

ASSIGNMENT 5

Question 1:

a) Initial Accuracy of the code with given inputs

[illegible]

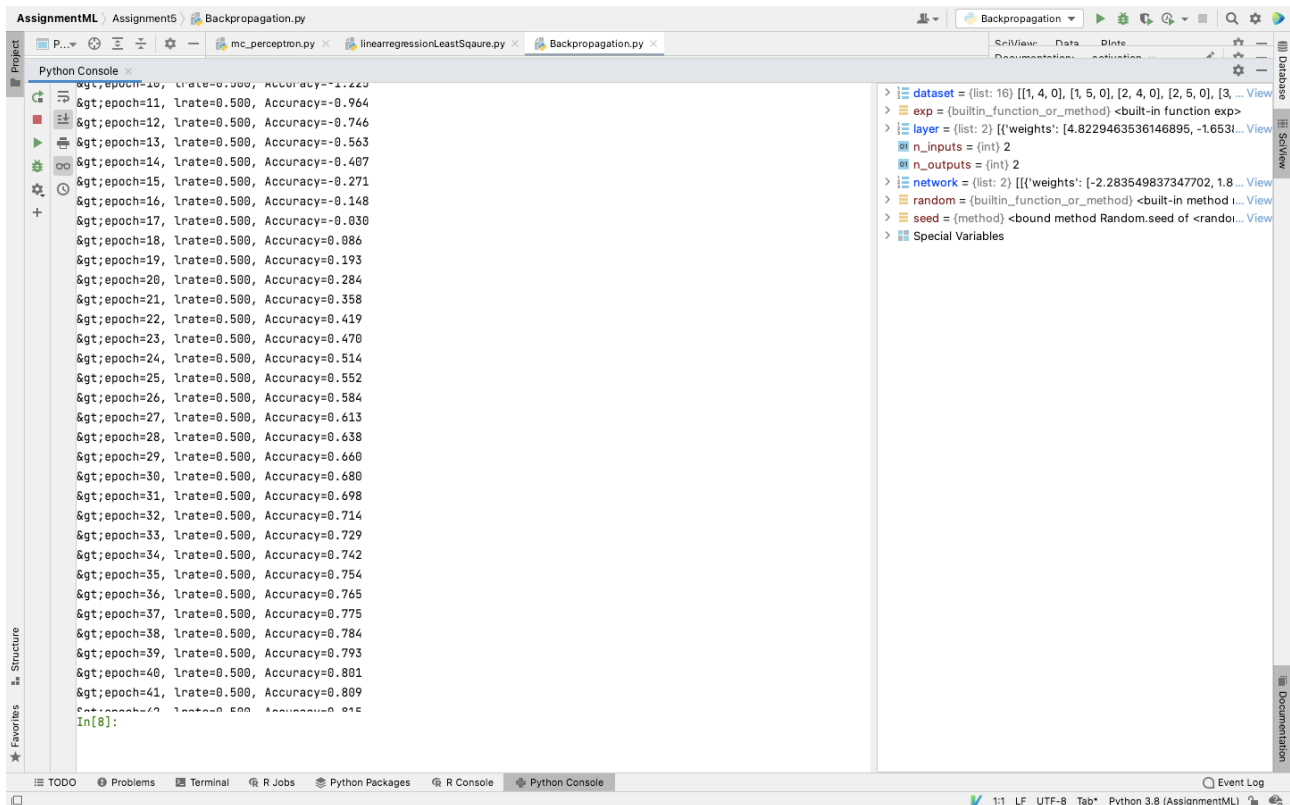
The screenshot displays a Jupyter Notebook environment with three open files: `P...py`, `mc_perceptron.py`, and `Backpropagation.py`. The active file is `Backpropagation.py`, which contains a series of epochs from 71 to 99. Each epoch's output shows the learning rate (`lrate`) and accuracy. The accuracy starts at approximately 0.772 for epoch 71 and increases steadily, reaching about 0.859 by epoch 99.

The right-hand pane shows the interactive code execution area. It includes a variable inspector for `dataset`, `exp`, `layer`, `n_inputs`, `n_outputs`, `network`, `random`, and `seed`. Below this, there are two printed outputs:

```
{'weights': [-2.556753573045669, 1.9966019304139861, 0.2665212937193951], 'output': 0.082560117566315216, 'delta':  
{'weights': [4.288386729533528, 0.8209593947585816, -2.397570537706321], 'output': 0.09495368785437644, 'delta':
```

The bottom status bar indicates the current state: "Event Log" on the left, "Python Console" in the center, and "Jupyter 3.8 (AssignmentML)" on the right.

b) Initial Accuracy of the code with some more inputs



```
AssignmentML / Assignment5 / Backpropagation.py
Python Console
> &gt; epoch=10, lrate=0.500, Accuracy=-1.223
> &gt; epoch=11, lrate=0.500, Accuracy=-0.964
> &gt; epoch=12, lrate=0.500, Accuracy=-0.746
> &gt; epoch=13, lrate=0.500, Accuracy=-0.563
> &gt; epoch=14, lrate=0.500, Accuracy=-0.407
> &gt; epoch=15, lrate=0.500, Accuracy=-0.271
> &gt; epoch=16, lrate=0.500, Accuracy=-0.148
> &gt; epoch=17, lrate=0.500, Accuracy=-0.030
> &gt; epoch=18, lrate=0.500, Accuracy=0.086
> &gt; epoch=19, lrate=0.500, Accuracy=0.193
> &gt; epoch=20, lrate=0.500, Accuracy=0.284
> &gt; epoch=21, lrate=0.500, Accuracy=0.358
> &gt; epoch=22, lrate=0.500, Accuracy=0.419
> &gt; epoch=23, lrate=0.500, Accuracy=0.470
> &gt; epoch=24, lrate=0.500, Accuracy=0.514
> &gt; epoch=25, lrate=0.500, Accuracy=0.552
> &gt; epoch=26, lrate=0.500, Accuracy=0.584
> &gt; epoch=27, lrate=0.500, Accuracy=0.613
> &gt; epoch=28, lrate=0.500, Accuracy=0.638
> &gt; epoch=29, lrate=0.500, Accuracy=0.660
> &gt; epoch=30, lrate=0.500, Accuracy=0.680
> &gt; epoch=31, lrate=0.500, Accuracy=0.698
> &gt; epoch=32, lrate=0.500, Accuracy=0.714
> &gt; epoch=33, lrate=0.500, Accuracy=0.729
> &gt; epoch=34, lrate=0.500, Accuracy=0.742
> &gt; epoch=35, lrate=0.500, Accuracy=0.754
> &gt; epoch=36, lrate=0.500, Accuracy=0.765
> &gt; epoch=37, lrate=0.500, Accuracy=0.775
> &gt; epoch=38, lrate=0.500, Accuracy=0.784
> &gt; epoch=39, lrate=0.500, Accuracy=0.793
> &gt; epoch=40, lrate=0.500, Accuracy=0.801
> &gt; epoch=41, lrate=0.500, Accuracy=0.809
In[8]:
> dataset = (list: 16) [[1, 4, 0], [1, 5, 0], [2, 4, 0], [2, 5, 0], [3, ... View
> exp = (builtin_function_or_method) <built-in function exp>
> layer = (list: 2) [{'weights': [4.8229463536146895, -1.6531... View
> n_inputs = (int) 2
> n_outputs = (int) 2
> network = (list: 2) [[{'weights': [-2.283549837347702, 1.8... View
> random = (builtin_function_or_method) <built-in method i... View
> seed = (method) <bound method Random.seed of <randoi... View
> Special Variables
```

c) When we increases the Learning rate from 0.05 to 0.5, the sum_error increase too much and results in degradation of Accuracy of the system.

from math import exp

from random import seed

from random import random

Step 1 Initialise the network

def initialise_net(no_input, no_hidden, no_output):

net = list()

hid_layer = [{'weights':[random() for i in range(no_input + 1)]} for i in range(no_hidden)]

net.append(hid_layer)

```

out_layer = [{ 'weights': [random() for i in range(no_hidden + 1)] } for i in range(no_output)]
net.append(out_layer)
return net

```

Step2 Calculate Activation Function

```

def activate(weight, input):
    activation = weight[-1]
    for i in range(len(weight)-1):
        activation += weight[i] * input[i]
    return activation

```

Step 3 we have to transfer the activation of neuron

```

def transfer(activation):
    return 1.0 / (1.0 + exp(-activation))

```

Step 4 Forward propagated input to the neural output

```

def forward_propagate(net, r):
    input = r
    for layer in net:
        new_input = []
        for neuron in layer:
            activation = activate(neuron['weight'], input)
            neuron['output'] = transfer(activation)
            new_input.append(neuron['output'])
        input = new_input
    return input

```

Step 5 Calculate the derivative of an neuron output

```

def transfer_derivative(output):
    return output * (1.0 - output)

```

Step 6 Backpropagate error and store in neurons

```

def back_prop_err(net, expect):

```

```

for i in reversed(range(len(net))):
    layer = net[i]
    err = list()
    if i != len(net)-1:
        for j in range(len(layer)):
            err1= 0.0
            for neuron in network[i + 1]:
                err1 += (neuron['weights'][j] * neuron['delta'])
            err.append(err1)
    else:
        for j in range(len(layer)):
            neuron = layer[j]
            errors.append(expected[j] - neuron['output'])
    for j in range(len(layer)):
        neuron = layer[j]
        neuron['delta'] = errors[j] * transfer_derivative(neuron['output'])

```

Step 7

```

def update_weights(net, r, learn_rate):
    for i in range(len(net)):
        input = r[:-1]
        if i != 0:
            input = [neuron['output'] for neuron in network[i - 1]]
        for neuron in net[i]:
            for j in range(len(input)):
                neuron['weights'][j] += learn_rate * neuron['delta'] * input[j]
            neuron['weights'][-1] += l_rate * neuron['delta']

```

Train a network for a fixed number of epochs

```

def train_network(net, train, learn_rate, no_epochs, no_output):
    for epoch in range(no_epochs):
        sum_err = 0
        for r in train:

```

```

        out = forward_propagate(net, r)
        expected = [0 for i in range(no_output)]
        expected[r[-1]] = 1
        sum_error += sum([(expected[i]-outputs[i])**2 for i in
range(len(expected))])
        back_pro_err(net, expected)
        update_weights(net, r, learn_rate)
    print('epoch=%d, lrate=%.3f, error=%.3f' % (epoch, l_rate, sum_error))

```

Test training backprop algorithm

```

seed(1)
dataset = [[1,4,0],
            [1,5,0],
            [2,4,0],
            [2,5,0],
            [3,1,1],
            [3,2,1],
            [4,1,1],
            [4,2,1]]
no_input = len(dataset[0]) - 1
no_output = len(set([row[-1] for row in dataset]))
net = initialise_net(no_input, 2, no_output)
train_network(network, dataset, 0.5, 100, no_outputs)
for layer in network:
    print(layer)

```

Question 2)

```

-1.0 1.0 -2.0 -1.0 1.0 -4.0 1 -1
-2.0 -2.0 -2.0 -1.0 0.0 -3.0 1 -1
1.0 1.0 -2.0 -1.0 0.0 -3.0 1 -1
1.0 2.0 -2.0 -1.0 0.0 -3.0 1 -1
2.0 -1.0 -2.0 -1.0 0.0 -3.0 1 -1
2.0 0.0 -2.0 -1.0 0.0 -3.0 1 -1
-1.0 2.0 -2.0 -1.0 2.0 -3.0 1 -1
-2.0 1.0 -2.0 -1.0 2.0 -3.0 1 -1
-1.0 1.0 -2.0 -1.0 2.0 -3.0 1 -1
-2.0 -2.0 -2.0 -1.0 1.0 -2.0 1 -1
1.0 1.0 -2.0 -1.0 1.0 -2.0 1 -1
1.0 2.0 -2.0 -1.0 1.0 -2.0 1 -1
2.0 -1.0 -2.0 -1.0 1.0 -2.0 1 -1
2.0 0.0 -2.0 -1.0 1.0 -2.0 1 -1
-1.0 2.0 -2.0 -1.0 1.0 -2.0 1 -1
-2.0 1.0 -2.0 -1.0 1.0 -2.0 1 -1
-1.0 1.0 -2.0 -1.0 1.0 -2.0 1 -1
-2.0 -2.0 -2.0 -1.0 0.0 -1.0 1 -1
1.0 1.0 -2.0 -1.0 0.0 -1.0 1 -1
1.0 2.0 -2.0 -1.0 0.0 -1.0 1 -1
2.0 -1.0 -2.0 -1.0 0.0 -1.0 1 -1
2.0 0.0 -2.0 -1.0 2.0 -2.0 1 -1
-1.0 2.0 -2.0 -1.0 2.0 -2.0 1 -1
-2.0 1.0 -2.0 -1.0 2.0 -2.0 1 -1
-1.0 1.0 -2.0 -1.0 2.0 -2.0 1 -1
-2.0 -2.0 -2.0 -1.0 1.0 -1.0 1 -1
1.0 1.0 -2.0 -1.0 -1.0 -3.0 1 -1
1.0 2.0 -2.0 -1.0 -1.0 -3.0 1 -1
2.0 -1.0 -2.0 -1.0 -1.0 -3.0 1 -1
2.0 0.0 -2.0 -1.0 1.0 -4.0 1 -1
-1.0 2.0 -2.0 -1.0 1.0 -4.0 1 -1
-2.0 1.0 -2.0 -1.0 1.0 -4.0 1 -1
-1.0 1.0 -2.0 -1.0 1.0 -4.0 1 -1
-2.0 -2.0 -2.0 -1.0 0.0 -3.0 1 -1
1.0 1.0 -2.0 -1.0 0.0 -3.0 1 -1

```

```
+ Code + Text
[18] 1.0 1.0 -0.52000000000000002 -1.6699999999999997 1.8599999999999999 -1.9999999999999998 1 1
1.0 2.0 -0.52000000000000002 -1.6699999999999997 1.8499999999999999 -2.01 1 1
2.0 -1.0 -0.52000000000000002 -1.6699999999999997 1.8499999999999999 -2.01 1 1
```

- best parameters:

```
[19] max_accuracy, w1_max, w2_max, w3_max, w4_max, b1_max, b2_max, lr_max
(0.875, -3, -2, -2, -1, -1, -1, 1)
```

- On the Test Data:

```
[24] # test dataset
X_test = [[1,1],[1,2],[2,-1],[2,0],[-1,2],[-2,1],[-1,1],[-2,-2],[-3,-2],[-4,-2]]
y_test = [1, 1, 1, 1, 3, 3, 3, 4, 4, 4]
```

```
def test_function(w1, w2, w3, w4, b1, b2):  
    # SET ALL PARAMETERS AND VARIABLES  
    x = X_test # input  
    target = y_test # output  
  
    # threshold  
    threshold1 = 0.5  
    threshold2 = 0.5  
  
    # BASIC PERCEPTRON LEARNING PROCESS  
    out_test = []  
    for i in range(len(x)): # loop for each row in x  
        x1 = float(x[i][0])  
        x2 = float(x[i][1])
```

RAM

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test_function(w1_max, w2_max, w3_max, w4_max, b1_max, b2_max)

1.0 1.0 -3 -2 -2 -1 -1 -1

1.0 2.0 -3 -2 -2 -1 -1 -1

2.0 -1.0 -3 -2 -2 -1 -1 -1

2.0 0.0 -3 -2 -2 -1 -1 -1

-1.0 2.0 -3 -2 -2 -1 -1 -1

-2.0 1.0 -3 -2 -2 -1 -1 -1

-1.0 1.0 -3 -2 -2 -1 -1 -1

-2.0 -2.0 -3 -2 -2 -1 -1 -1

-3.0 -2.0 -3 -2 -2 -1 -1 -1

-4.0 -2.0 -3 -2 -2 -1 -1 -1

TEST RESULTS:

Final weights:-3,-2,-2,-1

Final predicted output: [1, 1, 1, 1, 1, 4, 1, 4, 4, 4]

accuracy: 0.7

0.7

0s

completed at 22:10



```

#import required packages
%matplotlib inline
import os
import numpy as np
import pandas as pd
from sklearn.metrics import precision_score,
recall_score, accuracy_score, confusion_matrix
import seaborn as sns
from sklearn import preprocessing
# Inputs and labels
X_data = [[1,1],[1,2],[2,-1],[2,0],[-1,2],[-2,1],[-1,1],
[-2,-2]]
Y_data = [1,1,2,2,3,3,4,4]
def calculate_y_in(x_1, x_2, w_1, w_2, w_3, w_4, b_1,
b_2):
    y_in_1 = w_1 * x_1 + w_2 * x_2 + b_1
    y_in_2 = w_3 * x_1 + w_4 * x_2 + b_2
    print(x_1, x_2, w_1, w_2, w_3, w_4, b_1, b_2)
    return y_in_1, y_in_2

#Update Weight
def update_w(w_1, x_1, w_2, x_2, w_3, w_4, l_r, z):
    w_1_new = w_1 + l_r * z[0] * x_1
    w_2_new = w_2 + l_r * z[0] * x_2
    w_3_new = w_3 + l_r * z[1] * x_1
    w_4_new = w_4 + l_r * z[1] * x_2

    return w_1_new, w_2_new, w_3_new, w_4_new

def class_to_category(y):
    if y == 1: return np.array([0, 0])
    if y == 2: return np.array([0, 1])
    if y == 3: return np.array([1, 0])
    return np.array([1, 1])

# Activation Function
def activation_function(y_in):
    sigmoid = (1/(1 + np.exp(-y_in)))
    return sigmoid
def train_function(w_1, w_2, w_3, w_4, b_1, b_2, l_r):
    x = X_data
    target = Y_data

```



```

threshold1 = 0.5
threshold2 = 0.5
epoch = 20

for e in range(epoch): # loop for each epoch
    out = []
    for i in range(len(x)): # loop for each row in x
        x_1 = float(x[i][0])
        x_2 = float(x[i][1])

        y_in_1, y_in_2 = calculate_y_in(x_1, x_2, w_1, w_2,
w_3, w_4, b_1, b_2) # calculate yin
        y_act_1 = activation_function(y_in_1)
        y_act_2 = activation_function(y_in_2)

        if y_act_1 > threshold1 and y_act_2 > threshold2:
            y = 4
        elif y_act_1 > threshold1 and y_act_2 <
threshold2:
            y = 3
        elif y_act_1 < threshold1 and y_act_2 > threshold2:
            y = 2
        else:
            y = 1

        if y != target[i]:
            loss = class_to_category(target[i]) -
class_to_category(y)
            w_1, w_2, w_3, w_4 = update_w(w_1, x_1, w_2, x_2,
w_3, w_4, l_r, loss)
            out.append(y) # append all prediction in 'out'

    # performance evaluation
    accuracy = accuracy_score(target, out)
    print("Weights:[{:.2f},{:.2f},{:.2f},{:.2f}] and
Accuracy:{:.2f}".format(w_1,w_2,w_3,w_4,accuracy))
    return accuracy

w1_a = [-3, -2, 0, 1]
w2_a = [-2, -1, 1, 2]
w3_a = [-2, -1, 1, 2]
w4_a = [-2, -1, 0, 2]

```

```

b1_a = [-1, 1]
b2_a = [-1, 1]
lr_a = [0.001, 0.005, 0.05, 1,]

maximum_accuracy = 0
w_1_maximum = 0
w_2_maximum = 0
w_3_maximum = 0
w_4_maximum = 0
b_1_maximum = 0
b_2_maximum = 0
l_r_maximum = 0

for w_1 in w_1_a:
    for w_2 in w_2_a:
        for w_3 in w_3_a:
            for w_4 in w_4_a:
                for b_1 in b_1_a:
                    for b_2 in b_2_a:
                        for l_r in l_r_a:
                            accuracy = train_function(w_1, w_2, w_3,
w_4, b_1, b_2, lr)
                            if accuracy > max_accuracy:
                                max_accuracy = accuracy
                                w_1_maximum = w_1
                                w_2_maximum = w_2
                                w_3_maximum = w_3
                                w_4_maximum = w_4
                                b_1_maximum = b_1
                                b_2_maximum = b_2
                                l_r_maximum = l_r
maximum_accuracy, w_1_maximum, w_2_maximum, w_3_maximum,
w_4_maximum, b_1_maximum, b_2_maximum, l_r_maximum

#Testing
X_test = [[1,1],[1,2],[2,-1],[2,0],[-1,2],[-2,1],[-1,1],
[-2,-2], [-3,-2],[-4,-2]]
y_test = [1, 1, 2, 2, 3, 3, 3, 4, 4, 4]

```

```

print(maximum_accuracy, w_1_maximum, w_2_maximum,
w_3_maximum, w_4_maximum, b_1_maximum, b_2_maximum,
l_r_maximum)

def test_function(w_1, w_2, w_3, w_4, b_1, b_2):
    # SET ALL PARAMETERS AND VARIABLES
    x = X_test # input
    target = y_test # output

    # threshold
    threshold1 = 0.5
    threshold2 = 0.5

    # BASIC PERCEPTRON LEARNING PROCESS
    out_test = []
    for i in range(len(x)): # loop for each row in x
        x_1 = float(x[i][0])
        x_2 = float(x[i][1])

        y_in_1, y_in_2 = calculate_y_in(x_1, x_2, w_1, w_2,
w_3, w_4, b_1, b_2) # calculate yin
        y_act_1 = activation_function(yin1)
        y_act_2 = activation_function(yin2)

        if y_act_1 > threshold1 and y_act_2 > threshold2:
            y = 4
        elif y_act_1 > threshold1 and y_act_2 < threshold2:
            y = 3
        elif y_act_1 < threshold1 and y_act_2 > threshold2:
            y = 2
        else:
            y = 1
        out_test.append(y) # append all prediction in 'out'

    print("\n TEST RESULTS:\n")
    print("Final weights:{},{},{},{}".format(w1,w2,w3,w4))
    print("Final predicted output:",out_test)

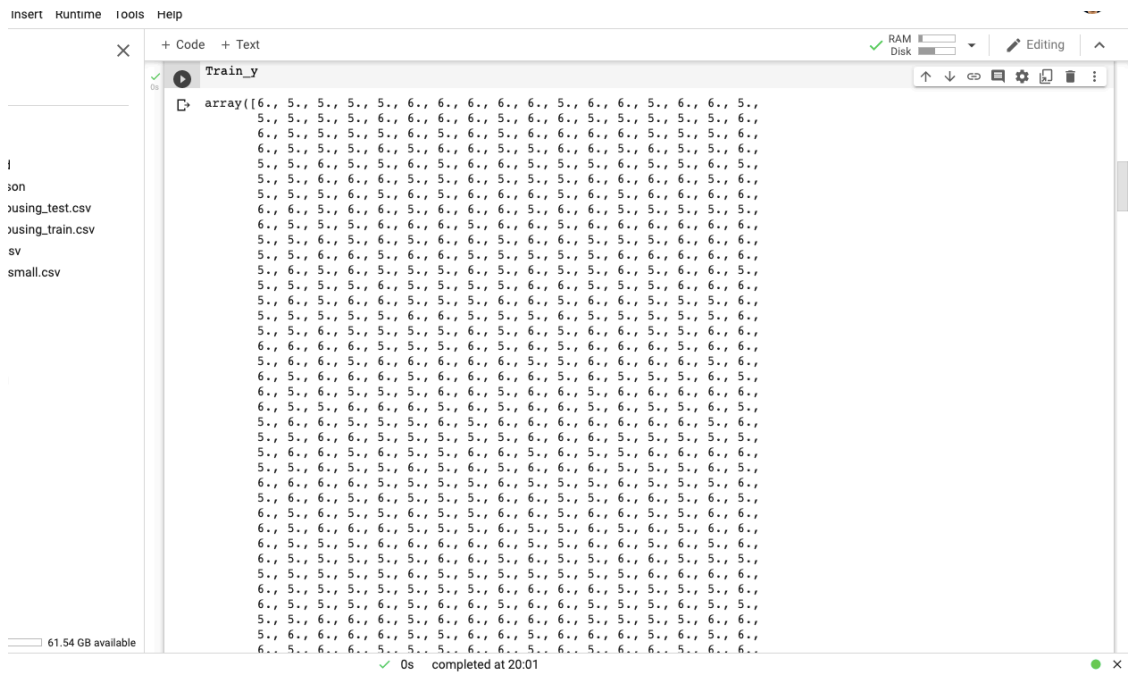
    # performance evaluation
    accuracy = accuracy_score(y_test,out_test)
    print("accuracy:",accuracy)

```

```
return accuracy
```

```
test_function(w_1_maximum, w_2_maximum, w_3_maximum,  
w_4_maximum, b_1_maximum, b2_maximum)
```

Question 3)



```
from tensorflow.keras import optimizers, losses, metrics
model = Sequential()
from keras.utils.vis_utils import plot_model
model.add(Dense(12, input_dim=64, activation='sigmoid'))
model.add(Dense(5, activation='sigmoid'))
model.add(Dense(1, activation='sigmoid'))

model.compile(optimizer=optimizers.Adam(learning_rate=0.001), loss='binary_crossentropy')
model.fit(Train_X, Train_y, batch_size=64, epochs=1000, verbose=2)
model.evaluate(Train_X, Train_y)
model.summary()
plot_model(model, to_file='model_plot.png', show_shapes=True, show_layer_names=True)
```

```
... Epoch 1/1000
12/12 - 0s - loss: 1.2357
Epoch 2/1000
12/12 - 0s - loss: 0.2882
Epoch 3/1000
12/12 - 0s - loss: -6.1252e-01
Epoch 4/1000
12/12 - 0s - loss: -1.3817e+00
Epoch 5/1000
12/12 - 0s - loss: -1.9045e+00
Epoch 6/1000
12/12 - 0s - loss: -2.2934e+00
Epoch 7/1000
12/12 - 0s - loss: -2.6417e+00
Epoch 8/1000
12/12 - 0s - loss: -2.9803e+00
Epoch 9/1000
12/12 - 0s - loss: -3.3090e+00
Epoch 10/1000
12/12 - 0s - loss: -3.6271e+00
Epoch 11/1000
```

```
Executing (23s) Cell > fit() > __call__() > _call() > __call__() > _call_flat() > call() > quick_execute()
```

+ Code+ Text

RAM
Disk

Editing

Model: "sequential_9"

Layer (type)

Output Shape

Param #

dense_27 (Dense)

(None, 12)

780

dense_28 (Dense)

(None, 5)

65

dense_29 (Dense)

(None, 1)

6

Total params: 851

Trainable params: 851

Non-trainable params: 0

dense_27_input: InputLayer

input: [(None, 64)]

output: [(None, 64)]

dense_27: Dense

input: (None, 64)

output: (None, 12)

dense_28: Dense

input: (None, 12)

output: (None, 5)

dense_29: Dense

input: (None, 5)

output: (None, 1)

25s

completed at 20:03

```

from numpy import loadtxt
from keras.models import Sequential
from keras.layers import Dense

#Importing the dataset
Train_X = dataset = loadtxt('TrainX.csv', delimiter=',')
Train_y = dataset = loadtxt('TrainY.csv', delimiter=',')
Test_X = dataset = loadtxt('TestX.csv', delimiter=',')
Test_y = dataset = loadtxt('TestY.csv', delimiter=',')

Train_X.shape
model = Sequential()
model.add(Dense(128, input_dim=64, activation='relu'))
model.add(Dense(64, activation='relu'))
model.add(Dense(1, activation='sigmoid'))

from tensorflow.keras import optimizers, losses, metrics
model = Sequential()

from keras.utils.vis_utils import plot_model
model.add(Dense(12, input_dim=64, activation='sigmoid'))
model.add(Dense(4, activation='sigmoid'))
model.add(Dense(1, activation='sigmoid'))


model.compile(optimizer=optimizers.Adam(learning_rate=0.001),loss='binary_crossentropy',metrics=['accuracy'])
model.fit(Train_X,Train_y,batch_size=64,epochs=10,verbose=2)
model.evaluate(Train_X, Train_y)
model.summary()
plot_model(model, to_file='model_plot.png', show_shapes=True, show_layer_names=True)


#required libraries
import numpy as np
import math
import matplotlib.pyplot as plt
import matplotlib.colors
import time

```

```

import pandas as pd
from sklearn.model_selection import train_test_split
from sklearn.metrics import accuracy_score,
mean_squared_error, log_loss
from tqdm import tqdm_notebook

from IPython.display import HTML
import warnings
from sklearn.preprocessing import OneHotEncoder
from sklearn.datasets import make_blobs

import torch
import torch.nn.functional as F
warnings.filterwarnings('ignore')

#converting the numpy array to torch tensors
#Train_y --> (5,6) -- (0,1)
#Test_y --> (5,6) -- (0,1)
for x in range(len(Train_y)):
    if Train_y[x,] == 5:
        Train_y[x,] = 0.0
    else:
        Train_y[x,] = 1.0

for x in range(len(Test_y)):
    if Test_y[x,] == 5:
        Test_y[x,] = 0.0
    else:
        Test_y[x,] = 1.0

X_train = torch.tensor(X_train).float()
Y_train = torch.tensor(Y_train).long()
X_val = torch.tensor(X_val).float()
Y_val = torch.tensor(Y_val).long()
print(X_train.shape, Y_train.shape)

#function for computing forward pass in the network
def model(x):
    A1 = torch.matmul(x, weights1) + bias1 # 753 * 5

```



```

    H1 = A1.sigmoid() # 753 * 5
    A2 = torch.matmul(H1, weights2) + bias2 # (N, 2) x
(2, 4) -> (N, 4)
    H2 = A2.exp()/A2.exp().sum(-1).unsqueeze(-1) # (N, 4)
#applying softmax at output layer.
    return H2

```

```

#function to calculate loss of a function.
#y_hat -> predicted & y -> actual
def loss_fn(y_hat, y):
    return -(y_hat[range(y.shape[0])], y].log()).mean()

```

```

#function to calculate accuracy of model
def accuracy(y_hat, y):
    pred = torch.argmax(y_hat, dim=1)
    return (pred == y).float().mean()

```

```

torch.manual_seed(0)
weights1 = (torch.randn(64, 5) / math.sqrt(2)).float()
weights1.requires_grad_()
bias1 = torch.zeros(5, requires_grad=True)
weights2 = torch.randn(5, 2) / math.sqrt(2)
weights2.requires_grad_()
bias2 = torch.zeros(2, requires_grad=True)

```

```

learning_rate = 0.2
epochs = 30
loss_arr = []
acc_arr = []

```

```

for epoch in range(epochs):
    y_hat = model(X_train)
    loss = F.cross_entropy(y_hat, Y_train)
    loss.backward()
    loss_arr.append(loss.item())
    acc_arr.append(accuracy(y_hat, Y_train))

```

```

with torch.no_grad():
    weights1 -= weights1.grad * learning_rate
    bias1 -= bias1.grad * learning_rate
    weights2 -= weights2.grad * learning_rate

```

- ▶ `loss_arr, acc_arr`

0.86350513081878561,
 0.7774642109870911,
 0.6932287216186523,
 0.6296347379684448,
 0.5724744721347046,
 0.525789201259613,
 0.49190765619277954,
 0.4662156415119171,
 0.44561383128662,
 0.429636770057678,
 0.4181194042588708,
 0.4093566238001575,
 0.40208104252815247,
 0.39547044038772543,
 0.389049232006073,
 0.38295228820991516,
 0.3774395287036896,
 0.37271174788475037,
 0.368787229611267,
 0.36553463339805603,
 0.3627281780312915,
 0.36023190371715393,
 0.3579065284636687,
 0.3557584781436982,
 0.3537191152572632,
 0.351727553844452,
 0.3499111533164978,
 0.3481464385984328,
 0.34649723768234253,
 0.34496662020683291,
 ...

[Show all](#)

```
[3.484146438985328,  
0.346497337366234253,  
0.34469666202068329],  
[tensor(0.2736),  
tensor(0.3639),  
tensor(0.5671),  
tensor(0.6321),  
tensor(0.7437),  
tensor(0.8566),  
tensor(0.8938),  
tensor(0.9177),  
tensor(0.9336),  
tensor(0.9548),  
tensor(0.9575),  
tensor(0.9588),  
tensor(0.9602),  
tensor(0.9655),  
tensor(0.9695),  
tensor(0.9734),  
tensor(0.9761),  
tensor(0.9774),  
tensor(0.9777),  
tensor(0.9774),  
tensor(0.9788),  
tensor(0.9801),  
tensor(0.9827),  
tensor(0.9841),  
tensor(0.9854),  
tensor(0.9867),  
tensor(0.9894),  
tensor(0.9987),  
tensor(0.9987),  
tensor(0.9987)]]
```