

Homework 1

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1 Exercises 1.1 - 5

Algorithm 1 Finding common elements in two sorted lists

Input: An array $A_1[0..m-1]$ for m sorted numbers;

Another sorted array $A_2[0..n-1]$ with n numbers;

Output: Ensemble of classifiers on the current batch, A_c ;

```
1:  $i \leftarrow 0$ 
2: while  $(i < m) \text{ and } (j < n)$  do
3:   if  $A_1[i] == A_2[j]$  then
4:      $\text{print } A[i]$ 
5:      $i \leftarrow i + 1$ 
6:      $j \leftarrow j + 1$ 
7:   else if  $A_1[i] > A_2[j]$  then
8:      $j \leftarrow j + 1$ 
9:   else
10:     $i \leftarrow i + 1$ 
11:   end if
12: end while
```

2 Exercises 1.1 - 6

a.

$m = 31415, n = 14142$

Step 1: $r = 31415 \bmod 14142 = 3131, m \leftarrow 14142, n \leftarrow 3131$

Step 2: $r = 14142 \bmod 3131 = 1618, m \leftarrow 3131, n \leftarrow 1618$

Step 3: $r = 3131 \bmod 1618 = 1513, m \leftarrow 1618, n \leftarrow 1513$

Step 4: $r = 1618 \bmod 1513 = 105, m \leftarrow 1513, n \leftarrow 105$

Step 5: $r = 1513 \bmod 105 = 43, m \leftarrow 105, n \leftarrow 43$

Step 6: $r = 105 \bmod 43 = 19, m \leftarrow 43, n \leftarrow 19$

Step 7: $r = 43 \bmod 19 = 5, m \leftarrow 19, n \leftarrow 5$

Step 8: $r = 19 \bmod 5 = 4, m \leftarrow 5, n \leftarrow 4$

Step 9: $r = 5 \bmod 4 = 1, m \leftarrow 4, n \leftarrow 1$

Step 10: $r = 4 \bmod 1 = 0, m \leftarrow 1, n \leftarrow 0$

Step 11: return 1

b.

Using consecutive integer checking algorithm, every time the value of t is decreased, it takes two divisions. There are 28284 divisions in total.

Using Euclid's algorithm, there are 10 divisions.

Euclid's algorithm is $28284/10 = 2828.4$ times faster in terms of divisions.

3 Exercises 1.1 - 7

Prove the equality $\gcd(m, n) = \gcd(n, m \bmod n)$ for every pair of positive integers m and n .

4 Exercises 1.2 - 4

Algorithm 2 finding real roots

Input: arbitrary real coefficients a , b , and c

```
1:  $d \leftarrow b^2 - 4 * a * c$ 
2: if  $d < 0$  then
3:   return false
4: else if  $d = 0$  then
5:    $x_1 \leftarrow (-b + \text{sqrt}(d)) / (2 * a)$ 
6:   return  $x_1$ 
7: else if  $d > 0$  then
8:    $x_1 \leftarrow (-b + \text{sqrt}(d)) / (2 * a)$ 
9:    $x_2 \leftarrow (-b - \text{sqrt}(d)) / (2 * a)$ 
10:  return  $x_1, x_2$ 
11: end if
```

5 Exercises 1.2 - 9

6 Exercises 1.3 - 1