- tematic bias, the author consider in figure 7 (top row) the distribution of similarity for student pairs who shared classes with that for student pairs who did not. As expected from figure 6, students who shared classes (fig. 7, pt. B) are, on average, much more similar than students who did not (pt. A). However, its higher average notwithstanding, the distribution in part B of figure 7 also exhibits higher variance (1.8) than that in part A (1.3); thus, the potential for differences in similarity to impact tie formation is not in fact diminished for pairs who share classes versus those who do not. As a further check the authors compare distributions of similarity for pairs who share implicit foci (fig. 7, pt. D) with those who do not (pt. C). In this way, the concern can be properly addressed.