

Attention-Driven Sentiment and the Business Cycle

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The views expressed do not necessarily reflect the views of the Federal Reserve Bank of Chicago or the Federal Reserve System.

Motivation

Expectations Matter

- Economic decisions are based on agents' perceptions and expectations
- Yet, the expectation formation process is still not fully understood
- Surveys of consumer beliefs reveal many puzzling features relative to FIRE

This Paper

- Document new facts about consumer beliefs: single factor, stagflationary beliefs
- Develop a TANK model with rational inattention to explain these facts and assess aggregate implications
- Provide evidence for the model's mechanism: attention-based, supply-side views

Preview: Single Factor Model and Stagflationary Beliefs

Single Factor Model

- Use survey data to show consumer beliefs are well-described by a single factor
- This factor behaves like sentiment where “optimistic” consumers forecast typical expansionary outcomes:
 - Falling unemployment and improving business conditions
 - Improving personal financial conditions
 - Forward- and backward-looking beliefs

Stagflationary Beliefs

- Lower “sentiment” is associated with higher inflation expectations
- ⇒ The positive correlation in inflation and unemployment expectations are a reflection of the broader single factor phenomena (Kamdar 2019; C�dia et al 2024)

Preview: TANK Model

Model Overview

- We develop a TANK model where rationally inattentive consumers face fundamental uncertainty about demand and supply shocks
- Optimal information-gathering economizes on information costs and compresses the dimensionality of consumer beliefs
- We derive conditions under which households relying on labor income
 - Optimally devote more attention to supply shocks
 - Thus, inflation is perceived as countercyclical

Dynamics

- HtM agents \Rightarrow aggregate consumption reacts more to demand shocks than in RANK
- Inattention \Rightarrow inattentive agent decisions underreact relative to full-information
- However, when inattentive hand-to-mouth agents make active decisions about labor supply, consumption can overreact to demand shocks \implies additional amplification

Preview: Tests of the Model Mechanism

Test the key model mechanism: attention-based supply-side view of the economy

Attention

- More “inattentive” consumers have a more stagflationary view

Supply-Side Reasoning

- Consumers who give supply-side explanations for their beliefs have a more stagflationary view

Sentiment Response to Shocks

- In local projections, beliefs reacts to supply shocks but not demand shocks

Single Factor, Stagflationary Beliefs

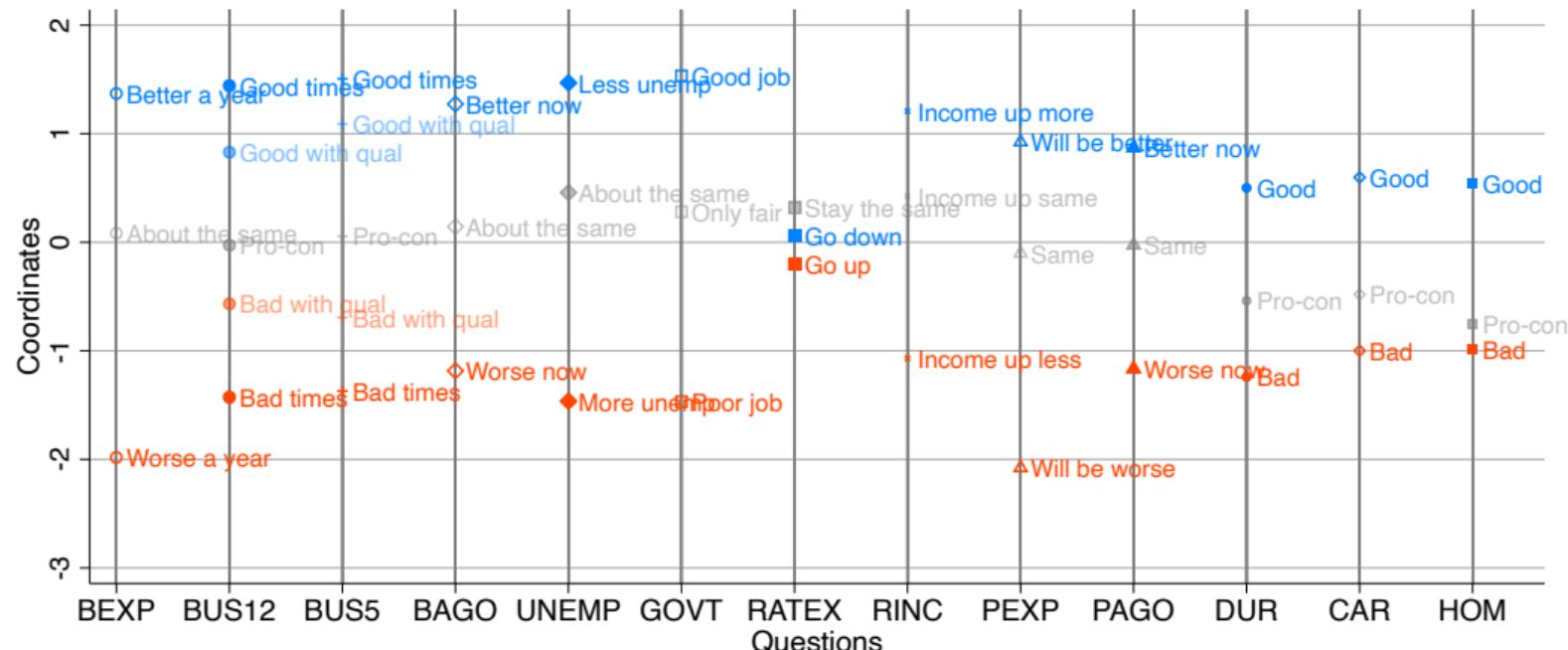
Survey Data

Michigan Survey of Consumers (MSC)

- Monthly, consumer survey of ≈ 500 (1978-present)
- Rotating panel (up to 2x)
- Questions about aggregate and personal economic conditions (forward- and backward-looking)
- Most questions have categorical answers
 - Inflation expectations and a few others are numerical
- Results are similar using the NY Fed Survey of Consumer Expectations

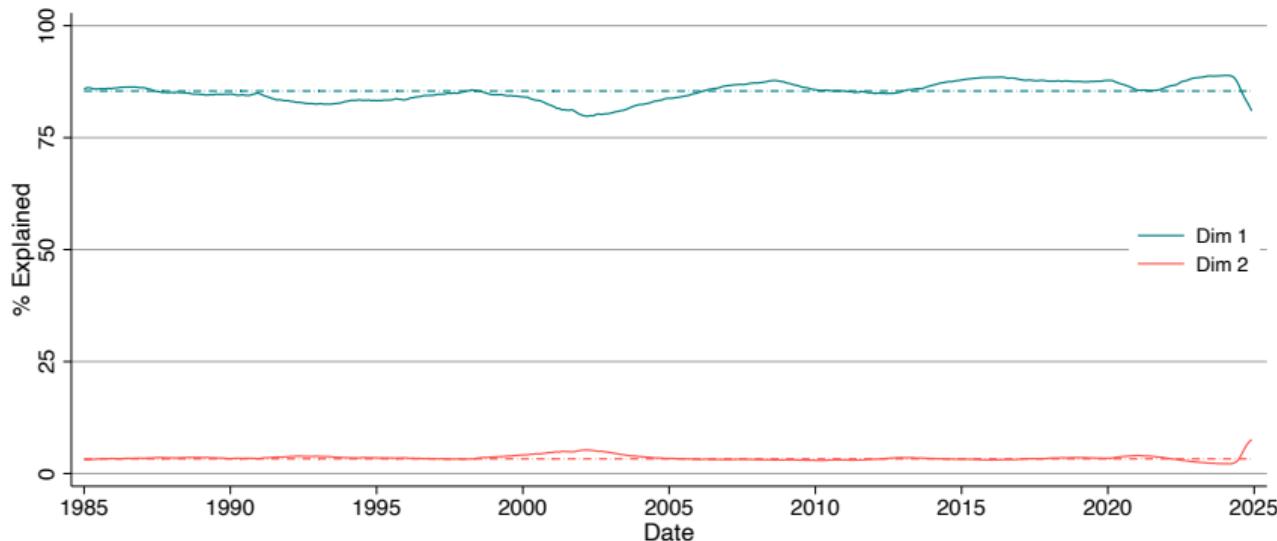
Consumers: MCA Estimated Loadings of First Component

- Baseline MCA: include all categorical questions asked continuously since 1980
- Responses associated with more traditionally “optimistic” outlooks have high and positive loadings (blue); and “pessimistic” responses have negative loadings (red)



Consumers: One-Factor Belief Structure

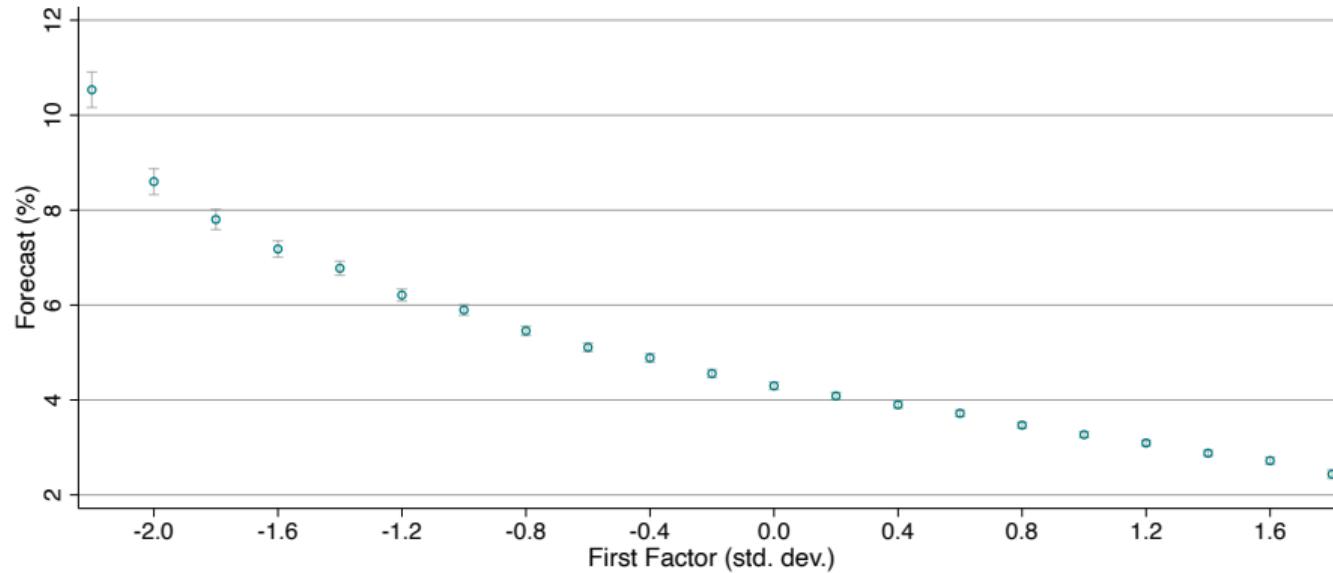
- The first component (sentiment) explains over 80% of the variation (dashed line)
- This is also true if we use rolling window MCAs (solid line)



- Estimating the MCA on demographic subgroups yields similar results in terms of (i) fraction explained and (ii) the correlation with our baseline MCA

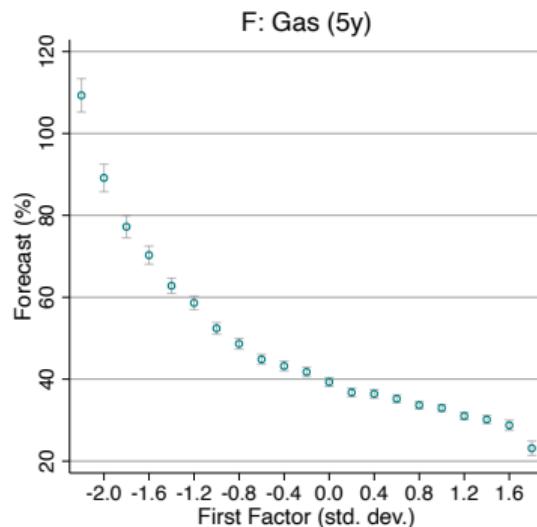
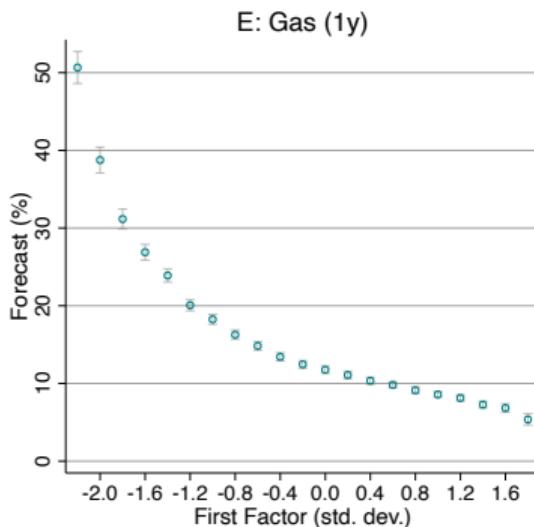
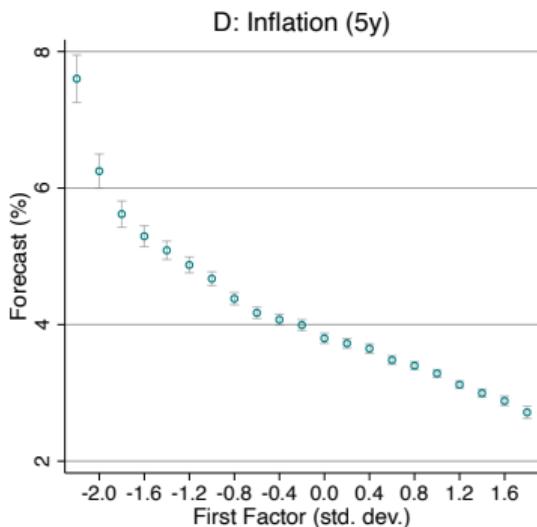
Stagflationary Beliefs: Short-Run Inflation

- The first factor (sentiment) is predictive of expected inflation
- Optimistic consumers have lower $E_{i,t}[\pi_{t+12}]$ (and vice versa) \Rightarrow stagflationary beliefs



Stagflationary Beliefs: Long-Run Inflation and Gas Price Inflation

- Optimistic consumers have lower long-run inflation expectations, and lower gas price expectations (short and long horizons) \Rightarrow stagflationary beliefs



Stagflationary Beliefs: Robustness

- We find stagflationary beliefs **across demographic groups**
 - Education, income, investments, political affiliation
- We find stagflationary beliefs **across time**
- Alternative approach: include inflation expectations into the MCA
 - The first dimension still explains over 80% of beliefs
 - The estimated loading on inflation is negative: higher sentiment, lower inflation expectations
- Professional forecasters have a larger factor structure to their beliefs and do not have stagflationary views

Model

Model: Overview

Questions:

- Under what conditions do agents form beliefs consistent with empirics?
- What are the aggregate implications?

Model:

- Firms: differentiated firms face pricing frictions and produce using labor
- Households: some have access to financial markets (“capitalists”); others do not and consume all income each period (“hand-to-mouth”) (Bilbiie, 2020)
- Innovation: add rational inattention to hand-to-mouth households (Sims, 2003)
- Shocks: aggregate discount rate (“demand”) and labor disutility shock (“supply”)

Households: Capitalists

- Capitalist households, $j \in (\lambda, 1]$, are denoted with " \mathcal{K} "
- They maximize lifetime discounted expected utility:

$$\mathbb{E}_0 \sum_{t=0}^{\infty} \beta^t u(C_t^{\mathcal{K}}, N_t^{\mathcal{K}}; \mathbf{Z}_t)$$

subject to:

$$C_t^{\mathcal{K}} + Q_t B_t^{\mathcal{K}} = B_{t-1}^{\mathcal{K}} + W_t N_t^{\mathcal{K}} + T_t^{\mathcal{K}}$$

- **Standard:** FIRE; choose consumption, labor, saving to max lifetime expected utility
- Note \mathbf{Z}_t contains aggregate shocks (discount factor Ψ_t and labor disutility Γ_t)

$$u(C_t^j, N_t^j; \mathbf{Z}_t) = \Psi_t \left[\frac{(C_t^j)^{1-\varsigma} - 1}{1-\varsigma} - \Gamma_t \frac{(N_t^j)^{1+\varphi}}{1+\varphi} \right]$$

Model: Firms

- Firms maximize discounted expected profits:

$$\mathbb{E}_t \sum_{k=0}^{\infty} \theta^k Q_{t,t+k}^{\mathcal{K}} \left[(1 + \tau^{\mathcal{K}}) (P_t(i)/P_{t+k}) Y_{t+k}(i) - W_{t+k} N_{t+k}(i) - T_{t+k}^F \right]$$

- subject to:
 - **Production function:** $Y_t(i) = N_t(i)$
 - **CES Demand:** $C_t(i) = \left(\frac{P_t(i)}{P_t} \right)^{-\epsilon} C_t$
- **Standard:** Calvo, CES demand, monopolistically competitive firms, production subsidy
- **Non-standard:** Firms are owned by \mathcal{K} households \Rightarrow SDF is of \mathcal{K} households and expectations are taken under FIRE

Model: Government

- Fiscal authority sets optimal production subsidy \Rightarrow markups are zero in steady state
- The production subsidy is financed by lump-sum taxes on firms
- Profits paid to \mathcal{K} households are taxed (τ^D) and redistributed to H households
- Central bank sets the nominal rate i_t

Households: Hand-to-Mouth

- Hand-to-mouth households, $j \in [0, \lambda]$, are denoted with “H”
- H households cannot borrow or save
- Face **information constraints and do not observe current or past variables** perfectly
- Collect noisy signals s_t^j (more precise signals are more costly); expectations are formed with respect to the information set (the history of signals)

$$\left\{ s_{\tau}^j \right\}_{\tau \leq t} \equiv \mathcal{I}_t^j$$

- Denote the expectation operator of household j as $E_t^j \neq \mathbb{E}_t$

Households: Hand-to-Mouth Maximization

- Budget constraint:

$$C_t^{H,j} = W_t N_t^{H,j} + T_t^H$$

- How can this bind?
 - We assume there is a head of household that collects information, tells the worker how much to work, then the shopper takes the wage income and consumes
 - Labor is the active choice and consumption is the residual
- H households maximize:

$$E_t^j U(N_t^{H,j}; \mathbf{x}_t) - \mu l(\mathbf{x}_t; \mathcal{I}_t^j | \mathcal{I}_{t-1}^j)$$

by choosing the distribution of signals \mathbf{s}_t^j and labor supply $N_t^{H,j}$, taking \mathcal{I}_{t-1}^j as given

- \mathbf{x}_t contains Z_t and anything affecting W_t and T_t^H

Model: Aggregation, Linearization, Optimality

- Average consumption and labor supply of the H households:

$$C_t^H \equiv \frac{1}{\lambda} \int_0^\lambda C_t^{H,j} dj \text{ and } N_t^H \equiv \frac{1}{\lambda} \int_0^\lambda N_t^{H,j} dj$$

- Aggregate consumption and labor supply (log-linearized around symmetric ss):

$$y_t = \lambda c_t^H + (1 - \lambda) c_t^K \text{ and } n_t = \lambda n_t^H + (1 - \lambda) n_t^K$$

- Capitalist household optimality conditions:

$$w_t = \gamma_t + \varsigma c_t^K + \varphi n_t^K \text{ and } \mathbb{E}_t \Delta c_{t+1}^K = \varsigma^{-1} (i_t - \mathbb{E}_t \pi_{t+1} - v_t)$$

- $\gamma_t = \log \Gamma_t$ is the aggregate labor disutility shock
- $v_t = -\mathbb{E}_t \Delta \psi_{t+1} = -\mathbb{E}_t \Delta \log \Psi_{t+1}$ is the aggregate discount factor shock
- New Keynesian Phillips curve:

$$\pi_t = \kappa_w w_t + \beta \mathbb{E}_t \pi_{t+1}$$

Model: FIRE Benchmark

- Under full information (like in Bilbiie, 2020):

$$(\varsigma + \varphi)n_t^{H*} = \chi_n w_t - \gamma_t \quad \text{and} \quad (\varsigma + \varphi)c_t^{H*} = \chi_c w_t - \gamma_t$$

where $\chi_n \equiv 1 - \varsigma (1 - \tau^D / \lambda)$ and $\chi_c \equiv 1 + \varphi (1 - \tau^D / \lambda)$

- Optimal labor choice responds to the wage (w_t)
 - χ_n is proportional to the elasticity of labor supply to the wage
 - χ_n is a function of preferences (ς), transfers (τ^D), and share of H households (λ)
- Optimal labor choice also responds to the labor disutility shock (γ_t)
- With information frictions, H households are unable to pick n_t^{H*} perfectly
 - Nor will the average across H households be the FIRE benchmark

Model: Equilibrium

- H labor supply:

$$\begin{aligned} n_t^{H,j} &= K \left(\frac{\chi_n w_t - \gamma_t}{\varsigma + \varphi} + \eta_t^j \right) + (1 - K) \tilde{n}_t^{H,j} \\ \implies n_t^H &= K \left(\frac{\chi_n w_t - \gamma_t}{\varsigma + \varphi} \right) + (1 - K) m_t \text{ where } m_t \equiv \frac{1}{\lambda} \int_0^\lambda \tilde{n}_t^{H,j} dj \end{aligned}$$

- Aggregate priors, m_t , is a state variable
- The optimal signal will put nonzero weight on $m_t \implies$ “infinite regress” and AR(∞) aggregate dynamics
- We have some general results about beliefs and dynamics in the paper
- One takeaway: H households will have a single factor belief structure
 - H households make one choice \implies at most one signal

IID Setting: Aggregate Labor Choice

- Suppose shocks are IID
- Priors are at steady state, so H aggregate labor choice:

$$n_t^H = Kn_t^{H,*} \propto K(\chi_n w_t - \gamma_t)$$

where

- $n_t^{H,*}$ is the H aggregate labor choice under the FIRE bench
- K is the Kalman gain
- w_t , the real wage, is function of both demand and supply shocks
- γ_t is the supply shock
- χ_n is proportional to the FIRE elasticity of labor supply to wage (endogenous)

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Correlations: Physical and Beliefs

- Under what conditions...
 1. is the (unconditional) correlation of output and inflation positive
 2. while posterior beliefs feature negative correlation?
- First holds if demand shocks are sufficiently volatile and/or the response of output and inflation to demand shocks is sufficiently strong

Correlations: Physical and Beliefs

- Under what conditions...
 1. is the (unconditional) correlation of output and inflation positive
 2. while posterior beliefs feature negative correlation?
- First holds if demand shocks are sufficiently volatile and/or the response of output and inflation to demand shocks is sufficiently strong
- For the second, belief correlations depend crucially on χ_n
- If $\chi_n = 0$ (log-utility and no transfers), then optimal labor choice...
 - is independent of the real wage due to offsetting income and substitution effects
 - is only a function of supply shocks, and so H households choose to only learn about supply shocks (regardless of their volatility)
 - \Rightarrow Posterior beliefs inherit the properties of the model conditional on supply shocks

Correlations: Physical and Beliefs

- If $\chi_n \neq 0$, posterior beliefs of output and inflation can be negatively or positively correlated (exact conditions are in the paper)
- How would the belief correlation be positive? If $|\chi_n|$ large and volatility of supply shocks is small:
 - The optimal signal will place weight on the real wage which will be largely driven by demand rather than supply shocks
 - Posterior beliefs will inherit the conditional response of the model to demand shocks, resulting in a positive correlation in beliefs
- Under reasonable parameters: supply shocks are not very volatile and χ_n is small \Rightarrow output and inflation will be positively correlated, while beliefs will feature a negative correlation

Dynamics: Analytical Second Derivatives and Intuition, Demand

- In TANK, demand shocks are amplified if $\chi_n \leq 1$ (Bilbiie, 2020)
- In limit of no H agents ($\lambda \rightarrow 0$) and no information costs ($K \rightarrow 1$), conditional responses wrt the fraction of hand-to-mouth (λ) and information costs ($-K$) are:

$$\lim -\frac{\partial^2 C_{y,v}}{\partial \lambda \partial K} = \begin{cases} > 0 & \text{if } \chi_n < 0 \\ < 0 & \text{if } 0 < \chi_n \leq 1 \end{cases}$$

where $C_{y,v}$ is the response of output to a demand shock

- In response to a **demand shock**, in the FIRE-RANK limit, output and **wage ↑**
 - If $\chi_n < 0$, H households want to ↓ labor, due to info costs will not reduce labor as much as FIRE \implies TANK amplifies demand shocks, and info costs add further amplification
 - If $0 < \chi_n \leq 1$, H households want to ↑ labor, due to info costs will not increase labor as much as FIRE \implies TANK amplifies demand shocks, but info costs weaken it

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Dynamics: Analytical Second Derivatives and Intuition, Supply

- In TANK, supply shocks are mitigated if $\chi_n \leq 1$ (Bilbiie, 2020)
- In limit of no H agents ($\lambda \rightarrow 0$) and no information costs ($K \rightarrow 1$), conditional responses wrt the fraction of hand-to-mouth (λ) and information costs ($-K$) are:

$$\lim -\frac{\partial^2 C_{y,\gamma}}{\partial \lambda \partial K} > 0$$

where $C_{y,\gamma}$ is the response of output to a supply shock

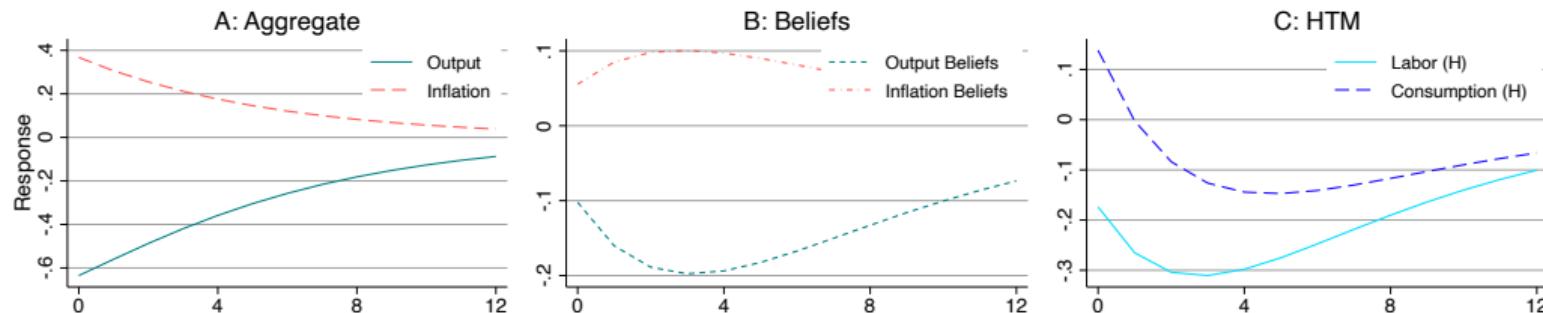
- In response to a **supply shock**, if the central bank is responding to strongly to inflation, wages will not move much and H choices will be driven by γ_t
 - H households will ↓ labor, but due to info costs by less than under FIRE \implies info costs dampen reaction to supply shocks (more mitigation relative to TANK)

Dynamics: Persistent Shocks

- Shocks follow AR(1) processes
- Assume $\chi_n = 0$ (log utility and no transfers)
 - Work in progress: $\chi_n \neq 0$. Implies AR(∞) dynamics, but main results go through
- In response to supply and demand shocks, assess how
 1. the beliefs of HtM households evolve
 2. the labor and consumption decisions of HtM households evolve
 3. macroeconomic dynamics
- Assess the importance of priors, by assuming households ex-ante believe a supply-driven recession is likely
- Calibration

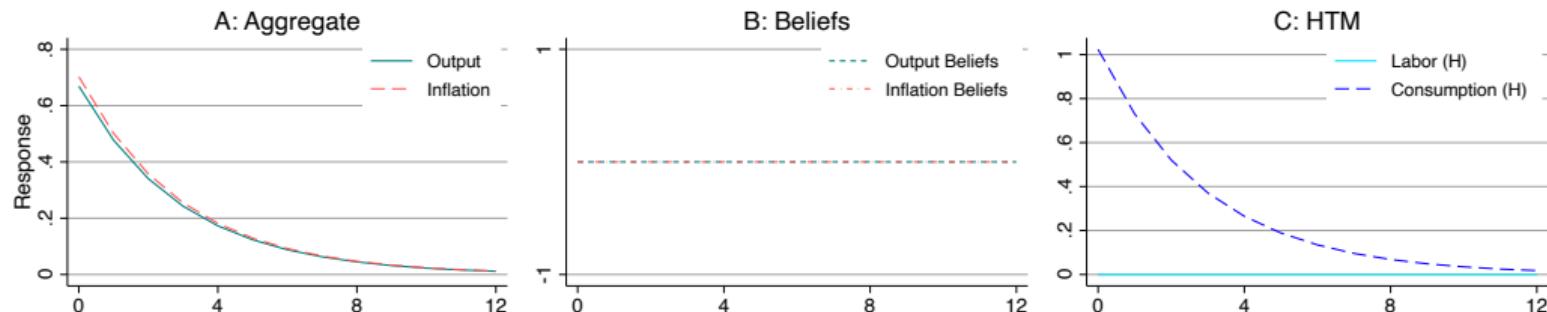
Response: Supply Shock

- In response to a supply shock, inflation rises and output falls
- H households learn about supply, their inflation beliefs rise and output beliefs fall
- H labor supply falls, but less than in FIRE, and consumption rises



Response: Demand Shock

- In response to a demand shock, **inflation and output rise**
- **H** households do not learn about demand and their beliefs are unaffected
- **H** labor supply is unaffected, but consumption rises



Tests of the Model

Qualitative Testable Implications

Is there empirical support for attention-based supply-side views?

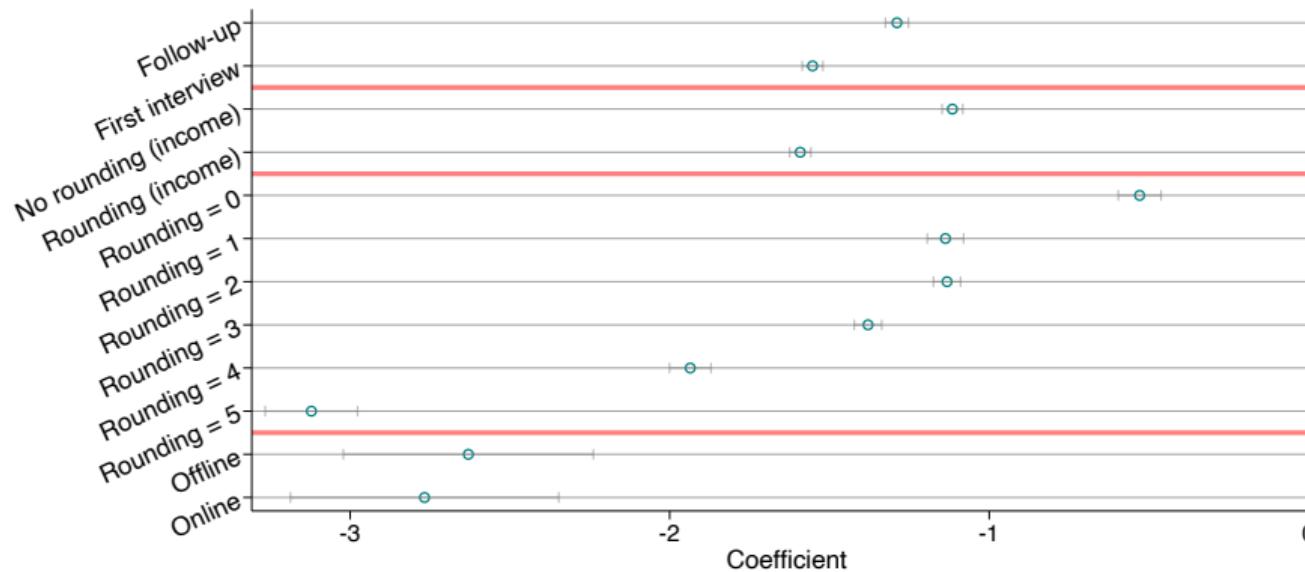
Predictions

- Less attentive households hold more stagflationary beliefs
- Respondents giving supply-based reasoning hold more stagflationary beliefs
- Sentiment responds to supply but not demand shocks
- ⇒ Results rule out other stories for supply-side beliefs

Attention and Stagflationary Views

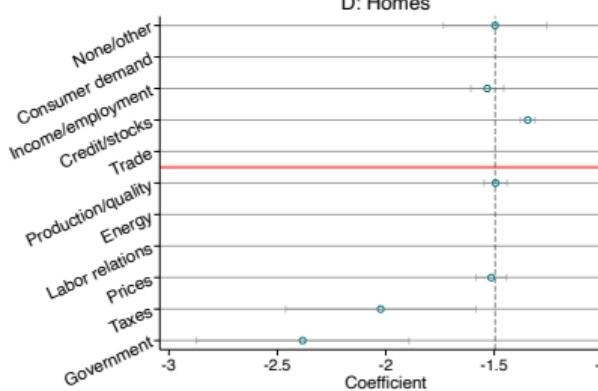
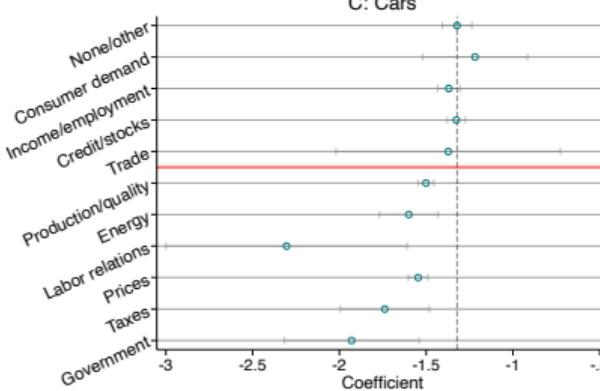
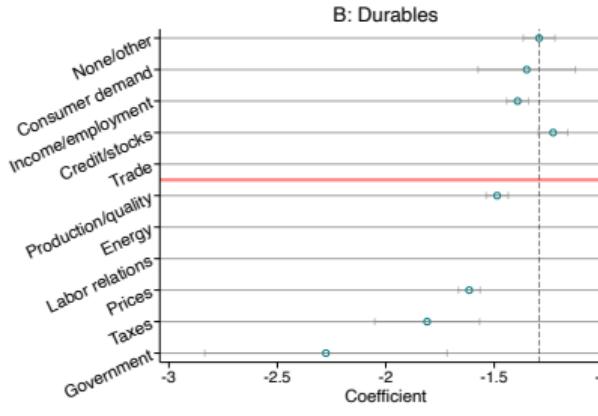
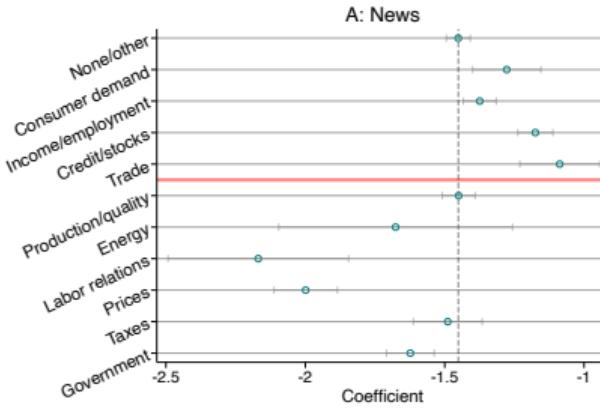
- Less attention \implies more stagflationary views

$$E_{i,t}[\pi_{t+12}] = \sum_{j \in \mathcal{J}} \beta^j \hat{f}_{i,t} \times \mathbb{1}\{a_{i,t} = j\} + X_{i,t} + \epsilon_{i,t}$$



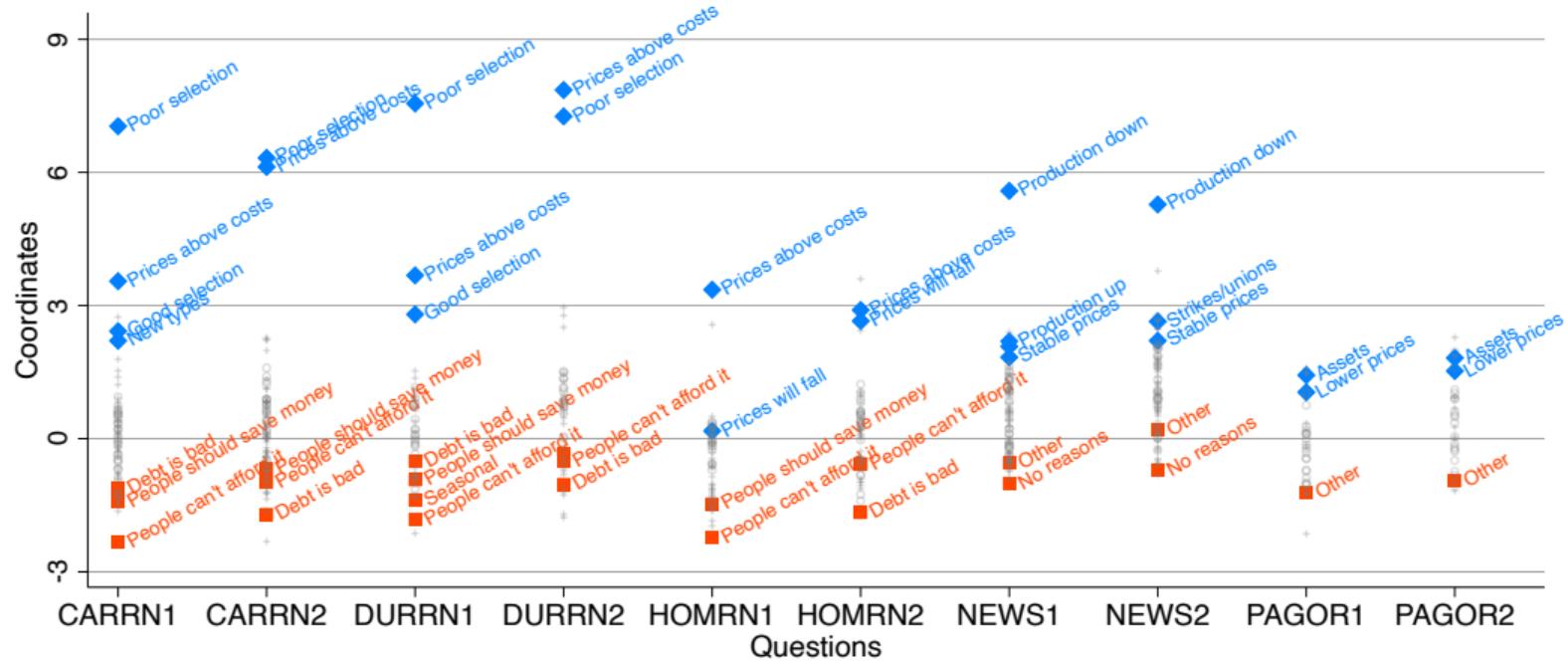
Supply-Side Reasoning and Stagflationary Views

- More “supply” reasoning \implies more stagflationary views



Reasoning in an MCA

- Include the raw reasoning categories (≈ 575) in the MCA
- First factor is essentially the same as our baseline sentiment factor
- The second factor appears to be a measure of supply-side beliefs



Supply-Side Reasoning

- We calculate the fitted second component, \hat{r}_i, t
- If individuals mention supply-side reasoning, they have more stagflationary beliefs

	(1)	(2)	(3)	(4)
$\hat{f}_{i,t}$	-1.404*** (0.013)	-0.737*** (0.012)	-6.941*** (0.081)	-14.107*** (0.173)
$\hat{f}_{i,t} \times \hat{r}_{i,t}$	-0.088*** (0.013)	-0.018* (0.011)	-1.492*** (0.081)	-1.513*** (0.168)
R-sq	0.142	0.092	0.143	0.134
Obs.	298,691	227,166	175,962	197,386

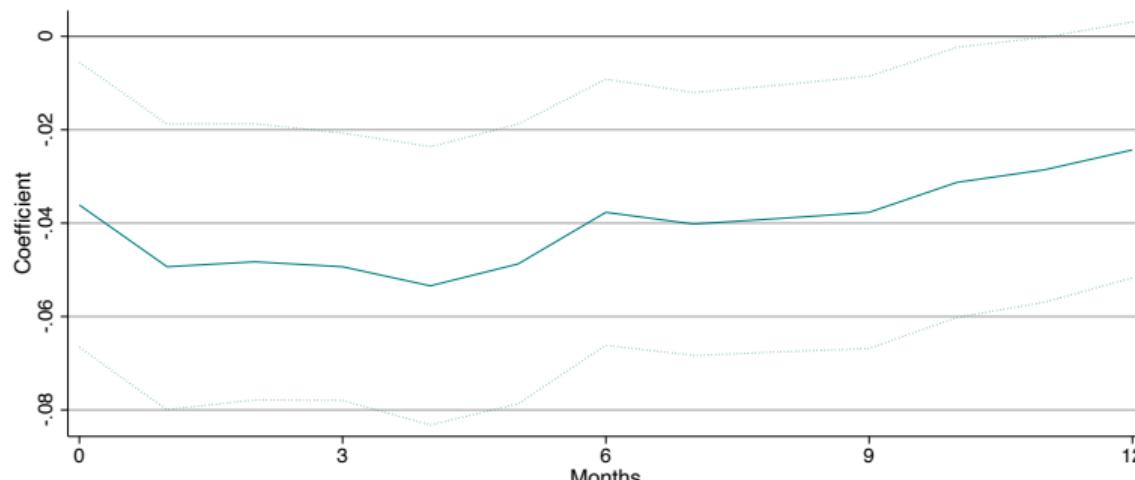
Notes: Dependent variables are (1) one-year inflation expectations, (2) five-year inflation expectations (3) one-year gas inflation expectations (4) five-year gas inflation expectations. Time fixed effects and \hat{r}_i, t are included as controls.

Belief Response to Oil Supply Shocks

- Do beliefs react to supply shocks more than demand shocks?
- Conduct a local projection of the cross-section of sentiment on oil supply shocks (Kanzig, 2021) clustered at the month:

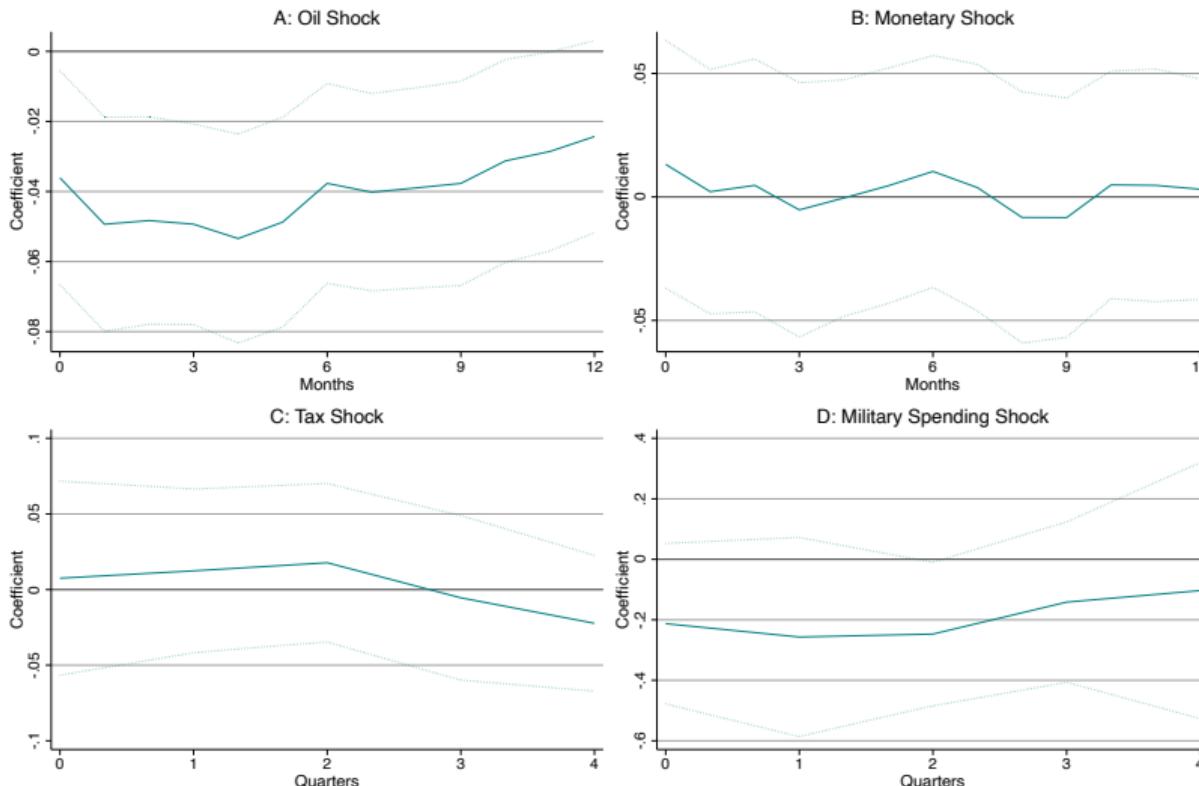
$$\hat{f}_{i,t+h} = \alpha_h + \theta_h \hat{p}_t + \Gamma_h X_t + u_{i,t+h}$$

- Following a negative oil supply shock, sentiment falls



Belief Response to Demand Shocks

- Beliefs do not react to monetary policy, tax, or military spending shocks



Conclusion

- Single Factor and Stagflationary Beliefs
 - Consumers' expectations exhibit a low-factor structure...
 - ...and believe inflation is countercyclical
- TANK Model Featuring Rational Inattention
 - Agents economize information costs and obtain a single signal (single factor belief model)
 - This strategy typically implies higher precision in beliefs about supply-driven recessions and less about demand-driven recessions (countercyclical inflation beliefs)
- Direct Evidence of Attention-Based Supply-Side Views
 - Stagflationary beliefs are strongest among (i) inattentive consumers and (ii) consumers who give supply-based reasoning
 - ... providing direct evidence for attention-based supply-side beliefs

Dynamics: First Derivatives and Intuition

- In the limit of no H agents ($\lambda \rightarrow 0$) and no information costs ($K \rightarrow 1$), conditional responses wrt the fraction of hand-to-mouth (λ) are:

$$\frac{\partial C_{y,v}}{\partial \lambda} \rightarrow \frac{\varphi(1 - \chi_n)}{(\varsigma + (\varsigma + \varphi)\kappa_w\phi_\pi)^2}, \quad \frac{\partial C_{y,\gamma}}{\partial \lambda} \rightarrow \frac{\varsigma\varphi(1 - \chi_n)}{(\varsigma + \varphi)(\varsigma + (\varsigma + \varphi)\kappa_w\phi_\pi)^2}$$

- Amplification of the output response to demand shocks (if $\chi_n \leq 1$)
 - A demand shock \uparrow desired S consumption; output and wages \uparrow in the RANK benchmark
 - A wage increase (all else equal) induces a larger positive consumption response of H households relative to S households
- Mitigation of the output response to supply shocks (if $\chi_n \leq 1$)
 - A supply shock \downarrow output, but wages \uparrow in the RANK benchmark
 - A wage increase (all else equal) puts more upward pressure on H consumption relative to S consumption

back

Calibration

Parameter	Value	Description	Target
Panel A:			
β	0.9975	Discount Factor	Long-run rate
ς	1.0	CRRA	Log-utility, $\chi_n = 0$
$\frac{\tau^D}{\lambda}$	0.0	Transfers	Log-utility, $\chi_n = 0$
λ	0.33	Hand-to-Mouth	Fraction 1/3
ϕ_π	1.5	Taylor Rule	Inflation Coeff.
ϕ_y	0.1	Taylor Rule	Output Coeff.
Panel B:			
φ	0.5305	$\sigma(w_t)$	1.5682
κ_w	0.198	$\rho(y_t, \pi_t)$	0.0689
ρ_v	0.7131	$\rho(y_t, y_{t-1})$	0.8074
ρ_γ	0.8242	$\rho(\pi_t, \pi_{t-1})$	0.749
σ_v	0.7616	$\sigma(y_t)$	1.5757
σ_γ	1.7847	$\sigma(\pi_t)$	1.2007
K	0.149	$\rho(\hat{\pi}_t^j, \pi_t)$	0.3306

back