MINI-PROJECT 2: Classify handwritten digits with Convolutional Neural Network (CNN)

1. Introduction

In the lab, we implemented the program to recognize handwritten digits using the Convolutional Neural Network model on the H7 board.

We first used python, TensorFlow, and Google Colab to train the CNN model in the cloud. The MNIST database for handwritten digits was used as the training set. The training images all have 1 channel and 28 pixels by 28 pixels for their size.

After the training, we implemented the functional modules for CNN and the CNN image classifiers on the H7 board. The CNN structure we designed is shown below:

the output width, output height, and the number of channels are shown in the screenshot below:

Layer (type)	Output Shape	Param #
conv2d_2 (Conv2D)	(None, 28, 28, 16)	160
max_pooling2d_2 (MaxPooling 2D)	(None, 14, 14, 16)	0
conv2d_3 (Conv2D)	(None, 14, 14, 32)	4640
<pre>max_pooling2d_3 (MaxPooling 2D)</pre>	(None, 7, 7, 32)	0
flatten_1 (Flatten)	(None, 1568)	0
dense_1 (Dense)	(None, 10)	15690

For the convolution layer, we first padded the input matrix with zeros on four of the outer edges, then convolve the padded input with the filter and stride the filter across the padded matrix. After the striding, we applied ReLU to every element to eliminate the negative results.

For the pooling layer, we applied max pooling for each 2*2 block of the input, thus returning a matrix with $\frac{1}{2}$ side length on each side.

For the dense layer, after applying the neuron weight and the bias to the input, we

$$P(y = j \mid \mathbf{x}) = rac{e^{\mathbf{x}^\mathsf{T} \mathbf{w}_j}}{\sum_{k=1}^K e^{\mathbf{x}^\mathsf{T} \mathbf{w}_k}}$$

applied the softmax function

for normalization and produce

the discrete probability distribution vector for each digit.

The accuracy for the training in the designed structure was evaluated by python and recorded as below:

2. Result

The program failed to recognize the digit 8 from the provided test images while recognizing the rest test images successfully. The details are shown below:

2.1. Check number 0:

```
308
           /* USER CODE BEGIN 3 */
309
           sprintf(name, "num0.bmp");
           file ready = 0;
310
           read hmn(name).
311
😑 Console 🦹 Problems 🕠 Executables 🖳 Debugger Console
Port 0 🖾
prediction of number 0 is 0.999992667281863
prediction of number 1 is 0.0000000000000000
prediction of number 2 is 0.000000004888817
prediction of number 3 is 0.000000000000037
prediction of number 4 is 0.0000000000000000
prediction of number 5 is 0.000000000000237
prediction of number 6 is 0.000000000000001
prediction of number 7 is 0.000000000000000
prediction of number 8 is 0.000007327829033
prediction of number 9 is 0.0000000000000012
```

2.2. Check number 1:

```
/* USER CODE BEGIN 3 */
           sprintf(name, "num1.bmp");
309
 310
           file ready = 0;
Console Problems  Executables  Debugger Cons
Port 0 🖂
prediction of number 0 is 0.000000000000000
prediction of number 1 is 0.999999999980961
prediction of number 2 is 0.000000000019039
prediction of number 3 is 0.000000000000000
prediction of number 4 is 0.000000000000000
prediction of number 5 is 0.000000000000000
prediction of number 6 is 0.000000000000000
prediction of number 7 is 0.000000000000000
prediction of number 8 is 0.000000000000000
prediction of number 9 is 0.000000000000000
```

2.3. Check number 2:

```
308
           /* USER CODE BEGIN 3 */
           sprintf(name, "num2.bmp");
309
 310
           file ready = 0;
           read bmp(name);
311
🔁 Console 🦃 Problems 👔 Executables 🖳 Debugger Console
Port 0 🟻
prediction of number 0 is 0.000000000000000
prediction of number 1 is 0.000000000000000
prediction of number 2 is 1.000000000000000
prediction of number 3 is 0.000000000000000
prediction of number 4 is 0.000000000000000
prediction of number 5 is 0.000000000000000
prediction of number 6 is 0.000000000000000
prediction of number 7 is 0.000000000000000
prediction of number 8 is 0.000000000000000
prediction of number 9 is 0.000000000000000
```

2.4. Check number 3:

```
/* USER CODE BEGIN 3 */
 308
309
           sprintf(name, "num3.bmp");
           file_ready = 0;
 310
311
           read bmp(name);
📃 Console 🤰 Problems 🕠 Executables 🛮 🖳 Debugger Consol
Port 0 🖾
prediction of number 0 is 0.000000000000000
prediction of number 1 is 0.000000000000000
prediction of number 2 is 0.000000000000000
prediction of number 3 is 0.999999797032286
prediction of number 4 is 0.000000000000000
prediction of number 5 is 0.000000202967713
prediction of number 6 is 0.000000000000000
prediction of number 7 is 0.000000000000000
prediction of number 8 is 0.000000000000000
prediction of number 9 is 0.000000000000000
```

2.5. Check number 4:

```
308
           /* USER CODE BEGIN 3 */
<u>a</u>309
           sprintf(name, "num4.bmp");
           file ready = 0;
 310
           read hmn(name).
A311
😑 Console 🦹 Problems 🕠 Executables 🖳 Debugger Console
Port 0 🖾
prediction of number 0 is 0.000000000000000
prediction of number 1 is 0.000000000000000
prediction of number 2 is 0.000000000000000
prediction of number 3 is 0.0000000000000000
prediction of number 4 is 1.0000000000000000
prediction of number 5 is 0.000000000000000
prediction of number 6 is 0.000000000000000
prediction of number 7 is 0.000000000000000
prediction of number 8 is 0.000000000000000
prediction of number 9 is 0.000000000000000
```

2.6. Check number 5:

```
/* USER CODE BEGIN 3 */
           sprintf(name, "num5.bmp");
           file ready = 0;
 310
           read bmp(name);
 311
📃 Console 🦃 Problems 🕠 Executables 🖳 Debugger Console
Port 0 🟻
prediction of number 0 is 0.000000000000000
prediction of number 1 is 0.000000000000000
prediction of number 2 is 0.000000000000000
prediction of number 3 is 0.000000000000000
prediction of number 4 is 0.000000000000000
prediction of number 5 is 1.000000000000000
prediction of number 6 is 0.000000000000000
prediction of number 7 is 0.000000000000000
prediction of number 8 is 0.000000000000000
prediction of number 9 is 0.000000000000000
```

2.7. Check number 6:

```
/* USER CODE BEGIN 3 */
           sprintf(name, "num6.bmp");
§309
           file ready = 0;
😑 Console 🦃 Problems 🕡 Executables 🔛 Debugger Consc
Port 0 🖾
prediction of number 0 is 0.000000000000000
prediction of number 1 is 0.000000000000000
prediction of number 2 is 0.0000000000000000
prediction of number 3 is 0.000000000000000
prediction of number 4 is 0.000000000000000
prediction of number 5 is 0.000000000599480
prediction of number 6 is 0.999999999400520
prediction of number 7 is 0.000000000000000
prediction of number 8 is 0.000000000000000
prediction of number 9 is 0.000000000000000
```

2.8. Check number 7:

```
/* USER CODE BEGIN 3 */
 308
           sprintf(name, "num7.bmp");
           file ready = 0;
 310
           read bmp(name);
😑 Console 🧖 Problems 🜘 Executables 🖳 Debugger Console
Port 0 🛭
prediction of number 0 is 0.000000000000000
prediction of number 1 is 0.000010782232172
prediction of number 2 is 0.000000000004559
prediction of number 3 is 0.000000000000112
prediction of number 4 is 0.000000000000000
prediction of number 5 is 0.000000000000000
prediction of number 6 is 0.000000000000000
prediction of number 7 is 0.999989217763128
prediction of number 8 is 0.000000000000029
prediction of number 9 is 0.000000000000000
```

2.9. Check number 8:

```
/* USER CODE BEGIN 3 */
 308
           sprintf(name, "num8.bmp");
 309
 310
           file ready = 0;
           read bmp(name);
₿311
📃 Console 🤰 Problems 🕠 Executables 🛮 🖳 Debugger Consc
Port 0 🛭
prediction of number 0 is 0.000000000000000
prediction of number 1 is 0.000000000000000
prediction of number 2 is 0.000000000000000
prediction of number 3 is 0.000000275727878
prediction of number 4 is 0.000000000000000
prediction of number 5 is 0.000381166275216
prediction of number 6 is 0.999616711888520
prediction of number 7 is 0.000000000000000
prediction of number 8 is 0.000001846108386
prediction of number 9 is 0.000000000000000
```

2.10. Check number 9:

```
308
           /* USER CODE BEGIN 3 */
           sprintf(name, "num9.bmp");
309
 310
           file ready = 0;
           read bmp(name);
311
Console Problems  Executables  Debugger Console
Port 0 🖾
prediction of number 0 is 0.000000000000000
prediction of number 1 is 0.000000000245994
prediction of number 2 is 0.000000001384368
prediction of number 3 is 0.009116702831457
prediction of number 4 is 0.0000000000000021
prediction of number 5 is 0.000000000031443
prediction of number 6 is 0.000000000000000
prediction of number 7 is 0.171443969332484
prediction of number 8 is 0.000000001549626
prediction of number 9 is 0.819439324624608
```

3. Discussion

We planned to have two convolution layers and two pooling layers in the first place. When we first tested our model, however, we used very small numbers for each convolution layer channel. (6 for each.) This led to many failures in the digit recognition. Only half of the test images were recognized. As we increased the number of channels, the program worked better.

Still, the program is not able to recognize 8. We tried to modify the "epochs" in the training steps as the project instruction suggested. Unfortunately, there was a limited improvement and the digit 8 was still not recognized. Further testing and modifications are needed for fixing this issue.

4. Code

4.1. main():

```
241
         /* USER CODE BEGIN 3 */
242
243
         sprintf(name, "num9.bmp");
244
         file ready = 0;
245
         read_bmp(name);
246
         if (file_ready == 1) {
247
             out img = ProcessBmp(rtext);
248
             break;
 249
         }
 250
       }
 251
252
       //read in parameters
253
       sprintf(name, "b1.txt");
254
       float * b1 = read_txt(name, 16);
255
 256
       sprintf(name, "w1.txt");
 257
       float * w1 = read_txt(name, 144);
 258
 259
       sprintf(name, "b2.txt");
260
       float * b2 = read_txt(name, 32);
261
262
       sprintf(name, "w2.txt");
 263
       float * w2 = read_txt(name, 4608);
 264
 265
       sprintf(name, "bc.txt");
 266
       float * bc = read_txt(name, 10);
 267
268
       sprintf(name, "fc.txt");
 269
       float * fc = read_txt(name, 15680);
270
```

```
271
      // perform NN operation
272
       float *result_conv_1 = (float *)malloc(28*28*16*sizeof(float));
273
       conv(out_img, w1, b1, result_conv_1, 28, 28, 1, 3, 16);
274
275
      float *result_pool_1 = (float *)malloc(14*14*16*sizeof(float));
276
       pool(result_conv_1, result_pool_1, 28, 28, 16, 2);
277
       free(result conv 1);
278
       free(w1);
279
       free(b1);
280
281
       float *result conv 2 = (float *)malloc(14*14*32*sizeof(float));
282
       conv(result_pool_1, w2, b2, result_conv_2, 14, 14, 16, 3, 32);
283
       free(result_pool_1);
284
285
       float *result pool_2 = (float *)malloc(7*7*32*sizeof(float));
286
       pool(result_conv_2, result_pool_2, 14, 14, 32, 2);
287
       free(result_conv_2);
288
       free(w2);
289
       free(b2);
290
291
       double *result_dense = (double *)malloc(10*sizeof(double));
292
       dense(result pool 2, fc, bc, result dense, 7*7*32, 10);
293
       free(result_pool_2);
294
295
       for (int i=0;i<10;i++){
296
           printf("prediction of number %d is %.15f\n", i, result_dense[i]);
297
298
       free(result_dense);
299
300
      while(1);
301
      /* USER CODE END 3 */
302 }
```

4.2. Convolution function:

```
102⊕ void padding(float input[],int input height, int input width){
103
          int input size = input height * input width;
104
          float input_1[input_size];
105
          for (int i = 0; i < input_size; i++) {
106
              input 1[i] = input[i];
107
          }
108
109
          int padwid = input width + 2;
110
          int padheight = input height +2;
111
          int padsize = padwid * padheight;
112
113
          for (int i = 0; i < padwid; i++) {
114
              input[i] = 0;
115
          }
116
          for (int i= padwid * (input_height + 1); i < padsize; i++) {</pre>
117
118
              input[i] = 0;
119
120
121
          for (int i = padwid; i < padwid * (input height + 1); i++){</pre>
122
               if (i% padwid == 0 | i % padwid == padwid-1) {
123
                input[i] = 0;
124
125
               else {
126
                input[i] = input 1[i-(padwid+1)-((int)(i/padwid)-1)*2];
127
128
          }
129
     }
130
```

```
1310 void conv (float input[], float kernel[], float bias[], float result[], int input_height, int input_width, int input_channel, int kernel_size, int kernel_channel)
132 {
133
         padding(input, input_height, input_width);
134
         int result_size = input_height * input_width * kernel_channel;
135
         float sum;
136
         for(int n=0;n<kernel_channel;n++){
137
             for (int i=0;i<input_height;i++){
138
                 for (int j=0;j<input width;j++){
139
                     sum=0:
140
                     for(int k=0;k<kernel channel;k++){
                         sum+=(input[(i+0)*input_channel*kernel_channel+j*kernel_channel+k]*kernel[0*kernel_channel*kernel_channel+k*kernel_channel+h])
141
142
                                 +(input[(i+0)*16*kernel channel+k|j+1)*kernel channel+k|*kernel[1*kernel channel*kernel channel+k*kernel channel+h])
                                 +(input[(i+0)*input_channel*kernel_channel+(j+2)*kernel_channel+k]*kernel[2*kernel_channel*kernel_channel+k*kernel_channel+n]);
143
                         sum+=(input[(i+1)*input_channel*kernel_channel+j*kernel_channel+k]*kernel[3*kernel_channel*kernel_channel+k*kernel_channel+h])
144
                                 +(input[(i+1)*16*kernel_channel+k(j+1)*kernel_channel+k)*kernel[4*kernel_channel*kernel_channel+k*kernel_channel+n])
145
                                 +(input[(i+1)*input_channel*kernel_channel+(j+2)*kernel_channel+k]*kernel[[5*kernel_channel*kernel_channel+k*kernel_channel+k];
146
147
                         sum+=(input[(i+2)*input_channel*kernel_channel+j*kernel_channel+k]*kernel[6*kernel_channel*kernel_channel+k*kernel_channel+n])
148
                                 +(input[(i+2)*16*kernel channel+k(j+1)*kernel channel+k]*kernel[7*kernel channel*kernel channel+k*kernel channel+h])
                                 +(input[(i+2)*input_channel*kernel_channel+(j+2)*kernel_channel+k]*kernel[8*kernel_channel*kernel_channel+k*kernel_channel+n]);
149
150
151
                     sum+=bias[n];
                     result[i*input_height*kernel_channel+j*kernel_channel+n]=sum;
153
154
                 }
             }
155
156
157
         //ReLU: Applied to every number after convolution
158
         for (int i = 0; i < result size; i++) {
159
             if (result[i] < 0) { result[i] = 0; }</pre>
160
161 }
```

4.3. Pooling function:

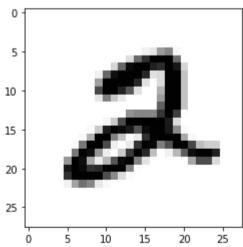
```
163@ void pool(float input[], float output[], int height, int width, int channel, int pool_size)
164 {
165
         float a, b;
         for (int k = 0; k < (height/pool size)*(width/pool size)*channel; k=k+(height/pool size)){</pre>
166
167
             for (int i = 0; i < (height/pool_size); i++) {</pre>
168
                 a = fmax(input[pool_size*(i+k)+pool_size*k], input[pool_size*(i+k)+pool_size*k+1]);
                 b = fmax(input[pool_size*(i+k)+pool_size*k +width], input[pool_size*(i+k)+pool_size*k + width +1]);
169
170
                 output[i+k] = fmax (a,b);
171
172
         }
173 }
```

4.4. Dense function:

```
175@ void dense(float input[], float kernel[], float bias[], double output[], int input_size, int output_size)
 177
          float y[output size];
 178
              for (int i = 0; i < output_size; i++){</pre>
 179
                  double sum = 0;
 180
                  for (int j=0; j<input_size; j++){</pre>
 181
                      sum = sum + kernel[i+output_size*j]*input[j];
 182
 183
                  y[i] = sum + bias[i];
              }
 184
 185
 186
              double total = 0;
              for (int i = 0; i < output size; i++){
 187
 188
                  total = total + exp(y[i]);
 189
              }
 190
              for (int i = 0; i < output_size; i++){</pre>
 191
 192
                  output[i] = exp(y[i]) / total;
 193
 194 }
195
```

Python Code

```
#import libraries for nerualnet, math and visualization
from future import absolute import, division, print function, unicode literals
try:
 # %tensorflow version only exists in Colab.
 %tensorflow version 2.x
except Exception:
  pass
import tensorflow as tf
import numpy as np
import matplotlib.pyplot as plt
from tensorflow.keras import datasets, layers, models
print(tf. version )
     2.7.0
#set seed just for the demonstration
#tf.random.set seed(1000);
#load in the MNIST dataset for training and testing
(train images, train labels), (test images, test labels) = datasets.mnist.load data()
#Plot an image to see what it looks like
plt.figure()
plt.imshow(train images[5], cmap=plt.cm.binary)
plt.grid(False)
plt.show()
       0
```



```
#TODO: Modify the CNN structure for a slimer network
#Build the neuralnet model
#model = models.Sequential()
#model.add(layers.Conv2D(32, (3, 3), activation='relu', input_shape=(28, 28, 1), padding='san
#model.add(layers.MaxPooling2D((2, 2)))
#model.add(layers.Conv2D(64, (3, 3), activation='relu', padding='same'))
#model.add(layers.MaxPooling2D((2, 2)))
```

```
#model.add(layers.Conv2D(64, (3, 3), activation='relu', padding='same'))
#model.add(layers.MaxPooling2D((2, 2)))
#model.add(layers.Flatten())
#model.add(layers.Dense(10, activation='softmax'))
#diem
model = models.Sequential()
model.add(layers.Conv2D(16, (3, 3), activation='relu', input_shape=(28, 28, 1), padding='same
model.add(layers.MaxPooling2D((2, 2)))
model.add(layers.Conv2D(32, (3, 3), activation='relu', padding='same'))
model.add(layers.MaxPooling2D((2, 2)))
#model.add(layers.Conv2D(6, (3, 3), activation='relu', padding='same'))
#model.add(layers.MaxPooling2D((2, 2)))
model.add(layers.Flatten())
model.add(layers.Dense(10, activation='softmax'))
#Review the overall model structure
model.summary()
```

Model: "sequential 1"

Layer (type)	Output Shape	Param #
conv2d_2 (Conv2D)	(None, 28, 28, 16)	160
<pre>max_pooling2d_2 (MaxPooling 2D)</pre>	(None, 14, 14, 16)	0
conv2d_3 (Conv2D)	(None, 14, 14, 32)	4640
<pre>max_pooling2d_3 (MaxPooling 2D)</pre>	(None, 7, 7, 32)	0
flatten_1 (Flatten)	(None, 1568)	0
dense_1 (Dense)	(None, 10)	15690
Total params: 20,490		=======

Trainable params: 20,490 Non-trainable params: 0

```
#Review the overall model structure
#model.summary()
#Reshape the image so it can train in batch (and fit the model's input shape)
train images = train images.reshape((60000, 28, 28, 1))
test_images = test_images.reshape((10000, 28, 28, 1))
#Training the model
#Hint: change optimizer to 'sgd', and increase epochs if result is bad.
```

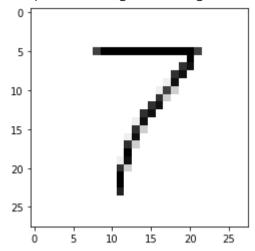
```
model.compile(optimizer='adam',
   loss='sparse categorical crossentropy',
   metrics=['accuracy'])
model.fit(train images, train labels, epochs=20)
 Epoch 1/20
 Epoch 2/20
 Epoch 3/20
 Epoch 4/20
 Epoch 5/20
 Epoch 6/20
 Epoch 7/20
 Epoch 8/20
 Epoch 9/20
 Epoch 10/20
 Epoch 11/20
 Epoch 12/20
 Epoch 13/20
 Epoch 14/20
 Epoch 15/20
 Epoch 16/20
 Epoch 17/20
 Epoch 18/20
 Epoch 19/20
 Epoch 20/20
 1875/1875 [=================== ] - 43s 23ms/step - loss: 0.0219 - accuracy: 0
 <keras.callbacks.History at 0x7effd1b8c4d0>
```

```
#Evaluate the performance with testing dataset
print("Accuracy of this model is:")
model.evaluate(test_images, test_labels)
```

4

```
[0.13846145570278168, 0.9842000007629395]
#View the total number of parameters, so it doesn't overflow the LCDK's memory
print("Total amount of parameter of model is:", model.count params())
     Total amount of parameter of model is: 20490
#Example for extract parameter form the first conv layer
#TODO: you need to actually modify model.layers[XXXX], this XXX to fit your actually layer nu
t1, t2 = model.layers[0].get weights()
np.savetxt('w1.txt', t1.flatten(), delimiter=',',fmt='%.16f')
np.savetxt('b1.txt', t2.flatten(), delimiter=',',fmt='%.16f')
#Example for extract parameter form the second conv layer
#TODO: you need to actually modify model.layers[XXXX], this XXX to fit your actually layer nu
#And do it multiple times to save all the layer with parameters
t1, t2 = model.layers[2].get weights()
np.savetxt('w2.txt', t1.flatten(), delimiter=',',fmt='%.16f')
np.savetxt('b2.txt', t2.flatten(), delimiter=',',fmt='%.16f')
# t1, t2 = model.layers[4].get weights()
# np.savetxt('w3.txt', t1.flatten(), delimiter=',',fmt='%.16f')
# np.savetxt('b3.txt', t2.flatten(), delimiter=',',fmt='%.16f')
t1, t2 = model.layers[5].get weights()
np.savetxt('fc.txt', t1.flatten(), delimiter=',',fmt='%.16f')
np.savetxt('bc.txt', t2.flatten(), delimiter=',',fmt='%.16f')
import cv2
im = cv2.imread("num7.bmp")
im = cv2.flip(im,0)
im = im[:,:,0]
for i in range (28):
  for j in range (28):
    im[i,j]=255 -im[i,j]
im.shape
     (28, 28)
plt.imshow(im, cmap=plt.cm.binary)
```

<matplotlib.image.AxesImage at 0x7effd18bcbd0>



im = im.reshape(1,28,28,1)

model.predict(im)

```
array([[6.9705730e-35, 1.5201940e-16, 1.3742151e-22, 2.0156587e-24,
        1.5461872e-13, 1.7622024e-19, 2.1085472e-21, 1.0000000e+00,
        2.8086321e-19, 6.5138695e-19]], dtype=float32)
```