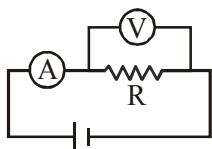


**TEST PAPER OF JEE(MAIN) EXAMINATION – 2019****(Held On Thursday 10<sup>th</sup> JANUARY, 2019) TIME : 02 : 30 PM To 05 : 30 PM****PHYSICS**

1. Two forces P and Q of magnitude 2F and 3F, respectively, are at an angle  $\theta$  with each other. If the force Q is doubled, then their resultant also gets doubled. Then, the angle is :  
 (1)  $30^\circ$  (2)  $60^\circ$  (3)  $90^\circ$  (4)  $120^\circ$

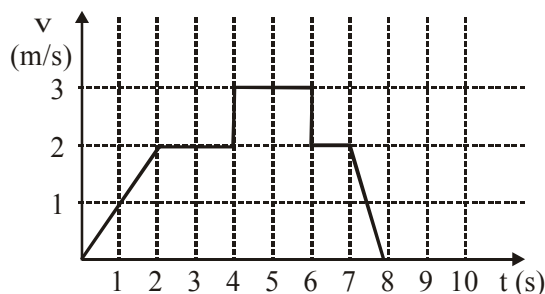
2. The actual value of resistance R, shown in the figure is  $30\Omega$ . This is measured in an experiment as shown using the standard formula  $R = \frac{V}{I}$ , where V and I are the readings of the voltmeter and ammeter, respectively. If the measured value of R is 5% less, then the internal resistance of the voltmeter is :



- (1)  $350\Omega$  (2)  $570\Omega$  (3)  $35\Omega$  (4)  $600\Omega$

3. An unknown metal of mass 192 g heated to a temperature of  $100^\circ\text{C}$  was immersed into a brass calorimeter of mass 128 g containing 240 g of water a temperature of  $8.4^\circ\text{C}$ . Calculate the specific heat of the unknown metal if water temperature stabilizes at  $21.5^\circ\text{C}$  (Specific heat of brass is  $394\text{ J kg}^{-1}\text{ K}^{-1}$ )  
 (1)  $1232\text{ J kg}^{-1}\text{ K}^{-1}$  (2)  $458\text{ J kg}^{-1}\text{ K}^{-1}$   
 (3)  $654\text{ J kg}^{-1}\text{ K}^{-1}$  (4)  $916\text{ J kg}^{-1}\text{ K}^{-1}$

4. A particle starts from the origin at time  $t = 0$  and moves along the positive x-axis. The graph of velocity with respect to time is shown in figure. What is the position of the particle at time  $t = 5\text{ s}$  ?



- (1) 6 m (2) 9 m (3) 3 m (4) 10 m

5. The self induced emf of a coil is 25 volts. When the current in it is changed at uniform rate from 10 A to 25 A in 1s, the change in the energy of the inductance is :

- (1) 437.5 J (2) 637.5 J  
 (3) 740 J (4) 540 J

6. A current of 2 mA was passed through an unknown resistor which dissipated a power of 4.4 W. Dissipated power when an ideal power supply of 11V is connected across it is :

- (1)  $11 \times 10^{-5}\text{ W}$  (2)  $11 \times 10^{-4}\text{ W}$   
 (3)  $11 \times 10^5\text{ W}$  (4)  $11 \times 10^{-3}\text{ W}$

7. The diameter and height of a cylinder are measured by a meter scale to be  $12.6 \pm 0.1$  cm and  $34.2 \pm 0.1$  cm, respectively. What will be the value of its volume in appropriate significant figures ?
- (1)  $4260 \pm 80$  cm<sup>3</sup>      (2)  $4300 \pm 80$  cm<sup>3</sup>  
(3)  $4264.4 \pm 81.0$  cm<sup>3</sup>      (4)  $4264 \pm 81$  cm<sup>3</sup>
8. At some location on earth the horizontal component of earth's magnetic field is  $18 \times 10^{-6}$  T. At this location, magnetic needle of length 0.12 m and pole strength 1.8 Am is suspended from its mid-point using a thread, it makes  $45^\circ$  angle with horizontal in equilibrium. To keep this needle horizontal, the vertical force that should be applied at one of its ends is :
- (1)  $3.6 \times 10^{-5}$  N      (2)  $6.5 \times 10^{-5}$  N  
(3)  $1.3 \times 10^{-5}$  N      (4)  $1.8 \times 10^{-5}$  N
9. The modulation frequency of an AM radio station is 250 kHz, which is 10% of the carrier wave. If another AM station approaches you for license what broadcast frequency will you allot ?
- (1) 2750 kHz      (2) 2000 kHz  
(3) 2250 kHz      (4) 2900 kHz
10. A hoop and a solid cylinder of same mass and radius are made of a permanent magnetic material with their magnetic moment parallel to their respective axes. But the magnetic moment of hoop is twice of solid cylinder. They are placed in a uniform magnetic field in such a manner that their magnetic moments make a small angle with the field. If the oscillation periods of hoop and cylinder are  $T_h$  and  $T_c$  respectively, then :
- (1)  $T_h = 0.5 T_c$       (2)  $T_h = 2 T_c$   
(3)  $T_h = 1.5 T_c$       (4)  $T_h = T_c$
11. The electric field of a plane polarized electromagnetic wave in free space at time  $t = 0$  is given by an expression
- $$\vec{E}(x, y) = 10\hat{j} \cos [(6x + 8z)]$$
- The magnetic field  $\vec{B}$  (x, z, t) is given by : (c is the velocity of light)
- (1)  $\frac{1}{c}(6\hat{k} + 8\hat{i})\cos[(6x - 8z + 10ct)]$   
(2)  $\frac{1}{c}(6\hat{k} - 8\hat{i})\cos[(6x + 8z - 10ct)]$   
(3)  $\frac{1}{c}(6\hat{k} + 8\hat{i})\cos[(6x + 8z - 10ct)]$   
(4)  $\frac{1}{c}(6\hat{k} - 8\hat{i})\cos[(6x + 8z + 10ct)]$

**12.** Consider the nuclear fission

Given that the binding energy/nucleon of  $\text{Ne}^{20}$ ,  $\text{He}^4$  and  $\text{C}^{12}$  are, respectively, 8.03 MeV, 7.07 MeV and 7.86 MeV, identify the correct statement :

- (1) 8.3 MeV energy will be released
- (2) energy of 12.4 MeV will be supplied
- (3) energy of 11.9 MeV has to be supplied
- (4) energy of 3.6 MeV will be released

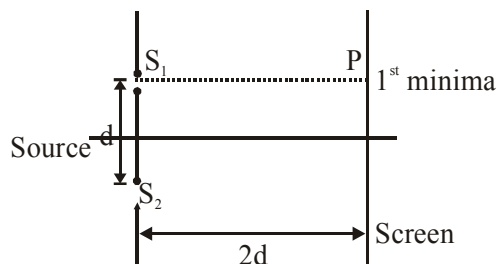
- 13.** Two vectors  $\vec{A}$  and  $\vec{B}$  have equal magnitudes. The magnitude of  $(\vec{A} + \vec{B})$  is 'n' times the magnitude of  $(\vec{A} - \vec{B})$ . The angle between  $\vec{A}$  and  $\vec{B}$  is :

- (1)  $\sin^{-1} \left[ \frac{n^2 - 1}{n^2 + 1} \right]$       (2)  $\cos^{-1} \left[ \frac{n - 1}{n + 1} \right]$   
(3)  $\cos^{-1} \left[ \frac{n^2 - 1}{n^2 + 1} \right]$       (4)  $\sin^{-1} \left[ \frac{n - 1}{n + 1} \right]$

- 14.** A particle executes simple harmonic motion with an amplitude of 5 cm. When the particle is at 4 cm from the mean position, the magnitude of its velocity in SI units is equal to that of its acceleration. Then, its periodic time in seconds is :

- (1)  $\frac{7}{3}\pi$       (2)  $\frac{3}{8}\pi$   
(3)  $\frac{4\pi}{3}$       (4)  $\frac{8\pi}{3}$

15. Consider a Young's double slit experiment as shown in figure. What should be the slit separation  $d$  in terms of wavelength  $\lambda$  such that the first minima occurs directly in front of the slit ( $S_1$ ) ?



- (1)  $\frac{\lambda}{2(5-\sqrt{2})}$  (2)  $\frac{\lambda}{(5-\sqrt{2})}$   
 (3)  $\frac{\lambda}{(\sqrt{5}-2)}$  (4)  $\frac{\lambda}{2(\sqrt{5}-2)}$

16. The eye can be regarded as a single refracting surface. The radius of curvature of this surface is equal to that of cornea (7.8 mm). This surface separates two media of refractive indices 1 and 1.34. Calculate the distance from the refracting surface at which a parallel beam of light will come to focus.

- (1) 2 cm (2) 1 cm  
 (3) 3.1 cm (4) 4.0 cm

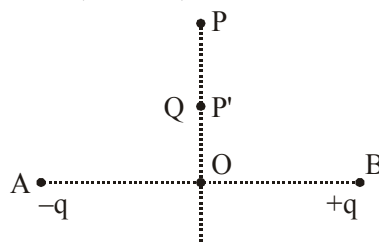
17. Half mole of an ideal monoatomic gas is heated at constant pressure of 1 atm from 20 °C to 90°C. Work done by gas is close to : ( Gas constant  $R = 8.31 \text{ J/mol.K}$ )  
 (1) 73 J (2) 291 J (3) 581 J (4) 146 J

18. A metal plate of area  $1 \times 10^{-4} \text{ m}^2$  is illuminated by a radiation of intensity  $16 \text{ mW/m}^2$ . The work function of the metal is 5 eV. The energy of the incident photons is 10 eV and only 10% of it produces photo electrons. The number of emitted photo electrons per second and their maximum energy, respectively, will be : [ $1 \text{ eV} = 1.6 \times 10^{-19} \text{ J}$ ]

- (1)  $10^{10}$  and 5 eV (2)  $10^{14}$  and 10 eV  
 (3)  $10^{12}$  and 5 eV (4)  $10^{11}$  and 5 eV

19. Charges  $-q$  and  $+q$  located at A and B, respectively, constitute an electric dipole. Distance  $AB = 2a$ , O is the mid point of the dipole and OP is perpendicular to AB. A charge Q is placed at P where  $OP = y$  and  $y \gg 2a$ . The charge Q experiences an electrostatic force F. If Q is now moved along the equatorial line

to P' such that  $OP' = \left(\frac{y}{3}\right)$ , the force on Q will be close to :  $\left(\frac{y}{3} \gg 2a\right)$



- (1)  $\frac{F}{3}$  (2)  $3F$  (3)  $9F$  (4)  $27F$

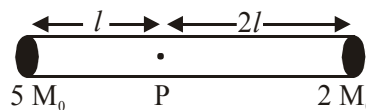
- 20.** Two stars of masses  $3 \times 10^{31}$  kg each, and at distance  $2 \times 10^{11}$  m rotate in a plane about their common centre of mass O. A meteorite passes through O moving perpendicular to the star's rotation plane. In order to escape from the gravitational field of this double star, the minimum speed that meteorite should have at O is : (Take Gravitational constant  $G = 6.67 \times 10^{-11} \text{ Nm}^2 \text{ kg}^{-2}$ )

- (1)  $1.4 \times 10^5 \text{ m/s}$       (2)  $24 \times 10^4 \text{ m/s}$   
 (3)  $3.8 \times 10^4 \text{ m/s}$       (4)  $2.8 \times 10^5 \text{ m/s}$

- 21.** A closed organ pipe has a fundamental frequency of 1.5 kHz. The number of overtones that can be distinctly heard by a person with this organ pipe will be : (Assume that the highest frequency a person can hear is 20,000 Hz)

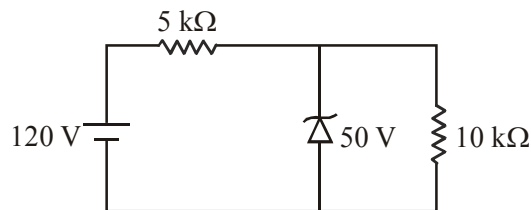
- (1) 7      (2) 5      (3) 6      (4) 4

- 22.** A rigid massless rod of length  $3l$  has two masses attached at each end as shown in the figure. The rod is pivoted at point P on the horizontal axis (see figure). When released from initial horizontal position, its instantaneous angular acceleration will be :



- (1)  $\frac{g}{2l}$       (2)  $\frac{7g}{3l}$       (3)  $\frac{g}{13l}$       (4)  $\frac{g}{3l}$

- 23.** For the circuit shown below, the current through the Zener diode is :



- (1) 5 mA      (2) Zero      (3) 14 mA      (4) 9 mA

- 24.** Four equal point charges  $Q$  each are placed in the  $xy$  plane at  $(0, 2)$ ,  $(4, 2)$ ,  $(4, -2)$  and  $(0, -2)$ . The work required to put a fifth charge  $Q$  at the origin of the coordinate system will be :

(1)  $\frac{Q^2}{2\sqrt{2}\pi\epsilon_0}$                       (2)  $\frac{Q^2}{4\pi\epsilon_0}\left(1+\frac{1}{\sqrt{5}}\right)$   
 (3)  $\frac{Q^2}{4\pi\epsilon_0}\left(1+\frac{1}{\sqrt{3}}\right)$                       (4)  $\frac{Q^2}{4\pi\epsilon_0}$

- 25.** A cylindrical plastic bottle of negligible mass is filled with 310 ml of water and left floating in a pond with still water. If pressed downward slightly and released, it starts performing simple harmonic motion at angular frequency  $\omega$ . If the radius of the bottle is 2.5 cm then  $\omega$  close to : (density of water =  $10^3 \text{ kg / m}^3$ )

(1)  $5.00 \text{ rad s}^{-1}$                       (2)  $1.25 \text{ rad s}^{-1}$   
 (3)  $3.75 \text{ rad s}^{-1}$                       (4)  $2.50 \text{ rad s}^{-1}$

- 26.** A parallel plate capacitor having capacitance 12 pF is charged by a battery to a potential difference of 10 V between its plates. The charging battery is now disconnected and a porcelain slab of dielectric constant 6.5 is slipped between the plates the work done by the capacitor on the slab is :

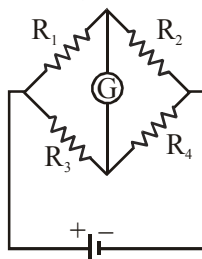
(1) 692 pJ                                      (2) 60 pJ  
 (3) 508 pJ                                      (4) 560 pJ

- 27.** Two kg of a monoatomic gas is at a pressure of  $4 \times 10^4 \text{ N/m}^2$ . The density of the gas is  $8 \text{ kg / m}^3$ . What is the order of energy of the gas due to its thermal motion ?

(1)  $10^3 \text{ J}$                                       (2)  $10^5 \text{ J}$   
 (3)  $10^6 \text{ J}$                                       (4)  $10^4 \text{ J}$

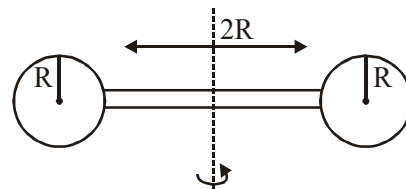
28. A particle which is experiencing a force, given by  $\vec{F} = 3\vec{i} - 12\vec{j}$ , undergoes a displacement of  $\vec{d} = 4\vec{i}$ . If the particle had a kinetic energy of 3 J at the beginning of the displacement, what is its kinetic energy at the end of the displacement ?  
 (1) 15 J    (2) 10 J    (3) 12 J    (4) 9 J

29. The Wheatstone bridge shown in Fig. here, gets balanced when the carbon resistor used as  $R_1$  has the colour code ( Orange, Red, Brown). The resistors  $R_2$  and  $R_4$  are  $80\Omega$  and  $40\Omega$ , respectively. Assuming that the colour code for the carbon resistors gives their accurate values, the colour code for the carbon resistor, used as  $R_3$ , would be :



- (1) Red, Green, Brown  
 (2) Brown, Blue, Brown  
 (3) Grey, Black, Brown  
 (4) Brown, Blue, Black

30. Two identical spherical balls of mass  $M$  and radius  $R$  each are stuck on two ends of a rod of length  $2R$  and mass  $M$  (see figure). The moment of inertia of the system about the axis passing perpendicularly through the centre of the rod is :



- (1)  $\frac{152}{15}MR^2$                       (2)  $\frac{17}{15}MR^2$   
 (3)  $\frac{137}{15}MR^2$                       (4)  $\frac{209}{15}MR^2$

**TEST PAPER OF JEE(MAIN) EXAMINATION – 2019****(Held On Thursday 10<sup>th</sup> JANUARY, 2019) TIME : 02 : 30 PM To 05 : 30 PM****CHEMISTRY**

1. An ideal gas undergoes isothermal compression from 5 m<sup>3</sup> against a constant external pressure of 4 Nm<sup>-2</sup>. Heat released in this process is used to increase the temperature of 1 mole of Al. If molar heat capacity of Al is 24 J mol<sup>-1</sup> K<sup>-1</sup>, the temperature of Al increases by :

(1)  $\frac{3}{2}$  K      (2)  $\frac{2}{3}$  K      (3) 1 K      (4) 2 K

2. The 71<sup>st</sup> electron of an element X with an atomic number of 71 enters into the orbital :  
(1) 4f      (2) 6p      (3) 6s      (4) 5d

3. The number of 2-centre-2-electron and 3-centre-2-electron bonds in B<sub>2</sub>H<sub>6</sub>, respectively, are :  
(1) 2 and 4      (2) 2 and 1  
(3) 2 and 2      (4) 4 and 2

4. The amount of sugar (C<sub>12</sub>H<sub>22</sub>O<sub>11</sub>) required to prepare 2 L of its 0.1 M aqueous solution is :  
(1) 68.4 g    (2) 17.1 g    (3) 34.2 g    (4) 136.8 g

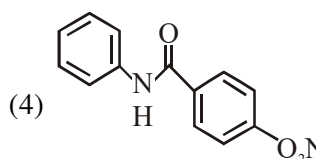
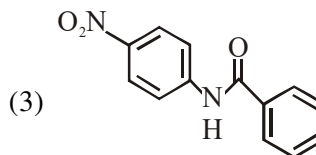
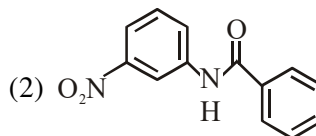
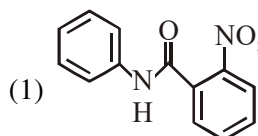
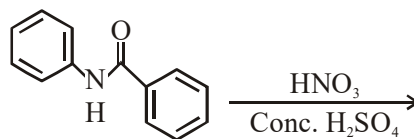
5. Among the following reactions of hydrogen with halogens, the one that requires a catalyst is :

(1)  $\text{H}_2 + \text{I}_2 \rightarrow 2\text{HI}$       (2)  $\text{H}_2 + \text{F}_2 \rightarrow 2\text{HF}$   
(3)  $\text{H}_2 + \text{Cl}_2 \rightarrow 2\text{HCl}$     (4)  $\text{H}_2 + \text{Br}_2 \rightarrow 2\text{HBr}$

6. Sodium metal on dissolution in liquid ammonia gives a deep blue solution due to the formation of:

(1) sodium ion-ammonia complex  
(2) sodamide  
(3) sodium-ammonia complex  
(4) ammoniated electrons

7. What will be the major product in the following mononitration reaction ?



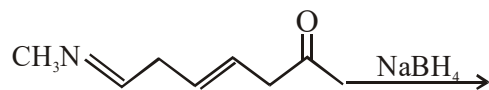


8. In the cell  $\text{Pt(s)}|\text{H}_2(\text{g}, 1\text{bar})|\text{HCl(aq)}|\text{Ag(s)}|\text{Pt(s)}$  the cell potential is 0.92 when a  $10^{-6}$  molal HCl solution is used. The standard electrode potential of  $(\text{AgCl}/\text{Ag}, \text{Cl}^-)$  electrode is :

$$\left\{ \text{given, } \frac{2.303RT}{F} = 0.06\text{V at } 298\text{K} \right\}$$

- (1) 0.20 V (2) 0.76 V (3) 0.40 V (4) 0.94 V

9. The major product of the following reaction is:

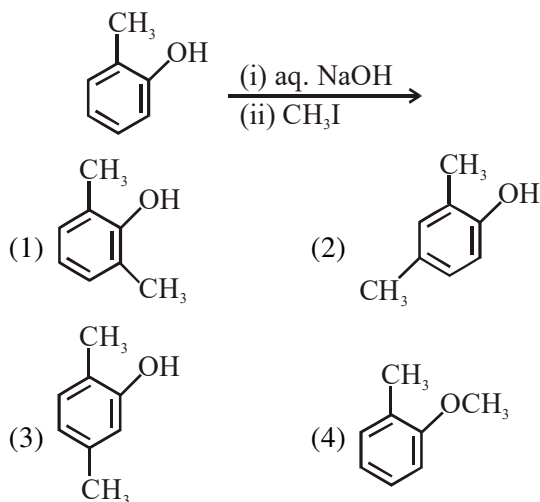


- (1)  $\text{CH}_3\text{N}=\text{CH}-\text{CH}_2-\text{CH}=\text{CH}-\text{CH}_2-\text{CH}(\text{OH})\text{CH}_3$   
 (2)  $\text{CH}_3\text{N}=\text{CH}-\text{CH}_2-\text{CH}_2-\text{CH}_2-\text{CH}_2-\text{CH}_2-\text{CH}(\text{OH})\text{CH}_3$   
 (3)  $\text{CH}_3\text{N}-\text{CH}_2-\text{CH}_2-\text{CH}_2-\text{CH}=\text{CH}-\text{CH}_2-\text{CH}(\text{OH})\text{CH}_3$   
 (4)  $\text{CH}_3\text{N}-\text{CH}_2-\text{CH}_2-\text{CH}_2-\text{CH}_2-\text{CH}_2-\text{CH}_2-\text{CH}(\text{OH})\text{CH}_3$

10. The pair that contains two P–H bonds in each of the oxoacids is :

- (1)  $\text{H}_3\text{PO}_2$  and  $\text{H}_4\text{P}_2\text{O}_5$   
 (2)  $\text{H}_4\text{P}_2\text{O}_5$  and  $\text{H}_4\text{P}_2\text{O}_6$   
 (3)  $\text{H}_3\text{PO}_3$  and  $\text{H}_3\text{PO}_2$   
 (4)  $\text{H}_4\text{P}_2\text{O}_5$  and  $\text{H}_3\text{PO}_3$

11. The major product of the following reaction is:



12. The difference in the number of unpaired electrons of a metal ion in its high-spin and low-spin octahedral complexes is two. The metal ion is :

- (1)  $\text{Fe}^{2+}$  (2)  $\text{Co}^{2+}$  (3)  $\text{Mn}^{2+}$  (4)  $\text{Ni}^{2+}$

13. A compound of formula  $\text{A}_2\text{B}_3$  has the hcp lattice. Which atom forms the hcp lattice and what fraction of tetrahedral voids is occupied by the other atoms :

- (1) hcp lattice-A,  $\frac{2}{3}$  Tetrahedral voids-B  
 (2) hcp lattice-B,  $\frac{1}{3}$  Tetrahedral voids-A  
 (3) hcp lattice-B,  $\frac{2}{3}$  Tetrahedral voids-A  
 (4) hcp lattice-A  $\frac{1}{3}$  Tetrahedral voids-B

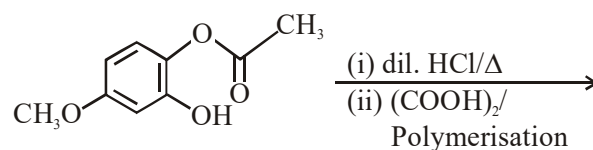
- 14.** The reaction that is NOT involved in the ozone layer depletion mechanism in the stratosphere is:

- (1)  $\text{HOCl(g)} \xrightarrow{h\nu} \dot{\text{O}}\text{H(g)} + \dot{\text{Cl}}\text{(g)}$
- (2)  $\text{CF}_2\text{Cl}_2\text{(g)} \xrightarrow{uv} \dot{\text{Cl}}\text{(g)} + \dot{\text{C}}\text{F}_2\text{Cl(g)}$
- (3)  $\text{CH}_4 + 2\text{O}_3 \rightarrow 3\text{CH}_2=\text{O} + 3\text{H}_2\text{O}$
- (4)  $\text{Cl}\dot{\text{O}}\text{(g)} + \text{O(g)} \rightarrow \dot{\text{Cl}}\text{(g)} + \text{O}_2\text{(g)}$

- 15.** The process with negative entropy change is :

- (1) Dissolution of iodine in water
- (2) Synthesis of ammonia from  $\text{N}_2$  and  $\text{H}_2$
- (3) Dissolution of  $\text{CaSO}_4\text{(s)}$  to  $\text{CaO(s)}$  and  $\text{SO}_3\text{(g)}$
- (4) Sublimation of dry ice

- 16.** The major product of the following reaction is:

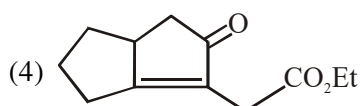
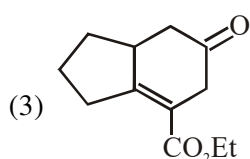
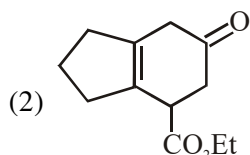
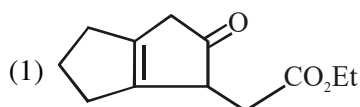
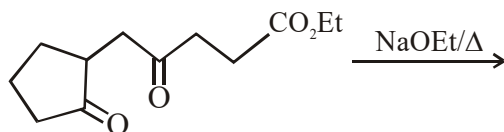


- (1)
- (2)
- (3)
- (4)

- 17.** A reaction of cobalt(III) chloride and ethylenediamine in a 1 : 2 mole ratio generates two isomeric products A (violet coloured) B (green coloured). A can show optical activity, B is optically inactive. What type of isomers does A and B represent ?

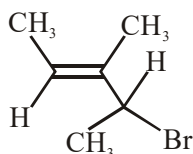
- (1) Geometrical isomers
- (2) Ionisation isomers]
- (3) Coordination isomers
- (4) Linkage isomers

18. The major product obtained in the following reaction is :



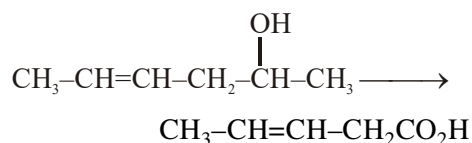
19. Which of the following tests cannot be used for identifying amino acids ?  
 (1) Biuret test (2) Xanthoproteic test  
 (3) Barfoed test (4) Ninhydrin test

20. What is the IUPAC name of the following compound ?



- (1) 3-Bromo-1, 2-dimethylbut-1-ene]  
 (2) 4-Bromo-3-methylpent-2-ene  
 (3) 2-Bromo-3-methylpent-3-ene  
 (4) 3-Bromo-3-methyl-1, 2-dimethylprop-1-ene

21. Which is the most suitable reagent for the following transformation ?



- (1) alkaline  $\text{KMnO}_4$  (2)  $\text{I}_2/\text{NaOH}$   
 (3) Tollen's reagent (4)  $\text{CrO}_2/\text{CS}_2$

22. The correct match between item 'I' and item 'II' is :

Item 'I' (compound)	Item 'II' (reagent)
(A) Lysine	(P) 1-naphthol
(B) Furfural	(Q) ninhydrin
(C) Benzyl alcohol	(R) $\text{KMnO}_4$
(D) Styrene	(S) Ceric ammonium nitrate

- (1) (A)→(Q), (B)→(P), (C)→(S), (D)→(R)  
 (2) (A)→(Q), (B)→(R), (C)→(S), (D)→(P)  
 (3) (A)→(Q), (B)→(P), (C)→(R), (D)→(S)  
 (4) (A)→(R), (B)→(P), (C)→(Q), (D)→(S)

23. In the reaction of oxalate with permanganate in acidic medium, the number of electrons involved in producing one molecule of  $\text{CO}_2$  is :

- (1) 10 (2) 2 (3) 1 (4) 5

24. 5.1g  $\text{NH}_4\text{SH}$  is introduced in 3.0 L evacuated flask at  $327^\circ\text{C}$ . 30% of the solid  $\text{NH}_4\text{SH}$  decomposed to  $\text{NH}_3$  and  $\text{H}_2\text{S}$  as gases. The  $K_p$  of the reaction at  $327^\circ\text{C}$  is ( $R = 0.082 \text{ L atm mol}^{-1}\text{K}^{-1}$ , Molar mass of S = 32 g  $\text{mol}^{-1}$ , molar mass of N = 14g  $\text{mol}^{-1}$ )

- (1)  $1 \times 10^{-4} \text{ atm}^2$  (2)  $4.9 \times 10^{-3} \text{ atm}^2$   
 (3)  $0.242 \text{ atm}^2$  (4)  $0.242 \times 10^{-4} \text{ atm}^2$

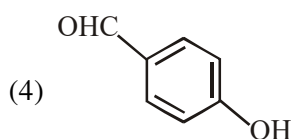
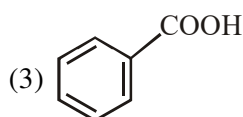
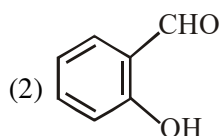
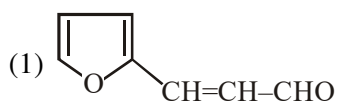
**25.** The electrolytes usually used in the electroplating of gold and silver, respectively, are :

- (1)  $[\text{Au}(\text{OH})_4]^-$  and  $[\text{Ag}(\text{OH})_2]^-$   
 (2)  $[\text{Au}(\text{CN})_2]^-$  and  $[\text{Ag} \text{Cl}_2]^-$   
 (3)  $[\text{Au}(\text{NH}_3)_2]^+$  and  $[\text{Ag}(\text{CN})_2]^-$   
 (4)  $[\text{Au}(\text{CN})_2]^-$  and  $[\text{Ag}(\text{CN})_2]^-$

**26.** Elevation in the boiling point for 1 molal solution of glucose is 2 K. The depression in the freezing point of 2 molal solutions of glucose in the same solvent is 2 K. The relation between  $K_b$  and  $K_f$  is:

- (1)  $K_b = 0.5 K_f$                       (2)  $K_b = 2 K_f$   
 (3)  $K_b = 1.5 K_f$                       (4)  $K_b = K_f$

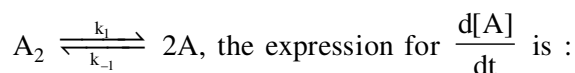
**27.** An aromatic compound 'A' having molecular formula  $\text{C}_7\text{H}_6\text{O}_2$  on treating with aqueous ammonia and heating forms compound 'B'. The compound 'B' on reaction with molecular bromine and potassium hydroxide provides compound 'C' having molecular formula  $\text{C}_6\text{H}_7\text{N}$ . The structure of 'A' is :



**28.** The ground state energy of hydrogen atom is  $-13.6 \text{ eV}$ . The energy of second excited state  $\text{He}^+$  ion in  $\text{eV}$  is :

- (1)  $-6.04$     (2)  $-27.2$     (3)  $-54.4$     (4)  $-3.4$

**29.** For an elementary chemical reaction,



- (1)  $2k_1[\text{A}_2] - k_{-1}[\text{A}]^2$       (2)  $k_1[\text{A}_2] - k_{-1}[\text{A}]^2$   
 (3)  $2k_1[\text{A}_2] - 2k_{-1}[\text{A}]^2$       (4)  $k_1[\text{A}_2] + k_{-1}[\text{A}]^2$

**30.** Haemoglobin and gold sol are examples of :

- (1) negatively charged sols  
 (2) positively charged sols  
 (3) negatively and positively charged sols, respectively  
 (4) positively and negatively charged sols, respectively

**TEST PAPER OF JEE(MAIN) EXAMINATION – 2019****(Held On Thursday 10<sup>th</sup> JANUARY, 2019) TIME : 2 : 30 PM To 5 : 30 PM****MATHEMATICS**

1. Let  $z = \left(\frac{\sqrt{3}}{2} + \frac{i}{2}\right)^5 + \left(\frac{\sqrt{3}}{2} - \frac{i}{2}\right)^5$ . If  $R(z)$  and  $I[z]$

respectively denote the real and imaginary parts of  $z$ , then :

- (1)  $R(z) > 0$  and  $I(z) > 0$   
 (2)  $R(z) < 0$  and  $I(z) > 0$   
 (3)  $R(z) = -3$   
 (4)  $I(z) = 0$

2. Let  $a_1, a_2, a_3, \dots, a_{10}$  be in G.P. with  $a_i > 0$  for  $i = 1, 2, \dots, 10$  and  $S$  be the set of pairs  $(r, k)$ ,  $r, k \in \mathbb{N}$  (the set of natural numbers) for which

$$\begin{vmatrix} \log_e a_1^r a_2^k & \log_e a_2^r a_3^k & \log_e a_3^r a_4^k \\ \log_e a_4^r a_5^k & \log_e a_5^r a_6^k & \log_e a_6^r a_7^k \\ \log_e a_7^r a_8^k & \log_e a_8^r a_9^k & \log_e a_9^r a_{10}^k \end{vmatrix} = 0$$

Then the number of elements in  $S$ , is :

- (1) Infinitely many      (2) 4  
 (3) 10      (4) 2

3. The positive value of  $\lambda$  for which the co-efficient of  $x^2$  in the expression

$$x^2 \left( \sqrt{x} + \frac{\lambda}{x^2} \right)^{10} \text{ is } 720, \text{ is :}$$

- (1)  $\sqrt{5}$       (2) 4  
 (3)  $2\sqrt{2}$       (4) 3

4. The value of  $\cos \frac{\pi}{2^2} \cdot \cos \frac{\pi}{2^3} \cdot \dots \cdot \cos \frac{\pi}{2^{10}} \cdot \sin \frac{\pi}{2^{10}}$  is :

- (1)  $\frac{1}{256}$       (2)  $\frac{1}{2}$   
 (3)  $\frac{1}{512}$       (4)  $\frac{1}{1024}$

5. The value of  $\int_{-\pi/2}^{\pi/2} \frac{dx}{[x] + [\sin x] + 4}$ , where  $[t]$

denotes the greatest integer less than or equal to  $t$ , is :

(1)  $\frac{1}{12}(7\pi + 5)$                       (2)  $\frac{3}{10}(4\pi - 3)$

(3)  $\frac{1}{12}(7\pi - 5)$                       (4)  $\frac{3}{20}(4\pi - 3)$

6. If the probability of hitting a target by a shooter, in any shot, is  $1/3$ , then the minimum number of independent shots at the target required by him so that the probability of hitting the target

at least once is greater than  $\frac{5}{6}$ , is :

(1) 6                                              (2) 5  
(3) 4                                              (4) 3

7. If mean and standard deviation of 5 observations  $x_1, x_2, x_3, x_4, x_5$  are 10 and 3, respectively, then the variance of 6 observations  $x_1, x_2, \dots, x_5$  and  $-50$  is equal to :

(1) 582.5                                              (2) 507.5  
(3) 586.5                                              (4) 509.5

8. The length of the chord of the parabola  $x^2 = 4y$  having equation  $x - \sqrt{2}y + 4\sqrt{2} = 0$  is :

(1)  $2\sqrt{11}$                                               (2)  $3\sqrt{2}$   
(3)  $6\sqrt{3}$                                               (4)  $8\sqrt{2}$

9. Let  $A = \begin{bmatrix} 2 & b & 1 \\ b & b^2 + 1 & b \\ 1 & b & 2 \end{bmatrix}$  where  $b > 0$ . Then the

minimum value of  $\frac{\det(A)}{b}$  is :

- (1)  $\sqrt{3}$                                       (2)  $-\sqrt{3}$   
 (3)  $-2\sqrt{3}$                                       (4)  $2\sqrt{3}$

10. The tangent to the curve,  $y = xe^{x^2}$  passing through the point  $(1, e)$  also passes through the point :

- (1)  $\left(\frac{4}{3}, 2e\right)$                                       (2)  $(2, 3e)$   
 (3)  $\left(\frac{5}{3}, 2e\right)$                                       (4)  $(3, 6e)$

11. The number of values of  $\theta \in (0, \pi)$  for which the system of linear equations

$$x + 3y + 7z = 0$$

$$-x + 4y + 7z = 0$$

$$(\sin 3\theta)x + (\cos 2\theta)y + 2z = 0$$

has a non-trivial solution, is :

- (1) One                                              (2) Three  
 (3) Four                                              (4) Two

12. If  $\int_0^x f(t)dt = x^2 + \int_x^1 t^2 f(t)dt$ , then  $f'(1/2)$  is :

- (1)  $\frac{6}{25}$  (2)  $\frac{24}{25}$   
 (3)  $\frac{18}{25}$  (4)  $\frac{4}{5}$

13. Let  $f : (-1,1) \rightarrow \mathbb{R}$  be a function defined by  $f(x) = \max\{-|x|, -\sqrt{1-x^2}\}$ . If  $K$  be the set of all points at which  $f$  is not differentiable, then  $K$  has exactly :

- (1) Three elements (2) One element  
 (3) Five elements (4) Two elements

14. Let  $S = \left\{ (x,y) \in \mathbb{R}^2 : \frac{y^2}{1+r} - \frac{x^2}{1-r} = 1 \right\}$ , where  $r \neq \pm 1$ . Then  $S$  represents :

- (1) A hyperbola whose eccentricity is  $\frac{2}{\sqrt{r+1}}$ ,  
 where  $0 < r < 1$ .  
 (2) An ellipse whose eccentricity is  $\frac{1}{\sqrt{r+1}}$ ,  
 where  $r > 1$   
 (3) A hyperbola whose eccentricity is  $\frac{2}{\sqrt{1-r}}$ ,  
 when  $0 < r < 1$ .  
 (4) An ellipse whose eccentricity is  $\sqrt{\frac{2}{r+1}}$ ,  
 when  $r > 1$



15. If  $\sum_{r=0}^{25} \left\{ {}^{50}C_r \cdot {}^{50-r}C_{25-r} \right\} = K \left( {}^{50}C_{25} \right)$ , then K is equal to :  
 (1)  $2^{25} - 1$  (2)  $(25)^2$  (3)  $2^{25}$  (4)  $2^{24}$

16. Let N be the set of natural numbers and two functions f and g be defined as  $f, g : N \rightarrow N$   
 such that :  $f(n) = \begin{cases} \frac{n+1}{2} & \text{if n is odd} \\ \frac{n}{2} & \text{if n is even} \end{cases}$   
 and  $g(n) = n - (-1)^n$ . The fog is :  
 (1) Both one-one and onto  
 (2) One-one but not onto  
 (3) Neither one-one nor onto  
 (4) onto but not one-one

17. The values of  $\lambda$  such that sum of the squares of the roots of the quadratic equation,  $x^2 + (3 - \lambda)x + 2 = \lambda$  has the least value is :  
 (1) 2 (2)  $\frac{4}{9}$   
 (3)  $\frac{15}{8}$  (4) 1

18. Two vertices of a triangle are (0,2) and (4,3). If its orthocentre is at the origin, then its third vertex lies in which quadrant ?  
 (1) Fourth  
 (2) Second  
 (3) Third  
 (4) First

- 19.** Two sides of a parallelogram are along the lines,  $x + y = 3$  and  $x - y + 3 = 0$ . If its diagonals intersect at (2,4), then one of its vertex is :
- (1) (2,6)                      (2) (2,1)  
 (3) (3,5)                      (4) (3,6)

- 20.** Let  $\vec{\alpha} = (\lambda - 2)\vec{a} + \vec{b}$  and  $\vec{\beta} = (4\lambda - 2)\vec{a} + 3\vec{b}$  be two given vectors where vectors  $\vec{a}$  and  $\vec{b}$  are non-collinear. The value of  $\lambda$  for which vectors  $\vec{\alpha}$  and  $\vec{\beta}$  are collinear, is :

- (1) -3                              (2) 4  
 (3) 3                                (4) -4

- 21.** The value of  $\cot\left(\sum_{n=1}^{19}\cot^{-1}\left(1+\sum_{p=1}^n2p\right)\right)$  is :

- (1)  $\frac{22}{23}$       (2)  $\frac{23}{22}$       (3)  $\frac{21}{19}$       (4)  $\frac{19}{21}$

- 22.** With the usual notation, in  $\Delta ABC$ , if  $\angle A + \angle B = 120^\circ$ ,  $a = \sqrt{3} + 1$  and  $b = \sqrt{3} - 1$ , then the ratio  $\angle A : \angle B$ , is :
- (1) 7 : 1                              (2) 5 : 3  
 (3) 9 : 7                              (4) 3 : 1

- 23.** The plane which bisects the line segment joining the points  $(-3, -3, 4)$  and  $(3, 7, 6)$  at right angles, passes through which one of the following points ?
- |                  |                  |
|------------------|------------------|
| (1) $(4, -1, 7)$ | (2) $(4, 1, -2)$ |
| (3) $(-2, 3, 5)$ | (4) $(2, 1, 3)$  |

- 24.** Consider the following three statements :  
 $P$  : 5 is a prime number.  
 $Q$  : 7 is a factor of 192.  
 $R$  : L.C.M. of 5 and 7 is 35.  
 Then the truth value of which one of the following statements is true ?
- (1)  $(P \wedge Q) \vee (\sim R)$   
 (2)  $(\sim P) \wedge (\sim Q \wedge R)$   
 (3)  $(\sim P) \vee (Q \wedge R)$   
 (4)  $P \vee (\sim Q \wedge R)$
- 25.** On which of the following lines lies the point of intersection of the line,  $\frac{x-4}{2} = \frac{y-5}{2} = \frac{z-3}{1}$  and the plane,  $x + y + z = 2$  ?
- (1)  $\frac{x-2}{2} = \frac{y-3}{2} = \frac{z+3}{3}$   
 (2)  $\frac{x-4}{1} = \frac{y-5}{1} = \frac{z-5}{-1}$   
 (3)  $\frac{x-1}{1} = \frac{y-3}{2} = \frac{z+4}{-5}$   
 (4)  $\frac{x+3}{3} = \frac{4-y}{3} = \frac{z+1}{-2}$

26. Let  $f$  be a differentiable function such that

$$f'(x) = 7 - \frac{3f(x)}{4x}, (x > 0) \text{ and } f(1) \neq 4.$$

Then  $\lim_{x \rightarrow 0^+} xf\left(\frac{1}{x}\right)$ :

- (1) Exists and equals 4
- (2) Does not exist
- (3) Exist and equals 0
- (4) Exists and equals  $\frac{4}{7}$

27. A helicopter is flying along the curve given by  $y - x^{3/2} = 7$ , ( $x \geq 0$ ). A soldier positioned at the point  $\left(\frac{1}{2}, 7\right)$  wants to shoot down the helicopter when it is nearest to him. Then this nearest distance is :

- (1)  $\frac{1}{2}$
- (2)  $\frac{1}{3}\sqrt{\frac{7}{3}}$
- (3)  $\frac{1}{6}\sqrt{\frac{7}{3}}$
- (4)  $\frac{\sqrt{5}}{6}$

28. If  $\int x^5 e^{-4x^3} dx = \frac{1}{48} e^{-4x^3} f(x) + C$ , where  $C$  is a constant of integration, then  $f(x)$  is equal to :

- (1)  $-4x^3 - 1$                       (2)  $4x^3 + 1$   
(3)  $-2x^3 - 1$                       (4)  $-2x^3 + 1$

29. The curve amongst the family of curves, represented by the differential equation,  $(x^2 - y^2)dx + 2xy dy = 0$  which passes through  $(1,1)$  is :

- (1) A circle with centre on the y-axis  
(2) A circle with centre on the x-axis  
(3) An ellipse with major axis along the y-axis  
(4) A hyperbola with transverse axis along the x-axis

30. If the area of an equilateral triangle inscribed in the circle,  $x^2 + y^2 + 10x + 12y + c = 0$  is  $27\sqrt{3}$  sq. units then  $c$  is equal to :

(1) 20

(2) 25

(3) 13

(4) -25