Data Mining With Python and R Tutorials

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Welcome to my Data Mining With Python and R tutorials! In these tutorials, you will learn a wide array of concepts about Python and R programing in Data Mining.

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CHAPTER

ONE

PREFACE

1.1 About this tutorial

This document is a summary of my Data Mining Methds & Application (STAT 577) course in University of Tennessee at Knoxville. You may download and distribute it. Please be aware, however, that the note contains typos as well as inaccurate or incorrect description. At here, I would like to thank Dr. Haileab Hilafu for providing some of his R code and homework solutions. I also would like to thank Bo Gao, Le Yin, Chen Wen, Jian Sun and Huan Chen for the valuable disscussion and thank the generous anonymous authors for providing the detailed solutions and source code on the Internet. Without those help, those tutorials would not have been possible to be made. In those tutorials, I try to use the detailed demo code to show how to use each functions in R and Python to do data mining. If you find your work wasn't cited in this note, please feel free to let me know.

Although I am by no means an data mining programming expert, I decided that it would be useful for me to share what I learned about data mining programming in the form of easy tutorials with detailed example. I hope those tutorials will be a valuable tool for your studies.

The tutorials assume that the reader has a preliminary knowledge of programing and unix. And this document is generated automatically by using sphinx.

1.2 Motivation for this tutorial

Data mining is a relatively new, while the technology is not. Here are the sevaral main motivation for this tutorial:

- 1. It is no exaggeration to say that data mining has thunderstorms impacted on our real lives. I have great interest in data mining and am eager to learn those technologies.
- 2. Fortunely, I had a chance to register Dr. Haileab Hilafu's Data Mining Methds & Application class. Dr.Haileab Hilafu and his class inspired me to do a better job.
- 3. However, I still found that learning data mining programing was a difficult process. I have to Google it and identify which one is true. It was hard to find detailed examples which I can easily learned the full process in one file.
- 4. Good sources are expensive for a graduate student.

1.3 Feedback and suggestions

Your comments and suggestions are highly appreciated. I am more than happy to receive corrections, suggestions or feedbacks through email (Wenqiang Feng: wfeng1@vols.utk.edu) for improvements.

PYTHON OR R FOR DATA ANALYSIS?

Note: Sharpening the knife longer can make it easier to hack the firewood – old Chinese proverb

There is an old Chinese proverb that Says 'sharpening the knife longer can make it easier to hack the firewood'. In other words, take extra time to get it right in the preparation phase and then the work will be easier. So it is worth to take several minites to think about which programming language is better for you.

When you google it, you will get many useful results. Here are some valueable information from Quora:

2.1 Ponder over questions

- Six questions to ponder over from Vipin Tyagi at Quora
 - 1. Is your problem is purely data analysis based or mixed one involving mathematics, machine-learning, artificial intelligence based?
 - 2. What are the commonly used tools in your field?
 - 3. What is the programming expertise of your human resources?
 - 4. What level of visualization you require in your presentations?
 - 5. Are you academic, research-oriented or commercial professional?
 - 6. Do you have access to number of data analytic softwares for doing your assignment?

2.2 Comparison List

• comparative list from Yassine Alouini at Quora

	R	Python
advantages	 great for prototyping great for statistical analysis nice IDE 	 great for scripting and automating your different data mining pipelines integrates easily in a production workflow can be used across different parts of your software engineering team scikit-learn library is awesome for machine-learning tasks. Ipython is also a powerful tool for exploratory analysis and presentations
disadvantages	 syntax could be obscure libraries documentation isn't always user friendly harder to integrate to a production workflow. 	 It isn't as thorough for statistical analysis as R learning curve is steeper than R, since you can do much more with Python

2.3 My Opinions

In my opinion, **R** and **Python** are both choice. Since they are open-source softwares (open-source is always good in my eyes) and are free to download. If you are a beginer without any programming experience and only want to do some data analysis, I would definitely suggest to use **R**. Otherwise, I would suggest to use both.

CHAPTER

THREE

GETTING STARTED

Note: Good tools are prerequisite to the successful execution of a job – old Chinese proverb

Let's keep sharpening our tools. A good programming platform can save you lots of troubles and time. Herein I will only present how to install my favorite programming platform for R and Python and only show the easiest way which I know to install them on Linux system. If you want to install on the other operator system, you can Google it. In this section, you may learn how to install R, Python and the corresponding programming platform and package.

3.1 Installing programming language

• Installing R

Go to Ubuntu Software Center and follow the following steps:

- 1. Open Ubuntu Software Center
- 2. Search for r-base
- 3. And click Install

Or Open your terminal and using the following command:

```
sudo apt-get update
sudo apt-get install r-base
```

• Insralling Python

Go to Ubuntu Software Center and follow the following steps:

- 1. Open Ubuntu Software Center
- 2. Search for python
- 3. And click Install

Or Open your terminal and using the following command:

```
sudo apt-get install build-essential checkinstall
sudo apt-get install libreadline-gplv2-dev libncursesw5-dev libssl-

→dev

libsqlite3-dev tk-dev libgdbm-dev libc6-dev libbz2-dev
sudo apt-get install python
sudo easy_install pip
sudo pip install ipython
```

3.2 Installing programming platform

My favorite programming platform for R is definitely **RStudio** IDE and for Python is **Eclipse+Pydev**.

• Installing RStudio

Go to Ubuntu Software Center and follow the following steps:

- 1. Open Ubuntu Software Center
- 2. Search for RStudio
- 3. And click Install

• Installing Eclipse + Pydev

• Installing Eclipse

Go to Ubuntu Software Center and follow the following steps:

- 1. Open Ubuntu Software Center
- 2. Search for Eclipse
- 3. And click Install
- Installing Pydev
 - 1. Open Eclipse
 - 2. Go to Eclipse Marketplace
 - 3. Search for Pydev
 - 4. And click Pydev- Python IDE for Eclipse

Here is the video tutorial for installing Pydev for Eclipse on Youtube: Pydev on Youtube

3.3 Installing package

• Installing package for R

Install package for R in RStudio os super easy, I will use tree package as a example:

```
install.packages("tree")
```

The following are the top 20 R machine learning and data science packages from Bhavya Geethika, you may want to install all of them.

- e1071 Functions for latent class analysis, short time Fourier transform, fuzzy clustering, support vector machines, shortest path computation, bagged clustering, naive Bayes classifier etc (142479 downloads)
- rpart Recursive Partitioning and Regression Trees. (135390)
- **igraph** A collection of network analysis tools. (122930)
- nnet Feed-forward Neural Networks and Multinomial Log-Linear Models. (108298)
- randomForest Breiman and Cutler's random forests for classification and regression. (105375)
- caret package (short for Classification And REgression Training) is a set of functions that attempt to streamline the process for creating predictive models. (87151)
- **kernlab** Kernel-based Machine Learning Lab. (62064)
- glmnet Lasso and elastic-net regularized generalized linear models. (56948)
- **ROCR** Visualizing the performance of scoring classifiers. (51323)
- **gbm** Generalized Boosted Regression Models. (44760)
- party A Laboratory for Recursive Partitioning. (43290)
- arules Mining Association Rules and Frequent Itemsets. (39654)
- tree Classification and regression trees. (27882)
- klaR Classification and visualization. (27828)
- **RWeka** R/Weka interface. (26973)
- **ipred** Improved Predictors. (22358)
- lars Least Angle Regression, Lasso and Forward Stagewise. (19691)
- earth Multivariate Adaptive Regression Spline Models. (15901)
- **CORElearn** Classification, regression, feature evaluation and ordinal evaluation. (13856)
- **mboost** Model-Based Boosting. (13078)

• Installing package for Python

Install package or modules for Python in Linux can also be quite easy. Here I will only present installation by using pip.

Installing pip

```
sudo easy_install pip
```

• Installing numpy

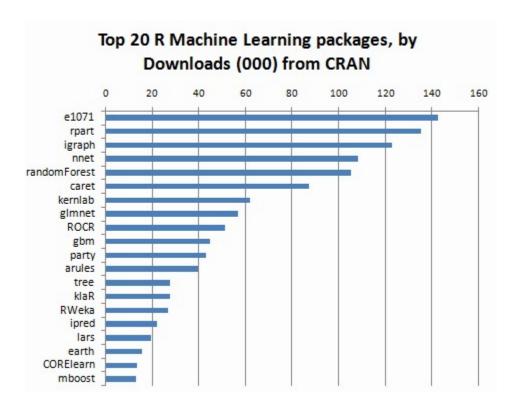


Fig. 1: Top 20 R Machine Learning and Data Science packages. From http://www.kdnuggets.com/2015/06/top-20-r-machine-learning-packages.html

pip install numpy

Installing pandas

pip install pandas

• Installing scikits-learn

pip install -U scikit-learn

The following are the best Python modules for data mining from kdnuggets, you may also want to install all of them.

- 1. Basics
- numpy numerical library, http://numpy.scipy.org/
- scipy Advanced math, signal processing, optimization, statistics, http://www.scipy.org/
- matplotlib, python plotting Matplotlib, http://matplotlib.org
- 2. Machine Learning and Data Mining
- MDP, a collection of supervised and unsupervised learning algorithms, http://pypi.python.org/pypi/ MDP/2.4

- mlpy, Machine Learning Python, http://mlpy.sourceforge.net
- NetworkX, for graph analysis, http://networkx.lanl.gov/
- Orange, Data Mining Fruitful & Fun, http://biolab.si
- pandas, Python Data Analysis Library, http://pandas.pydata.org
- pybrain, http://pybrain.org
- scikits-learn Classic machine learning algorithms Provide simple an efficient solutions to learning problems, http://scikit-learn.org/stable/
- 3. Natural Language
- NLTK, Natural Language Toolkit, http://nltk.org
- 4. For web scraping
- Scrapy, An open source web scraping framework for Python, http://scrapy.org
- urllib/urllib2

Herein I would like to add one more important package **Theano** for deep learning and **textmining** for text mining:

- Theano, deep learning, http://deeplearning.net/tutorial/
- **textmining**, text mining, https://pypi.python.org/pypi/textmining/1.0

DATA ANALYSIS PROCEDURES

Note: Know yourself and know your enemy, and you will never be defeated – idiom, from Sunzi's Art of War

4.1 procedures

Data mining is a complex process that aims to discover patterns in large data sets starting from a collection of exsting data. In my opinion, data minig contains four main steps:

- 1. **Collecting data**: This is a complex step, I will assume we have already gotten the datasets.
- 2. **Pre-processing**: In this step, we need to try to understand your data, denoise, do dimentation reduction and select proper predictors etc.
- 3. **Feeding data mining**: In this step, we need to use your data to feed your model.
- 4. **Post-processing**: In this step, we need to interpret and evaluate your model.

In this section, we will try to know our enemy – datasets. We will learn how to load data, how to understand data with statistics method and how to underdtand data with visualization. Next, we will start with Loading Datasets for the Pre-processing.

4.2 Datasets in this Tutorial

The datasets for this tutorial are available to download: Heart, Energy Efficiencey. Those data are from my course matrials, the copyrights blongs to the original authors.

4.3 Loading Datasets

There are two main data formats ".csv" and ".xlsx". We will show how to load those two types of data in **R** and **Python**, respectively.

1. Loading datasets in R

• Loading *.csv format data

```
# set the path or enverionment
setwd("/home/feng/R-language/sat577/HW#4/data")
# read data set
rawdata = read.csv("spam.csv")
```

• Loading *.xlsx format data

```
# set the path or enverionment
setwd("~/Dropbox/R-language/sat577/")

#install.packages("readxl") # CRAN version
library(readxl)

# read data set
energy_eff=read_excel("energy_efficiency.xlsx")
```

2. Loading datasets in Python

• Loading *.csv format data

• Loading *.xlsx format data

4.4 Understand Data With Statistics methods

After we get the data in hand, then we can try to understand them. I will use "Heart.csv" dataset as a example to demonstrate how to use those statistics methods.

1. Summary of the data

It is always good to have a glance over the summary of the data. Since from the summary you will know some statistics features of your data, and you will also know whether you data contains missing data or not.

• Summary of the data in R

```
summary(rawdata)
```

Then you will get

> summary(rawdata)			
Age	Sex	ChestPain	
→RestBP			
	Min. :0.0000	asymptomatic:144	Min.
⇒ : 94.0			
1st Qu.:48.00	1st Qu.:0.0000	nonanginal : 86	1st_
→Qu.:120.0			
Median :56.00	Median :1.0000	nontypical : 50	ш
→Median :130.0			
Mean :54.44	Mean :0.6799	typical : 23	ш
→Mean :131.7			
3rd Qu.:61.00	3rd Qu.:1.0000		3rd_
→Qu.:140.0	1 0000		
Max. :77.00	Max. :1.0000		Max.
→ :200.0			
Chol	Fbs	RestECG	MaxHR
II			Min.
→ : 71.0	.0.0000	.0.000	
	1st Qu.:0.0000	1st Qu.:0.0000	1st.
→Qu.:133.5	100 20.1010000	100 20.10.000	100
Median :241.0	Median :0.0000	Median :1.0000	
→Median :153.0			_
Mean :246.7	Mean :0.1485	Mean :0.9901	Mean _
3rd Qu.:275.0	3rd Qu.:0.0000	3rd Qu.:2.0000	3rd_
→Qu.:166.0			
II	Max. :1.0000	Max. :2.0000	Max
ExAng	Oldpeak	Slope	Ca
	Min. :0.00	Min. :1.000 Mi	ın. 👅
→:0.0000	1 - 4 0 - 0 0 0	1 - 1 0 - 1 0 0 0 1 -	
1st Qu.:0.0000 →:0.0000	IST QU.:0.00	ısı Qu.:1.000 18	st Qu.
→:0.0000 Median :0.0000	Median •0 90	Median • 2 000 Ma	edian.
→:0.0000	riculan .0.00	rieutan .Z.000 Me	TULAII_
Mean :0.3267	Mean :1.04	Mean :1.601 Me	ean
→:0.6722	110411 .1.04	113411 11.001 110	saii 👅
3rd Qu.:1.0000	3rd Qu.:1.60	3rd Qu.:2.000 31	rd Qu.
→:1.0000	2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	. 2 –	2
Max. :1.0000	Max. :6.20	Max. :3.000 Ma	ax.
⇔: 3.0000			_
		(continues on	nevt page)

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```
Thal AHD
fixed : 18 No :164
normal :166 Yes:139
reversable:117
NA's : 2
```

• Summary of the data in Python

```
print "data summary"
print rawdata.describe()
```

Then you will get

Age		RestBP	Chol	
→ Fbs RestECG	\			
count 303.000000		303.000000	303.000000	303.
→000000 303.0000				
mean 54.438944		131.689769	246.693069	0.
→148515 0.9900		15 500540	E1 00000	0
std 9.038662 →356198 0.9949		17.599748	51.776918	0.
min 29.00000		94.000000	126.000000	0.
→000000 0.00000		94.000000	126.000000	0.
25% 48.00000		120.000000	211.000000	0.
→000000 0.00000		120.000000	211.000000	0.
50% 56.000000		130.000000	241.000000	0.
→000000 1.0000				
75% 61.000000		140.000000	275.000000	0.
→000000 2.0000	00			
max 77.000000	1.000000	200.000000	564.000000	1.
→000000 2.0000	00			
MaxHR	-	-	-	
count 303.000000	303.000000	303.000000	303.000000	299.
→000000 mean 149.607261	0 206722	1 020604	1.600660	0.
mean 149.607261 →672241	0.326733	1.039604	1.60060	0.
std 22.875003	0.469794	1.161075	0.616226	0.
→937438	0.405754	1.101073	0.010220	0.
min 71.000000	0.000000	0.000000	1.000000	0.
→ 000000				
25% 133.500000	0.000000	0.000000	1.000000	0.
→ 000000				
50% 153.000000	0.000000	0.800000	2.000000	0.
→000000				
75% 166.000000	1.000000	1.600000	2.000000	1.
→ 000000				
	4 000000	C 200000	2 000000	2
max 202.000000 →000000	1.000000	6.200000	3.000000	3.

2. The size of the data

Sometimes we also need to know the size or dimension of our data. Such as when you need to extract the response from the dataset, you need the number of column, or when you try to split your data into train and test data set, you need know the number of row.

• Checking size in **R**

```
dim(rawdata)
```

Or you can use the following code

```
nrow=nrow(rawdata)
ncol=ncol(rawdata)
c(nrow, ncol)
```

Then you will get

```
> dim(rawdata)
[1] 303 14
```

Checking size in Python

```
nrow, ncol = rawdata.shape
print nrow, ncol
```

or you can use the follwing code

```
nrow=rawdata.shape[0] #gives number of row count
ncol=rawdata.shape[1] #gives number of col count
print nrow, ncol
```

Then you will get

```
Raw data size
303 14
```

3. Data format of the predictors

Data format is also very important, since some functions or methods can not be applied to the qualitative data, you need to remove those predictors or transform them into quantitative data.

• Checking data format in R

```
# install the package
install.packages("mlbench")
library(mlbench)
sapply(rawdata, class)
```

Then you will get

```
> sapply(rawdata, class)
Age Sex ChestPain RestBP Chol Fbs ____

RestECG (continues on next page)
```

(continued from previous page)

```
"integer" "integer" "factor" "integer" "integer"

y"integer"

MaxHR    ExAng Oldpeak    Slope    Ca    Thal

AHD

"integer" "integer" "numeric" "integer" "integer" "factor"

y"factor"
```

• Checking data format in **Pyhton**

```
print rawdata.dtypes
```

Then you will get

```
Data Format:
          int64
Age
           int64
Sex
ChestPain object
RestBP
          int64
Chol
           int64
Fbs
           int64
ros
RestECG
           int64
           int64
MaxHR
ExAng
           int64
ExAng int64 Oldpeak float64
Slope
           int64
Ca
         float64
Thal
          object
AHD
           object
dtype: object
```

4. The column names

• Checking column names of the data in **R**

```
colnames(rawdata)
attach(rawdata) # enable you can directly use name as_
predictors
```

Then you will get

```
> colnames(rawdata)
[1] "Age" "Sex" "ChestPain" "RestBP" "Chol"
[6] "Fbs" "RestECG" "MaxHR" "ExAng" "Oldpeak"
[11] "Slope" "Ca" "Thal" "AHD"
```

• Checking column names of the data in **Python**

```
colNames = rawdata.columns.tolist()
print "Column names:"
print colNames
```

Then you will get

```
Column names:
['Age', 'Sex', 'ChestPain', 'RestBP', 'Chol', 'Fbs', 'RestECG

→', 'MaxHR',

'ExAng', 'Oldpeak', 'Slope', 'Ca', 'Thal', 'AHD']
```

5. The first or last parts of the data

• Checking first parts of the data in **R**

```
head(rawdata)
```

Then you will get

```
> head(rawdata)
          ChestPain RestBP Chol Fbs RestECG MaxHR ExAng
  Age Sex
→Oldpeak
                                                 0 _
                      145 233
1 63 1
             typical
                                1
                                          150
   2.3
2 67
       1 asymptomatic
                      160 286
                                       2
                                          108
                                0
                                                 1 _
   1.5
                      120 229
3 67
       1 asymptomatic
                                          129
                                                 1 _
                                0
   2.6
  37 1
                                                 0 _
4
         nonanginal
                      130 250
                                0
                                          187
   3.5
5
         nontypical
                      130 204
                                                 0 _
  41 0
                                0
                                          172
   1.4
                                                 0 _
6 56 1 nontypical 120 236 0
                                      0 178
   0.8
   Slope Ca
               Thal AHD
1
     3 0
             fixed No
     2 3
2
             normal Yes
3
     2 2 reversable Yes
     3 0 normal No
4
5
     1 0
            normal No
     1 0
6
             normal No
```

• Checking first parts of the data in Python

```
print "\n Sample data:"
print(rawdata.head(6))
```

Then you will get

```
Sample data:
             ChestPain RestBP Chol Fbs RestECG
   Age Sex
→MaxHR ExAng Oldpeak \
                                                150_
0 63 1
               typical
                         145
                              233
                                   1
                                            2
   0
           2.3
   67
       1 asymptomatic
                         160
                              286
                                    0
                                                108
           1.5
    1
        1 asymptomatic
                         120 229
                                                129
           2.6
                                       (continues on next page)
```

							(continu	ued from previo	us page)
3	37	1	nonanginal		130	250	0	0	187
\hookrightarrow	0		3.5						
4	41	0	nontypical		130	204	0	2	172 <u> </u>
\hookrightarrow	0		1.4						
5	56	1	nontypical		120	236	0	0	178_
\hookrightarrow	0		0.8						
	Slope	Ca	Thal	AHD					
0	3	0	fixed	No					
1	2	3	normal	Yes					
2	2	2	reversable	Yes					
3	3	0	normal	No					
4	1	0	normal	No					
5	1	0	normal	No					
1									

You can use the samilar way to check the last part of the data, for simplicity, i will skip it.

6. Correlation Matrix

• Computing correlation matrix in **R**

```
# get numerical data and remove NAN
numdata=na.omit(rawdata[,c(1:2,4:12)])
# computing correlation matrix
cor(numdata)
```

Then you will get

```
> cor(numdata)
            Age
                      Sex
                               RestBP
                                             Chol
        1.00000000 -0.09181347 0.29069633 0.203376601
Age
→128675921
    -0.09181347 1.00000000 -0.06552127 -0.195907357
→045861783
       0.29069633 -0.06552127 1.00000000 0.132284171
RestBP
→177623291
        0.20337660 -0.19590736 0.13228417 1.000000000 0.
Chol
→006664176
       0.12867592 0.04586178 0.17762329 0.006664176 1.
→000000000
RestECG 0.14974915 0.02643577 0.14870922 0.164957542 0.
→058425836
MaxHR -0.39234176 -0.05206445 -0.04805281 0.002179081 -0.
→003386615
ExAng
      0.09510850 0.14903849 0.06588463 0.056387955 0.
→011636935
Oldpeak 0.19737552 0.11023676 0.19161540 0.040430535 0.
→009092935
Slope 0.15895990 0.03933739 0.12110773 -0.009008239 0.
→053776677
```

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```
0.119000487
        0.36260453 0.09318476 0.09877326
→145477522
          RestECG
                        MaxHR
                                    ExAng
                                              Oldpeak
    Slope
        0.14974915 -0.392341763
                               0.09510850 0.197375523
Age
→158959901
        0.02643577 -0.052064447
                                0.14903849
                                          0.110236756
→039337394
RestBP 0.14870922 -0.048052805
                               0.06588463 0.191615405
→121107727
                                0.05638795 0.040430535 -0.
Chol 0.16495754 0.002179081
→009008239
Fbs
        0.05842584 -0.003386615 0.01163693 0.009092935
→053776677
RestECG 1.00000000 -0.077798148 0.07408360 0.110275054
→128907169
MaxHR -0.07779815 1.000000000 -0.37635897 -0.341262236 -0.
→381348495
ExAng 0.07408360 -0.376358975 1.00000000 0.289573103
→254302081
Oldpeak 0.11027505 -0.341262236 0.28957310 1.000000000
→579775260
Slope 0.12890717 -0.381348495 0.25430208 0.579775260
→000000000
Ca 0.12834265 -0.264246253 0.14556960 0.295832115
→110119188
           Ca
        0.36260453
Age
        0.09318476
Sex
RestBP
        0.09877326
        0.11900049
Chol
Fbs
        0.14547752
RestECG 0.12834265
MaxHR -0.26424625
ExAng
        0.14556960
Oldpeak 0.29583211
Slope
        0.11011919
Ca
        1.00000000
```

• Computing correlation matrix in **Python**

```
print "\n correlation Matrix"
print rawdata.corr()
```

Then you will get

```
correlation Matrix

Age Sex RestBP Chol Fbs ...

→RestECG MaxHR \

Age 1.000000 -0.097542 0.284946 0.208950 0.118530 0.

→148868 -0.393806
```

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```
(continued from previous page)
       -0.097542 1.000000 -0.064456 -0.199915 0.047862
\rightarrow021647 -0.048663
RestBP 0.284946 -0.064456 1.000000 0.130120 0.175340
                                                           0.
\rightarrow 146560 - 0.045351
Chol
        0.208950 -0.199915 0.130120
                                      1.000000 0.009841
\hookrightarrow171043 -0.003432
        0.118530 0.047862 0.175340
                                      0.009841 1.000000
\hookrightarrow 069564 -0.007854
RestECG 0.148868 0.021647 0.146560 0.171043 0.069564
→000000 -0.083389
      -0.393806 - 0.048663 - 0.045351 - 0.003432 - 0.007854 - 0.
MaxHR
→083389 1.000000
ExAng
      0.091661 0.146201 0.064762 0.061310 0.025665
\rightarrow 084867 - 0.378103
Oldpeak 0.203805 0.102173 0.189171 0.046564 0.005747
                                                           \cap
→114133 -0.343085
        0.161770 0.037533 0.117382 -0.004062 0.059894
Slope
                                                           0.
→133946 -0.385601
        0.362605 0.093185 0.098773 0.119000 0.145478 0.
Ca
→128343 -0.264246
         ExAng Oldpeak
                            Slope
                                           Ca
         0.091661 0.203805 0.161770 0.362605
Age
Sex
        0.146201 0.102173 0.037533 0.093185
RestBP
        0.064762 0.189171 0.117382 0.098773
Chol
        0.061310 0.046564 -0.004062 0.119000
Fbs
        0.025665 0.005747 0.059894 0.145478
RestECG 0.084867 0.114133 0.133946 0.128343
MaxHR -0.378103 -0.343085 -0.385601 -0.264246
ExAng
        1.000000 0.288223 0.257748 0.145570
Oldpeak 0.288223 1.000000 0.577537 0.295832
Slope
        0.257748 0.577537 1.000000 0.110119
Ca
        0.145570 0.295832 0.110119 1.000000
```

7. covariance Matrix

• Computing covariance matrix in **R**

```
# get numerical data and remove NAN
numdata=na.omit(rawdata[,c(1:2,4:12)])
# computing covariance matrix
cov(numdata)
```

Then you will get

```
> cov(numdata)
                 Age
                                Sex
                                          RestBP
                                                           Chol
        Fbs
                                                     95.2454603
         81.3775448 -0.388397567 46.4305852
Age
\rightarrow 0.411909946
Sex
         -0.3883976 0.219905277 -0.5440170
                                                    -4.7693542
                                                                  0.
<u></u>

→007631703
                                                    (continues on next page)
```

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RestBP 46.4305852 -0.544016969 313.4906736 121.5937353			(conti	nued from previous page)
1.16001885 Chol 95.2454603 -4.769354223 121.5937353 2695.14426160.122769410 Fbs 0.4119099 0.007631703 1.1160019 0.12276940.125923099 RestECG 1.3440551 0.012334179 2.6196943 8.52047090.020628044 MaxHR -81.2442706 -0.560447577 -19.5302126 2.59681040.027586362 Exhng 0.4034028 0.032861215 0.5484838 1.37640010.01941595 Oldpeak 2.0721791 0.060162510 3.9484299 2.44276780.03755247 Slope 0.8855132 0.011391439 1.3241566 -0.28879260.011784247 Ca 3.0663958 0.040964288 1.6394357 5.79138520.018393975 RestECG MaxHR ExAng OldpeakSlope 0.8855132 Sex 0.01233418 -0.56044758 0.032861215 0.0601625100.01139144 RestEBP 2.61969428 -19.53021257 0.548483760 3.9484298890.0139144 RestEBP 2.61969428 -19.53021257 0.548483760 3.9484298890.01139124 FestEGC 0.988992166 -1.77682880 0.001941595 0.0037552470.01178425 RestECG 0.98992166 -1.77682880 0.034656910 0.1276907360.07920136 MaxHR -1.77682880 526.92866602 -4.062052479 -9.1168716755.40571480 ExAng 0.03465691 -4.06205248 0.221072479 0.1584554780.07383673 0.0693828 Sex 0.04096429 RestBP 1.639433570 Chol 5.79138515 Fbs 0.04839398 RestECG 0.11970551 -5.68626967 0.064162421 0.3227525760.06374717 Ca Age 3.06639582 Sex 0.04096429 RestBP 1.63943570 Chol 5.79138515 Fbs 0.04839398 RestECG 0.11970551 MaxHR -5.68626967	RestBP 46.4305852	-0.544016969	313.4906736	121.5937353
□0.122769410 Fbs				_
□0.122769410 Fbs	Chol 95.2454603	-4.769354223	121.5937353	2695.1442616
RestECG 1.3440551 0.012334179 2.6196943 8.5204709 0.020628044 MaxHR −81.2442706 −0.560447577 −19.5302126 2.5968104 − 0.027586362 ExAng 0.4034028 0.032861215 0.5484838 1.3764001 0.001941595 Oldpeak 2.0721791 0.060162510 3.9484299 2.4427678 0.003755247 Slope 0.8855132 0.011391439 1.3241566 −0.2887926 0.011784247 Ca 3.0663958 0.040964288 1.6394357 5.7913852 0.048393975 RestECG MaxHR ExAng Oldpeak 35lope Age 1.34405513 −81.24427061 0.403402842 2.072179076 0.88551323 Sex 0.01233418 −0.56044758 0.032861215 0.060162510 0.01139144 RestEBP 2.61969428 −19.53021257 0.548483760 3.948429889 1.32415658 Chol 8.52047092 2.59681040 1.376400081 2.442767839 − 0.228879262 Fbs 0.02062804 −0.02758636 0.001941595 0.003755247 0.01178425 RestECG 0.98992166 −1.77682880 0.034656910 0.127690736 0.0178920136 MaxHR −1.77682880 526.92866602 −4.062052479 −9.116871675 − 0.01789263 ExAng 0.03465691 −4.06205248 0.221072479 0.158455478 0.0.17383673 Oldpeak 0.12769074 −9.11687168 0.158455478 1.354451303 0.14667415 Slope 0.07920136 −5.40571480 0.073836726 0.416674149 0.038133824 Ca 0.11970551 −5.68626967 0.064162421 0.322752576 0.038133824 Ca 0.11970551 −5.68626967 0.064162421 0.322752576 0.038133824 Ca 0.01970551 −5.68626967 0.064162421 0.322752576 0.038133824 Ca 0.01970551 −5.68626967 0.064162421 0.322752576 0.038133824 Ca 0.0496429 RestEBF 1.63943570 Chol 5.79138515 Fbs 0.04839398 RestECG 0.11970551 MaxHR −5.68626967				_
RestECG 1.3440551 0.012334179 2.6196943 8.5204709 0.020628044 MaxHR −81.2442706 −0.560447577 −19.5302126 2.5968104 − 0.027586362 ExAng 0.4034028 0.032861215 0.5484838 1.3764001 0.001941595 Oldpeak 2.0721791 0.060162510 3.9484299 2.4427678 0.003755247 Slope 0.8855132 0.011391439 1.3241566 −0.2887926 0.011784247 Ca 3.0663958 0.040964288 1.6394357 5.7913852 0.048393975 RestECG MaxHR ExAng Oldpeak 35lope Age 1.34405513 −81.24427061 0.403402842 2.072179076 0.88551323 Sex 0.01233418 −0.56044758 0.032861215 0.060162510 0.01139144 RestEBP 2.61969428 −19.53021257 0.548483760 3.948429889 1.32415658 Chol 8.52047092 2.59681040 1.376400081 2.442767839 − 0.228879262 Fbs 0.02062804 −0.02758636 0.001941595 0.003755247 0.01178425 RestECG 0.98992166 −1.77682880 0.034656910 0.127690736 0.0178920136 MaxHR −1.77682880 526.92866602 −4.062052479 −9.116871675 − 0.01789263 ExAng 0.03465691 −4.06205248 0.221072479 0.158455478 0.0.17383673 Oldpeak 0.12769074 −9.11687168 0.158455478 1.354451303 0.14667415 Slope 0.07920136 −5.40571480 0.073836726 0.416674149 0.038133824 Ca 0.11970551 −5.68626967 0.064162421 0.322752576 0.038133824 Ca 0.11970551 −5.68626967 0.064162421 0.322752576 0.038133824 Ca 0.01970551 −5.68626967 0.064162421 0.322752576 0.038133824 Ca 0.01970551 −5.68626967 0.064162421 0.322752576 0.038133824 Ca 0.0496429 RestEBF 1.63943570 Chol 5.79138515 Fbs 0.04839398 RestECG 0.11970551 MaxHR −5.68626967	Fbs 0.4119099	0.007631703	1.1160019	0.1227694 _
	→ 0.125923099			
MaxHR -81.2442706 -0.560447577 -19.5302126 2.5968104 -	RestECG 1.3440551	0.012334179	2.6196943	8.5204709
□0.027586362 ExAng	→ 0.020628044			
ExAng 0.4034028 0.032861215 0.5484838 1.3764001 0.001941595 0ldpeak 2.0721791 0.060162510 3.9484299 2.4427678 0.0037755247 Slope 0.8855132 0.011391439 1.3241566 -0.2887926 0.0.011784247 Ca 3.0663958 0.040964288 1.6394357 5.7913852 0.0.048393975 RestECG MaxHR ExAng Oldpeak 0.08855132 Sex 0.01233418 -0.56044758 0.032861215 0.060162510 0.0.88551323 Sex 0.01233418 -0.56044758 0.032861215 0.060162510 0.0.1319144 RestBP 2.61969428 -19.53021257 0.548483760 3.948429889 0.1.32415658 Chol 8.52047092 2.59681040 1.376400081 2.442767839 -0.28879262 Fbs 0.02062804 -0.02758636 0.001941595 0.003755247 0.01178425 RestECG 0.98992166 -1.77682880 0.034656910 0.127690736 0.0.07920136 MaxHR -1.77682880 526.92866602 -4.062052479 -9.116871675 -0.540571480 ExAng 0.03465691 -4.06205248 0.221072479 0.158455478 0.0.07383673 Oldpeak 0.12769074 -9.11687168 0.158455478 1.354451303 0.0.41667415 Slope 0.07920136 -5.40571480 0.073836726 0.416674149 0.0.38133824 Ca 0.11970551 -5.68626967 0.064162421 0.322752576 0.0.06374717 Ca Age 3.06639582 Sex 0.04096429 RestBP 1.63943570 Chol 5.79138515 Fbs 0.04839398 RestECG 0.11970551 MaxHR -5.68626967	MaxHR -81.2442706	-0.560447577	-19.5302126	2.5968104 -
□0.001941595 Oldpeak 2.0721791 0.060162510 3.9484299 2.4427678 □0.003755247 Slope 0.8855132 0.011391439 1.3241566 -0.2887926 □0.011784247 Ca 3.0663958 0.040964288 1.6394357 5.7913852 □0.048393975 RestECG MaxHR ExAng Oldpeak □3.88551323 Sex 0.01233418 -0.56044758 0.032861215 0.060162510 □0.88551323 Sex 0.01233418 -0.56044758 0.032861215 0.060162510 □0.88551323 Sex 0.01233418 -0.56044758 0.032861215 0.060162510 □0.01139144 RestEP 2.61969428 -19.53021257 0.548483760 3.948429889 □1.32415658 Chol 8.52047092 2.59681040 1.376400081 2.442767839 □0.28879262 Fbs 0.02062804 -0.02758636 0.001941595 0.003755247 □0.01178425 RestECG 0.98992166 -1.77682880 0.034656910 0.127690736 □0.07920136 MaxHR -1.77682880 526.92866602 -4.062052479 -9.116871675 -□5.40571480 ExAng 0.03465691 -4.06205248 0.221072479 0.158455478 □0.07383673 0ldpeak 0.12769074 -9.11687168 0.158455478 1.354451303 □0.41667415 Slope 0.07920136 -5.40571480 0.073836726 0.416674149 □0.38133824 Ca 0.11970551 -5.68626967 0.064162421 0.322752576 □0.06374717 Ca Age 3.06639582 Sex 0.04096429 RestEP 1.63943570 Chol 5.79138515 Fbs 0.04839398 RestECG 0.111970551 MaxHR -5.68626967	→ 0.027586362			
Oldpeak 2.0721791 0.060162510 3.9484299 2.4427678 □ □0.003755247 Slope 0.8855132 0.011391439 1.3241566 -0.2887926 □ □0.011784247 Ca 3.0663958 0.040964288 1.6394357 5.7913852 □ □0.048393975 RestECG MaxHR ExAng Oldpeak □ □Slope Age 1.34405513 -81.24427061 0.403402842 2.072179076 □ □0.88551323 Sex 0.01233418 -0.56044758 0.032861215 0.060162510 □ □0.01139144 RestBP 2.61969428 -19.53021257 0.548483760 3.948429889 □ □1.32415658 Chol 8.52047092 2.59681040 1.376400081 2.442767839 - □ □0.28879262 Fbs 0.02062804 -0.02758636 0.001941595 0.003755247 □ □0.01178425 RestECG 0.98992166 -1.77682880 0.034656910 0.127690736 □ □0.07920136 MaxHR -1.77682880 526.92866602 -4.062052479 -9.116871675 - □ □5.40571480 ExAng 0.03465691 -4.06205248 0.221072479 0.158455478 □ □0.07383673 Oldpeak 0.12769074 -9.11687168 0.158455478 1.354451303 □ □0.41667415 Slope 0.07920136 -5.40571480 0.073836726 0.416674149 □ □0.38133824 Ca 0.11970551 -5.68626967 0.064162421 0.322752576 □ □0.06374717		0.032861215	0.5484838	1.3764001 _
□0.003755247 Slope 0.8855132 0.011391439 1.3241566 -0.2887926 □0.011784247 Ca 3.0663958 0.040964288 1.6394357 5.7913852 □0.048393975 RestECG MaxHR ExAng Oldpeak □0.88551323 Sex 0.01233418 -0.56044758 0.032861215 0.060162510 □0.01139144 RestEP 2.61969428 -19.53021257 0.548483760 3.948429889 □1.32415658 Chol 8.52047092 2.59681040 1.376400081 2.442767839 -□0.28879262 Fbs 0.02062804 -0.02758636 0.001941595 0.003755247 □0.01178425 RestECG 0.98992166 -1.77682880 0.034656910 0.127690736 □0.07920136 MaxHR -1.77682880 526.92866602 -4.062052479 -9.116871675 -□5.40571480 ExAng 0.03465691 -4.06205248 0.221072479 0.158455478 □0.07383673 0ldpeak 0.12769074 -9.11687168 0.158455478 1.354451303 □0.034656915 □0.07920136 -5.40571480 0.07383673 0ldpeak 0.12769074 -9.11687168 0.158455478 1.354451303 □0.38133824 Ca 0.11970551 -5.68626967 0.064162421 0.322752576 □0.06374717 Ca Age 3.06639582 Sex 0.04096429 RestEP 1.63943570 Chol 5.79138515 Fbs 0.04839398 RestECG 0.11970551 MaxHR -5.68626967				
Slope 0.8855132 0.011391439 1.3241566 -0.2887926 . →0.011784247 Ca 3.0663958 0.040964288 1.6394357 5.7913852 . →0.048393975 RestECG MaxHR ExAng Oldpeak . →Slope Age 1.34405513 -81.24427061 0.403402842 2.072179076 . →0.88551323 Sex 0.01233418 -0.56044758 0.032861215 0.060162510 . →0.01139144 RestEP 2.61969428 -19.53021257 0.548483760 3.948429889 . →1.32415658 Chol 8.52047092 2.59681040 1.376400081 2.442767839 - →0.28879262 Fbs 0.02062804 -0.02758636 0.001941595 0.003755247 . →0.01178425 RestECG 0.99892166 -1.77682880 0.034656910 0.127690736 . →0.07920136 MaxHR -1.77682880 526.92866602 -4.062052479 -9.116871675 - →5.40571480 ExAng 0.03465691 -4.06205248 0.221072479 0.158455478 . →0.017383673 Oldpeak 0.12769074 -9.11687168 0.158455478 1.354451303 . →0.41667415 Slope 0.07920136 -5.40571480 0.073836726 0.416674149 . →0.38133824 Ca 0.11970551 -5.68626967 0.064162421 0.322752576 . →0.06374717 Ca Age 3.06639582 Sex 0.04096429 RestBP 1.63943570 Chol 5.79138515 Fbs 0.04839398 RestECG 0.11970551 MaxHR -5.68626967	_	0.060162510	3.9484299	2.4427678 _
□ 0.011784247 Ca 3.0663958 0.040964288 1.6394357 5.7913852 □ 0.048393975 RestECG MaxHR ExAng Oldpeak □ Slope Age 1.34405513 -81.24427061 0.403402842 2.072179076 □ 0.88551323 Sex 0.01233418 -0.56044758 0.032861215 0.060162510 □ 0.01139144 RestBP 2.61969428 -19.53021257 0.548483760 3.948429889 □ 1.32415658 Chol 8.52047092 2.59681040 1.376400081 2.442767839 - □ 0.28879262 Fbs 0.02062804 -0.02758636 0.001941595 0.003755247 □ 0.01178425 RestECG 0.98992166 -1.77682880 0.034656910 0.127690736 □ □ 0.07920136 MaxHR -1.77682880 526.92866602 -4.062052479 -9.116871675 - □ 5.40571480 ExAng 0.03465691 -4.06205248 0.221072479 0.158455478 □ □ 0.07383673 Oldpeak 0.12769074 -9.11687168 0.158455478 1.354451303 □ □ 0.41667415 Slope 0.07920136 -5.40571480 0.073836726 0.416674149 □ □ 0.38133824 Ca 0.11970551 -5.68626967 0.064162421 0.322752576 □ □ 0.06374717				
Ca 3.0663958 0.040964288 1.6394357 5.7913852	_	0.011391439	1.3241566	-0.2887926 _
→0.048393975 RestECG MaxHR ExAng Oldpeak →Slope Age 1.34405513 -81.24427061 0.403402842 2.072179076 ↓ -0.88551323 Sex 0.01233418 -0.56044758 0.032861215 0.060162510 ↓ -0.01139144 RestBP 2.61969428 -19.53021257 0.548483760 3.948429889 ↓ -1.32415658 Chol 8.52047092 2.59681040 1.376400081 2.4427678390.28879262 Fbs 0.02062804 -0.02758636 0.001941595 0.003755247 ↓ -0.01178425 RestECG 0.98992166 -1.77682880 0.034656910 0.127690736 ↓ -0.07920136 MaxHR -1.77682880 526.92866602 -4.062052479 -9.1168716755.40571480 ExAng 0.03465691 -4.06205248 0.221072479 0.158455478 ↓ -0.07383673 Oldpeak 0.12769074 -9.11687168 0.158455478 1.354451303 ↓ -0.41667415 Slope 0.07920136 -5.40571480 0.073836726 0.416674149 ↓ -0.38133824 Ca 0.11970551 -5.68626967 0.064162421 0.322752576 ↓ -0.06374717				
RestECG MaxHR ExAng Oldpeak →Slope Age 1.34405513 -81.24427061 0.403402842 2.072179076 . →0.88551323 Sex 0.01233418 -0.56044758 0.032861215 0.060162510 . →0.01139144 RestBP 2.61969428 -19.53021257 0.548483760 3.948429889 . →1.32415658 Chol 8.52047092 2.59681040 1.376400081 2.442767839 - →0.28879262 Fbs 0.02062804 -0.02758636 0.001941595 0.003755247 . →0.01178425 RestECG 0.98992166 -1.77682880 0.034656910 0.127690736 . →0.07920136 MaxHR -1.77682880 526.92866602 -4.062052479 -9.116871675 - →5.40571480 ExAng 0.03465691 -4.06205248 0.221072479 0.158455478 . →0.07383673 Oldpeak 0.12769074 -9.11687168 0.158455478 1.354451303 . →0.41667415 Slope 0.07920136 -5.40571480 0.073836726 0.416674149 . →0.08133824 Ca 0.11970551 -5.68626967 0.064162421 0.322752576 . →0.06374717		0.040964288	1.6394357	5.7913852 _
-Slope Age 1.34405513 -81.24427061 0.403402842 2.072179076 -0.085551323 Sex 0.01233418 -0.56044758 0.032861215 0.060162510 -0.01139144 RestBP 2.61969428 -19.53021257 0.548483760 3.948429889 -1.32415658 Chol 8.52047092 2.59681040 1.376400081 2.4427678390.28879262 Fbs 0.02062804 -0.02758636 0.001941595 0.003755247 -0.01178425 RestECG 0.98992166 -1.77682880 0.034656910 0.1276907360.07920136 MaxHR -1.77682880 526.92866602 -4.062052479 -9.1168716755.40571480 ExAng 0.03465691 -4.06205248 0.221072479 0.1584554780.07383673 Oldpeak 0.12769074 -9.11687168 0.158455478 1.3544513030.41667415 Slope 0.07920136 -5.40571480 0.073836726 0.4166741490.038133824 Ca 0.11970551 -5.68626967 0.064162421 0.3227525760.06374717				
Age 1.34405513 -81.24427061 0.403402842 2.072179076		MaxHR	ExAng	Oldpeak
Sex 0.01233418 -0.56044758 0.032861215 0.0601625100.01139144 RestBP 2.61969428 -19.53021257 0.548483760 3.9484298891.32415658 Chol 8.52047092 2.59681040 1.376400081 2.4427678390.28879262 Fbs 0.02062804 -0.02758636 0.001941595 0.0037552470.01178425 RestECG 0.98992166 -1.77682880 0.034656910 0.1276907360.07920136 MaxHR -1.77682880 526.92866602 -4.062052479 -9.1168716755.40571480 ExAng 0.03465691 -4.06205248 0.221072479 0.1584554780.07383673 Oldpeak 0.12769074 -9.11687168 0.158455478 1.3544513030.41667415 Slope 0.07920136 -5.40571480 0.073836726 0.4166741490.38133824 Ca 0.11970551 -5.68626967 0.064162421 0.3227525760.06374717				
Sex		-81.24427061	0.403402842	2.072179076 _
→0.01139144 RestBP 2.61969428 -19.53021257 0.548483760 3.948429889 →1.32415658 Chol 8.52047092 2.59681040 1.376400081 2.442767839 - →0.28879262 Fbs 0.02062804 -0.02758636 0.001941595 0.003755247 →0.01178425 RestECG 0.98992166 -1.77682880 0.034656910 0.127690736 →0.07920136 MaxHR -1.77682880 526.92866602 -4.062052479 -9.116871675 - →5.40571480 ExAng 0.03465691 -4.06205248 0.221072479 0.158455478 →0.07383673 Oldpeak 0.12769074 -9.11687168 0.158455478 1.354451303 →0.41667415 Slope 0.07920136 -5.40571480 0.073836726 0.416674149 →0.38133824 Ca 0.11970551 -5.68626967 0.064162421 0.322752576 →0.06374717				
RestBP 2.61969428 -19.53021257 0.548483760 3.948429889 ↓ 1.32415658 Chol 8.52047092 2.59681040 1.376400081 2.442767839 - →0.28879262 Fbs 0.02062804 -0.02758636 0.001941595 0.003755247 ↓ →0.01178425 RestECG 0.98992166 -1.77682880 0.034656910 0.127690736 ↓ →0.07920136 MaxHR -1.77682880 526.92866602 -4.062052479 -9.116871675 - →5.40571480 ExAng 0.03465691 -4.06205248 0.221072479 0.158455478 ↓ →0.07383673 Oldpeak 0.12769074 -9.11687168 0.158455478 1.354451303 ↓ →0.41667415 Slope 0.07920136 -5.40571480 0.073836726 0.416674149 ↓ →0.38133824 Ca 0.11970551 -5.68626967 0.064162421 0.322752576 ↓ →0.06374717 Ca Age 3.06639582 Sex 0.04096429 RestBP 1.63943570 Chol 5.79138515 Fbs 0.04839398 RestECG 0.11970551 MaxHR -5.68626967		-0.56044758	0.032861215	0.060162510
→1.32415658 Chol 8.52047092 2.59681040 1.376400081 2.442767839 - →0.28879262 Fbs 0.02062804 -0.02758636 0.001941595 0.003755247 →0.01178425 RestECG 0.98992166 -1.77682880 0.034656910 0.127690736 . →0.07920136 MaxHR -1.77682880 526.92866602 -4.062052479 -9.116871675 - →5.40571480 ExAng 0.03465691 -4.06205248 0.221072479 0.158455478 . →0.07383673 Oldpeak 0.12769074 -9.11687168 0.158455478 1.354451303 . →0.41667415 Slope 0.07920136 -5.40571480 0.073836726 0.416674149 . →0.38133824 Ca 0.11970551 -5.68626967 0.064162421 0.322752576 . →0.06374717		40 50004055		
Chol 8.52047092 2.59681040 1.376400081 2.442767839 - →0.28879262 Fbs 0.02062804 -0.02758636 0.001941595 0.003755247 □ →0.01178425 RestECG 0.98992166 -1.77682880 0.034656910 0.127690736 □ →0.07920136 MaxHR -1.77682880 526.92866602 -4.062052479 -9.116871675 - →5.40571480 ExAng 0.03465691 -4.06205248 0.221072479 0.158455478 □ →0.07383673 Oldpeak 0.12769074 -9.11687168 0.158455478 1.354451303 □ →0.41667415 Slope 0.07920136 -5.40571480 0.073836726 0.416674149 □ →0.38133824 Ca 0.11970551 -5.68626967 0.064162421 0.322752576 □ →0.06374717		-19.53021257	0.548483760	3.948429889
→0.28879262 Fbs		0 50601040	1 276400001	0 440767000
Fbs 0.02062804 -0.02758636 0.001941595 0.003755247 →0.01178425 RestECG 0.98992166 -1.77682880 0.034656910 0.127690736 →0.07920136 MaxHR -1.77682880 526.92866602 -4.062052479 -9.116871675 - →5.40571480 ExAng 0.03465691 -4.06205248 0.221072479 0.158455478 →0.07383673 Oldpeak 0.12769074 -9.11687168 0.158455478 1.354451303 →0.41667415 Slope 0.07920136 -5.40571480 0.073836726 0.416674149 →0.38133824 Ca 0.11970551 -5.68626967 0.064162421 0.322752576 →0.06374717 Ca Age 3.06639582 Sex 0.04096429 RestBP 1.63943570 Chol 5.79138515 Fbs 0.04839398 RestECG 0.11970551 MaxHR -5.68626967		2.59681040	1.3/6400081	2.442/6/839 -
→0.01178425 RestECG 0.98992166 -1.77682880 0.034656910 0.127690736 →0.07920136 MaxHR -1.77682880 526.92866602 -4.062052479 -9.116871675 - →5.40571480 ExAng 0.03465691 -4.06205248 0.221072479 0.158455478 →0.07383673 Oldpeak 0.12769074 -9.11687168 0.158455478 1.354451303 →0.41667415 Slope 0.07920136 -5.40571480 0.073836726 0.416674149 →0.38133824 Ca 0.11970551 -5.68626967 0.064162421 0.322752576 →0.06374717 Ca Age 3.06639582 Sex 0.04096429 RestBP 1.63943570 Chol 5.79138515 Fbs 0.04839398 RestECG 0.11970551 MaxHR -5.68626967		0 02750626	0 001041505	0 002755247
RestECG 0.98992166 -1.77682880 0.034656910 0.127690736		-0.02/36636	0.001941393	0.003/3324/
→0.07920136 MaxHR −1.77682880 526.92866602 −4.062052479 −9.116871675 − →5.40571480 ExAng 0.03465691 −4.06205248 0.221072479 0.158455478 □ →0.07383673 Oldpeak 0.12769074 −9.11687168 0.158455478 1.354451303 □ →0.41667415 Slope 0.07920136 −5.40571480 0.073836726 0.416674149 □ →0.38133824 Ca 0.11970551 −5.68626967 0.064162421 0.322752576 □ →0.06374717 Ca Age 3.06639582 Sex 0.04096429 RestBP 1.63943570 Chol 5.79138515 Fbs 0.04839398 RestECG 0.11970551 MaxHR −5.68626967		1 77602000	0 024656010	0 127600726
MaxHR -1.77682880 526.92866602 -4.062052479 -9.116871675 - →5.40571480 ExAng 0.03465691 -4.06205248 0.221072479 0.158455478 □ →0.07383673 Oldpeak 0.12769074 -9.11687168 0.158455478 1.354451303 □ →0.41667415 Slope 0.07920136 -5.40571480 0.073836726 0.416674149 □ →0.38133824 Ca 0.11970551 -5.68626967 0.064162421 0.322752576 □ →0.06374717		-1.77002000	0.034030910	0.12/090/30
ExAng 0.03465691 -4.06205248 0.221072479 0.158455478 →0.07383673 Oldpeak 0.12769074 -9.11687168 0.158455478 1.354451303 →0.41667415 Slope 0.07920136 -5.40571480 0.073836726 0.416674149 →0.38133824 Ca 0.11970551 -5.68626967 0.064162421 0.322752576 →0.06374717 Ca Age 3.06639582 Sex 0.04096429 RestBP 1.63943570 Chol 5.79138515 Fbs 0.04839398 RestECG 0.11970551 MaxHR -5.68626967		526 92866602	_/ 062052/79	_9 116871675 _
ExAng 0.03465691 -4.06205248 0.221072479 0.158455478 →0.07383673 Oldpeak 0.12769074 -9.11687168 0.158455478 1.354451303 →0.41667415 Slope 0.07920136 -5.40571480 0.073836726 0.416674149 →0.38133824 Ca 0.11970551 -5.68626967 0.064162421 0.322752576 →0.06374717		320.32000002	4.002032473	J.1100/10/J
→0.07383673 Oldpeak 0.12769074 -9.11687168 0.158455478 1.354451303 →0.41667415 Slope 0.07920136 -5.40571480 0.073836726 0.416674149 →0.38133824 Ca 0.11970551 -5.68626967 0.064162421 0.322752576 →0.06374717		-4 06205248	0 221072479	0 158455478
Oldpeak 0.12769074 -9.11687168 0.158455478 1.354451303 →0.41667415 Slope 0.07920136 -5.40571480 0.073836726 0.416674149 →0.38133824 Ca 0.11970551 -5.68626967 0.064162421 0.322752576 →0.06374717		4.00203240	0.221072179	0.130433470
→0.41667415 Slope 0.07920136 -5.40571480 0.073836726 0.416674149 →0.38133824 Ca 0.11970551 -5.68626967 0.064162421 0.322752576 →0.06374717		-9.11687168	0.158455478	1.354451303
Slope 0.07920136 -5.40571480 0.073836726 0.416674149 →0.38133824 Ca 0.11970551 -5.68626967 0.064162421 0.322752576 →0.06374717		0 0 0 0	, , _ , , , , , , , , , , , , , , , , ,	
→0.38133824 Ca		-5.40571480	0.073836726	0.416674149
Ca 0.11970551 -5.68626967 0.064162421 0.322752576 →0.06374717 Ca Age 3.06639582 Sex 0.04096429 RestBP 1.63943570 Chol 5.79138515 Fbs 0.04839398 RestECG 0.11970551 MaxHR -5.68626967	_			
Ca Age 3.06639582 Sex 0.04096429 RestBP 1.63943570 Chol 5.79138515 Fbs 0.04839398 RestECG 0.11970551 MaxHR -5.68626967		-5.68626967	0.064162421	0.322752576
Ca Age 3.06639582 Sex 0.04096429 RestBP 1.63943570 Chol 5.79138515 Fbs 0.04839398 RestECG 0.11970551 MaxHR -5.68626967				
Sex 0.04096429 RestBP 1.63943570 Chol 5.79138515 Fbs 0.04839398 RestECG 0.11970551 MaxHR -5.68626967				
Sex 0.04096429 RestBP 1.63943570 Chol 5.79138515 Fbs 0.04839398 RestECG 0.11970551 MaxHR -5.68626967	Age 3.06639582			
Chol 5.79138515 Fbs 0.04839398 RestECG 0.11970551 MaxHR -5.68626967	_			
Fbs 0.04839398 RestECG 0.11970551 MaxHR -5.68626967	RestBP 1.63943570			
RestECG 0.11970551 MaxHR -5.68626967	Chol 5.79138515			
MaxHR -5.68626967	Fbs 0.04839398			
	RestECG 0.11970551			
ExAna 0.06416242	MaxHR -5.68626967			
	ExAng 0.06416242			
Oldpeak 0.32275258 (continues on next page)	Oldpeak 0.32275258			

(continues on next page)

(continued from previous page)

```
Slope 0.06374717
Ca 0.87879060
```

• Computing covariance matrix in **Python**

```
print "\n covariance Matrix"
print rawdata.corr()
```

Then you will get

covariance Matrix						
	Age	Sex	RestBP	Chol	Fbs_	
→ RestI						
Age	81.697419	-0.411995	45.328678	97.787489	0.	
→381614	1.338797					
Sex		0.218368	-0.530107	-4.836994	0.	
	0.010065					
		-0.530107	309.751120	118.573339	1.	
	2.566455					
Chol	97.787489	-4.836994	118.573339	2680.849190	0.	
→ 181496	8.811521					
Fbs	0.381614	0.007967	1.099207	0.181496	0.	
→ 126877	0.024654					
	1.338797	0.010065	2.566455	8.811521	0.	
→024654	0.989968					
		-0.520184	-18.258005	-4.064651	-0.	
	-1.897941					
1 -	0.389220	0.032096	0.535473	1.491345	0.	
	0.039670					
	2.138850	0.055436	3.865638	2.799282	0.	
	0.131850	0.10000	1 000000	0 100500	0	
1 -	0.901034	0.010808	1.273053	-0.129598	0.	
	0.082126	0 040064	1 (2042)	F 70120F	0	
Ca	3.066396	0.040964	1.639436	5.791385	0.	
→ 048394	0.119706					
	MaxHR	ExAng	Oldpeak	Slope	Ca	
Age	-81.423065	_		=	66396	
Sex	-0.520184			0.010808 0.0	40964	
RestBP	-18.258005	0.535473	3.865638	1.273053 1.6	39436	
Chol	-4.064651	1.491345	2.799282 -	-0.129598 5.7	91385	
Fbs	-0.063996	0.004295	0.002377	0.013147 0.0	48394	
RestECG	-1.897941	0.039670	0.131850	0.082126 0.1	19706	
MaxHR	523.265775	-4.063307	-9.112209 -	-5.435501 -5.6	86270	
ExAng	-4.063307	0.220707	0.157216	0.074618 0.0	64162	
Oldpeak	-9.112209	0.157216	1.348095	0.413219 0.3	22753	
Slope	-5.435501	0.074618	0.413219	0.379735 0.0	63747	
Ca	-5.686270	0.064162	0.322753	0.063747 0.8	78791	

4.5 Understand Data With Visualization

A picture is worth a thousand words. You will see the powerful impact of the figures in this section.

- 1. Summary plot of data in figure
 - Summary plot in R

```
# plot of the summary
plot(rawdata)
```

Then you will get Figure Summary plot of the data with R.

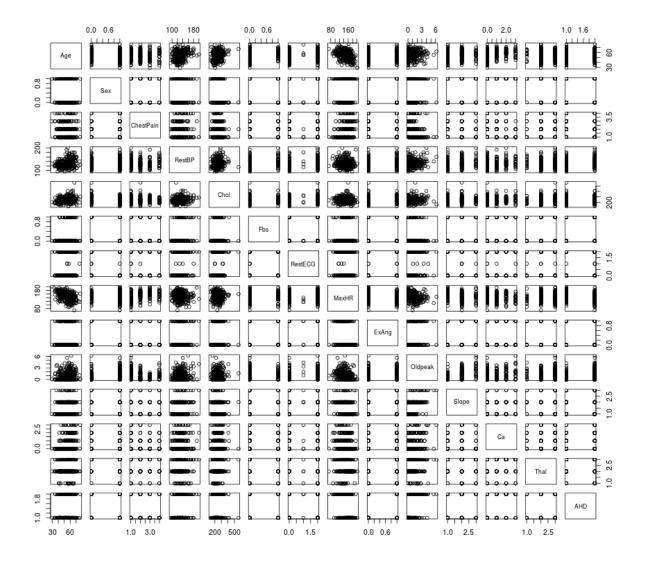


Fig. 1: Summary plot of the data with R.

• Summary plot in **Python**

```
# plot of the summary
plot(rawdata)
```

Then you will get Figure Summary plot of the data with Python.

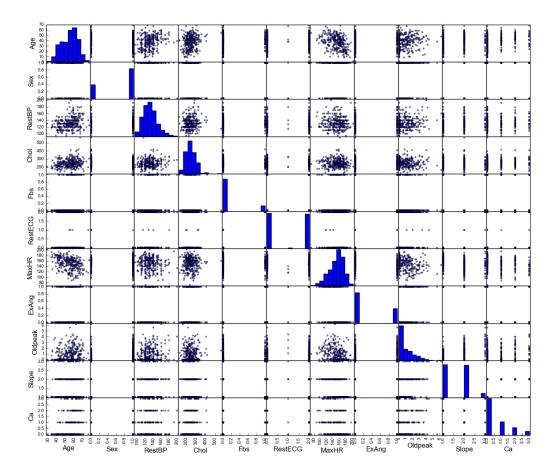


Fig. 2: Summary plot of the data with Python.

2. Histogram of the quantitative predictors

• Histogram in R

```
# Histogram with normal curve plot
dev.off()
Nvars=ncol(numdata)
name=colnames(numdata)
par(mfrow = c (4,3))
for (i in 1:Nvars)
  x<- numdata[,i]</pre>
                                                     (continues on next page)
```

Then you will get Figure *Histogram with normal curve plot in R*.

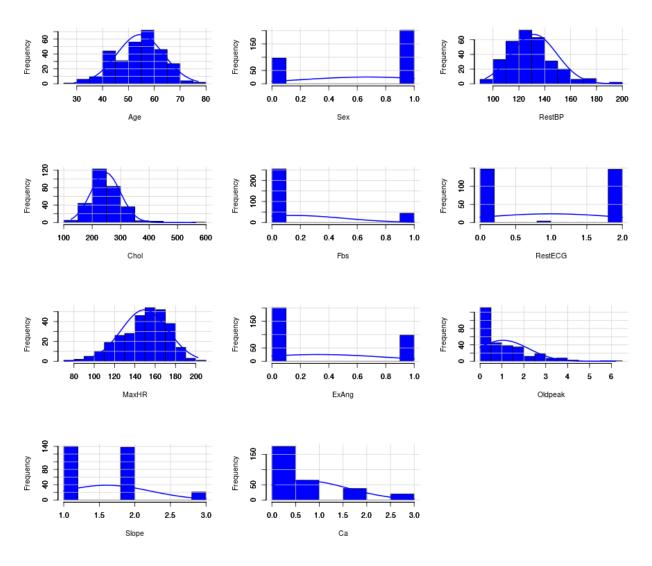


Fig. 3: Histogram with normal curve plot in R.

• Histogram in in **Python**

```
# Histogram
rawdata.hist()
plt.show()
```

Then you will get Figure Histogram in Python.

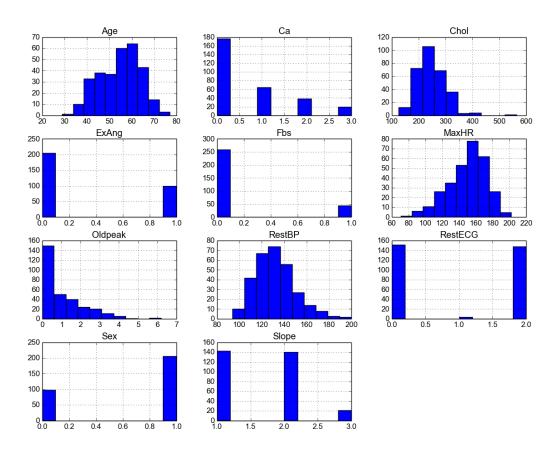


Fig. 4: Histogram in Python.

3. Boxplot of the quantitative predictors

• Boxplot in **R**

continued from previous page)
boxplot(numdata[,i],data=numdata,main=name[i])
}

Then you will get Figure Boxplots in R.

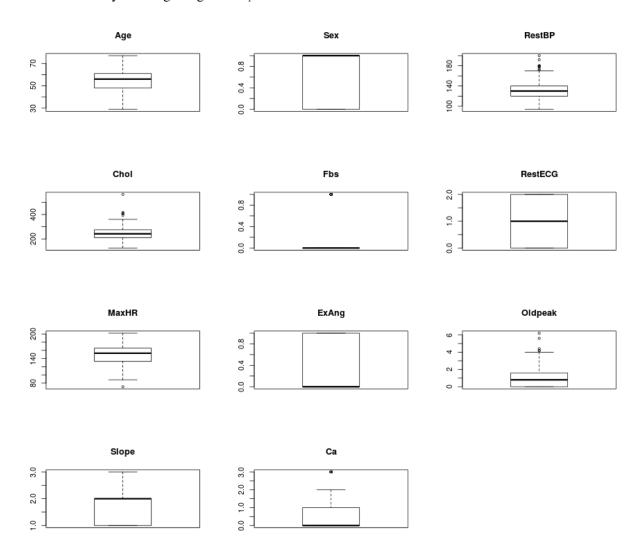


Fig. 5: Boxplots in R.

• Boxplot in Python

```
# boxplot
pd.DataFrame.boxplot(rawdata)
plt.show()
```

Then you will get Figure Histogram in Python.

4. Correlation Matrix plot of the quantitative predictors

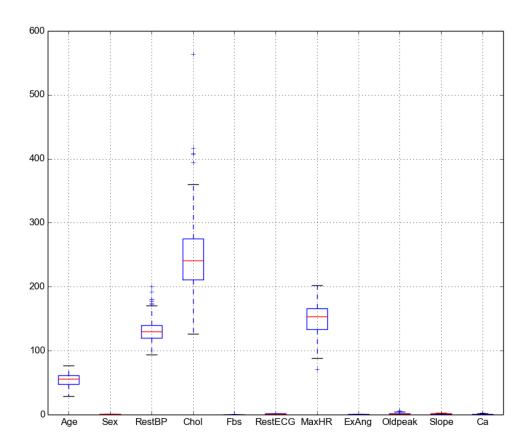


Fig. 6: Histogram in Python.

• Correlation Matrix plot in R

```
dev.off()
# laod cocorrelation Matrix plot lib
library(corrplot)
M <- cor(numdata)
#par(mfrow =c (1,2))
#corrplot(M, method = "square")
corrplot.mixed(M)</pre>
```

Then you will get Figure Correlation Matrix plot in R.

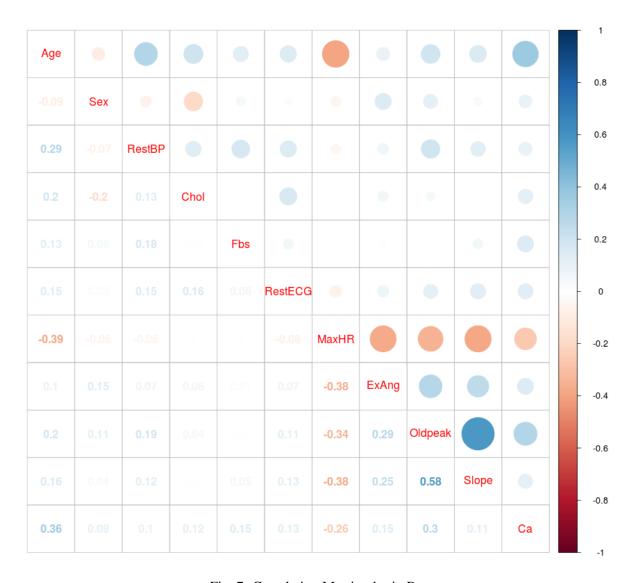


Fig. 7: Correlation Matrix plot in R.

• Correlation Matrix plot in Python

```
# cocorrelation Matrix plot
pd.DataFrame.corr(rawdata)
plt.show()
```

Then you will get get Figure Correlation Matrix plot in Python.

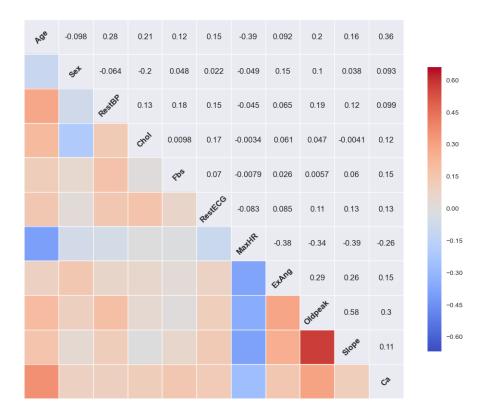


Fig. 8: Correlation Matrix plot in Python.

4.6 Source Code for This Section

The code for this section is available for download for R, for Python,

• R Source code

```
# summary of the data
summary(rawdata)
# plot of the summary
plot (rawdata)
dim(rawdata)
head (rawdata)
tail(rawdata)
colnames(rawdata)
attach (rawdata)
# get numerical data and remove NAN
numdata=na.omit(rawdata[,c(1:2,4:12)])
cor (numdata)
cov (numdata)
dev.off()
# laod cocorrelation Matrix plot lib
library(corrplot)
M <- cor(numdata)</pre>
\#par(mfrow = c (1,2))
#corrplot(M, method = "square")
corrplot.mixed(M)
nrow=nrow(rawdata)
ncol=ncol(rawdata)
c(nrow, ncol)
Nvars=ncol(numdata)
# checking data format
typeof(rawdata)
install.packages("mlbench")
library(mlbench)
sapply(rawdata, class)
dev.off()
name=colnames(numdata)
Nvars=ncol(numdata)
# boxplot
par(mfrow = c (4,3))
for (i in 1:Nvars)
  #boxplot(numdata[,i]~numdata[,Nvars],data=data,main=name[i])
 boxplot(numdata[,i],data=numdata,main=name[i])
}
```

```
# Histogram with normal curve plot
dev.off()
Nvars=ncol(numdata)
name=colnames(numdata)
par(mfrow = c (3, 5))
for (i in 1:Nvars)
 x<- numdata[,i]</pre>
  h<-hist(x, breaks=10, freq=TRUE, col="blue", xlab=name[i], main=
            font.lab=1)
  axis(1, tck=1, col.ticks="light gray")
  axis(1, tck=-0.015, col.ticks="black")
  axis(2, tck=1, col.ticks="light gray", lwd.ticks="1")
  axis(2, tck=-0.015)
  xfit < -seq(min(x), max(x), length=40)
 yfit<-dnorm(xfit, mean=mean(x), sd=sd(x))</pre>
 yfit <- yfit*diff(h$mids[1:2])*length(x)</pre>
  lines(xfit, yfit, col="blue", lwd=2)
library(reshape2)
library(ggplot2)
d \leftarrow melt(diamonds[,-c(2:4)])
ggplot(d, aes(x = value)) +
  facet_wrap(~variable, scales = "free_x") +
  geom_histogram()
```

• Python Source code

```
1 1 1
Created on Apr 25, 2016
test code
@author: Wengiang Feng
import pandas as pd
#import numpy as np
import matplotlib.pyplot as plt
from pandas.tools.plotting import scatter_matrix
from docutils.parsers.rst.directives import path
if __name__ == '__main__':
   path = '~/Dropbox/MachineLearningAlgorithms/python_code/data/
→Heart.csv¹
   rawdata = pd.read_csv(path)
   print "data summary"
    print rawdata.describe()
    # summary plot of the data
    scatter_matrix(rawdata, figsize=[15,15])
```

```
plt.show()
   # Histogram
   rawdata.hist()
   plt.show()
   # boxplot
   pd.DataFrame.boxplot(rawdata)
   plt.show()
   print "Raw data size"
   nrow, ncol = rawdata.shape
   print nrow, ncol
   path = ('/home/feng/Dropbox/MachineLearningAlgorithms/python_
→code/data/'
   'energy_efficiency.xlsx')
   path
   rawdataEnergy= pd.read_excel (path, sheetname=0)
   nrow=rawdata.shape[0] #gives number of row count
   ncol=rawdata.shape[1] #gives number of col count
   print nrow, ncol
   col names = rawdata.columns.tolist()
   print "Column names:"
   print col_names
   print "Data Format:"
   print rawdata.dtypes
   print "\nSample data:"
   print(rawdata.head(6))
   print "\n correlation Matrix"
   print rawdata.corr()
   # cocorrelation Matrix plot
   pd.DataFrame.corr(rawdata)
   plt.show()
   print "\n covariance Matrix"
   print rawdata.cov()
   print rawdata[['Age','Ca']].corr()
   pd.DataFrame.corr(rawdata)
   plt.show()
   # define colors list, to be used to plot survived either red_
\hookrightarrow (=0) or green (=1)
                                                     (continues on next page)
```

```
colors=['red','green']
   # make a scatter plot
   rawdata.info()
   from scipy import stats
   import seaborn as sns # just a conventional alias, don't_
⇒know why
   sns.corrplot(rawdata) # compute and plot the pair-wise_
\hookrightarrow correlations
   # save to file, remove the big white borders
   #plt.savefig('attribute_correlations.png', tight_layout=True)
   plt.show()
   attr = rawdata['Age']
   sns.distplot(attr)
   plt.show()
   sns.distplot(attr, kde=False, fit=stats.gamma);
   plt.show()
   # Two subplots, the axes array is 1-d
   plt.figure(1)
   plt.title('Histogram of Age')
   plt.subplot(211) # 21,1 means first one of 2 rows, 1 col
   sns.distplot(attr)
   plt.subplot(212) # 21,2 means second one of 2 rows, 1 col
   sns.distplot(attr, kde=False, fit=stats.gamma);
   plt.show()
```

FIVE

PRE-PROCESSING PROCEDURES

Note: Well begun is half done – old Chinese proverb

In my opinion, preprocessing is crucial for the data mining algorithms. If you get a good pre-processing, you will definitely get a beeter result. In this section, we will learn how to do a proper pre-processing in $\bf R$ and $\bf Python$.

5.1 Rough Pre-processing

· dealing with missing data

Usually, we have two popular way to deal with the missing data: replacing by 0 or replacing by mean value.

- dealing with missing data in R
- dealing with missing data in Python

5.2 Source Code for This Section

The code for this section is available for download for R, for Python,

· R Source code

```
dim(rawdata)
head(rawdata)
tail(rawdata)
colnames(rawdata)
attach (rawdata)
# get numerical data and remove NAN
numdata=na.omit(rawdata[,c(1:2,4:12)])
cor(numdata)
cov (numdata)
dev.off()
# laod cocorrelation Matrix plot lib
library(corrplot)
M <- cor(numdata)
\#par(mfrow = c (1,2))
#corrplot(M, method = "square")
corrplot.mixed(M)
nrow=nrow(rawdata)
ncol=ncol(rawdata)
c(nrow, ncol)
Nvars=ncol(numdata)
# checking data format
typeof(rawdata)
install.packages("mlbench")
library(mlbench)
sapply(rawdata, class)
dev.off()
name=colnames(numdata)
Nvars=ncol(numdata)
# boxplot
par(mfrow = c (4,3))
for (i in 1:Nvars)
  #boxplot(numdata[,i]~numdata[,Nvars],data=data,main=name[i])
 boxplot(numdata[,i],data=numdata,main=name[i])
# Histogram with normal curve plot
dev.off()
Nvars=ncol(numdata)
name=colnames(numdata)
par(mfrow = c (3,5))
for (i in 1:Nvars)
```

```
x<- numdata[,i]</pre>
  h<-hist(x, breaks=10, freq=TRUE, col="blue", xlab=name[i], main=
\hookrightarrow " ,
             font.lab=1)
  axis(1, tck=1, col.ticks="light gray")
  axis(1, tck=-0.015, col.ticks="black")
  axis(2, tck=1, col.ticks="light gray", lwd.ticks="1")
  axis(2, tck=-0.015)
  xfit < -seq(min(x), max(x), length=40)
 yfit<-dnorm(xfit, mean=mean(x), sd=sd(x))</pre>
  yfit <- yfit*diff(h$mids[1:2])*length(x)</pre>
 lines(xfit, yfit, col="blue", lwd=2)
library(reshape2)
library(ggplot2)
d \leftarrow melt(diamonds[,-c(2:4)])
ggplot(d, aes(x = value)) +
  facet_wrap(~variable, scales = "free_x") +
  geom_histogram()
```

• Python Source code

```
1.1.1
Created on Apr 25, 2016
test code
@author: Wengiang Feng
import pandas as pd
#import numpy as np
import matplotlib.pyplot as plt
from pandas.tools.plotting import scatter_matrix
from docutils.parsers.rst.directives import path
if __name__ == '__main__':
    path ='~/Dropbox/MachineLearningAlgorithms/python_code/data/
→Heart.csv'
   rawdata = pd.read_csv(path)
    print "data summary"
    print rawdata.describe()
    # summary plot of the data
    scatter matrix(rawdata, figsize=[15,15])
    plt.show()
    # Histogram
    rawdata.hist()
    plt.show()
```

```
# boxplot
   pd.DataFrame.boxplot(rawdata)
   plt.show()
   print "Raw data size"
   nrow, ncol = rawdata.shape
   print nrow, ncol
   path = ('/home/feng/Dropbox/MachineLearningAlgorithms/python_
→code/data/'
   'energy_efficiency.xlsx')
   path
   rawdataEnergy= pd.read_excel(path, sheetname=0)
   nrow=rawdata.shape[0] #gives number of row count
   ncol=rawdata.shape[1] #gives number of col count
   print nrow, ncol
   col names = rawdata.columns.tolist()
   print "Column names:"
   print col_names
   print "Data Format:"
   print rawdata.dtypes
   print "\nSample data:"
   print(rawdata.head(6))
   print "\n correlation Matrix"
   print rawdata.corr()
   # cocorrelation Matrix plot
   pd.DataFrame.corr(rawdata)
   plt.show()
   print "\n covariance Matrix"
   print rawdata.cov()
   print rawdata[['Age','Ca']].corr()
   pd.DataFrame.corr(rawdata)
   plt.show()
   # define colors list, to be used to plot survived either red_
\rightarrow (=0) or green (=1)
   colors=['red','green']
   # make a scatter plot
    rawdata.info()
```

```
from scipy import stats
   import seaborn as sns # just a conventional alias, don't...
\rightarrow know why
   sns.corrplot(rawdata) # compute and plot the pair-wise_
→correlations
   # save to file, remove the big white borders
   #plt.savefig('attribute_correlations.png', tight_layout=True)
   plt.show()
   attr = rawdata['Age']
   sns.distplot(attr)
   plt.show()
   sns.distplot(attr, kde=False, fit=stats.gamma);
   plt.show()
   # Two subplots, the axes array is 1-d
   plt.figure(1)
   plt.title('Histogram of Age')
   plt.subplot(211) # 21,1 means first one of 2 rows, 1 col
   sns.distplot(attr)
   plt.subplot(212) # 21,2 means second one of 2 rows, 1 col
   sns.distplot(attr, kde=False, fit=stats.gamma);
   plt.show()
```

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SUMMARY OF DATA MINING ALGORITHMS

Note: Know yourself and know your enemy, and you will never be defeated—idiom, from Sunzi's Art of War

Although the tutorials presented here is not plan to focuse on the theoretical frameworks of Data Mining, it is still worth to understand how they are works and know what's the assumption of those algorithm. This is an important steps to know ourselves.

6.1 Diagram of Data Mining Algorithms

An awesome Tour of Machine Learning Algorithms was published online by Jason Brownlee in 2013, it still is a good category diagram.

6.2 Categories of Data Mining Algorithms

- 0. Dimensionality Reduction Algorithms
- Principal Component Analysis (PCA)
- Nonnegative Matrix Factorization (NMF)
- Independent Component Analysis (ICA)
- Linear Discriminant Analysis (LDA)
- 1. Regression Algorithms
- Ordinary Least Squares Regression (OLSR)
- Linear Regression
- Logistic Regression
- 2. Regularization Algorithms
- Ridge Regression

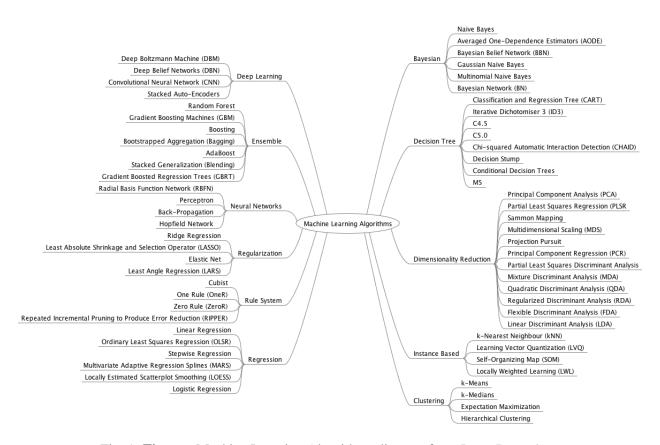


Fig. 1: Figure: Machine Learning Algorithms diagram from Jason Brownlee.

- Least Absolute Shrinkage and Selection Operator (LASSO)
- Elastic Net
- Least-Angle Regression (LARS)
- 3. Decision Tree Algorithms
- Classification and Regression Tree (CART)
- Conditional Decision Trees
- 5. Bayesian Algorithms
- Naive Bayes
- 6. Clustering Algorithms
- k-Means
- k-Medians
- Expectation Maximisation (EM)
- Hierarchical Clustering
- 8. Artificial Neural Network Algorithms
- Perceptron
- Back-Propagation
- Hopfield Network
- Radial Basis Function Network (RBFN)
- 9. Deep Learning Algorithms
- Deep Boltzmann Machine (DBM)
- Deep Belief Networks (DBN)
- 11. Ensemble Algorithms
 - Boosting
 - Bootstrapped Aggregation (Bagging)
 - AdaBoost
 - Gradient Boosting Machines (GBM)
 - Gradient Boosted Regression Trees (GBRT)
 - · Random Forest



DIMENSION REDUCTION ALGORITHMS

7.1 What is dimension reduction?

In machine learning and statistics, dimensionality reduction or dimension reduction is the process of reducing the number of random variables under consideration, via obtaining a set "uncorrelated" principle variables. It can be divided into feature selection and feature extraction. https://en.wikipedia.org/wiki/Dimensionality_reduction

7.2 Singular Value Decomposition (SVD)

At here, I will recall the three types of the SVD method, since some authors confused the definitions of these SVD method. SVD method is important for the dimension reduction algorithms, such as Truncated Singular Value Decomposition (tSVD) can be used to do the dimension reduction directly, and the Full Rank Singular Value Decomposition (SVD) can be applied to do Principal Component Analysis (PCA), since PCA is a specific case of SVD.

1. Full Rank Singular Value Decomposition (SVD)

Suppose $\mathbf{X} \in \mathbb{R}^{n \times p}$, (p < n), then

$$\mathbf{X}_{n \times p} = \mathbf{U}_{n \times n} \mathbf{\Sigma}_{n \times p} \mathbf{V}^{T},$$

is called a full rank SVD of X and

- σ_i Sigular calues and $\Sigma = diag(\sigma_1, \sigma_2, \cdots, \sigma_p) \in \mathbb{R}^{n \times p}$
- u_i left singular vectors, $\mathbf{U} = [u_1, u_2, \cdots, u_n]$ and \mathbf{U} is unitary.
- v_i -right singular vectors, $\mathbf{V} = [v_1, v_2, \cdots, v_p]$ and \mathbf{V} is unitary.

2. Reduced Singular Value Decomposition (rSVD)

Suppose $\mathbf{X} \in \mathbb{R}^{n \times p}$, (n < p), then

$$\mathbf{X}_{n \times p} = \mathbf{\hat{U}}_{n \times p} \mathbf{\hat{\Sigma}}_{p \times p} \mathbf{\hat{V}}^{T},$$

is called a Reduced Singular Value Decomposition **rSVD** of **X** and

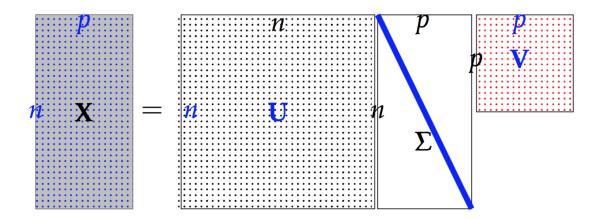


Fig. 1: Singular Value Decomposition

- σ_i Sigular calues and $\hat{\Sigma} = diag(\sigma_1, \sigma_2, \cdots, \sigma_p) \in \mathbb{R}^{p \times p}$
- u_i left singular vectors, $\hat{\mathbf{U}} = [u_1, u_2, \cdots, u_p]$ is column-orthonormal matrix.
- v_i right singular vectors, $\hat{\mathbf{V}} = [v_1, v_2, \cdots, v_p]$ is column-orthonormal matrix.

3. Truncated Singular Value Decomposition (tSVD)

Suppose $\mathbf{X} \in \mathbb{R}^{n \times p}$, (r < p), then

$$\mathbf{X}_{n \times p} = \mathbf{\hat{U}}_{n \times r} \mathbf{\hat{\Sigma}}_{r \times r} \mathbf{\hat{V}}^{T}, \tag{7.1}$$

is called a Truncated Singular Value Decomposition tSVD of X and

- σ_i Sigular calues and $\hat{\Sigma} = diag(\sigma_1, \sigma_2, \cdots, \sigma_r) \in \mathbb{R}^{r \times r}$
- u_i left singular vectors, $\hat{\mathbf{U}} = [u_1, u_2, \cdots, u_r]$ is column-orthonormal matrix.
- v_i right singular vectors, $\hat{\mathbf{V}} = [v_1, v_2, \cdots, v_p]$ is column-orthonormal matrix.

Figure *Truncated Singular Value Decomposition* indictes that the dimension of $\hat{\mathbf{U}}$ is smaller than \mathbf{X} . We can use this property to do the dimension reduction. But, usually, we will use SVD to compute the Principal Components. We will learn more details in next section.

7.3 Principal Component Analysis (PCA)

Usually, there are two ways to implement the PCA. Principal Component Analysis (PCA) is a specific case of SVD.

$$\mathbf{X}_{n \times p} = \hat{\mathbf{U}} \tag{7.2}$$

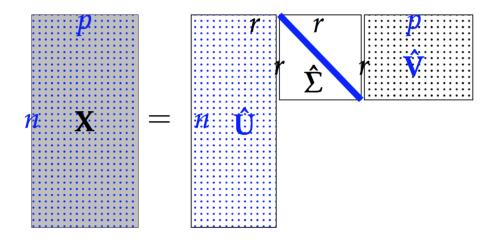


Fig. 2: Truncated Singular Value Decomposition

7.4 Independent Component Analysis (ICA)

7.5 Nonnegative matrix factorization (NMF)

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EIGHT

REGRESSION ALGORITHM

- 8.1 Ordinary Least Squares Regression (OLSR)
- 8.2 Linear Regression (LR)
- 8.3 Logistic Regression (logR)

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NINE

CLASSIFICATION ALGORITHMS

- 9.1 Logistic Regression (LR)
- 9.2 k-Nearest Neighbour (kNN)
- 9.3 Linear Discriminant Analysis (LDA)
- 9.4 Quadratic Discriminant Analysis (QDA)

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TEN

REGULARIZATION ALGORITHMS

- 10.1 Subset Selection (SubS)
- 10.2 Ridge Regression (Ridge)
- 10.3 Least Absolute Shrinkage and Selection Operator (IASSO)

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СНАРТ	ER
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RESAMPLING ALGORITHMS

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