



# A combinatorial evolutionary algorithm for unrelated parallel machine scheduling problem with sequence and machine-dependent setup times, limited worker resources and learning effect

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## ABSTRACT

The existing papers on unrelated parallel machine scheduling problem with sequence and machine-dependent setup times (UPMSP-SMDST) ignore the worker resources and learning effect. Given the influence and potential of human factors and learning effect in real production systems to improve production efficiency and decrease production cost, we propose a UPMSP-SMDST with limited worker resources and learning effect (NUPMSP). In the NUPMSP, the workers have learning ability and are categorized to different skill levels, i.e., a worker's skill level for a machine is changing with his accumulating operation times on the same machine. A combinatorial evolutionary algorithm (CEA) which integrates a list scheduling (*LS*) heuristic, the shortest setup time first (*SST*) rule and an earliest completion time first (*ECT*) rule is presented to solve the NUPMSP. In the experimental phase, 72 benchmark instances of NUPMSP are constructed to test the performance of the CEA and facilitate future study. The Taguchi method is used to obtain the best combination of key parameters of the CEA. The effectiveness of the *LS*, *SST* and *ECT* is verified based on 15 benchmark instances. Extensive experiments conducted to compare the CEA with some well-known algorithms confirm that the proposed CEA is superior to these algorithms in terms of solving accuracy and efficiency.

## 1. Introduction

Unrelated parallel machine scheduling problem (UPMSP) with sequence and machine-dependent setup times (UPMSP-SMDST) is an extension of classical parallel machine scheduling problem, in which machines are non-identical and jobs' setup times depend on both sequence and machines. It is very difficult to tackle even if there is only one machine which is equivalent to the traveling salesman problem and has been proven to be NP-hard problem (Błażewicz, Ecker, Pesch, Schmidt, & Weglarz, 1996). However, due to the broad application in many real production systems such as truss industry (Rabadi, Moraga, & Al-Salem, 2006), printed writing board manufacturing industry (S.-W. Lin & Ying, 2014), photolithography workshop in Semiconductor manufacturing (Bitar, Dauzere-Peres, Yugma, & Roussel, 2016) and Heating, Ventilation and Air Conditioning factory (Perez-Gonzalez, Fernandez-Viagas, Zamora Garcia, & Framinan, 2019), the UPMSP-SMDST has become a research hotspot in the latest two decades.

Rabadi, et al. (2006) were among the first to consider UPMSP-

SMDST. They proposed a new metaheuristic for randomized priority search to address it with the criterion of minimizing the makespan. Later, some single-objective algorithms also have been proposed to optimize the makespan of UPMSP-SMDST, including two stage ant colony optimization algorithm (Arnaout, Rabadi, & Musa, 2010), improved genetic algorithm (Vallada & Ruiz, 2011), variable neighborhood descent search algorithm (Fleszar, Charalambous, & Hindi, 2012), restricted simulated annealing algorithm (Ying, Lee, & Lin, 2012), modified hybrid artificial bee colony algorithm (S.-W. Lin & Ying, 2014), immune inspired algorithm (Marinho Diana, de Franca Filho, de Souza, & de Almeida Vitor, 2015), improved combinatorial benders decomposition (Abreu Gomes & Mateus, 2017), improved firefly algorithm (Ezugwu & Akutsah, 2018), novel constraint programming approach (Gedik, Kalathia, Egilmez, & Kirac, 2018) and enhanced symbiotic organisms search algorithm (Ezugwu, 2019). For the mathematical model of UPMSP-SMDST with makespan minimization, Avalos-Rosales, Angel-Bello, and Alvarez (2015) proposed several mixed integer programming models, which are much better than previous

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models in solving instance size. Bozorgirad and Logendran (2012) investigated an extension of UPMS-P-SMDST, in which jobs were clustered in different groups, setup times were only considered between groups, and job ready times and machine availability times were considered as well. They constructed an improved tabu search algorithm for their problem with the objective of minimizing the sum of total weighted completion time and total weighted tardiness. Costa, Cappadonna, and Fichera (2013) studied the UPMS-P-SMDST with limited multi-skilled workers who were responsible to perform setup activities and developed a hybrid genetic algorithm to solve the problem. A similar model was proposed by Bektur and Sarac (2019), who considered a common server instead of multi-skilled workers to perform sequence-dependent setup activity. They were the first to use the tabu search algorithm for their problem with minimum total weighted tardiness. Y.-K. Lin and Hsieh (2014) researched the UPMS-P-SMDST with constraints that different jobs had different ready times. They proposed an iterated hybrid metaheuristic for their problem whose objective was the minimum total weighted tardiness. Rauchecker and Schryen (2019) tackled the UPMS-P-SMDST considering machine eligibility constraints with the criterion of minimum total weighted completion time. They proposed an exact branch and price algorithm for their problem, in which a parallelization strategy was incorporated to speed up the computing efficiency. Perez-Gonzalez, et al. (2019) added the machine eligibility and job due dates restrictions into UPMS-P-SMDST to minimize the total tardiness. Several adaptive methods based on similar problem and five constructive heuristics were presented for their problem.

Apart from the single-objective algorithms, some studies have focused on multi-objective algorithms for the UPMS-P-SMDST. For example, Torabi, Sahebjamnia, Mansouri, and Bajestani (2013) studied a multi-objective UPMS-P-SMDST with three performance criteria of minimum total weighted flow time, minimum total weighted tardiness and minimum total machine load variation. They proposed a multi-objective particle swarm optimization algorithm for their model, in which they considered secondary resource constraints for jobs, uncertainty in processing time and due date. Xue, Rui, Yu, Sang, and Liu (2019) investigated a bi-objective UPMS-P-SMDST considering machines' processing speed, whose criteria were to minimize both makespan and total carbon emission. They proposed an estimation of distribution evolution memetic algorithm for addressing the problem. M. Wang and Pan (2019) proposed a bi-objective UPMS-P-SMDST considering preventive maintenance and designed a novel imperialist competitive algorithm to minimize makespan and total tardiness.

Through the review of related work on UPMS-P-SMDST above, we observe that few researchers consider the limited worker resources and no previous work has studied the UPMS-P-SMDST taking limited worker resources and learning effect into consideration simultaneously. Possible reasons for this have been discussed by some researchers. Othman, Gouw, and Bhuiyan (2012) outlined some reasons for ignoring human resources, such as humans are hard to be modeled since they are too abstract and people are adaptive. Lei and Guo (2014) stated that some traditional scheduling problems assumed that workers were plentiful and the labor cost was lower than that of machines, which contradicts reality. In the real production systems, the worker resources are the key elements which cannot be ignored in a production system, and the machines would be in idle state when they are waiting for setup server/workers, indicating that a well schedule on worker resources can effectively improve the production efficiency (Bektur & Sarac, 2019; Costa, et al., 2013; Huang, Cai, & Zhang, 2010). Some researchers, such as Bautista, Alfaro-Pozo, and Batalla-Garcia (2015), Touat, Bouzidi-Hassini, Benbouzid-Sitayeb, and Benhamou (2017), G. Gong, Chiong, Deng, and Gong (2019), Sheikhalishahi, Eskandari, Mashayekhi, and Azadeh (2019), Yepes-Borrero, Villa, Perea, and Pablo Caballero-Villalobos (2020) and G. Gong, et al. (2020), emphasized that the human factors should be considered in the manufacturing systems for their potential to improve production efficiency and decrease

production cost, especially in highly-manual mixed-model assembly systems (Ostermeier, 2019). Some scholars have further pointed out that both processing time of jobs (Anzanello & Fogliatto, 2010; Hamta, Ghomi, Jolai, & Shirazi, 2013; C. Wu, Lee, & Liou, 2013; R. Wu, Li, Guo, & Xu, 2018) and setup times (Exposito-Izquierdo, Angel-Bello, Melian-Batista, Alvarez, & Baez, 2019; J.-B. Wang, et al., 2009) can be reduced attributing to the learning effect of workers. D. Biskup (1999) have pointed out that, along with the accumulating repetitions on the same machine, the workers' skills will continuously improve and their operating speed to perform setup activities will increase. He further claimed that it is more reasonable to apply learning effect to the setup times if production process is fully automated (Dirk Biskup, 2008). The latest study about learning effect on setup times was presented by Exposito-Izquierdo et al. (2019), but the human resource constraints were ignored.

Inspired by these findings, we originally consider the worker resources and their learning effects simultaneously into UPMS-P-SMDST. This is significant to bridge the theoretical gaps and guide practical production. We denote this new model as NUPMSP throughout this paper. The proposed NUPMSP simultaneously considers the energy consumption and processing time related factors, which means that the proposed model can provide guidance of production for the managers aiming at decreasing production cost and protecting the environment. Given the effectiveness of evolutionary algorithms in solving NP-hard scheduling problems (Gao, et al., 2019; Soares & Carvalho, 2020; X. Wu & Che, 2019) and the characteristics of the proposed model, a new combinatorial evolutionary algorithm (CEA) is designed to solve the NUPMSP with two optimization objectives, in which some effective operators including an initialization operator with three new methods, a mutation operator and a selection operator are presented to help the CEA to obtain a high-quality population. In the experiment phase, a total of 72 NUPMSP benchmark instances are constructed; the effectiveness of the proposed initialization operator is verified based on 15 constructed benchmark instances; extensive experiment carried out verify that the proposed NUPMSP is superior to the nondominated neighbor immune algorithm (NNIA) (M. Gong, Jiao, Du, & Bo, 2008) and the non-dominated genetic algorithm-II (NSGA-II) (Deb, Pratap, Agarwal, & Meyarivan, 2002).

## 2. Mathematical programming model of the proposed NUPMSP

The model of NUPMSP can be described as follows. There are a set of  $n + 1$  independent jobs  $N = \{J_0, J_1, \dots, J_n\}$  where  $J_0$  denotes a dummy job, a set of  $w$  multi-skilled workers  $W = \{W_1, W_2, \dots, W_w\}$  and a set of  $m$  ( $m > w$ ) unrelated parallel machines  $M = \{M_1, M_2, \dots, M_m\}$  whose process is fully-automated. Each job except  $J_0$  has to be processed on exactly one machine out of the set  $M$  and its processing time varies with machines. Before a job is processed, a basic setup time for the job is required, which is sequence and machine dependent. For the factor of workers, their duty is to perform setup activities and they are featured with different initial skill levels for different machines and with the same learning rate.  $\eta_{lk}$  is used as a coefficient which reflects the initial skill level of worker  $l$  on machine  $k$  and  $\alpha$  is defined as the learning effect. This means that the setup times are also worker dependent. Due to the learning effect, the processing efficiency of a worker will increase, but it will stop when it reaches a given highest skill level  $d$  (Azzouz, Ennigrou, & Ben Said, 2018). For the factor of green indicator, the total energy consumption (TEC) of machines under different states is considered.

The objectives of the investigated problem are to minimize the maximum completion time among all jobs ( $C_{max}$ ) and the TEC. The TEC mainly includes two parts: the energy consumption in processing stage of each job and the energy consumption in standby state including the setup stage for each operation. The scheduling consists of three sub-problems: a) assigning a machine for each job; b) determining the job sequence on each machine; c) selecting a worker for the setup activity of each job before processing.

Some assumptions are put forward:

- 1) Preemption is not allowed;
- 2) Each machine cannot process more than one job at a time;
- 3) Each worker can perform at most one setup activity at a time;
- 4) A machine is not allowed to turn off before all jobs allocated to the machine are finished;
- 5) All jobs, workers and machines are available at time zero;
- 6) A dummy job  $J_0$  has been processed on each machine at time zero;
- 7) The actual setup time of  $J_i$ , which is performed by  $W_l$  and processed immediately after  $J_g$  on  $M_k$ , is calculated by formula (1) adapted from Dirk Biskup (2008).

$$Ts_{ijkl} = \max\{\eta_{lk}s_{gik}A_{ilk}^a, d \cdot s_{gik}\} \quad (1)$$

Where  $A_{ilk}$  is the number of times of  $W_l$  operating  $M_k$  before the machine processing  $J_i$ ,  $d$  is the limiting coefficient of workers and  $s_{gik}$  denotes the basic setup time of  $J_i$  which is immediately processed after  $J_g$  on  $M_k$ .

Indices:

- $i, j, g$ : indices of jobs,  $i, j, g = 0, 1, \dots, n$ ;
- $k$ : index of machines,  $k = 1, 2, \dots, m$ ;
- $l, h$ : index of workers,  $l, h = 1, 2, \dots, w$  ( $w < m$ );
- $r$ : sequential index of setup activities performed by the same worker, where  $r \leq n$  is a positive integer;
- $t, e$ : position index on each machine, where  $t = 0$  denotes the dummy position to assign the dummy job;

Parameters:

- $n$ : total number of jobs;
- $w$ : total number of workers;
- $m$ : total number of machines;
- $p_{ik}$ : the processing time of  $J_i$  on  $M_k$ ;
- $\eta_{lk}$ : the initial coefficient of  $W_l$  on  $M_k$ ;
- $a$ : the learning effect of workers;
- $d$ : the limiting coefficient of workers;
- $C_i$ : the completion time of  $J_i$ ;
- $CM_k$ : the maximum completion time of jobs processed on  $M_k$ ;
- $CS_i$ : the completion time of the setup activity of  $J_i$ ;
- $A_{ikt}$ : the number of times of  $W_l$  operating  $M_k$  before the machine processing the job on its  $t$ th position;
- $s_{jik}$ : the basic setup time of  $J_j$  on  $M_k$ , immediately after  $J_i$  has been processed on  $M_k$ ;
- $Ts_{ijkl}$ : the actual setup time of  $J_j$  performed by  $W_l$  if  $J_j$  is processed immediately after  $J_i$  on  $M_k$ ;
- $PP_k$ : the processing power of  $M_k$ ;
- $SP_k$ : the standby power of  $M_k$ ;
- $B$ : a big enough number;

Decision variables:

$$x_{iktl} = \begin{cases} 1 & \text{if } J_i \text{ is assigned to position } t \text{ on } M_k \\ & \text{and its setup activity is performed by } W_l \\ 0 & \text{otherwise} \end{cases}$$

$$z_{ilr} = \begin{cases} 1 & \text{if the setup activity of } J_i \text{ is processed} \\ & \text{in the } r\text{th position on worker } l \\ 0 & \text{otherwise} \end{cases}$$

The mathematical models for UPMS-P-SMDST proposed by Avalos-Rosales, et al. (2015) and Abreu Gomes and Mateus (2017) provide a great reference for us to build the model. By referring to these models, the mathematical model of the proposed problem can be described as follows:

$$\min C_{max} \quad (2)$$

$$\min TEC = \sum_{k=1}^m \sum_{l=1}^w \sum_{i=1}^n \sum_{t=1}^n x_{iktl} p_{ik} PP_k + \sum_{k=1}^m \left[ CM_k - \sum_{l=1}^w \sum_{i=1}^n \sum_{t=1}^n x_{iktl} p_{ik} \right] SP_k \quad (3)$$

Subject to:

$$\sum_{k=1}^m \sum_{l=1}^w \sum_{t=1}^n x_{iktl} = 1, \forall i = 1, 2, \dots, n \quad (4)$$

$$\sum_{l=1}^w \sum_{t=1}^n x_{iktl} \leq 1, \forall t = 1, 2, \dots, n; k = 1, 2, \dots, m \quad (5)$$

$$\sum_{l=1}^w \sum_{i=1}^n x_{ik(t+1)l} \leq \sum_{l=1}^w \sum_{i=1}^n x_{iktl}, \quad \forall t = 1, 2, \dots, n-1; k = 1, 2, \dots, m \quad (6)$$

$$\sum_{l=1}^w \sum_{r=1}^n z_{ilr} = 1, \forall i = 1, 2, \dots, n \quad (7)$$

$$\sum_{t=1}^n z_{ilr} \leq 1, \forall l = 1, 2, \dots, w; r = 1, 2, \dots, n \quad (8)$$

$$\sum_{i=1}^n z_{ilr} \geq \sum_{i=1}^n z_{il(r+1)}, \forall l = 1, 2, \dots, w; r = 1, 2, \dots, n-1 \quad (9)$$

$$\sum_{r=1}^n z_{ilr} = \sum_{k=1}^m \sum_{t=1}^n x_{iktl}, \quad \forall i = 1, 2, \dots, n; l = 1, 2, \dots, w \quad (10)$$

$$C_g - CS_g \geq \sum_{k=1}^m \sum_{l=1}^w \sum_{t=1}^n x_{gkltl} p_{gk}, \forall g = 1, 2, \dots, n \quad (11)$$

$$A_{klt} = \max \left\{ \sum_{i=1}^n \sum_{e=1}^t x_{ikel}, 1 \right\}, \quad \forall k = 1, 2, \dots, m; t = 1, 2, \dots, n; l = 1, 2, \dots, w \quad (12)$$

$$Ts_{jikl} \geq \max\{\eta_{lk}s_{gik}(A_{klt})^a, d \cdot s_{gik}\} + B(x_{jk(t-1)h} + x_{iktl} - 2), \quad \forall i, t = 1, 2, \dots, n; j = 0, 1, \dots, n; i \neq j; k = 1, 2, \dots, m; h, l = 1, 2, \dots, w \quad (13)$$

$$CS_g - C_i \geq Ts_{igkl} + B(x_{ik(t-1)h} + x_{gkltl} - 2), \forall i = 0, 1, \dots, n; g, t = 1, 2, \dots, n; i \neq g; k = 1, 2, \dots, m; h, l = 1, 2, \dots, w \quad (14)$$

$$CS_i - CS_g \geq Ts_{jikl} + B(z_{il(r+1)} + z_{glr} + x_{jk(t-1)h} + x_{iktl} - 4) \quad \forall i, g, t = 1, 2, \dots, n; j = 0, 1, \dots, n; i \neq j; i \neq g; r = 1, 2, \dots, n-1; k = 1, 2, \dots, m; l, h = 1, 2, \dots, w; \quad (15)$$

$$C_{max} \geq C_i, \quad \forall i = 1, 2, \dots, n \quad (16)$$

$$CM_k \geq C_j + B \left( \sum_{l=1}^w \sum_{t=1}^n x_{jkltl} - 1 \right), \quad \forall j = 1, 2, \dots, n; k = 1, 2, \dots, m \quad (17)$$

$$C_0 = 0, x_{0k0l} = 1, Ts_{ijkl} \geq 0, \forall i = 1, 2, \dots, n; j = 0, 1, \dots, n; i \neq j; k = 1, 2, \dots, m; l = 1, 2, \dots, w \quad (18)$$

Equations (2)-(3) represent the objectives of minimizing makespan and *TEC* respectively. Constraint (4) ensures that each job is processed by only one machine with one position, and only one worker is selected to perform its setup activity. Constraint (5) ensures that at most one job is assigned to any position on a machine. Constraint (6) ensures that no vacant position exists before a filled position on a machine. Constraint (7) guarantees the setup activity of each job is performed at only one position on one worker. Constraint (8) ensures that at most one setup activity can be assigned to any position of any worker. Constraint (9) guarantees that there is no vacant position before a filled position of the

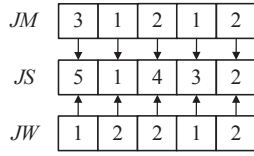


Fig. 1. An example of the solution representation.

same worker. Constraint (10) guarantees the relationship of  $z_{ilr}$  and  $x_{iktl}$ , which ensures that for any job  $J_i$ , only one worker performs its setup activity. Constraint (11) ensures that the completion time of a job is no less than the completion time of its setup activity plus the processing time of the job. Constraint (12) calculates the value of  $A_{ktl}$  and defines its minimum value as 1 to ensure that  $(A_{ktl})^a$  in constraint (13) is meaningful. Constraint (13) defines the lower bound of the actual setup time of  $J_i$  on  $M_k$ . Constraint (14) ensures that the gap between the completion time of the setup activity of a job and the completion time of the job's predecessor is no less than the setup time of the job. Constraint (15) guarantees the sequence constraint of setup activities processed by the same worker. Constraint (16) determines the makespan. Constraint (17) determines the maximum completion time of jobs assigned to each machine. Constraint (18) is sign constraints.

### 3. The proposed algorithm

In this section, we design a CEA for our NUPMSP. The main components of the CEA include four parts: solution representation, initialization, mutation and selection. The details of CEA are described as follows.

#### 3.1. Solution representation

A feasible solution of CEA for NUPMSP should solve three sub-problems: a) select a machine for each job; b) arrange the processing sequence of all jobs processed on the same machine; c) choose a suitable worker for each job's setup activity. Thereby, we propose an effective solution representation method with three vectors: job sequence (JS) vector, job-machine (JM) vector and job-worker (JW) vector. An example of this solution representation method is shown in Fig. 1, in which there are five jobs, three machines and two workers. The job, machine and worker sequences shown in Fig. 1 are as follows:  $(J_5, M_3, W_1)$ ,  $(J_1, M_1, W_2)$ ,  $(J_4, M_2, W_2)$ ,  $(J_3, M_1, W_1)$  and  $(J_2, M_2, W_2)$ , where  $(J_5, M_3, W_1)$  means that  $J_5$  is processed on  $M_3$  and its setup activity is executed by  $W_1$ ; others can be explained like this.

#### 3.2. Initialization

To produce high quality initial solutions, we used three methods: a) list scheduling (LS) heuristic proposed by Davis and Jaffe (1981); b) shortest setup time first (SST) rule (Pindeo, 2002); c) a earliest completion time first (ECT) rule designed by us. The LS heuristic is used

to select a suitable machine for each job, SST rule is introduced to optimize the job sequence on each machine, and ECT rule is designed to choose an appropriate worker for the setup activity of each job processed on each machine. A complete initial solution is generated through four steps as follows:

Step 1: Randomly generate a JS vector.

Step 2: For the JS vector, use the LS heuristic to select a machine for each job.

Step 3: Optimize the job sequence on each machine by SST rule.

Step 4: Carry out the ECT rule to determine a worker by which each job's setup activity is executed, to obtain the processing order shown as Fig. 1 and to compute the objectives.

Fig. 2 illustrates the steps about how to produce a high quality initial solution based on the given data in Tables 1 and 2. Fig. 3 is a Gantt chart based on the result in Fig. 2.

##### 3.2.1. LS heuristic

The LS heuristic is popular for assigning jobs effectively among several machines (X. Wu & Che, 2019). It depends on certain principle to select a machine for each job. Considering that the parallel machines are unrelated and one of the optimization objectives is makespan, we introduce a principle named processing efficiency to reflect the processing ability of each machine.

**Principle 1:** processing efficiency. We denote  $Te_{ik}$  as the processing efficiency of  $J_i$  on  $M_k$ , where  $Te_{ik} = (\min_{1 \leq k \leq m} p_{ik}) / p_{ik}$ .

Detailed steps of the LS heuristic used in this paper are depicted as follows:

Step 1: For each JS vector, set  $CM_k = 0$  for each  $M_k$  ( $k = 1, 2, \dots, m$ ) and calculate  $Te_{ik}$  for each job on each machine according to the job sequence in JS.

Step 2: Create a list  $l_k$  for each  $M_k$  by sorting all the unassigned jobs in non-increasing order of the values of  $Te_{ik}$ .

Step 3: If  $|JS| > 0$ , find  $M_k := \arg \min_{1 \leq k \leq m} CM_k$  (randomly select a machine if  $\min_{1 \leq k \leq m} CM_k$  exists on multiple machines) and find out the next unassigned job  $J_i$  in  $l_k$ ; otherwise, end the LS heuristic for this JS vector.

Step 4: If  $Te_{ik} > 1/\sqrt{m}$ , allocate  $M_k$  to process  $J_i$  and set  $CM_k := CM_k + p_{ik}$ ; otherwise, assign the big value  $B$  to  $C_k$  and return to step 3.

Step 5: Set  $l_k := l_k \setminus \{J_i\}$  for  $1 \leq k \leq m$  and set  $JS := JS \setminus \{J_i\}$ ; then return to step 3.

##### 3.2.2. SST rule

SST rule selects a job with the shortest setup time as the next job to be processed when the current job is finished, until all jobs have been assigned. It is similar to the nearest neighbor rule in Travelling Salesman Problem (TSP), which can effectively get a reasonable route. Due to the fact that both of the objectives can be minimized by reducing the total setup times and workers have the learning ability, the SST heuristic can

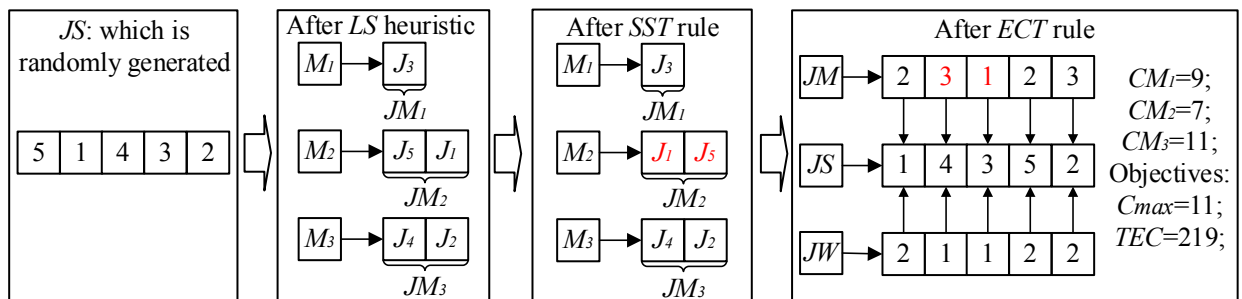


Fig. 2. Illustration of the Initialization procedure based on the data shown in Tables 1 and 2.

**Table 1**

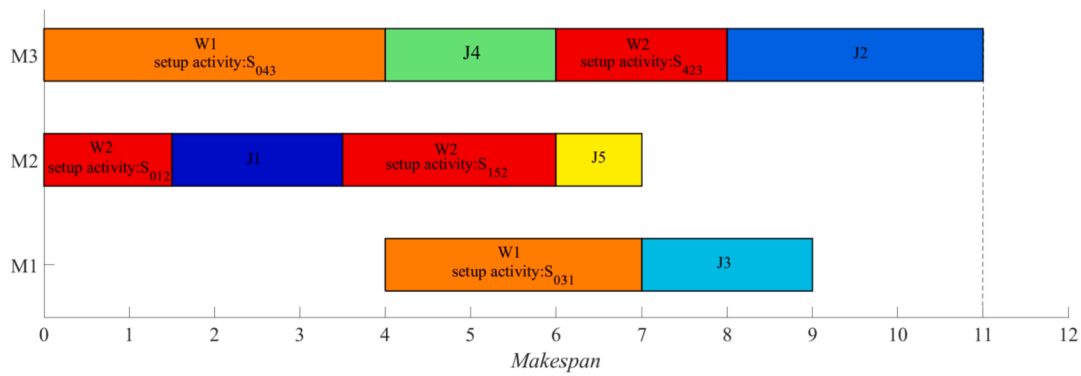
Relevant data of an example.

| $M_k$   | $P_{ik}$<br>$i = 1$ | $i = 2$ | $i = 3$ | $i = 4$ | $i = 5$ | $\eta_{lk}$<br>$l = 1$ | $l = 2$ | $a$    | $d$ | $PP_k$ | $SP_k$ |
|---------|---------------------|---------|---------|---------|---------|------------------------|---------|--------|-----|--------|--------|
| $k = 1$ | 4                   | 5       | 2       | 8       | 3       | 0.75                   | 1.5     | -0.152 | 0.5 | 11     | 5      |
| $k = 2$ | 2                   | 6       | 5       | 4       | 1       | 1.25                   | 0.5     |        |     | 16     | 2      |
| $k = 3$ | 5                   | 3       | 7       | 2       | 6       | 1                      | 1       |        |     | 14     | 6      |

**Table 2**

The setup times of the example shown in Table 1.

|         | $S_{ijk} (k=1)$<br>$i = 0$ | $i = 1$ | $i = 2$ | $i = 3$ | $i = 4$ | $i = 5$ | $S_{ijk} (k=2)$<br>$i = 0$ | $i = 1$ | $i = 2$ | $i = 3$ | $i = 4$ | $i = 5$ | $S_{ijk} (k=3)$<br>$i = 0$ | $i = 1$ | $i = 2$ | $i = 3$ | $i = 4$ | $i = 5$ |
|---------|----------------------------|---------|---------|---------|---------|---------|----------------------------|---------|---------|---------|---------|---------|----------------------------|---------|---------|---------|---------|---------|
| $j = 1$ | 2                          | 0       | 7       | 3       | 1       | 4       | 3                          | 0       | 1       | 5       | 7       | 6       | 2                          | 0       | 1       | 2       | 5       | 4       |
| $j = 2$ | 5                          | 4       | 0       | 8       | 4       | 1       | 6                          | 5       | 0       | 5       | 7       | 2       | 6                          | 5       | 0       | 1       | 2       | 5       |
| $j = 3$ | 4                          | 6       | 5       | 0       | 3       | 1       | 5                          | 6       | 7       | 0       | 2       | 8       | 5                          | 2       | 4       | 0       | 6       | 3       |
| $j = 4$ | 8                          | 4       | 6       | 1       | 0       | 2       | 1                          | 5       | 2       | 7       | 0       | 3       | 4                          | 5       | 2       | 6       | 0       | 1       |
| $j = 5$ | 7                          | 2       | 1       | 8       | 5       | 0       | 4                          | 5       | 8       | 1       | 6       | 0       | 7                          | 5       | 3       | 2       | 1       | 0       |

**Fig. 3.** The Gantt chart of the solution in Fig. 2.

have a positive impact on our performance criteria. Detailed steps of the SST rule used in this paper are described as below:

Step 1: We denote  $JM_k$  ( $k = 1, 2, \dots, m$ ) as the set of all jobs assigned to  $M_k$ , and assume a dummy job  $J_i$  ( $i = 0$ ) has been processed on  $M_k$  ( $k = 1, 2, \dots, m$ ). Then, set  $k = 1$ .

Step 2: If  $k \leq m$ , go to step 3; otherwise, end the SST rule.

Step 3: If  $|JM_k| > 0$ , select a job  $J_j \in JM_k$  with the minimum  $s_{ijk}$  and put it immediately after  $J_i$ . Then set  $JM_k := JM_k \setminus \{J_j\}$  and  $i := j$ . This means that  $J_j$  will be processed immediately after  $J_i$  and  $J_j$  will substitute  $J_i$  to choose a successor from  $JM_k$ .  $i = 0$  means  $J_j$  will be the first job processed on  $M_k$ .

Step 4: If  $|JM_k| = 0$ , set  $k := k + 1$  and return to step 2; otherwise, return to step 3.

### 3.2.3. ECT rule

After LS heuristic and SST rule, allocation of jobs to machines and jobs' sequence on each machine have been determined. To get a feasible solution shown as Fig. 1, we should select a worker for each job's setup activity and determine the processing order of all jobs. ECT rule is designed to choose an appropriate worker which can minimum the completion time of the current job, and to determine the scheduling sequence. Before detailing the steps of ECT rule, some parameters are introduced:  $RM_k$  denotes the ready time of  $M_k$  to process a new job;  $RW_l$  represents the ready time of  $W_l$  to perform a new setup activity;  $\mu_k$  is the index of the current job just completed on  $M_k$ ;  $CM_k$  represents the completion time of  $M_k$ . Detailed description of ECT rule is as follows:

Step 1: Input the results obtained by SST rule. We denote  $JM_k$  ( $k = 1, 2, \dots, m$ ) as the set of all jobs assigned to  $M_k$  and define  $S$  as the index of job's position in a scheduling sequence.

Step 2: Set  $RM_k = 0$  and  $\mu_k = 0$  for  $1 \leq k \leq m$ ,  $RW_l = 0$  for  $1 \leq l \leq w$  and  $S = 1$ .

Step 3: If  $RM_k = B$  ( $B$  is a large enough number) holds for each  $k \in \{1, 2, \dots, m\}$ , end the ECT rule and output the solution including its two objectives and  $CM_k$  for  $1 \leq k \leq m$ ; otherwise, go to step 4.

Step 4: Find  $M_k := \arg \min_{1 \leq k \leq m} RM_k$  (randomly select a machine if  $\min_{1 \leq k \leq m} RM_k$  exists on multiple machines).

Step 5: If  $|JM_k| > 0$ , find out the first job  $J_i$  in  $JM_k$  and set  $JM_k := JM_k \setminus \{J_i\}$ . Otherwise, set  $CM_k := RM_k$ , assign  $B$  to  $RM_k$  and return to step 3.

Step 6: Calculate the completion time  $C_i$  of  $J_i$  under each worker by formula (19), then select a worker  $W_l$  which can minimize the completion time of  $J_i$ .

Step 7: Update  $RM_k$  and  $RW_l$  by formulas (20) and (21) respectively, and set  $u_k := \tilde{i}$ .

Step 8: Put  $J_i$  in the position  $S$  and set  $S := S + 1$ . Then return to step 3.

$$C_i = \max\{RM_k, RW_l\} + \max\left\{\eta_{lk} s_{\mu_k \tilde{i} k} \left(\sum_{j=0, j \neq i}^n y_{j \tilde{i} k l}\right)^a, d \cdot s_{\mu_k \tilde{i} k}\right\} \quad (19)$$

$$RM_k = C_i \quad (20)$$

$$RW_l = C_i - p_{\tilde{i} k} \quad (21)$$

### 3.3. Mutation

Due to the rigid initialization procedure, the searching space cannot contain all the solution space and is easy to fall into local optimum. Thus, two mutation operators are designed to improve the diversity. One is called machine-oriented mutation which is based on machine load



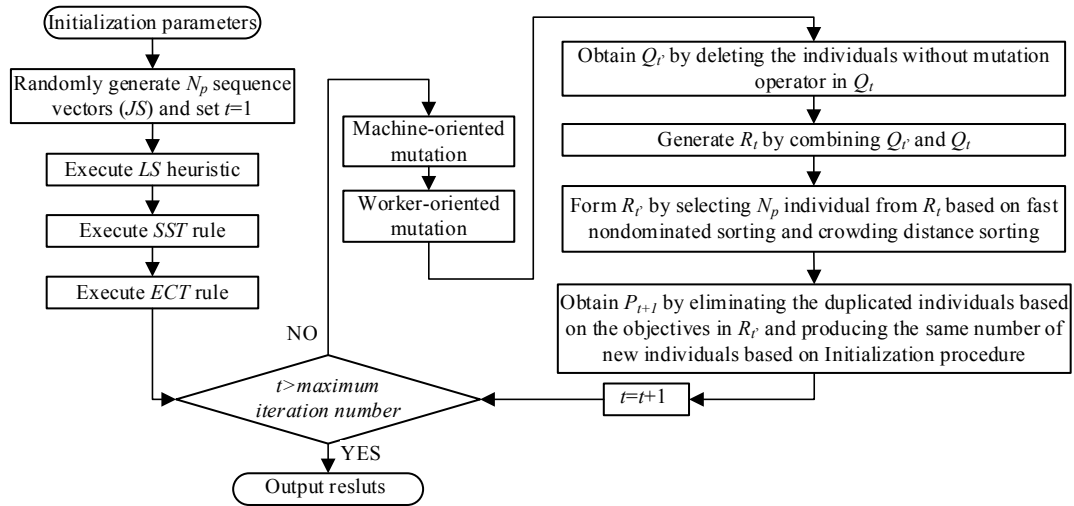


Fig. 4. The procedure of CEA.

balance and is similar to external insertion, the other is defined as worker-oriented mutation.

The detailed procedures of machine-oriented mutation and worker-oriented mutation are described in Algorithm 1 and Algorithm 2 respectively. It should be noted that the meanings of  $CM_k$ ,  $JM_k$ ,  $RM_k$ ,  $RW_b$ ,  $\mu_k$ ,  $S$  and  $B$  here refer to Section 3.2.3.

Algorithm 1: Machine-oriented mutation

1. **For** each individual  $ind$  **do**
2. Generate a random number between 0 and 1, denoted by  $R_{n1}$ ;
3. **If**  $R_{n1} < p_{m1}$  **do**  $\% p_{m1}$  is the machine-oriented mutation rate.
4. Calculate the fitness of each machine  $k$  in individual  $ind$  based on the equation  $f(k) = CM_k / \sum_{k=1}^m CM_k$ ;
5. Select a machine denoted as  $M_k$  via the roulette wheel rule based on  $f(k)$ ;
6. Randomly select a machine which is different from  $M_k$  and denote it as  $M_{k'}$ ;
7. Randomly select a job from  $JM_k$  and reallocate the job to  $JM_{k'}$ ;
8. Use the SST rule in Section 3.2.2 to optimize the job sequence in  $JM_k$  and  $JM_{k'}$ ;
9. Use the ECT rule in Section 3.2.3 to reselect a worker for each job on each machine in individual  $ind$ ;
10. **End If**
11. **End For**

Algorithm 2: Worker-oriented mutation

1. **For** each individual  $ind$  **do**
2. Generate a random number between 0 and 1, denoted by  $R_{n2}$ ;
3. **If**  $R_{n2} < p_{m2}$  **do**  $\% p_{m2}$  is the worker-oriented mutation rate.
4. Calculate the fitness of each machine in individual  $ind$  based on the equation  $f(k) = CM_k / \sum_{k=1}^m CM_k$ ;
5. Select a machine denoted as  $M_k$  via the roulette wheel rule based on  $f(k)$ ;
6. Select a machine, which is different from  $M_k$  and denote it as  $M_{k'}$ , via the roulette wheel rule based on the value  $(1 - f(k)) / \sum_{k=1}^m (1 - f(k))$  of each machine  $k$ ;
7. Randomly select a job from  $JM_k$  and randomly reassign a worker whose initial skill level is in the top half of all the workers to this job. Randomly select a job from  $JM_{k'}$  and randomly reassign a worker whose initial skill level is in the latter half of all the workers to this job;
8. Set  $RM_k = 0$  and  $\mu_k = 0$  for  $1 \leq k \leq m$ , and set  $S = 1$ ;
9. **while**  $RM_k = B$  is not hold for all machines **do**
10. Find  $M_{k'} := \arg \min_{1 \leq k \leq m} RM_k$  (randomly select a machine if  $\min_{1 \leq k \leq m} RM_k$  exists on multiple machines);
11. **If**  $|JM_{k'}| > 0$  **do**
12. Find out the first job  $J_i$  in  $JM_{k'}$  and the worker  $\tilde{l}$  corresponding to job  $J_i$ . Then put  $J_i$  in the position  $S$ , update  $RM_{k'}$  and  $RW_{\tilde{l}}$  by formulas (20) and (21) respectively,  $JM_{k'} := JM_{k'} \setminus \{J_i\}$ ,  $\mu_{k'} := \tilde{l}$  and  $S := S + 1$ .
13. **Else**
14. Set  $CM_{k'} := RM_{k'}$  and assign  $B$  to  $RM_{k'}$ ;
15. **End If**

(continued on next column)

(continued)

Algorithm 2: Worker-oriented mutation

16. **End while**
17. **End If**
18. **End For**

### 3.4. Selection

After mutation operator for the parent population, the offspring population is created. Then we should select individuals to compose a new population as the parent population of the next generation. In this paper, the selection operator is similar to elitist strategy used in NSGA-II. Suppose that  $P_t$  is  $t$ th generation's parent population and  $Q_t$  is the offspring population of  $P_t$ , where the size of both populations is  $N_p$ . To generate the next population  $P_{t+1}$  and conserve high-quality solutions at the same time, we should combine  $P_t$  and  $Q_t$ . However, some individuals without mutation operate exist double after this combination, which will reduce the diversity of the population. Here, an improved combination strategy is proposed and the detailed steps of the selection operator are described as follows:

- Step 1: Delete the individuals without mutation operator in  $Q_t$  and denote the remaining individuals as the set of  $Q_t$ .
- Step 2: Generate a combined population  $R_t = Q_t \cup Q_t$ .
- Step 3: Use the fast nondominated sorting and crowding distance sorting to select  $N_p$  individuals from  $R_t$ , and denote the set of  $N_p$  individuals as  $R_t$ .
- Step 4: Use the Initialization procedure described in Section 3.2 to generate new individuals, whose number is equal to that of the duplicated individuals in  $R_t$ , to substitute the duplicated individuals based on the objectives in  $R_t$ .
- Step 5: Form  $P_{t+1}$  by assigning  $R_t$  to  $P_{t+1}$ .

### 3.5. The procedure of CEA

According to the descriptions above, the overall procedure of CEA can be depicted as Fig. 4.

## 4. Experiments and results

In this section, three types of experiments are designed to evaluate the performance of CEA for NUPMSP. The first type of experiment is Taguchi analysis, which is used to select the suitable combination of critical parameters; the second type of experiment is carried out to

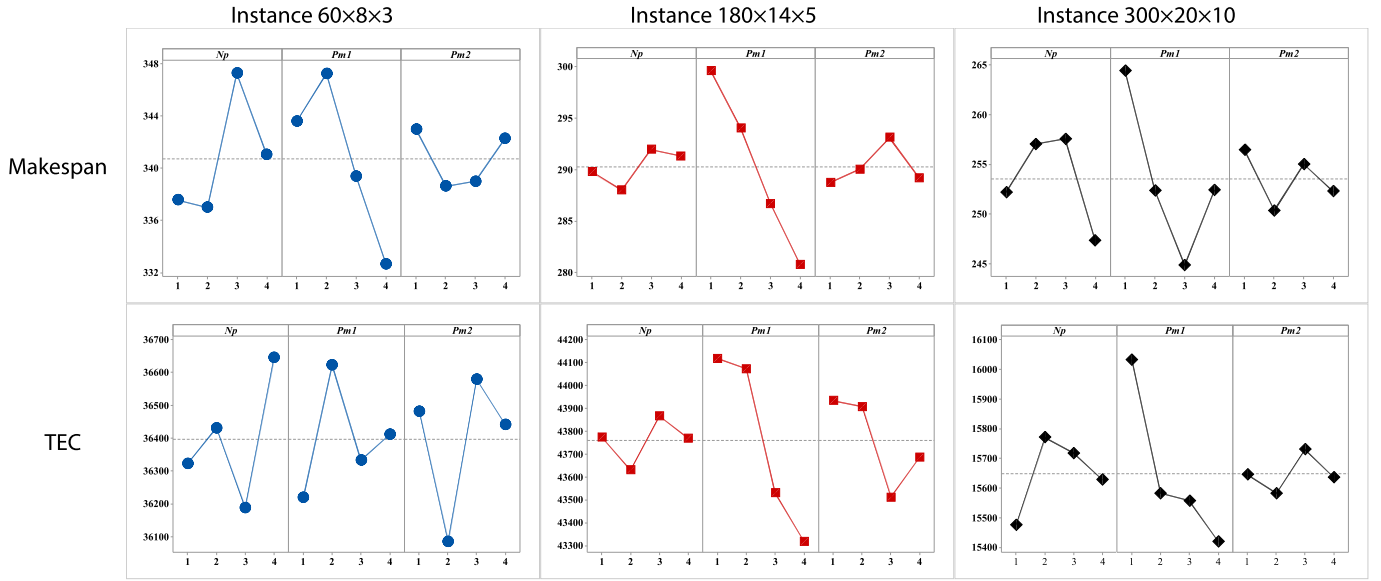


Fig. 5. Factor level trend of key parameters.

evaluate the validity of *LS* heuristic, *SST* rule and *ECT* rule; the last type of experiment is to test our CEA with other well-known algorithms, i.e., NNIA and NSGA-II. Note that all the algorithms here are coded in MATLAB R2016a and run on a computer with Inter Core i9-9900 k CPU at 3.60 GHz and 32 GB RAM.

#### 4.1. Instances construction

In this section, 72 instances are constructed for testing and the source data of each instance are generated as follows. The processing time and the initial sequence dependent setup time of each job processed on each machine are integers and are both generated based on method proposed by Costa, et al. (2013). For the initial coefficient of each worker,  $\eta_{ik}$  is randomly generated from the set {0.5, 0.75, 1, 1.25, 1.5}. In this paper, the learning effect  $\alpha$  of workers is the same and set  $\alpha = -0.152$  according to C. Wu, et al. (2013). The processing power and the idle power of each machine follow a uniform distribution [20, 40] and [10, 20] respectively. In the experiments, each instance is named as  $n \times m \times w$ , where  $n$  denotes the number of jobs,  $m$  denotes the number of machines and  $w$  denotes the number of workers. Inspired by Zhang, Deng, Gong, and Han (2019), the instances are divided into three scales: (a) small-scale instances where  $n \in \{40, 60, 80, 100\}$ ,  $m \in \{6, 8, 10\}$  and  $w \in \{3, 4\}$ ; (b) middle-scale instances where  $n \in \{140, 160, 180, 200\}$ ,  $m \in \{12, 14, 16\}$  and  $w \in \{5, 6\}$ ; (c) large-scale instances where  $n \in \{250, 300, 350, 400\}$ ,  $m \in \{18, 20, 22\}$  and  $w \in \{8, 10\}$ . All the data can be download via the link: <https://github.com/likezhang1990/NUPMSP-instances.git>.

#### 4.2. Performance metrics

In this paper, three well-known multi-objective metrics are considered to evaluate the performance of all tested algorithms. They are the C metric, the hypervolume indicator (*HV*) and the inverted generational distance (*IGD*), which can be depicted as [1]–[3].

[1] The value of  $C(A, B)$  represents the percentage of solutions in set  $B$  which are dominated by at least one solution in set  $A$ , i.e.,

$$C(A, B) = \frac{|\{x \in B | \exists y \in A : y \text{ dominates } x\}|}{|B|} \quad (22)$$

Therefore, the larger the  $C(A, B)$  is, the better  $A$  is.

[2] The *HV* indicator is a performance metric for indicating the quality of a non-dominated approximation set. It can be defined as follows:

$$HV(ref, A) = \lambda \left( \bigcup_{f \in A} [f_1, ref_1] \times \dots \times [f_m, ref_m] \right) \quad (23)$$

Where  $HV(ref, A)$  represent the size of the space covered by set  $A$ ,  $R = (r_1, r_2, \dots, r_m)^T$  is reference point chosen from the target space,  $\lambda$  is the Lebesgue measure and  $m$  here refers to the number of targets. The higher  $HV(ref, A)$  is, the better  $A$  is.

[3] The *IGD* of set  $A$  can be obtained by equation (24)

$$IGD(A, P^*) = \frac{1}{|P^*|} \sum_{x \in P^*} \min_{y \in A} d(x, y) \quad (24)$$

Where  $d(x, y)$  is the Euclidean distance between point  $x$  and  $y$ , and  $P^*$  is the Pareto optimal front. Here  $P^*$  is acquired by dealing with all the solutions obtained by all runs of all algorithms. The smaller  $IGD(A, P^*)$  is, the closer  $A$  is to the Pareto optimal front. Besides, the objectives of all solutions are normalized by equation (25).

$$\tilde{f}_i(x) = \frac{f_i(x) - f_i^{\min}}{f_i^{\max} - f_i^{\min}}, \quad i = 1, 2 \quad (25)$$

$f_i^{\min}$  and  $f_i^{\max}$  are the minimal and maximal value of  $i$ th objective in all solutions, respectively.

#### 4.3. Analysis of experiments results

##### 4.3.1. Parameter tuning

The proposed CEA has three key parameters, i.e., population size  $N_p$ , machine-oriented mutation probability  $p_{m1}$  and worker-oriented mutation probability  $p_{m2}$ . To select a suitable combination of these key parameters, the Taguchi method is carried out based on a small-scale instance  $60 \times 8 \times 3$ , a middle-scale instance  $180 \times 14 \times 5$  and a large-scale instance  $300 \times 20 \times 10$ . Each key parameter is considered to have four factor levels, which are  $N_p = \{50, 100, 150, 200\}$ ,  $p_{m1} = \{0.1, 0.2, 0.3, 0.4\}$  and  $p_{m2} = \{0.1, 0.2, 0.3, 0.4\}$ . For each combination, the CEA is run independently five times and the mean value of each objective of the Pareto optimal front obtained by these runs is selected to analyze the effect of this combination.

Based on the experiment results, the trend of each factor level is depicted in Fig. 5. In Fig. 5, the first row and the second row denote the effect of  $N_p$ ,  $p_{m1}$  and  $p_{m2}$  on makespan and *TEC* respectively.

From Fig. 5, we observe there is no distinct regularity between  $N_p$  and objectives. For the value of the optimization objectives, however,

**Table 3**

The comparison results of CEA and EA1.

| Benchmark     | C<br>C(CEA, EA1) | C(EA1, CEA) | HV<br>CEA       | EA1      | IGD<br>CEA | EA1      | time/s<br>CEA | EA1           |
|---------------|------------------|-------------|-----------------|----------|------------|----------|---------------|---------------|
| 40 × 8 × 3    | 1                | 0           | <b>0.176401</b> | 0.057487 | <b>0</b>   | 0.413059 | 28.07         | <b>26.79</b>  |
| 60 × 6 × 4    | 1                | 0           | <b>0.139488</b> | 0.023493 | <b>0</b>   | 0.773187 | 36.11         | <b>35.12</b>  |
| 80 × 6 × 3    | 1                | 0           | <b>0.192715</b> | 0.001978 | <b>0</b>   | 1.207774 | 47.75         | <b>43.45</b>  |
| 80 × 10 × 4   | 1                | 0           | <b>0.315037</b> | 0.043207 | <b>0</b>   | 0.815153 | 46.95         | <b>41.32</b>  |
| 100 × 10 × 3  | 1                | 0           | <b>0.264091</b> | 0.002975 | <b>0</b>   | 1.165858 | 52.85         | <b>51.76</b>  |
| 140 × 14 × 5  | 1                | 0           | <b>0.406864</b> | 0.022778 | <b>0</b>   | 1.018782 | <b>69.51</b>  | 71.27         |
| 160 × 12 × 6  | 1                | 0           | <b>0.273848</b> | 0.011369 | <b>0</b>   | 1.120342 | 81.94         | <b>73.01</b>  |
| 180 × 12 × 5  | 1                | 0           | <b>0.360152</b> | 0.003832 | <b>0</b>   | 1.241018 | <b>80.92</b>  | 83.72         |
| 180 × 16 × 6  | 1                | 0           | <b>0.348497</b> | 0.002808 | <b>0</b>   | 1.210553 | 89.50         | <b>88.95</b>  |
| 200 × 16 × 5  | 1                | 0           | <b>0.447582</b> | 0.004167 | <b>0</b>   | 1.250573 | <b>97.81</b>  | 101.28        |
| 250 × 20 × 8  | 1                | 0           | <b>0.370035</b> | 0.000648 | <b>0</b>   | 1.305765 | 119.84        | <b>116.65</b> |
| 300 × 18 × 10 | 1                | 0           | <b>0.372183</b> | 0.001314 | <b>0</b>   | 1.265421 | 157.07        | <b>145.07</b> |
| 350 × 18 × 8  | 1                | 0           | <b>0.447837</b> | 0.004798 | <b>0</b>   | 1.272546 | 179.14        | <b>163.15</b> |
| 350 × 22 × 10 | 1                | 0           | <b>0.428368</b> | 0.001705 | <b>0</b>   | 1.309948 | 190.08        | <b>167.50</b> |
| 400 × 22 × 8  | 1                | 0           | <b>0.483262</b> | 0.001755 | <b>0</b>   | 1.323147 | 223.86        | <b>184.51</b> |

Note: for each instance, significantly better results are marked in bold.

**Table 4**

The comparison results of CEA and EA2.

| Benchmark     | C<br>C(CEA, EA2) | C(EA2, CEA) | HV<br>CEA       | EA2      | IGD<br>CEA      | EA2      | time/s<br>CEA | EA2           |
|---------------|------------------|-------------|-----------------|----------|-----------------|----------|---------------|---------------|
| 40 × 8 × 3    | 1                | 0           | <b>0.120065</b> | 0.088115 | <b>0.002606</b> | 0.167001 | 28.07         | <b>26.57</b>  |
| 60 × 6 × 4    | 1                | 0           | <b>0.057447</b> | 0.015560 | <b>0</b>        | 0.508432 | 36.11         | <b>31.62</b>  |
| 80 × 6 × 3    | 1                | 0           | <b>0.032564</b> | 0.007041 | <b>0</b>        | 0.694190 | 47.75         | <b>41.98</b>  |
| 80 × 10 × 4   | 1                | 0           | <b>0.104024</b> | 0.014373 | <b>0</b>        | 0.707594 | 46.95         | <b>41.51</b>  |
| 100 × 10 × 3  | 1                | 0           | <b>0.067853</b> | 0.010064 | <b>0</b>        | 0.746158 | 52.85         | <b>45.35</b>  |
| 140 × 14 × 5  | 1                | 0           | <b>0.152455</b> | 0.015612 | <b>0</b>        | 0.850961 | 69.51         | <b>64.43</b>  |
| 160 × 12 × 6  | 1                | 0           | <b>0.144147</b> | 0.010009 | <b>0</b>        | 0.994372 | 81.94         | <b>72.58</b>  |
| 180 × 12 × 5  | 1                | 0           | <b>0.119025</b> | 0.000000 | <b>0</b>        | 1.154796 | 80.92         | <b>77.32</b>  |
| 180 × 16 × 6  | 1                | 0           | <b>0.172598</b> | 0.009402 | <b>0</b>        | 1.008510 | 89.50         | <b>81.38</b>  |
| 200 × 16 × 5  | 1                | 0           | <b>0.095296</b> | 0.002898 | <b>0</b>        | 1.022423 | 97.81         | <b>82.59</b>  |
| 250 × 20 × 8  | 1                | 0           | <b>0.181377</b> | 0.001075 | <b>0</b>        | 1.184056 | 119.84        | <b>103.82</b> |
| 300 × 18 × 10 | 1                | 0           | <b>0.196716</b> | 0.000912 | <b>0</b>        | 1.215303 | 157.07        | <b>118.40</b> |
| 350 × 18 × 8  | 1                | 0           | <b>0.186998</b> | 0.009013 | <b>0</b>        | 1.071018 | 179.14        | <b>148.29</b> |
| 350 × 22 × 10 | 1                | 0           | <b>0.194492</b> | 0.007340 | <b>0</b>        | 1.108243 | 190.08        | <b>139.31</b> |
| 400 × 22 × 8  | 1                | 0           | <b>0.153989</b> | 0.002843 | <b>0</b>        | 1.123926 | 223.86        | <b>155.99</b> |

Note: for each instance, significantly better results are marked in bold.

half of the six subgraphs get the minimum value at level 2 of  $N_p$ , which is higher than any other levels of  $N_p$ . Thus, we select level 2 of  $N_p$  (i.e.,  $N_p = 100$ ) for CEA. For  $p_{m1}$ , it is obvious to select level 4 of  $p_{m1}$  (i.e.,  $p_{m1} = 0.4$ ) for CEA. From Fig. 5, we see that the optimization target value decreases as  $p_{m1}$  increases in general, and for the value of the optimization objectives, two-thirds of the six subgraphs get the minimum value at level 4 of  $p_{m1}$ . For  $p_{m2}$ , we observe from Fig. 5 that the optimization

target value is most likely to get the minimum value at level 2 of  $p_{m2}$ . Thereby,  $p_{m2} = 0.2$  is considered for our CEA.

#### 4.3.2. Effect of LS, SST and ECT

According to the description in Section 3, mainly three constructions contribute to CEA, which are the LS, SST and ECT. To prove the effectiveness of LS, SST and ECT, we construct other three algorithms, i.e.,

**Table 5**

The comparison results of CEA and EA3.

| Benchmark     | C<br>C(CEA, EA3) | C(EA3, CEA) | HV<br>CEA       | EA3      | IGD<br>CEA | EA3      | time/s<br>CEA | EA3           |
|---------------|------------------|-------------|-----------------|----------|------------|----------|---------------|---------------|
| 40 × 8 × 3    | 1                | 0           | <b>0.223396</b> | 0.087697 | <b>0</b>   | 0.368333 | 28.07         | <b>26.94</b>  |
| 60 × 6 × 4    | 1                | 0           | <b>0.152893</b> | 0.015498 | <b>0</b>   | 0.835445 | 36.11         | <b>34.55</b>  |
| 80 × 6 × 3    | 1                | 0           | <b>0.113997</b> | 0.001875 | <b>0</b>   | 1.116081 | 47.75         | <b>42.58</b>  |
| 80 × 10 × 4   | 1                | 0           | <b>0.278756</b> | 0.020173 | <b>0</b>   | 0.956209 | 46.95         | <b>42.67</b>  |
| 100 × 10 × 3  | 1                | 0           | <b>0.282095</b> | 0.012955 | <b>0</b>   | 1.066538 | 52.85         | <b>50.43</b>  |
| 140 × 14 × 5  | 1                | 0           | <b>0.385360</b> | 0.011565 | <b>0</b>   | 1.107172 | 69.51         | <b>60.34</b>  |
| 160 × 12 × 6  | 1                | 0           | <b>0.376515</b> | 0.003442 | <b>0</b>   | 1.214702 | 81.94         | <b>67.64</b>  |
| 180 × 12 × 5  | 1                | 0           | <b>0.471445</b> | 0.008561 | <b>0</b>   | 1.203914 | 80.92         | <b>79.11</b>  |
| 180 × 16 × 6  | 1                | 0           | <b>0.383156</b> | 0.005554 | <b>0</b>   | 1.166581 | 89.50         | <b>72.42</b>  |
| 200 × 16 × 5  | 1                | 0           | <b>0.464630</b> | 0.010964 | <b>0</b>   | 1.062974 | 97.81         | <b>89.16</b>  |
| 250 × 20 × 8  | 1                | 0           | <b>0.520434</b> | 0.023001 | <b>0</b>   | 1.077978 | 119.84        | <b>118.36</b> |
| 300 × 18 × 10 | 1                | 0           | <b>0.646062</b> | 0.026897 | <b>0</b>   | 1.135166 | 157.07        | <b>142.98</b> |
| 350 × 18 × 8  | 1                | 0           | <b>0.555958</b> | 0.000985 | <b>0</b>   | 1.302212 | 179.14        | <b>167.10</b> |
| 350 × 22 × 10 | 1                | 0           | <b>0.640335</b> | 0.009807 | <b>0</b>   | 1.219025 | 190.08        | <b>166.65</b> |
| 400 × 22 × 8  | 1                | 0           | <b>0.588502</b> | 0.010950 | <b>0</b>   | 1.206066 | 223.86        | <b>178.44</b> |

Note: for each instance, significantly better results are marked in bold.



**Table 6**

The C, HV and IGD comparison of CEA, NNIA and NSGA-II.

| instance     | C<br>C(CEA,<br>NNIA) | C(NNIA,<br>CEA) | C(CEA,<br>NSGA-II) | C<br>(NSGA-<br>II,CEA) | HV<br>CEA       | NNIA     | NSGA-II  | IGD<br>CEA | NNIA            | NSGA-II   | time/s<br>CEA |
|--------------|----------------------|-----------------|--------------------|------------------------|-----------------|----------|----------|------------|-----------------|-----------|---------------|
| 40 × 6 × 3   | 1                    | 0               | 1                  | 0                      | <b>0.501403</b> | 0.174997 | 0        | 0          | 1.001701        | 2.067899  | 27.82         |
| 40 × 6 × 4   | 1                    | 0               | 1                  | 0                      | <b>0.541345</b> | 0.221338 | 0.005336 | 0          | 1.144825        | 2.793700  | 29.99         |
| 40 × 8 × 3   | 1                    | 0               | 1                  | 0                      | <b>0.614526</b> | 0.240467 | 0.011311 | 0          | 1.114489        | 2.406813  | 27.46         |
| 40 × 8 × 4   | 1                    | 0               | 1                  | 0                      | <b>0.683721</b> | 0.343803 | 0.045156 | 0          | 1.155560        | 3.009873  | 28.69         |
| 40 × 10 × 3  | 1                    | 0               | 1                  | 0                      | <b>0.612756</b> | 0.267870 | 0.004384 | 0          | 0.969632        | 2.479921  | 29.27         |
| 40 × 10 × 4  | 1                    | 0               | 1                  | 0                      | <b>0.651598</b> | 0.298697 | 0.007699 | 0          | 1.155926        | 3.048012  | 28.33         |
| 60 × 6 × 3   | 1                    | 0               | 1                  | 0                      | <b>0.608107</b> | 0.196819 | 0.006148 | 0          | 1.206281        | 2.431669  | 38.47         |
| 60 × 6 × 4   | 1                    | 0               | 1                  | 0                      | <b>0.626381</b> | 0.207368 | 0.012994 | 0          | 1.345371        | 2.805186  | 37.81         |
| 60 × 8 × 3   | 1                    | 0               | 1                  | 0                      | <b>0.679766</b> | 0.254763 | 0.005548 | 0          | 1.219353        | 2.859087  | 38.35         |
| 60 × 8 × 4   | 1                    | 0               | 1                  | 0                      | <b>0.591274</b> | 0.110591 | 0        | 0          | 1.313420        | 2.308497  | 36.35         |
| 60 × 10 × 3  | 1                    | 0               | 1                  | 0                      | <b>0.673676</b> | 0.213853 | 0.003948 | 0          | 1.242544        | 2.555728  | 40.68         |
| 60 × 10 × 4  | 1                    | 0               | 1                  | 0                      | <b>0.577062</b> | 0.084773 | 0        | 0          | 1.278479        | 2.069870  | 38.31         |
| 80 × 6 × 3   | 1                    | 0               | 1                  | 0                      | <b>0.650771</b> | 0.147249 | 0.005391 | 0          | 1.355336        | 2.341968  | 46.54         |
| 80 × 6 × 4   | 1                    | 0               | 1                  | 0                      | <b>0.644363</b> | 0.126127 | 0        | 0          | 1.303573        | 2.329219  | 43.54         |
| 80 × 8 × 3   | 1                    | 0               | 1                  | 0                      | <b>0.698966</b> | 0.142678 | 0.000997 | 0          | 1.334800        | 2.174929  | 43.14         |
| 80 × 8 × 4   | 1                    | 0               | 1                  | 0                      | <b>0.682477</b> | 0.176931 | 0.009163 | 0          | 1.361026        | 2.463044  | 40.10         |
| 80 × 10 × 3  | 1                    | 0               | 1                  | 0                      | <b>0.689156</b> | 0.172356 | 0.007819 | 0          | 1.358525        | 2.466524  | 45.20         |
| 80 × 10 × 4  | 1                    | 0               | 1                  | 0                      | <b>0.737123</b> | 0.212229 | 0.007963 | 0          | 1.359221        | 2.646405  | 41.55         |
| 100 × 6 × 3  | 1                    | 0               | 1                  | 0                      | <b>0.677948</b> | 0.138246 | 0.000759 | 0          | 1.395922        | 2.445244  | 54.84         |
| 100 × 6 × 4  | 1                    | 0               | 1                  | 0                      | <b>0.700197</b> | 0.134200 | 0.003562 | 0          | 1.387003        | 2.295261  | 57.11         |
| 100 × 8 × 3  | 1                    | 0               | 1                  | 0                      | <b>0.696317</b> | 0.115563 | 0        | 0          | 1.383655        | 2.322555  | 55.50         |
| 100 × 8 × 4  | 1                    | 0               | 1                  | 0                      | <b>0.718463</b> | 0.126039 | 0.005127 | 0          | 1.120998        | 1.768728  | 56.30         |
| 100 × 10 × 3 | 1                    | 0               | 1                  | 0                      | <b>0.715294</b> | 0.148866 | 0.007116 | 0          | 1.352186        | 2.263156  | 52.85         |
| 100 × 10 × 4 | 1                    | 0               | 1                  | 0                      | <b>0.749453</b> | 0.100896 | 0        | 0          | 1.330505        | 2.071065  | 59.56         |
| 140 × 12 × 5 | 1                    | 0               | 1                  | 0                      | <b>0.755403</b> | 0.190168 | 0        | 0          | 1.371924        | 2.688091  | 64.69         |
| 140 × 12 × 6 | 1                    | 0               | 1                  | 0                      | <b>0.764630</b> | 0.259560 | 0        | 0          | 1.383023        | 3.357198  | 65.18         |
| 140 × 14 × 5 | 1                    | 0               | 1                  | 0                      | <b>0.776723</b> | 0.228994 | 0.000127 | 0          | 1.395913        | 4.562723  | 69.95         |
| 140 × 14 × 6 | 1                    | 0               | 1                  | 0                      | <b>0.784045</b> | 0.234246 | 0        | 0          | 1.045416        | 1.967011  | 67.28         |
| 140 × 16 × 5 | 1                    | 0               | 1                  | 0                      | <b>0.758528</b> | 0.126597 | 0        | 0          | 1.194072        | 1.983017  | 66.91         |
| 140 × 16 × 6 | 1                    | 0               | 1                  | 0                      | <b>0.787388</b> | 0.709973 | 0.008020 | 0          | 0.605981        | 51.842462 | 66.11         |
| 160 × 12 × 5 | 0                    | 0               | 1                  | 0                      | <b>0.775817</b> | 0.727880 | 0        | 0.598952   | <b>0.354630</b> | 20.039824 | 73.01         |
| 160 × 12 × 6 | 1                    | 0               | 1                  | 0                      | <b>0.764838</b> | 0.064513 | 0        | 0          | 1.394157        | 1.969237  | 73.64         |
| 160 × 14 × 5 | 1                    | 0               | 1                  | 0                      | <b>0.774162</b> | 0.648567 | 0        | 0          | 1.188882        | 31.123178 | 73.59         |
| 160 × 14 × 6 | 1                    | 0               | 1                  | 0                      | <b>0.766755</b> | 0.483708 | 0        | 0          | 1.123633        | 8.186515  | 77.73         |
| 160 × 16 × 5 | 1                    | 0               | 1                  | 0                      | <b>0.770798</b> | 0.643197 | 0        | 0          | 1.222941        | 29.092472 | 79.14         |
| 160 × 16 × 6 | 1                    | 0               | 1                  | 0                      | <b>0.784177</b> | 0.462853 | 0        | 0          | 1.347473        | 7.088264  | 77.19         |
| 180 × 12 × 5 | 1                    | 0               | 1                  | 0                      | <b>0.789453</b> | 0.445454 | 0        | 0          | 1.294324        | 7.168520  | 86.70         |
| 180 × 12 × 6 | 1                    | 0               | 1                  | 0                      | <b>0.796243</b> | 0.523668 | 0.000252 | 0          | 1.324336        | 10.279342 | 87.02         |
| 180 × 14 × 5 | 1                    | 0               | 1                  | 0                      | <b>0.800677</b> | 0.086288 | 0.004581 | 0          | 1.401421        | 1.947298  | 78.52         |
| 180 × 14 × 6 | 1                    | 0               | 1                  | 0                      | <b>0.801382</b> | 0.099919 | 0        | 0          | 1.399751        | 2.140318  | 85.90         |
| 180 × 16 × 5 | 1                    | 0               | 1                  | 0                      | <b>0.822026</b> | 0.143496 | 0.014281 | 0          | 1.400467        | 2.082115  | 79.08         |
| 180 × 16 × 6 | 1                    | 0               | 1                  | 0                      | <b>0.802425</b> | 0.077427 | 0.001623 | 0          | 1.375545        | 1.876406  | 90.96         |
| 200 × 12 × 5 | 1                    | 0               | 1                  | 0                      | <b>0.780170</b> | 0.043541 | 0        | 0          | 1.408341        | 1.846278  | 89.57         |
| 200 × 12 × 6 | 1                    | 0               | 1                  | 0                      | <b>0.825200</b> | 0.073682 | 0.000149 | 0          | 1.362682        | 1.813930  | 90.53         |
| 200 × 14 × 5 | 1                    | 0               | 1                  | 0                      | <b>0.818229</b> | 0.057735 | 0.000379 | 0          | 1.370994        | 1.800598  | 92.86         |
| 200 × 14 × 6 | 1                    | 0               | 1                  | 0                      | <b>0.820076</b> | 0.076797 | 0.002771 | 0          | 1.402906        | 1.908537  | 93.75         |
|              | 1                    | 0               | 1                  | 0                      | <b>0.804360</b> | 0.089244 | 0.000261 | 0          | 1.390997        | 1.998202  | 82.44         |

(continued on next page)

Table 6 (continued)

| instance      | C<br>(CEA,<br>NNIA) | C(NNIA,<br>CEA) | C(CEA,<br>NSGA-II) | C<br>(NSGA-<br>II,CEA) | HV<br>CEA       | NNIA     | NSGA-II  | IGD<br>CEA | NNIA     | NSGA-II  | time/s<br>CEA |
|---------------|---------------------|-----------------|--------------------|------------------------|-----------------|----------|----------|------------|----------|----------|---------------|
| 40 × 6 × 3    | 1                   | 0               | 1                  | 0                      | <b>0.501403</b> | 0.174997 | 0        | 0          | 1.001701 | 2.067899 | 27.82         |
| 200 × 16 × 5  |                     |                 |                    |                        |                 |          |          |            |          |          |               |
| 200 × 16 × 6  | 1                   | 0               | 1                  | 0                      | <b>0.808347</b> | 0.062154 | 0        | 0          | 1.392830 | 1.909242 | 89.60         |
| 250 × 18 × 8  | 1                   | 0               | 1                  | 0                      | <b>0.804667</b> | 0        | 0.006556 | 0          | 1.405565 | 1.495224 | 106.77        |
| 250 × 18 × 10 | 1                   | 0               | 1                  | 0                      | <b>0.849015</b> | 0.050794 | 0.005530 | 0          | 1.407794 | 1.658819 | 98.92         |
| 250 × 20 × 8  | 1                   | 0               | 1                  | 0                      | <b>0.827688</b> | 0.024462 | 0        | 0          | 1.386098 | 1.637175 | 104.13        |
| 250 × 20 × 10 | 1                   | 0               | 1                  | 0                      | <b>0.847866</b> | 0.076287 | 0.012664 | 0          | 1.409814 | 1.720346 | 109.12        |
| 250 × 22 × 8  | 1                   | 0               | 1                  | 0                      | <b>0.840819</b> | 0.092569 | 0.044210 | 0          | 1.401867 | 1.732086 | 106.42        |
| 250 × 22 × 10 | 1                   | 0               | 1                  | 0                      | <b>0.832179</b> | 0.050170 | 0.004302 | 0          | 1.403646 | 1.731855 | 106.16        |
| 300 × 18 × 8  | 1                   | 0               | 1                  | 0                      | <b>0.825289</b> | 0.000577 | 0.015217 | 0          | 1.399225 | 1.195015 | 120.46        |
| 300 × 18 × 10 | 1                   | 0               | 1                  | 0                      | <b>0.836783</b> | 0        | 0.032972 | 0          | 1.408639 | 1.263023 | 128.12        |
| 300 × 20 × 8  | 1                   | 0               | 1                  | 0                      | <b>0.812751</b> | 0        | 0.007819 | 0          | 1.403220 | 1.449272 | 143.43        |
| 300 × 20 × 10 | 1                   | 0               | 1                  | 0                      | <b>0.824948</b> | 0.000220 | 0.001224 | 0          | 1.409564 | 1.466936 | 132.95        |
| 300 × 22 × 8  | 1                   | 0               | 1                  | 0                      | <b>0.836400</b> | 0.036623 | 0.000553 | 0          | 1.377431 | 1.678376 | 132.01        |
| 300 × 22 × 10 | 1                   | 0               | 1                  | 0                      | <b>0.847342</b> | 0.023446 | 0        | 0          | 1.408358 | 1.672163 | 131.85        |
| 350 × 18 × 8  | 1                   | 0               | 1                  | 0                      | <b>0.855785</b> | 0.036068 | 0.000154 | 0          | 1.407460 | 1.737076 | 145.92        |
| 350 × 18 × 10 | 1                   | 0               | 1                  | 0                      | <b>0.850001</b> | 0.014584 | 0        | 0          | 1.407758 | 1.619889 | 145.31        |
| 350 × 20 × 8  | 1                   | 0               | 1                  | 0                      | <b>0.847873</b> | 0.021625 | 0        | 0          | 1.379062 | 1.642631 | 159.30        |
| 350 × 20 × 10 | 1                   | 0               | 1                  | 0                      | <b>0.857111</b> | 0.014920 | 0        | 0          | 1.382366 | 1.590284 | 145.00        |
| 350 × 22 × 8  | 1                   | 0               | 1                  | 0                      | <b>0.851241</b> | 0.016185 | 0        | 0          | 1.399955 | 1.569131 | 153.53        |
| 350 × 22 × 10 | 1                   | 0               | 1                  | 0                      | <b>0.860440</b> | 0.025913 | 0.000542 | 0          | 1.406742 | 1.659968 | 152.62        |
| 400 × 18 × 8  | 1                   | 0               | 1                  | 0                      | <b>0.877507</b> | 0.030258 | 0.000939 | 0          | 1.397896 | 1.653239 | 163.41        |
| 400 × 18 × 10 | 1                   | 0               | 1                  | 0                      | <b>0.863917</b> | 0.012212 | 0        | 0          | 1.408170 | 1.600241 | 170.53        |
| 400 × 20 × 8  | 1                   | 0               | 1                  | 0                      | <b>0.863451</b> | 0.016100 | 0        | 0          | 1.410968 | 1.635552 | 172.47        |
| 400 × 20 × 10 | 1                   | 0               | 1                  | 0                      | <b>0.868198</b> | 0.006900 | 0        | 0          | 1.390142 | 1.528098 | 173.60        |
| 400 × 22 × 8  | 1                   | 0               | 1                  | 0                      | <b>0.849131</b> | 0.003208 | 0        | 0          | 1.385028 | 1.474195 | 171.05        |
| 400 × 22 × 10 | 1                   | 0               | 1                  | 0                      | <b>0.869410</b> | 0.021022 | 0.000408 | 0          | 1.410247 | 1.620921 | 179.91        |

Note: for each instance, significantly better results are marked in bold.

EA1, EA2 and EA3. EA1 denotes the CEA without *LS*, EA2 denotes the CEA without *SST* and EA3 denotes the CEA without *ECT*. 15 instances are selected from the instance set in Section 4.1 as the experiment benchmarks. For fairness, we set the same parameters obtained from Section 4.3.1 for EA1, EA2 and EA3, and the maximum iterations of these four algorithms are all set to 100, which is a moderate number.

The *LS* heuristic is carried out to select a machine for each job, so we randomly determine a machine for each job for EA1 while other operations are same to CEA. For EA2 without *SST*, it is easy to realize by deleting all the *SST* operations in CEA. In CEA, *ECT* exists in two places, i.e., initialization procedure (Section 3.2) and machine-oriented mutation (Section 3.3). Thus, in the algorithm of EA3 without *ECT*, a worker corresponding to each job is randomly chosen in the initialization procedure and the worker matching with a job will move along with the job

in the machine-oriented mutation.

Tables 3, 4 and 5 show the performance comparison between CEA and EA1, CEA and EA2, and CEA and EA3, respectively. Even though the computational time of CEA bigger than those of other three algorithms holds for almost all the benchmarks, the gap is not widely and the results of the three metrics clearly illustrate that CEA performs much better than EA1, EA2 and EA3, which demonstrates the effectiveness of *LS*, *SST* and *ECT*. Another meaningful phenomenon can be observed from Tables 3, 4 and 5 is that the values of *HV*(CEA) and *IGD* (EA1\ EA2\ EA3) both show increasing trend as the scale of instance increases, while the values of *HV*(EA1\ EA2\ EA3) and *IGD* (CEA) are almost constant, indicating that the *LS*, *SST* and *ECT* are more effectiveness for larger instances.

#### 4.3.3. Comparison of CEA with NNIA and NSGA-II

To further conform the validity of our proposed CEA, we compare it with NNIA and NSGA-II, which are the state-of-the-art multi-objective algorithms and have been widely used as the comparison algorithms. According to X. Wu and Che (2019), the parameters of NSGA-II are set as follows: the population size is 100, the crossover probability is 1 and the mutation probability is  $1/2n$ . The parameters of NNIA is same to NSGA-II. To ensure fairness, we record the run time of CEA for any instance and set it as the time limit for NNIA and NSGA-II when they run the same instance.

Table 6 shows the comparison results, which clearly certify the effectiveness of CEA. The three metrics of CEA are much better than NSGA-II for all test instances. From the  $C$ -metric,  $C(\text{CEA}, \text{NNIA}) = 1$  and  $C(\text{NNIA}, \text{CEA}) = 0$  hold for all instances except for instance  $160 \times 12 \times 5$ , demonstrating that all the solutions obtained by NNIA are dominated by those derived from CEA for any instance except instance  $160 \times 12 \times 5$ . But for instance  $160 \times 12 \times 5$ , the solutions obtained by CEA cannot be dominated by any solution obtained by NNIA. The reason for this phenomenon is probably the randomness of NNIA. Furthermore, the results of  $HV$  and  $IGD$  in Table 6 indicate that the quality of optimal Pareto fronts obtained by CEA is far better than those derived from NNIA and NSGA-II. In terms of  $HV$  and  $IGD$  for NNIA and NSGA-II, the results in Table 6 also indicate that NNIA outperforms NSGA-II for most instances.

## 5. Conclusion and future work

To conclude, we presented a new model of NUPMSP: unrelated parallel machine scheduling with sequence and machine-dependent setup times, limited worker resources, and learning effect. This model is the first to consider worker resources and learning effect in the context of unrelated parallel machine scheduling with sequence and machine-dependent setup times. It is also the first time to consider the processing time and  $TEC$  simultaneously, which helps operation managers to make balance between production efficiency and environmental protection. We propose an effective CEA to solve the NUPMSP, in which three methods including  $LS$  heuristic,  $SST$  rule and  $ECT$  rule are presented and combined to obtain a high-quality population. In our experiments, we first used the Taguchi method to obtain the optimum combination of the population size, machine-oriented mutation probability and worker-oriented mutation probability. Then, three experiments are carried out to prove the effectiveness of the proposed  $LS$  heuristic,  $SST$  rule and  $ECT$  rule based on 15 instances. Finally, extensively comparisons were conducted between our proposed CEA and other two well-known algorithms based on 72 instances. The experimental results demonstrated that the CEA can outperforms the other algorithms in almost all instances.

Our work is significant to bridge the theoretical gaps and guide practical production. Theoretically, we have pioneered a new research direction for the UPMSP-SMDST and have designed an effective combinatorial evolutionary algorithm to the proposed problem. Practically, our NUPMSP model can help manufacturing factories to schedule jobs and worker resources in a more reasonable manner, especially for the highly-manual mixed-model manufacturing factories, such as printing industries, in which workers are needed to reset each machine for the next job.

For future work, we will take the machine maintenance activities and human forgetting effect into account in our model. In addition, more efficient algorithms will be developed to solve the problem.

## CRedit authorship contribution statement

**Like Zhang:** Conceptualization, Methodology, Formal analysis, Writing - original draft. **Qianwang Deng:** Supervision, Funding acquisition, Resources. **Ruihang Lin:** Software, Validation. **Guiliang Gong:** Project administration. **Wenwu Han:** Project administration.

## Declaration of Competing Interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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