

# Compiles construction

Assignment 2

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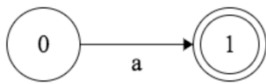
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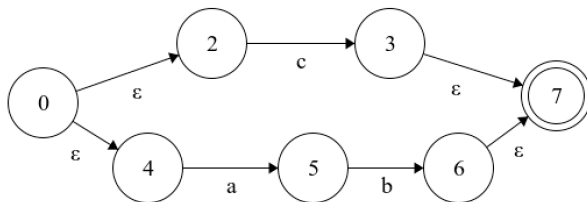
# Regex to NFA (using Thompson's Construction)

We are going to generate a NFA based on the regex  $a(c|ab)^*$ , but first we will split the regex in smaller automaton.

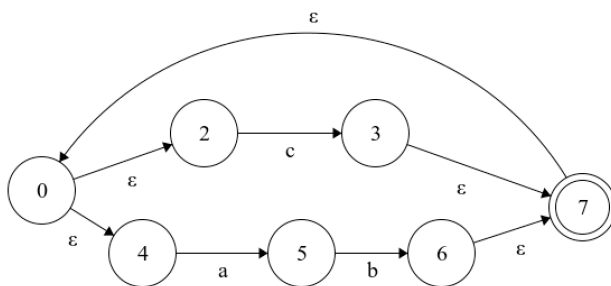
1.  $[a] \rightarrow a(c|ab)^*$



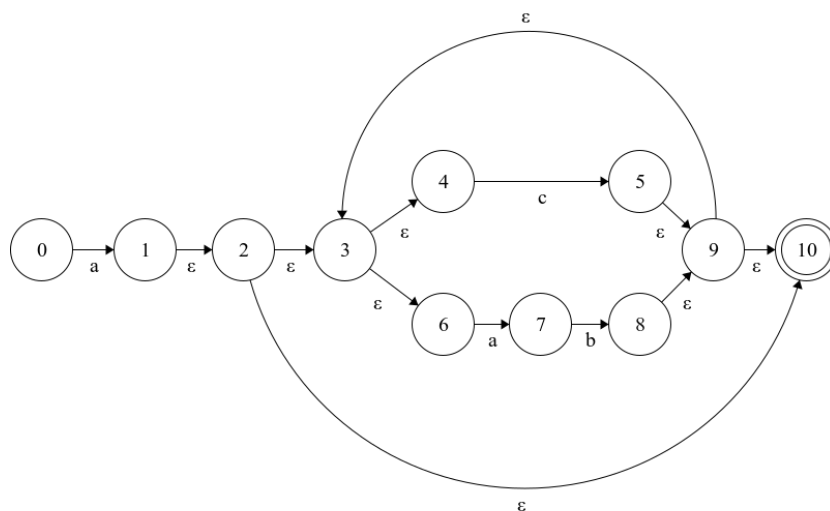
2.  $[c|ab] \rightarrow a(c|ab)^*$



3.  $[(c|ab)^*] \rightarrow a(c|ab)^*$



We can now complete the NFA from the parts we created.



# NFA to DFA (using Subset Construction)

## 1. E-closures from states given in the NFA:

For each state in  $Q'$ , find the possible set of states for each input symbol using transition function of NFA. If this set of states is not in  $Q'$ , add it to  $Q'$ .

state	e-closures
0	{0}
1	{1, 2, 3, 4, 6, 10}
2	{2, 3, 4, 6, 10}
3	{3, 4, 6}
4	{4}
5	{5, 9, 3, 4, 6, 10}
6	{6}
7	{7}
8	{8, 9, 3, 4, 6, 10}
9	{9, 3, 4, 6, 10}
10	{10}

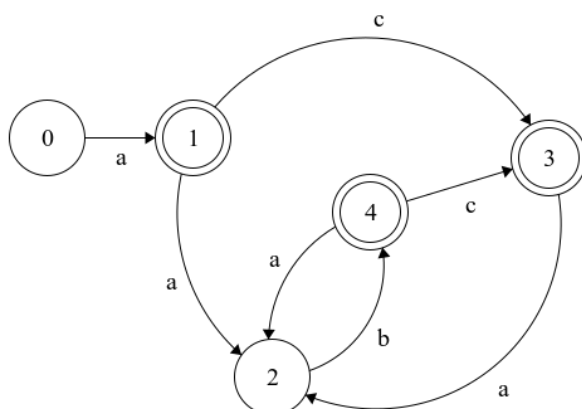
## 2. Transition table

Currently, state in  $Q'$  is  $q_0$ , find moves from  $q_0$  on the input symbols using transition function of NFA and update the transition table of DFA.

	N	states	a	a	b	c
->	0	[0]	[1, 2, 3, 4, 6, 10]	-	-	-
*	1	[1, 2, 3, 4, 6, 10]	-	7	-	[5, 9, 3, 4, 6, 10]
	2	[7]	-	-	[8, 9, 3, 4, 6, 10]	-
*	3	[5, 9, 3, 4, 6, 10]	-	7	-	[5, 9, 3, 4, 6, 10]
*	4	[8, 9, 3, 4, 6, 10]	-	7	-	[5, 9, 3, 4, 6, 10]

## 3. DFA-diagram:

The DFA based on the transition table

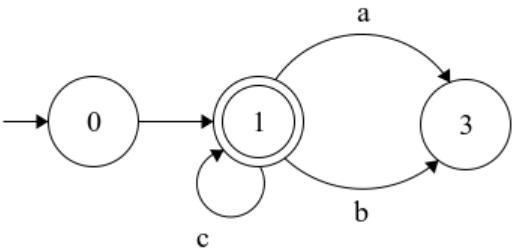


# DFA to Min DFA (based on Hopcroft's Algorithm)

Group states that behave identically

	N		a	a	b	c
->	0	[0]	x	-	-	-
*	1	[1, 3, 4]	-	x	-	x
	2	[2]	-	-	x	-

Min DFA diagram



# Direct-coded Scanner

Now that we created the min-DFA we can create a DC scanner based on that data.

```
/**
 * Scanner for the a(c|ab)* regex
 *
 * @param char *      the string to parse
 * @param int         the length of the string
 * @return char *|NULL
 */
char *scanner(char *stream, int pos = 0)
{
    char c;

    // label to scan for a character
state_init:
    c = stream[pos++];
    if (c == 'a') goto state_ca;
    if (pos == 1) goto state_err;
    else goto state_done;

    // label to scan for a|ab characters recursively
state_ca:
    c = stream[pos++];
    if (c == 'c') goto state_ca;
    else if (c == 'a') goto state_ab;
    else goto state_done;

    // label to scan for b character
state_ab:
    c = stream[pos++];
    if (c == 'b') goto state_ca;
    else goto state_err;

    // label to check if the end of the regex was reached
state_done:
    c = stream[pos-1];
    if (c == 32) goto state_succ;
    else goto state_err;

    // label for success
state_succ:
    return stream;

    // label for errors
state_err:
    return NULL;
}
```