

10/04/2019  
Morning

# **JEE (MAIN)-2019 (Online) Phase-2**

## **(Physics, Chemistry and Mathematics)**

Time : 3 hrs.

M.M. : 360

### **Important Instructions :**

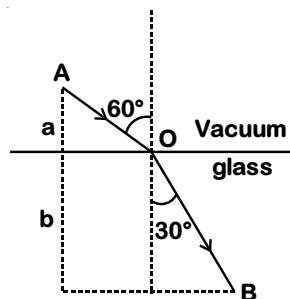
1. The test is of **3 hours** duration.
2. The Test Booklet consists of **90** questions. The maximum marks are **360**.
3. There are **three** parts in the question paper A, B, C consisting of **Physics, Chemistry and Mathematics** having 30 questions in each part of equal weightage.
4. Each question is allotted 4 (**four**) marks for each correct response.  $\frac{1}{4}$  (one-fourth) marks will be deducted for indicating incorrect response of each question. No deduction from the total score will be made if no response is indicated for an item in the answer sheet.
5. There is only one correct response for each question.

## PART-A : PHYSICS

1. Two coaxial discs, having moments of inertia  $I_1$  and  $\frac{I_1}{2}$ , are rotating with respective angular velocities  $\omega_1$  and  $\frac{\omega_1}{2}$  about their common axis. They are brought in contact with each other and thereafter they rotate with a common angular velocity. If  $E_f$  and  $E_i$  are the final and initial total energies, then  $(E_f - E_i)$  is :

- (1)  $-\frac{I_1 \omega_1^2}{12}$                       (2)  $\frac{3}{8} I_1 \omega_1^2$   
 (3)  $\frac{I_1 \omega_1^2}{6}$                         (4)  $-\frac{I_1 \omega_1^2}{24}$

2. A ray of light AO in vacuum is incident on a glass slab at angle  $60^\circ$  and refracted at angle  $30^\circ$  along OB as shown in the figure. The optical path length of light ray from A to B is :



- (1)  $\frac{2\sqrt{3}}{a} + 2b$                       (2)  $2a + \frac{2b}{\sqrt{3}}$   
 (3)  $2a + \frac{2b}{3}$                             (4)  $2a + 2b$

3. A ball is thrown upward with an initial velocity  $V_0$  from the surface of the earth. The motion of the ball is affected by a drag force equal to  $m\gamma v^2$  (where  $m$  is mass of the ball,  $v$  is its instantaneous velocity and  $\gamma$  is a constant). Time taken by the ball to rise to its zenith is :

- (1)  $\frac{1}{\sqrt{\gamma g}} \sin^{-1} \left( \sqrt{\frac{\gamma}{g}} V_0 \right)$   
 (2)  $\frac{1}{\sqrt{\gamma g}} \ln \left( 1 + \sqrt{\frac{\gamma}{g}} V_0 \right)$   
 (3)  $\frac{1}{\sqrt{\gamma g}} \tan^{-1} \left( \sqrt{\frac{\gamma}{g}} V_0 \right)$   
 (4)  $\frac{1}{\sqrt{2\gamma g}} \tan^{-1} \left( \sqrt{\frac{2\gamma}{g}} V_0 \right)$

4. A particle of mass  $m$  is moving along a trajectory given by

$$x = x_0 + a \cos \omega_1 t$$

$$y = y_0 + b \sin \omega_2 t$$

The torque, acting on the particle about the origin, at  $t = 0$  is :

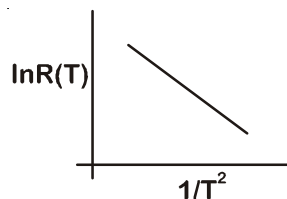
- (1)  $-m(x_0 b \omega_2^2 - y_0 a \omega_1^2) \hat{k}$
- (2)  $m(-x_0 b + y_0 a) \omega_1^2 \hat{k}$
- (3)  $+m y_0 a \omega_1^2 \hat{k}$
- (4) Zero

5. In a photoelectric effect experiment the threshold wavelength of light is 380 nm. If the wavelength of incident light is 260 nm, the maximum kinetic energy of emitted electrons will be :

$$\text{Given } E \text{ (in eV)} = \frac{1237}{\lambda \text{ (in nm)}}$$

- (1) 4.5 eV
- (2) 15.1 eV
- (3) 3.0 eV
- (4) 1.5 eV

6. In an experiment, the resistance of a material is plotted as a function of temperature (in some range). As shown in the figure, it is a straight line.



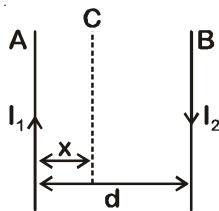
One may conclude that :

- (1)  $R(T) = \frac{R_0}{T^2}$
- (2)  $R(T) = R_0 e^{-T_0^2/T^2}$
- (3)  $R(T) = R_0 e^{-T^2/T_0^2}$
- (4)  $R(T) = R_0 e^{T^2/T_0^2}$

7. An npn transistor operates as a common emitter amplifier, with a power gain of 60 dB. The input circuit resistance is  $100 \Omega$  and the output load resistance is  $10 \text{ k}\Omega$ . The common emitter current gain  $\beta$  is :

- (1)  $10^4$
- (2)  $6 \times 10^2$
- (3)  $10^2$
- (4) 60

8. Two wires A and B are carrying currents  $I_1$  and  $I_2$  as shown in the figure. The separation between them is  $d$ . A third wire C carrying a current  $I$  is to be kept parallel to them at a distance  $x$  from A such that the net force acting on it is zero. The possible values of  $x$  are :



- (1)  $x = \pm \frac{I_1 d}{(I_1 - I_2)}$   
 (2)  $x = \left( \frac{I_1}{I_1 + I_2} \right) d$  and  $x = \left( \frac{I_2}{I_1 - I_2} \right) d$   
 (3)  $x = \left( \frac{I_2}{I_1 + I_2} \right) d$  and  $x = \left( \frac{I_2}{I_1 - I_2} \right) d$   
 (4)  $x = \left( \frac{I_1}{I_1 - I_2} \right) d$  and  $x = \left( \frac{I_2}{I_1 + I_2} \right) d$

9. A stationary source emits sound waves of frequency 500 Hz. Two observers moving along a line passing through the source detect sound to be of frequencies 480 Hz and 530 Hz. Their respective speeds are, in  $\text{ms}^{-1}$ ,

(Given speed of sound = 300 m/s)

- (1) 12, 16                      (2) 16, 14  
 (3) 8, 18                      (4) 12, 18

10. A transformer consisting of 300 turns in the primary and 150 turns in the secondary gives output power of 2.2 kW. If the current in the secondary coil is 10 A, then the input voltage and current in the primary coil are :

- (1) 440 V and 5 A              (2) 220 V and 20 A  
 (3) 220 V and 10 A            (4) 440 V and 20 A

11. A uniformly charged ring of radius  $3a$  and total charge  $q$  is placed in  $xy$ -plane centred at origin. A point charge  $q$  is moving towards the ring along the  $z$ -axis and has speed  $v$  at  $z = 4a$ . The minimum value of  $v$  such that it crosses the origin is :

- (1)  $\sqrt{\frac{2}{m} \left( \frac{1}{15} \frac{q^2}{4\pi\epsilon_0 a} \right)^{1/2}}$     (2)  $\sqrt{\frac{2}{m} \left( \frac{1}{5} \frac{q^2}{4\pi\epsilon_0 a} \right)^{1/2}}$   
 (3)  $\sqrt{\frac{2}{m} \left( \frac{4}{15} \frac{q^2}{4\pi\epsilon_0 a} \right)^{1/2}}$     (4)  $\sqrt{\frac{2}{m} \left( \frac{2}{15} \frac{q^2}{4\pi\epsilon_0 a} \right)^{1/2}}$

12.  $n$  moles of an ideal gas with constant volume heat capacity  $C_V$  undergo an isobaric expansion by certain volume. The ratio of the work done in the process, to the heat supplied is :

(1)  $\frac{4nR}{C_V + nR}$                       (2)  $\frac{nR}{C_V + nR}$   
 (3)  $\frac{4nR}{C_V - nR}$                       (4)  $\frac{nR}{C_V - nR}$

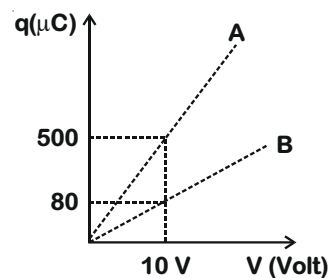
13. A  $25 \times 10^{-3} \text{ m}^3$  volume cylinder is filled with 1 mol of  $\text{O}_2$  gas at room temperature (300 K). The molecular diameter of  $\text{O}_2$ , and its root mean square speed, are found to be 0.3 nm and 200 m/s, respectively. What is the average collision rate (per second) for an  $\text{O}_2$  molecule ?

(1)  $\sim 10^{12}$                       (2)  $\sim 10^{10}$   
 (3)  $\sim 10^{11}$                       (4)  $\sim 10^{13}$

14. Two radioactive materials A and B have decay constants  $10\lambda$  and  $\lambda$ , respectively. If initially they have the same number of nuclei, then the ratio of the number of nuclei of A to that of B will be  $1/e$  after a time :

(1)  $\frac{1}{10\lambda}$                       (2)  $\frac{11}{10\lambda}$   
 (3)  $\frac{1}{9\lambda}$                       (4)  $\frac{1}{11\lambda}$

15. Figure shows charge ( $q$ ) versus voltage ( $V$ ) graph for series and parallel combination of two given capacitors. The capacitances are :

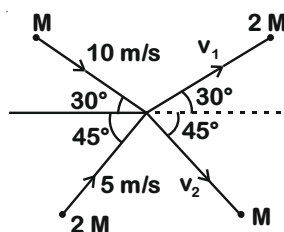


(1)  $40 \mu\text{F}$  and  $10 \mu\text{F}$                       (2)  $20 \mu\text{F}$  and  $30 \mu\text{F}$   
 (3)  $60 \mu\text{F}$  and  $40 \mu\text{F}$                       (4)  $50 \mu\text{F}$  and  $30 \mu\text{F}$

16. A message signal of frequency 100 MHz and peak voltage 100 V is used to execute amplitude modulation on a carrier wave of frequency 300 GHz and peak voltage 400 V. The modulation index and difference between the two side band frequencies are :

(1) 4 ;  $2 \times 10^8$  Hz      (2) 4 ;  $1 \times 10^8$  Hz  
 (3) 0.25 ;  $1 \times 10^8$  Hz    (4) 0.25 ;  $2 \times 10^8$  Hz

17. Two particles, of masses  $M$  and  $2M$ , moving, as shown, with speeds of 10 m/s and 5 m/s, collide elastically at the origin. After the collision, they move along the indicated directions with speeds  $v_1$  and  $v_2$ , respectively. The values of  $v_1$  and  $v_2$  are nearly :

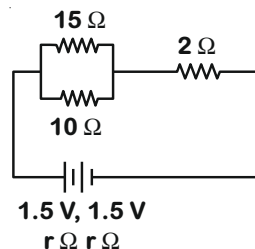


(1) 3.2 m/s and 12.6 m/s  
 (2) 3.2 m/s and 6.3 m/s  
 (3) 6.5 m/s and 3.2 m/s  
 (4) 6.5 m/s and 6.3 m/s

18. A moving coil galvanometer allows a full scale current of  $10^{-4}$  A. A series resistance of  $2 \text{ M}\Omega$  is required to convert the above galvanometer into a voltmeter of range 0 – 5 V. Therefore the value of shunt resistance required to convert the above galvanometer into an ammeter of range 0–10 mA is :

(1)  $200 \Omega$   
 (2)  $500 \Omega$   
 (3)  $100 \Omega$   
 (4)  $10 \Omega$

19. In the given circuit, an ideal voltmeter connected across the  $10 \Omega$  resistance reads 2 V. The internal resistance  $r$ , of each cell is :



(1)  $0.5 \Omega$   
 (2)  $0 \Omega$   
 (3)  $1.5 \Omega$   
 (4)  $1 \Omega$

=

20. The value of acceleration due to gravity at Earth's surface is  $9.8 \text{ ms}^{-2}$ . The altitude above its surface at which the acceleration due to gravity decreases to  $4.9 \text{ ms}^{-2}$ , is close to : (Radius of earth =  $6.4 \times 10^6 \text{ m}$ )

- (1)  $9.0 \times 10^6 \text{ m}$                       (2)  $6.4 \times 10^6 \text{ m}$   
(3)  $1.6 \times 10^6 \text{ m}$                       (4)  $2.6 \times 10^6 \text{ m}$

21. The ratio of surface tensions of mercury and water is given to be 7.5 while the ratio of their densities is 13.6. Their contact angles, with glass, are close to  $135^\circ$  and  $0^\circ$ , respectively. It is observed that mercury gets depressed by an amount  $h$  in a capillary tube of radius  $r_1$ , while water rises by the same amount  $h$  in a capillary tube of radius  $r_2$ . The ratio,  $(r_1/r_2)$ , is then close to :

- (1)  $4/5$                                       (2)  $2/3$   
(3)  $3/5$                                       (4)  $2/5$

22. A thin disc of mass  $M$  and radius  $R$  has mass per unit area  $\sigma(r) = kr^2$  where  $r$  is the distance from its centre. Its moment of inertia about an axis going through its centre of mass and perpendicular to its plane is :

- (1)  $\frac{MR^2}{3}$                                       (2)  $\frac{MR^2}{6}$   
(3)  $\frac{MR^2}{2}$                                       (4)  $\frac{2MR^2}{3}$

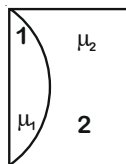
23. A cylinder with fixed capacity of 67.2 lit contains helium gas at STP. The amount of heat needed to raise the temperature of the gas by  $20^\circ\text{C}$  is : [Given that  $R = 8.31 \text{ J mol}^{-1}\text{K}^{-1}$ ]

- (1) 700 J  
(2) 350 J  
(3) 374 J  
(4) 748 J

24. A proton, an electron, and a Helium nucleus, have the same energy. They are in circular orbits in a plane due to magnetic field perpendicular to the plane. Let  $r_p$ ,  $r_e$  and  $r_{He}$  be their respective radii, then,

- (1)  $r_e < r_p < r_{He}$       (2)  $r_e > r_p = r_{He}$   
 (3)  $r_e < r_p = r_{He}$       (4)  $r_e > r_p > r_{He}$

25. One plano-convex and one plano-concave lens of same radius of curvature 'R' but of different materials are joined side by side as shown in the figure. If the refractive index of the material of 1 is  $\mu_1$  and that of 2 is  $\mu_2$ , then the focal length of the combination is :



- (1)  $\frac{R}{2(\mu_1 - \mu_2)}$   
 (2)  $\frac{R}{2 - (\mu_1 - \mu_2)}$   
 (3)  $\frac{R}{\mu_1 - \mu_2}$   
 (4)  $\frac{2R}{\mu_1 - \mu_2}$

26. The electric field of a plane electromagnetic wave is given by

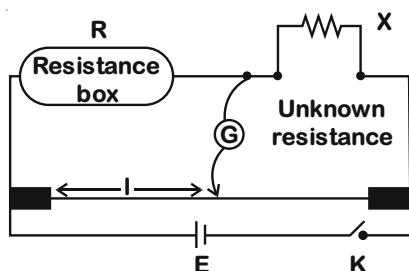
$$\vec{E} = E_0 \hat{i} \cos(kz) \cos(\omega t)$$

The corresponding magnetic field  $\vec{B}$  is then given by :

- (1)  $\vec{B} = \frac{E_0}{C} \hat{j} \sin(kz) \cos(\omega t)$   
 (2)  $\vec{B} = \frac{E_0}{C} \hat{j} \cos(kz) \sin(\omega t)$   
 (3)  $\vec{B} = \frac{E_0}{C} \hat{j} \sin(kz) \sin(\omega t)$   
 (4)  $\vec{B} = \frac{E_0}{C} \hat{k} \sin(kz) \cos(\omega t)$



27. In a meter bridge experiment, the circuit diagram and the corresponding observation table are shown in figure.



Sl. No	R ( $\Omega$ )	l (cm)
1.	1000	60
2.	100	13
3.	10	1.5
4.	1	1.0

Which of the readings is inconsistent ?

- (1) 3                                      (2) 2  
(3) 1                                      (4) 4

28. A current of 5 A passes through a copper conductor (resistivity =  $1.7 \times 10^{-8} \Omega \text{ m}$ ) of radius of cross-section 5 mm. Find the mobility of the charges if their drift velocity is  $1.1 \times 10^{-3} \text{ m/s}$ .

- (1)  $1.3 \text{ m}^2/\text{Vs}$   
(2)  $1.8 \text{ m}^2/\text{Vs}$   
(3)  $1.5 \text{ m}^2/\text{Vs}$   
(4)  $1.0 \text{ m}^2/\text{Vs}$

29. Given below in the left column are different modes of communication using the kinds of waves given in the right column.

- |                                |                   |
|--------------------------------|-------------------|
| A. Optical Fibre Communication | P. Ultrasound     |
| B. Radar                       | Q. Infrared Light |
| C. Sonar                       | R. Microwaves     |
| D. Mobile Phones               | S. Radio Waves    |

From the options given below, find the most appropriate match between entries in the left and the right column.

- (1) A-Q, B-S, C-P, D-R  
(2) A-Q, B-S, C-R, D-P  
(3) A-S, B-Q, C-R, D-P  
(4) A-R, B-P, C-S, D-Q

30. The displacement of a damped harmonic oscillator is given by

$$x(t) = e^{-0.1t} \cos(10\pi t + \phi). \text{ Here } t \text{ is in seconds.}$$

The time taken for its amplitude of vibration to drop to half of its initial value is close to :

- (1) 7 s  
(2) 27 s  
(3) 13 s  
(4) 4 s

## PART-B : CHEMISTRY

1. Consider the following statements

- (a) The pH of a mixture containing 400 mL of 0.1 M  $\text{H}_2\text{SO}_4$  and 400 mL of 0.1 M NaOH will be approximately 1.3.
- (b) Ionic product of water is temperature dependent.
- (c) A monobasic acid with  $K_a = 10^{-5}$  has a pH = 5. The degree of dissociation of this acid is 50%.
- (d) The Le Chatelier's principle is not applicable to common-ion effect.

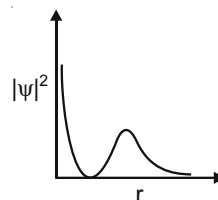
The correct statements are :

- (1) (a), (b) and (d)
- (2) (b) and (c)
- (3) (a) and (b)
- (4) (a), (b) and (c)

2. The oxoacid of sulphur that does not contain bond between sulphur atoms is :

- (1)  $\text{H}_2\text{S}_4\text{O}_6$
- (2)  $\text{H}_2\text{S}_2\text{O}_4$
- (3)  $\text{H}_2\text{S}_2\text{O}_7$
- (4)  $\text{H}_2\text{S}_2\text{O}_3$

3. The graph between  $|\psi|^2$  and  $r$  (radial distance) is shown below. This represents :



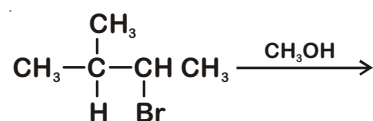
- (1) 1s orbital
- (2) 2s orbital
- (3) 2p orbital
- (4) 3s orbital

4. Which of the following is a condensation polymer ?

- (1) Nylon 6, 6
- (2) Teflon
- (3) Buna - S
- (4) Neoprene

5. The principle of column chromatography is :
- (1) Differential adsorption of the substances on the solid phase.
  - (2) Gravitational force.
  - (3) Differential absorption of the substances on the solid phase.
  - (4) Capillary action.

6. The major product of the following reaction is :



- (1)  $\begin{array}{c} \text{CH}_3 \\ | \\ \text{CH}_3 - \text{C} - \text{CH}_2\text{CH}_3 \\ | \\ \text{OCH}_3 \end{array}$  (2)  $\begin{array}{c} \text{CH}_3 \\ | \\ \text{CH}_3 - \text{C} - \text{CH} - \text{CH}_3 \\ | \quad | \\ \text{H} \quad \text{OCH}_3 \end{array}$
- (3)  $\begin{array}{c} \text{CH}_3 \\ | \\ \text{CH}_3 - \text{C} - \text{CH} = \text{CH}_2 \\ | \\ \text{H} \end{array}$  (4)  $\begin{array}{c} \text{CH}_3 \\ | \\ \text{CH}_3 - \text{C} = \text{CH} - \text{CH}_3 \end{array}$

7. Consider the statements S1 and S2 :

S1 : Conductivity always increases with decrease in the concentration of electrolyte.

S2 : Molar conductivity always increases with decrease in the concentration of electrolyte.

The correct option among the following is :

- (1) S1 is wrong and S2 is correct
- (2) S1 is correct and S2 is wrong
- (3) Both S1 and S2 are wrong
- (4) Both S1 and S2 are correct

8. Consider the following table :

Gas	a/(k Pa dm <sup>6</sup> mol <sup>-1</sup> )	b/(dm <sup>3</sup> mol <sup>-1</sup> )
A	642.32	0.05196
B	155.21	0.04136
C	431.91	0.05196
D	155.21	0.4382

a and b are van der Waals constants. The correct statement about the gases is :

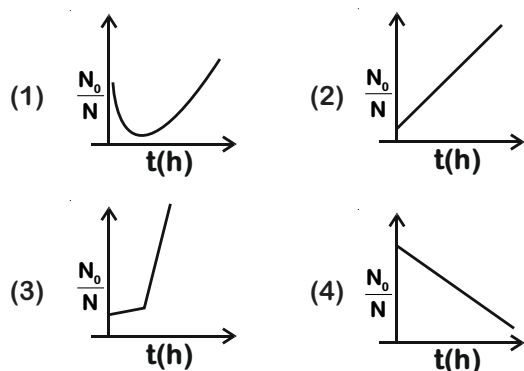
- (1) Gas C will occupy lesser volume than gas A; gas B will be lesser compressible than gas D
- (2) Gas C will occupy more volume than gas A; gas B will be more compressible than gas D
- (3) Gas C will occupy lesser volume than gas A; gas B will be more compressible than gas D
- (4) Gas C will occupy more volume than gas A; gas B will be lesser compressible than gas D

9. Amylopectin is composed of

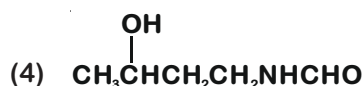
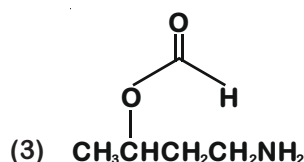
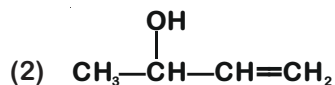
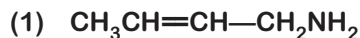
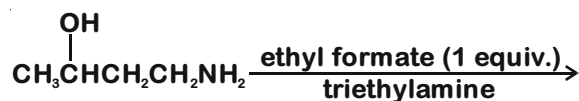
- (1)  $\beta$ -D-glucose,  $C_1-C_4$  and  $C_2-C_6$  linkages
- (2)  $\alpha$ -D-glucose,  $C_1-C_4$  and  $C_2-C_6$  linkages
- (3)  $\beta$ -D-glucose,  $C_1-C_4$  and  $C_1-C_6$  linkages
- (4)  $\alpha$ -D-glucose,  $C_1-C_4$  and  $C_1-C_6$  linkages

10. A bacterial infection in an internal wound grows as  $N'(t) = N_0 \exp(t)$ , where the time  $t$  is in hours. A dose of antibiotic, taken orally, needs 1 hour to reach the wound. Once it reaches there, the bacterial population goes down as

$\frac{dN}{dt} = -5N^2$ . What will be the plot of  $\frac{N_0}{N}$  vs.  $t$  after 1 hour ?



11. The major product of the following reaction is :



12. Consider the hydrated ions of  $\text{Ti}^{2+}$ ,  $\text{V}^{2+}$ ,  $\text{Ti}^{3+}$ , and  $\text{Sc}^{3+}$ . The correct order of their spin-only magnetic moments is :

- (1)  $\text{Sc}^{3+} < \text{Ti}^{3+} < \text{Ti}^{2+} < \text{V}^{2+}$
- (2)  $\text{Ti}^{3+} < \text{Ti}^{2+} < \text{Sc}^{3+} < \text{V}^{2+}$
- (3)  $\text{Sc}^{3+} < \text{Ti}^{3+} < \text{V}^{2+} < \text{Ti}^{2+}$
- (4)  $\text{V}^{2+} < \text{Ti}^{2+} < \text{Ti}^{3+} < \text{Sc}^{3+}$

13. The isoelectronic set of ions is :

- (1)  $\text{N}^{3-}$ ,  $\text{Li}^+$ ,  $\text{Mg}^{2+}$  and  $\text{O}^{2-}$
- (2)  $\text{Li}^+$ ,  $\text{Na}^+$ ,  $\text{O}^{2-}$  and  $\text{F}^-$
- (3)  $\text{N}^{3-}$ ,  $\text{O}^{2-}$ ,  $\text{F}^-$  and  $\text{Na}^+$
- (4)  $\text{F}^-$ ,  $\text{Li}^+$ ,  $\text{Na}^+$  and  $\text{Mg}^{2+}$

14. The alloy used in the construction of aircrafts is :

- (1) Mg - Zn                      (2) Mg - Sn
- (3) Mg - Mn                    (4) Mg - Al

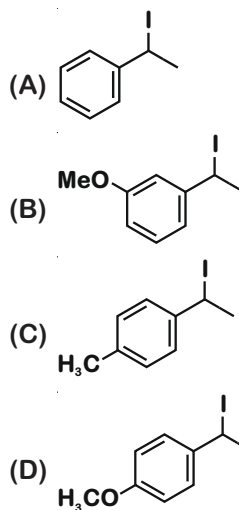
15. Ethylamine ( $\text{C}_2\text{H}_5\text{NH}_2$ ) can be obtained from N-ethylphthalimide on treatment with :

- (1)  $\text{NH}_2\text{NH}_2$                       (2)  $\text{NaBH}_4$
- (3)  $\text{H}_2\text{O}$                               (4)  $\text{CaH}_2$

16. A process will be spontaneous at all temperatures if :

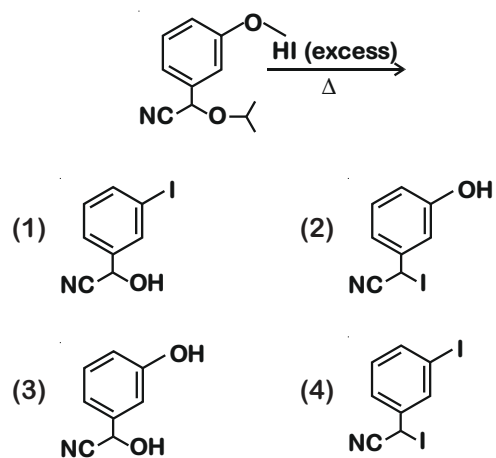
- (1)  $\Delta H < 0$  and  $\Delta S > 0$
- (2)  $\Delta H > 0$  and  $\Delta S < 0$
- (3)  $\Delta H > 0$  and  $\Delta S > 0$
- (4)  $\Delta H < 0$  and  $\Delta S < 0$

17. Increasing rate of  $\text{S}_{\text{N}}1$  reaction in the following compounds is :



- (1) (B) < (A) < (C) < (D)
- (2) (A) < (B) < (D) < (C)
- (3) (B) < (A) < (D) < (C)
- (4) (A) < (B) < (C) < (D)

18. The major product of the following reaction is :

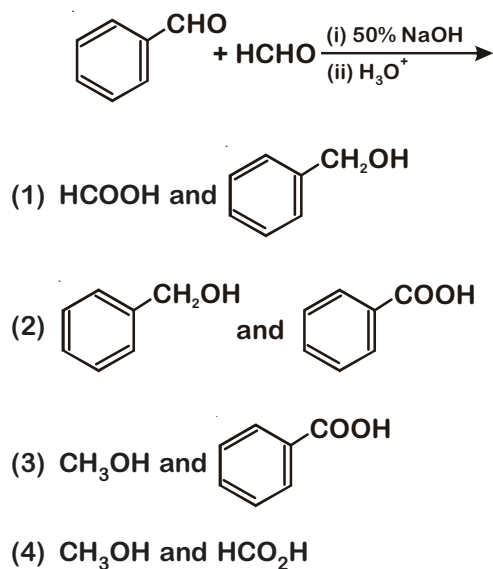


19. The species that can have a trans-isomer is :

(en = ethane-1, 2-diamine, ox = oxalate)

- (1)  $[\text{Zn}(\text{en})\text{Cl}_2]$
- (2)  $[\text{Pt}(\text{en})\text{Cl}_2]$
- (3)  $[\text{Cr}(\text{en})_2(\text{ox})]^+$
- (4)  $[\text{Pt}(\text{en})_2\text{Cl}_2]^{2+}$

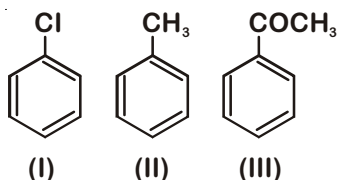
20. Major products of the following reaction are :



21. The correct order of catenation is :

- (1)  $C > Si > Ge \approx Sn$
- (2)  $C > Sn > Si \approx Ge$
- (3)  $Si > Sn > C > Ge$
- (4)  $Ge > Sn > Si > C$

22. The increasing order of the reactivity of the following compounds towards electrophilic aromatic substitution reactions is :



- |                    |                    |
|--------------------|--------------------|
| (1) $I < III < II$ | (2) $III < II < I$ |
| (3) $II < I < III$ | (4) $III < I < II$ |

23. During the change of  $O_2$  to  $O_2^-$ , the incoming electron goes to the orbital :

- |                |                     |
|----------------|---------------------|
| (1) $\pi 2p_x$ | (2) $\pi^* 2p_x$    |
| (3) $\pi 2p_y$ | (4) $\sigma^* 2p_z$ |

24. The regions of the atmosphere, where clouds form and where we live, respectively, are :

- (1) Troposphere and Troposphere
- (2) Stratosphere and Troposphere
- (3) Troposphere and Stratosphere
- (4) Stratosphere and Stratosphere

25. At room temperature, a dilute solution of urea is prepared by dissolving 0.60 g of urea in 360 g of water. If the vapour pressure of pure water at this temperature is 35 mmHg, lowering of vapour pressure will be : (molar mass of urea = 60 g mol<sup>-1</sup>)

- |                |                |
|----------------|----------------|
| (1) 0.031 mmHg | (2) 0.017 mmHg |
| (3) 0.028 mmHg | (4) 0.027 mmHg |

26. A gas undergoes physical adsorption on a surface and follows the given Freundlich adsorption isotherm equation

$$\frac{x}{m} = kp^{0.5}$$

Adsorption of the gas increases with :

- (1) Increase in p and decrease in T
- (2) Decrease in p and decrease in T
- (3) Increase in p and increase in T
- (4) Decrease in p and increase in T

27. The synonym for water gas when used in the production of methanol is :

- (1) fuel gas
- (2) syn gas
- (3) laughing gas
- (4) natural gas

28. At 300 K and 1 atmospheric pressure, 10 mL of a hydrocarbon required 55 mL of  $O_2$  for complete combustion, and 40 mL of  $CO_2$  is formed. The formula of the hydrocarbon is :

- (1)  $C_4H_{10}$
- (2)  $C_4H_8$
- (3)  $C_4H_6$
- (4)  $C_4H_7Cl$

29. Three complexes,  $[CoCl(NH_3)_5]^{2+}$ (I),  $[Co(NH_3)_5H_2O]^{3+}$ (II) and  $[Co(NH_3)_6]^{3+}$ (III) absorb light in the visible region. The correct order of the wavelength of light absorbed by them is :

- (1) (I) > (II) > (III)
- (2) (II) > (I) > (III)
- (3) (III) > (I) > (II)
- (4) (III) > (II) > (I)

30. Match the refining methods (Column I) with metals (Column II).

Column I (Refining methods)	Column II (Metals)
(I) Liquation	(a) Zr
(II) Zone Refining	(b) Ni
(III) Mond Process	(c) Sn
(IV) Van Arkel Method	(d) Ga
(1) (I)-(c); (II)-(a); (III)-(b); (IV)-(d)	
(2) (I)-(b); (II)-(d); (III)-(a); (IV)-(c)	
(3) (I)-(c); (II)-(d); (III)-(b); (IV)-(a)	
(4) (I)-(b); (II)-(c); (III)-(d); (IV)-(a)	



## PART-C : MATHEMATICS

1. All the pairs  $(x, y)$  that satisfy the inequality

$$2^{\sqrt{\sin^2 x - 2\sin x + 5}} \cdot \frac{1}{4^{\sin^2 y}} \leq 1 \text{ also satisfy the equation :}$$

- (1)  $\sin x = |\sin y|$
- (2)  $\sin x = 2 \sin y$
- (3)  $2 \sin x = \sin y$
- (4)  $2|\sin x| = 3 \sin y$

2. If  $a > 0$  and  $z = \frac{(1+i)^2}{a-i}$ , has magnitude  $\sqrt{\frac{2}{5}}$ , then  $\bar{z}$  is equal to :

- (1)  $-\frac{1}{5} + \frac{3}{5}i$
- (2)  $-\frac{3}{5} - \frac{1}{5}i$
- (3)  $\frac{1}{5} - \frac{3}{5}i$
- (4)  $-\frac{1}{5} - \frac{3}{5}i$

3. The number of 6 digit numbers that can be formed using the digits 0, 1, 2, 5, 7 and 9 which are divisible by 11 and no digit is repeated, is :

- (1) 72
- (2) 48
- (3) 60
- (4) 36

4. The value of  $\int_0^{2\pi} [\sin 2x(1 + \cos 3x)] dx$ , where  $[t]$  denotes the greatest integer function, is :

- (1)  $\pi$
- (2)  $-\pi$
- (3)  $-2\pi$
- (4)  $2\pi$

5. If  $\Delta_1 = \begin{vmatrix} x & \sin \theta & \cos \theta \\ -\sin \theta & -x & 1 \\ \cos \theta & 1 & x \end{vmatrix}$  and

$\Delta_2 = \begin{vmatrix} x & \sin 2\theta & \cos 2\theta \\ -\sin 2\theta & -x & 1 \\ \cos 2\theta & 1 & x \end{vmatrix}, x \neq 0$ ; then

for all  $\theta \in \left(0, \frac{\pi}{2}\right)$ :

(1)  $\Delta_1 + \Delta_2 = -2x^3$

(2)  $\Delta_1 - \Delta_2 = -2x^3$

(3)  $\Delta_1 + \Delta_2 = -2(x^3 + x - 1)$

(4)  $\Delta_1 - \Delta_2 = x(\cos 2\theta - \cos 4\theta)$

6. If  $f(x) = \begin{cases} \frac{\sin(p+1)x + \sin x}{x}, & x < 0 \\ q, & x = 0 \\ \frac{\sqrt{x+x^2} - \sqrt{x}}{x^{3/2}}, & x > 0 \end{cases}$

is continuous at  $x = 0$ , then the ordered pair  $(p, q)$  is equal to :

(1)  $\left(\frac{5}{2}, \frac{1}{2}\right)$

(2)  $\left(-\frac{3}{2}, \frac{1}{2}\right)$

(3)  $\left(-\frac{3}{2}, -\frac{1}{2}\right)$

(4)  $\left(-\frac{1}{2}, \frac{3}{2}\right)$

7. If the length of the perpendicular from the point  $(\beta, 0, \beta)$  ( $\beta \neq 0$ ) to the line,

$$\frac{x}{1} = \frac{y-1}{0} = \frac{z+1}{-1} \text{ is } \sqrt{\frac{3}{2}}, \text{ then } \beta \text{ is equal to :}$$

- (1)  $-1$  (2)  $-2$   
(3)  $1$  (4)  $2$

8.  $\lim_{n \rightarrow \infty} \left( \frac{(n+1)^{1/3}}{n^{4/3}} + \frac{(n+2)^{1/3}}{n^{4/3}} + \dots + \frac{(2n)^{1/3}}{n^{4/3}} \right)$  is equal to :

- (1)  $\frac{4}{3} (2)^{4/3}$  (2)  $\frac{3}{4} (2)^{4/3} - \frac{3}{4}$   
(3)  $\frac{4}{3} (2)^{3/4}$  (4)  $\frac{3}{4} (2)^{4/3} - \frac{4}{3}$

9. The line  $x = y$  touches a circle at the point  $(1, 1)$ . If the circle also passes through the point  $(1, -3)$ , then its radius is :

- (1)  $3\sqrt{2}$  (2)  $2$   
(3)  $2\sqrt{2}$  (4)  $3$

10. Which one of the following Boolean expressions is a tautology ?

- (1)  $(p \vee q) \vee (p \vee \sim q)$
- (2)  $(p \wedge q) \vee (p \wedge \sim q)$
- (3)  $(p \vee q) \wedge (p \vee \sim q)$
- (4)  $(p \vee q) \wedge (\sim p \vee \sim q)$

11. If  $\lim_{x \rightarrow 1} \frac{x^4 - 1}{x - 1} = \lim_{x \rightarrow k} \frac{x^3 - k^3}{x^2 - k^2}$ , then k is :

- (1)  $\frac{4}{3}$
- (2)  $\frac{3}{2}$
- (3)  $\frac{8}{3}$
- (4)  $\frac{3}{8}$

12. If a directrix of a hyperbola centred at the origin and passing through the point  $(4, -2\sqrt{3})$  is  $5x = 4\sqrt{5}$  and its eccentricity is e, then :

- (1)  $4e^4 + 8e^2 - 35 = 0$
- (2)  $4e^4 - 24e^2 + 35 = 0$
- (3)  $4e^4 - 12e^2 - 27 = 0$
- (4)  $4e^4 - 24e^2 + 27 = 0$

13. If the line  $x - 2y = 12$  is tangent to the ellipse

$\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$  at the point  $\left(3, \frac{-9}{2}\right)$ , then the length of the latus rectum of the ellipse is :

- (1) 5
- (2)  $8\sqrt{3}$
- (3)  $12\sqrt{2}$
- (4) 9

14. Let  $A(3, 0, -1)$ ,  $B(2, 10, 6)$  and  $C(1, 2, 1)$  be the vertices of a triangle and  $M$  be the mid point of  $AC$ . If  $G$  divides  $BM$  in the ratio,  $2 : 1$  then  $\cos(\angle GOA)$  ( $O$  being the origin) is equal to :

- (1)  $\frac{1}{6\sqrt{10}}$
- (2)  $\frac{1}{\sqrt{30}}$
- (3)  $\frac{1}{2\sqrt{15}}$
- (4)  $\frac{1}{\sqrt{15}}$

15. If the system of linear equations

$$x + y + z = 5$$

$$x + 2y + 2z = 6$$

$x + 3y + \lambda z = \mu$ , ( $\lambda, \mu \in \mathbb{R}$ ), has infinitely many solutions, then the value of  $\lambda + \mu$  is :

- (1) 10
- (2) 12
- (3) 7
- (4) 9

16. Assume that each born child is equally likely to be a boy or a girl. If two families have two children each, then the conditional probability that all children are girls given that at least two are girls is :

- (1)  $\frac{1}{11}$  (2)  $\frac{1}{12}$   
 (3)  $\frac{1}{10}$  (4)  $\frac{1}{17}$

17. If for some  $x \in \mathbb{R}$ , the frequency distribution of the marks obtained by 20 students in a test is :

Marks	2	3	5	7
Frequency	$(x+1)^2$	$2x-5$	$x^2-3x$	$x$

Then the mean of the marks is :

- (1) 3.2 (2) 3.0  
 (3) 2.5 (4) 2.8

18. If the circles  $x^2 + y^2 + 5Kx + 2y + K = 0$  and  $2(x^2 + y^2) + 2Kx + 3y - 1 = 0$ , ( $K \in \mathbb{R}$ ), intersect at the points P and Q, then the line  $4x + 5y - K = 0$  passes through P and Q, for :

- (1) Exactly one value of K  
 (2) Infinitely many values of K  
 (3) Exactly two values of K  
 (4) No value of K

19. The region represented by  $|x-y| \leq 2$  and  $|x+y| \leq 2$  is bounded by a :

- (1) Square of side length  $2\sqrt{2}$  units  
 (2) Square of area 16 sq. units  
 (3) Rhombus of side length 2 units  
 (4) Rhombus of area  $8\sqrt{2}$  sq. units

20. If  $a_1, a_2, a_3, \dots, a_n$  are in A.P. and  $a_1 + a_4 + a_7 + \dots + a_{16} = 114$ , then  $a_1 + a_6 + a_{11} + a_{16}$  is equal to :

- (1) 98                      (2) 38  
(3) 64                      (4) 76

21. If  $Q(0, -1, -3)$  is the image of the point  $P$  in the plane  $3x - y + 4z = 2$  and  $R$  is the point  $(3, -1, -2)$ , then the area (in sq. units) of  $\Delta PQR$  is :

- (1)  $\frac{\sqrt{65}}{2}$                       (2)  $\frac{\sqrt{91}}{4}$   
(3)  $2\sqrt{13}$                       (4)  $\frac{\sqrt{91}}{2}$

=                      =                      =                      =

23. If the coefficients of  $x^2$  and  $x^3$  are both zero, in the expansion of the expression  $(1 + ax + bx^2)(1 - 3x)^{15}$  in powers of  $x$ , then the ordered pair  $(a, b)$  is equal to :

- (1)  $(-54, 315)$   
(2)  $(28, 861)$   
(3)  $(-21, 714)$   
(4)  $28, 315$

22. Let  $f(x) = x^2, x \in \mathbb{R}$ . For any  $A \subseteq \mathbb{R}$ , define  $g(A) = \{x \in \mathbb{R} : f(x) \in A\}$ . If  $S = [0, 4]$ , then which one of the following statements is not true ?

- (1)  $f(g(S)) = S$                       (2)  $g(f(S)) = g(S)$   
(3)  $g(f(S)) \neq S$                       (4)  $f(g(S)) \neq f(S)$

24. The sum

$$\frac{3 \times 1^3}{1^2} + \frac{5 \times (1^3 + 2^3)}{1^2 + 2^2} + \frac{7 \times (1^3 + 2^3 + 3^3)}{1^2 + 2^2 + 3^2} + \dots$$

upto 10<sup>th</sup> term, is :

- (1) 620                      (2) 600  
(3) 680                      (4) 660

25. Let  $f(x) = e^x - x$  and  $g(x) = x^2 - x$ ,  $\forall x \in \mathbb{R}$ . Then the set of all  $x \in \mathbb{R}$ , where the function  $h(x) = (f \circ g)(x)$  is increasing, is :

- (1)  $\left[-1, \frac{-1}{2}\right] \cup \left[\frac{1}{2}, \infty\right)$       (2)  $[0, \infty)$   
(3)  $\left[0, \frac{1}{2}\right] \cup [1, \infty)$       (4)  $\left[\frac{-1}{2}, 0\right] \cup [1, \infty)$

26. If  $\alpha$  and  $\beta$  are the roots of the quadratic

equation,  $x^2 + x \sin \theta - 2 \sin \theta = 0$ ,  $\theta \in \left(0, \frac{\pi}{2}\right)$ , then

$\frac{\alpha^{12} + \beta^{12}}{(\alpha^{-12} + \beta^{-12}) \cdot (\alpha - \beta)^{24}}$  is equal to :

- (1)  $\frac{2^{12}}{(\sin \theta - 8)^6}$                       (2)  $\frac{2^{12}}{(\sin \theta - 4)^{12}}$   
(3)  $\frac{2^6}{(\sin \theta + 8)^{12}}$                       (4)  $\frac{2^{12}}{(\sin \theta + 8)^{12}}$

27. If  $y = y(x)$  is the solution of the differential

equation  $\frac{dy}{dx} = (\tan x - y) \sec^2 x$ ,  $x \in \left(-\frac{\pi}{2}, \frac{\pi}{2}\right)$ ,

such that  $y(0) = 0$ , then  $y\left(-\frac{\pi}{4}\right)$  is equal to :

- (1)  $\frac{1}{e} - 2$   
(2)  $\frac{1}{2} - e$   
(3)  $e - 2$   
(4)  $2 + \frac{1}{e}$



28. Let  $f : \mathbb{R} \rightarrow \mathbb{R}$  be differentiable at  $c \in \mathbb{R}$  and  $f(c) = 0$ . If  $g(x) = |f(x)|$ , then at  $x = c$ ,  $g$  is :

- (1) not differentiable if  $f'(c) = 0$
- (2) differentiable if  $f'(c) = 0$
- (3) not differentiable
- (4) differentiable if  $f'(c) \neq 0$

29. ABC is a triangular park with  $AB = AC = 100$  metres. A vertical tower is situated at the mid-point of BC. If the angles of elevation of the top of the tower at A and B are  $\cot^{-1}(3\sqrt{2})$  and  $\operatorname{cosec}^{-1}(2\sqrt{2})$  respectively, then the height of the tower (in metres) is :

- (1) 20
- (2)  $10\sqrt{5}$
- (3) 25
- (4)  $\frac{100}{3\sqrt{3}}$

30. If  $\int \frac{dx}{(x^2 - 2x + 10)^2}$

$$= A \left( \tan^{-1} \left( \frac{x-1}{3} \right) + \frac{f(x)}{x^2 - 2x + 10} \right) + C$$

where C is a constant of integration, then :

(1)  $A = \frac{1}{81}$  and  $f(x) = 3(x-1)$

(2)  $A = \frac{1}{54}$  and  $f(x) = 3(x-1)$

(3)  $A = \frac{1}{27}$  and  $f(x) = 9(x-1)$

(4)  $A = \frac{1}{54}$  and  $f(x) = 9(x-1)^2$

