

In [1]:

```
import pandas as pd
import numpy as np
import matplotlib.pyplot as plt
import scipy as sc
from scipy.stats import linregress
```

In [4]:

```
df = pd.read_csv("task2.csv", sep=";")
df = df[df.index > 0]
df
```

Out[4]:

| | Name | ВПАВ | Ввода | C | sigma | h | h1 | h2 | h3 | h4 | h6 |
|----|------|------|-------|----------|-----------|-------------|------|------|------|------|------|
| 1 | 1 | 1.0 | 29.0 | 0.006667 | 68.070860 | 3632.083333 | 3637 | 3612 | 3654 | 3616 | 3627 |
| 2 | 2 | 1.5 | 28.5 | 0.010000 | 66.132672 | 3528.666667 | 3532 | 3538 | 3537 | 3511 | 3509 |
| 3 | 3 | 2.0 | 28.0 | 0.013333 | 63.802473 | 3404.333333 | 3405 | 3396 | 3402 | 3419 | 3378 |
| 4 | 4 | 2.5 | 27.5 | 0.016667 | 61.430106 | 3277.750000 | 3270 | 3271 | 3276 | 3277 | 3269 |
| 5 | 5 | 3.5 | 26.5 | 0.023333 | 58.573582 | 3125.333333 | 3119 | 3154 | 3152 | 3104 | 3102 |
| 6 | 6 | 5.0 | 25.0 | 0.033333 | 54.533216 | 2909.750000 | 2907 | 2910 | 2905 | 2904 | 2924 |
| 7 | 7 | 7.5 | 22.5 | 0.050000 | 49.230920 | 2626.833333 | 2631 | 2634 | 2628 | 2630 | 2633 |
| 8 | 8 | 10.0 | 20.0 | 0.066667 | 44.451826 | 2371.833333 | 2384 | 2383 | 2393 | 2337 | 2359 |
| 9 | 9 | 15.0 | 15.0 | 0.100000 | 38.442036 | 2051.166667 | 2064 | 2036 | 2084 | 2030 | 2069 |
| 10 | 10 | 20.0 | 10.0 | 0.133333 | 34.560974 | 1844.083333 | 1844 | 1836 | 1850 | 1876 | 1831 |
| 11 | 11 | 30.0 | 0.0 | 0.200000 | 28.874477 | 1540.666667 | 1531 | 1527 | 1523 | 1546 | 1542 |
| 12 | 6Y | 5.0 | 25.0 | 0.033333 | 61.003735 | 3255.000000 | 3238 | 3231 | 3268 | 3233 | 3246 |
| 13 | 7Y | 7.5 | 22.5 | 0.050000 | 53.026084 | 2829.333333 | 2800 | 2823 | 2833 | 2836 | 2830 |
| 14 | 8Y | 10.0 | 20.0 | 0.066667 | 52.582534 | 2805.666667 | 2774 | 2805 | 2776 | 2802 | 2805 |
| 15 | 9Y | 15.0 | 15.0 | 0.100000 | 47.070957 | 2511.583333 | 2520 | 2516 | 2521 | 2536 | 2522 |
| 16 | 10Y | 20.0 | 10.0 | 0.133333 | 42.265312 | 2255.166667 | 2238 | 2291 | 2242 | 2230 | 2279 |
| 17 | 11Y | 30.0 | 0.0 | 0.200000 | 42.195031 | 2251.416667 | 2242 | 2240 | 2233 | 2246 | 2244 |

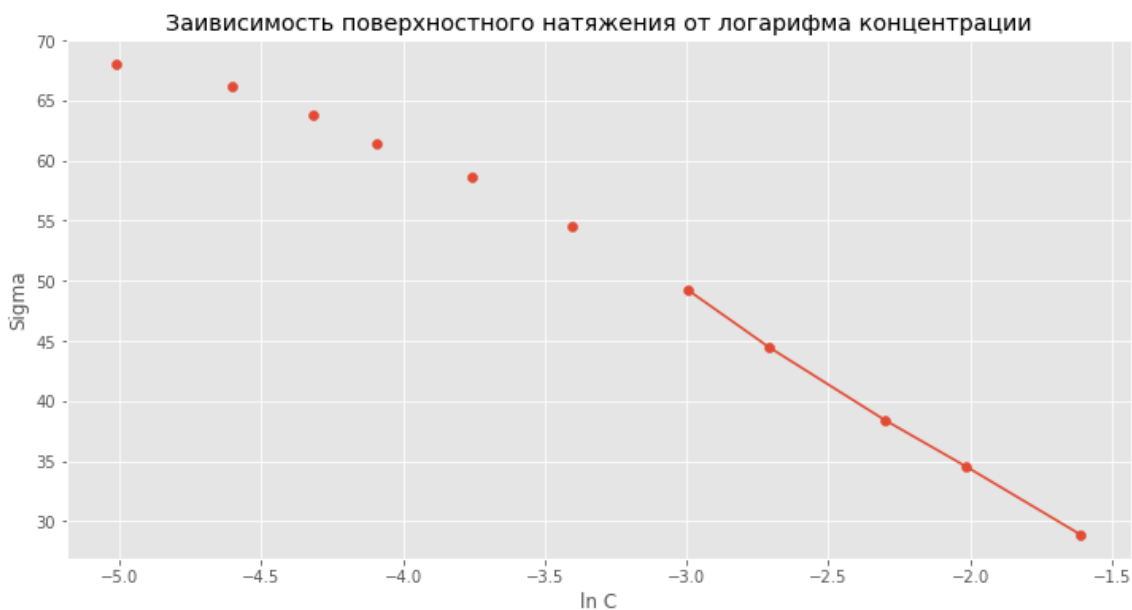
In [32]:

```
plt.figure(figsize=(12, 6))
plt.style.use("ggplot")
tmp = df[df.index < 12]
plt.scatter(np.log(tmp["C"]), tmp["sigma"])

tmp = df[(df.index < 12) & (df.index > 6)]
plt.plot(np.log(tmp["C"]), tmp["sigma"])
plt.title("Зависимость поверхностного натяжения от логарифма концентрации")
plt.xlabel("ln C")
plt.ylabel("Sigma")
slope, intercept, r_value, p_value, std_err = linregress(np.log(tmp["C"]), tmp["sigma"])
slope, intercept, r_value, p_value, std_err
```

Out[32]:

```
(-14.589271886782937,
 5.175333047657645,
 -0.9993560176529759,
 1.9615656380635667e-05,
 0.30243692027339886)
```



In [11]:

```
C1 = intercept
b = -slope
C1, b
```

Out[11]:

```
(5.175333047657645, 14.589271886782937)
```

In [12]:

```
sigma0 = 72.75
```

In [13]:

```
A = np.exp((sigma0 - C1) / b)
A
```

Out[13]:

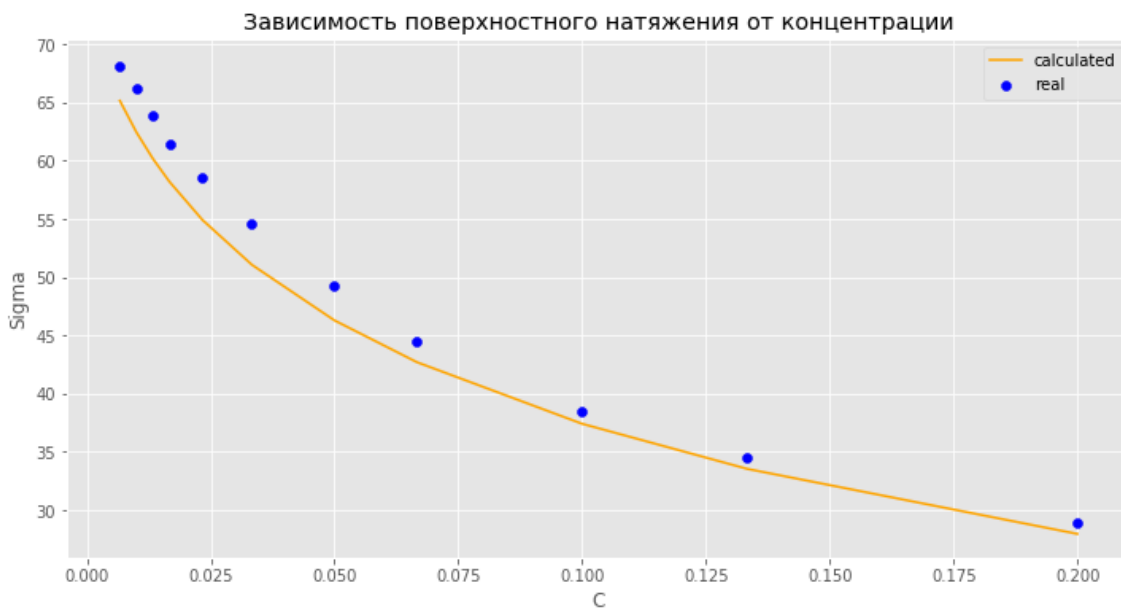
102.69930063530747

In [25]:

```
plt.figure(figsize=(12, 6))
df["sigmaR"] = sigma0 - b*np.log(1 + A * df["C"])
tmp = df[df.index < 12]
plt.plot(tmp["C"], tmp["sigmaR"], color="orange", label="calculated")
plt.scatter(tmp["C"], tmp["sigma"], color="blue", label="real")
plt.xlabel("C")
plt.ylabel("Sigma")
plt.title("Зависимость поверхностного натяжения от концентрации")
plt.legend()
```

Out[25]:

<matplotlib.legend.Legend at 0x7f3ccad6bf28>

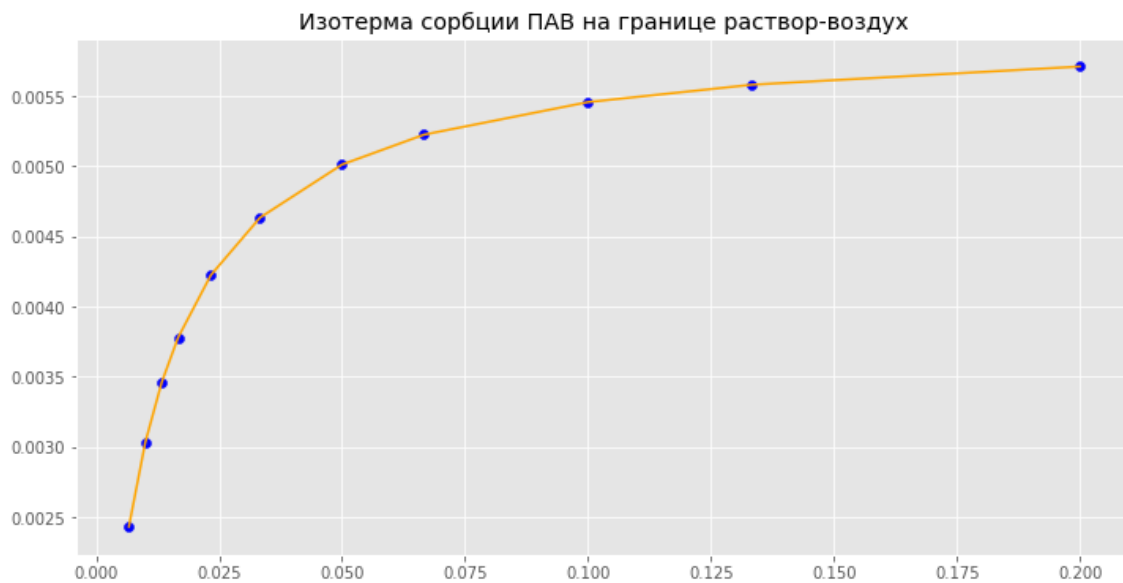


In [29]:

```
R = 8.314
T = 293.15
plt.figure(figsize=(12, 6))
df["Г"] = b / (R * T) * A * df["C"] / (1 + A * df["C"])
tmp = df[df.index < 12]
plt.title("Изотерма сорбции ПАВ на границе раствор-воздух")
plt.plot(tmp["C"], tmp["Г"], color="orange")
plt.scatter(tmp["C"], tmp["Г"], color="blue")
```

Out[29]:

<matplotlib.collections.PathCollection at 0x7f3cca9c3550>

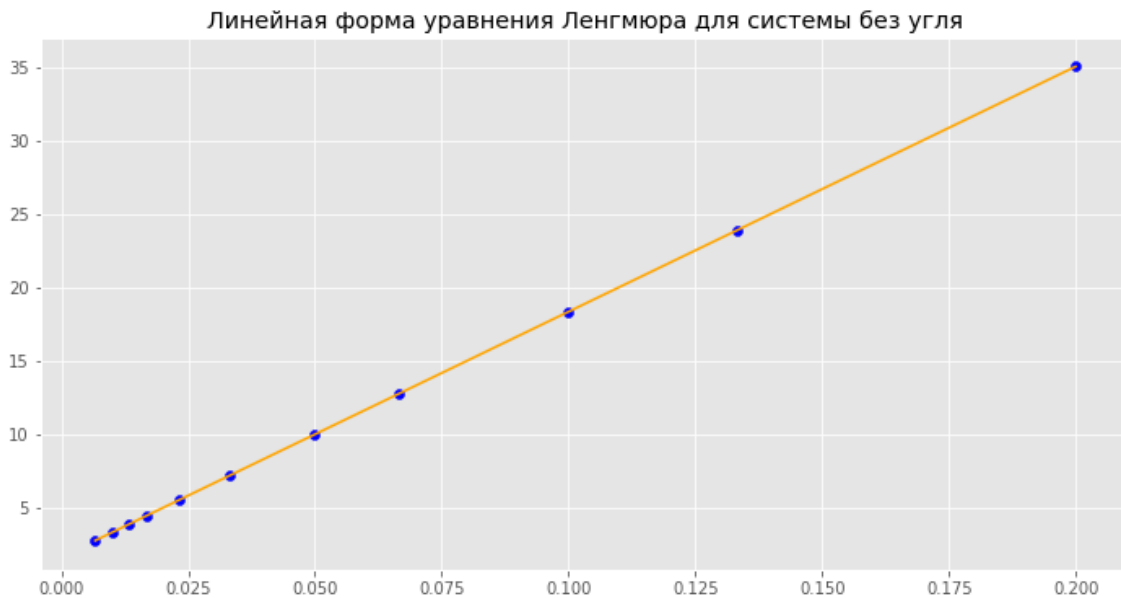


In [35]:

```
plt.figure(figsize=(12, 6))
plt.title("Линейная форма уравнения Ленгмюра для системы без угля")
tmp = df[df.index < 12]
plt.plot(tmp["C"], tmp["C"]/tmp["Г"], color="orange")
plt.scatter(tmp["C"], tmp["C"]/tmp["Г"], color="blue")
slope, intercept, r_value, p_value, std_err = linregress(tmp["C"], tmp["C"]/tmp["Г"])
slope, intercept, r_value, p_value, std_err
```

Out[35]:

```
(167.05762418534482, 1.626667593176494, 1.0, 5.8534851285390365e-90,
0.0)
```



In [36]:

```
Гm = 1/slope
Гm
```

Out[36]:

```
0.0059859584671845545
```

In [37]:

```
s0 = 1 / (Гm * 6.02e23)
s0
```

Out[37]:

```
2.7750435911186844e-22
```

In [38]:

```
delta0 = Гm * (12*5+11+17) / 1000 / 814
delta0
```

Out[38]:

```
6.471306451010328e-07
```

In []:

In [43]:

```
def sigma(C):  
    return sigma0 - b*np.log(1 + A * C)
```

In [44]:

```
def C(sigma):  
    return (np.exp((sigma0 - sigma)/b) - 1) / A
```

In []:

In [58]:

```
df["C*"] = C(df["sigma"])  
df["Γ*"] = (df["C"] - df["C*"]) * 30 / 1e6 / 1e-3
```

In []: