

Instructor: Wenqiang Feng

Name: _____ solutions _____

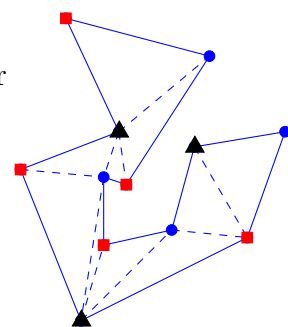
Using what you have learned answer the following questions. Show all work if you want partial credit. If a specific method is mentioned, make sure you show that you are using that method.

- (1) (6 points) Suppose the gallery has following polygon shape. To guard the gallery when it is closed, you need some surveillance system.
- How many cameras (cameras that can capture video at 360 degrees angle) need to be installed to cover all of your gallery?
 - Could you use 3-coloring of the vertices of a triangulated polygon to give the position of the cameras ?

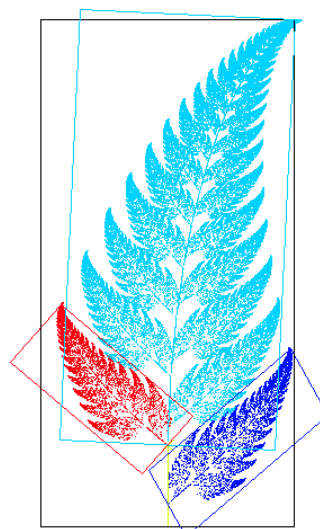
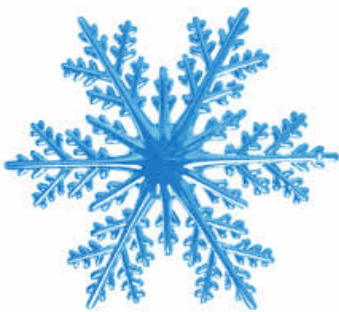
Solution. From the Art Gallery Theorem, we get the upper bounded of the number is

$$N_{\max} = \begin{cases} \frac{V}{3} & \text{if the quotient is integer} \\ \text{round}\left(\frac{V}{3}\right) & \text{if the quotient is not integer} \end{cases}$$

So, the $n_{\max} = \frac{12}{3} = 4$. But we only need 3 cameras to cover all of the gallery (see 3-coloring of the vertices of a triangulated polygon).



- (2) (4 points) Please write down the corresponding type of the symmetry?



1: _____ reflection _____ 2: _____ reflection or rotation _____ 3: _____ scaling _____

- (3) (Bonus 2 points) Please write down the details of how to derive the value of Golden Ratio. (mathematical formula and solving process.)

Solution.

$$\phi = 1 + \frac{1}{\phi} \rightarrow \phi^2 - \phi - 1 = 0$$

$$\phi = \frac{1 \pm \sqrt{5}}{2} (\phi > 0)$$

$$\phi = \frac{1 + \sqrt{5}}{2}$$