

```
import pandas as pd
df=pd.read_csv("Heart.csv")
```

```
print(df.to_string())
```

	Unnamed: 0	Age	Sex	ChestPain	RestBP	Chol	Fbs	RestECG	MaxHR	ExAng	Oldpeak	Slope	Ca	Thal	AHD
0	1	63	1	typical	145	233	1	2	150	0	2.3	3	0.0	fixed	No
1	2	67	1	asymptomatic	160	286	0	2	108	1	1.5	2	3.0	normal	Yes
2	3	67	1	asymptomatic	120	229	0	2	129	1	2.6	2	2.0	reversible	Yes
3	4	37	1	nonanginal	130	250	0	0	187	0	3.5	3	0.0	normal	No
4	5	41	0	nontypical	130	204	0	2	172	0	1.4	1	0.0	normal	No
5	6	56	1	nontypical	120	236	0	0	178	0	0.8	1	0.0	normal	No
6	7	62	0	asymptomatic	140	268	0	2	160	0	3.6	3	2.0	normal	Yes
7	8	57	0	asymptomatic	120	354	0	0	163	1	0.6	1	0.0	normal	No
8	9	63	1	asymptomatic	130	254	0	2	147	0	1.4	2	1.0	reversible	Yes
9	10	53	1	asymptomatic	140	203	1	2	155	1	3.1	3	0.0	reversible	Yes
10	11	57	1	asymptomatic	140	192	0	0	148	0	0.4	2	0.0	fixed	No
11	12	56	0	nontypical	140	294	0	2	153	0	1.3	2	0.0	normal	No
12	13	56	1	nonanginal	130	256	1	2	142	1	0.6	2	1.0	fixed	Yes
13	14	44	1	nontypical	120	263	0	0	173	0	0.0	1	0.0	reversible	No
14	15	52	1	nonanginal	172	199	1	0	162	0	0.5	1	0.0	reversible	No
15	16	57	1	nonanginal	150	168	0	0	174	0	1.6	1	0.0	normal	No
16	17	48	1	nontypical	110	229	0	0	168	0	1.0	3	0.0	reversible	Yes
17	18	54	1	asymptomatic	140	239	0	0	160	0	1.2	1	0.0	normal	No
18	19	48	0	nonanginal	130	275	0	0	139	0	0.2	1	0.0	normal	No
19	20	49	1	nontypical	130	266	0	0	171	0	0.6	1	0.0	normal	No
20	21	64	1	typical	110	211	0	2	144	1	1.8	2	0.0	normal	No
21	22	58	0	typical	150	283	1	2	162	0	1.0	1	0.0	normal	No
22	23	58	1	nontypical	120	284	0	2	160	0	1.8	2	0.0	normal	Yes
23	24	58	1	nonanginal	132	224	0	2	173	0	3.2	1	2.0	reversible	Yes
24	25	60	1	asymptomatic	130	206	0	2	132	1	2.4	2	2.0	reversible	Yes
25	26	50	0	nonanginal	120	219	0	0	158	0	1.6	2	0.0	normal	No
26	27	58	0	nonanginal	120	340	0	0	172	0	0.0	1	0.0	normal	No
27	28	66	0	typical	150	226	0	0	114	0	2.6	3	0.0	normal	No
28	29	43	1	asymptomatic	150	247	0	0	171	0	1.5	1	0.0	normal	No
29	30	40	1	asymptomatic	110	167	0	2	114	1	2.0	2	0.0	reversible	Yes
30	31	69	0	typical	140	239	0	0	151	0	1.8	1	2.0	normal	No
31	32	60	1	asymptomatic	117	230	1	0	160	1	1.4	1	2.0	reversible	Yes
32	33	64	1	nonanginal	140	335	0	0	158	0	0.0	1	0.0	normal	Yes
33	34	59	1	asymptomatic	135	234	0	0	161	0	0.5	2	0.0	reversible	No
34	35	44	1	nonanginal	130	233	0	0	179	1	0.4	1	0.0	normal	No
35	36	42	1	asymptomatic	140	226	0	0	178	0	0.0	1	0.0	normal	No
36	37	43	1	asymptomatic	120	177	0	2	120	1	2.5	2	0.0	reversible	Yes
37	38	57	1	asymptomatic	150	276	0	2	112	1	0.6	2	1.0	fixed	Yes
38	39	55	1	asymptomatic	132	353	0	0	132	1	1.2	2	1.0	reversible	Yes
39	40	61	1	nonanginal	150	243	1	0	137	1	1.0	2	0.0	normal	No
40	41	65	0	asymptomatic	150	225	0	2	114	0	1.0	2	3.0	reversible	Yes
41	42	40	1	typical	140	199	0	0	178	1	1.4	1	0.0	reversible	No
42	43	71	0	nontypical	160	302	0	0	162	0	0.4	1	2.0	normal	No
43	44	59	1	nonanginal	150	212	1	0	157	0	1.6	1	0.0	normal	No
44	45	61	0	asymptomatic	130	330	0	2	169	0	0.0	1	0.0	normal	Yes
45	46	58	1	nonanginal	112	230	0	2	165	0	2.5	2	1.0	reversible	Yes
46	47	51	1	nonanginal	110	175	0	0	123	0	0.6	1	0.0	normal	No
47	48	50	1	asymptomatic	150	243	0	2	128	0	2.6	2	0.0	reversible	Yes
48	49	65	0	nonanginal	140	417	1	2	157	0	0.8	1	1.0	normal	No
49	50	53	1	nonanginal	130	197	1	2	152	0	1.2	3	0.0	normal	No
50	51	41	0	nontypical	105	198	0	0	168	0	0.0	1	1.0	normal	No
51	52	65	1	asymptomatic	120	177	0	0	140	0	0.4	1	0.0	reversible	No
52	53	44	1	asymptomatic	112	290	0	2	153	0	0.0	1	1.0	normal	Yes
53	54	44	1	nontypical	130	219	0	2	188	0	0.0	1	0.0	normal	No
54	55	60	1	asymptomatic	130	253	0	0	144	1	1.4	1	1.0	reversible	Yes
55	56	54	1	asymptomatic	124	266	0	2	109	1	2.2	2	1.0	reversible	Yes
56	57	50	1	nonanginal	140	233	0	0	163	0	0.6	2	1.0	reversible	Yes

```
#a) Find standard deviation, variance of every numerical attribute.
```

```
df = df.apply(pd.to_numeric, errors='coerce')
```

```
print(df.std()) #Standard Deviation
```

```

Unnamed: 0    87.612784
Age           9.038662
Sex           0.467299
ChestPain      NaN
RestBP        17.599748
Chol          51.776918
Fbs           0.356198
RestECG       0.994971
MaxHR         22.875003
ExAng         0.469794
Oldpeak       1.161075
Slope         0.616226
Ca            0.937438

```

```

Thal      NaN
AHD       NaN
dtype: float64

```

```
print(df.var()) #Variance
```

```

Unnamed: 0    7676.000000
Age           81.697419
Sex           0.218368
ChestPain     NaN
RestBP        309.751120
Chol          2680.849190
Fbs           0.126877
RestECG       0.989968
MaxHR         523.265775
ExAng         0.220707
Oldpeak       1.348095
Slope         0.379735
Ca            0.878791
Thal          NaN
AHD           NaN
dtype: float64

```

```

#b) Find covariance and perform Correlation analysis using Correlation coefficient.
print(df.cov()) #Covariance

```

```

      Unnamed: 0      Age      Sex  ChestPain      RestBP  \
Unnamed: 0  7676.000000 -1.874172 -2.900662      NaN -33.966887
Age          -1.874172  81.697419 -0.411995      NaN  45.328678
Sex           -2.900662 -0.411995  0.218368      NaN -0.530107
ChestPain      NaN      NaN      NaN      NaN      NaN
RestBP        -33.966887  45.328678 -0.530107      NaN  309.751120
Chol          -433.301325  97.787489 -4.836994      NaN  118.573339
Fbs            -1.231788  0.381614  0.007967      NaN  1.099207
RestECG       -13.096026  1.338797  0.010065      NaN  2.566455
MaxHR         -211.413907 -81.423065 -0.520184      NaN -18.258005
ExAng          -0.016556  0.389220  0.032096      NaN  0.535473
Oldpeak       -12.246026  2.138850  0.055436      NaN  3.865638
Slope         -1.536424  0.901034  0.010808      NaN  1.273053
Ca              3.844223  3.066396  0.040964      NaN  1.639436
Thal           NaN      NaN      NaN      NaN      NaN
AHD            NaN      NaN      NaN      NaN      NaN

```

```

      Chol      Fbs      RestECG      MaxHR      ExAng      Oldpeak  \
Unnamed: 0 -433.301325 -1.231788 -13.096026 -211.413907 -0.016556 -12.246026
Age          97.787489  0.381614  1.338797  -81.423065  0.389220  2.138850
Sex          -4.836994  0.007967  0.010065  -0.520184  0.032096  0.055436
ChestPain      NaN      NaN      NaN      NaN      NaN      NaN
RestBP        118.573339  1.099207  2.566455 -18.258005  0.535473  3.865638
Chol          2680.849190  0.181496  8.811521  -4.064651  1.491345  2.799282
Fbs            0.181496  0.126877  0.024654  -0.063996  0.004295  0.002377
RestECG        8.811521  0.024654  0.989968  -1.897941  0.039670  0.131850
MaxHR          -4.064651 -0.063996 -1.897941  523.265775 -4.063307 -9.112209
ExAng           1.491345  0.004295  0.039670  -4.063307  0.220707  0.157216
Oldpeak         2.799282  0.002377  0.131850  -9.112209  0.157216  1.348095
Slope          -0.129598  0.013147  0.082126  -5.435501  0.074618  0.413219
Ca              5.791385  0.048394  0.119706  -5.686270  0.064162  0.322753
Thal           NaN      NaN      NaN      NaN      NaN      NaN
AHD            NaN      NaN      NaN      NaN      NaN      NaN

```

```

      Slope      Ca      Thal      AHD
Unnamed: 0 -1.536424  3.844223  NaN  NaN
Age          0.901034  3.066396  NaN  NaN
Sex          0.010808  0.040964  NaN  NaN
ChestPain      NaN      NaN  NaN  NaN
RestBP         1.273053  1.639436  NaN  NaN
Chol          -0.129598  5.791385  NaN  NaN
Fbs            0.013147  0.048394  NaN  NaN
RestECG        0.082126  0.119706  NaN  NaN
MaxHR         -5.435501 -5.686270  NaN  NaN
ExAng           0.074618  0.064162  NaN  NaN
Oldpeak         0.413219  0.322753  NaN  NaN
Slope          0.379735  0.063747  NaN  NaN
Ca              0.063747  0.878791  NaN  NaN
Thal           NaN      NaN  NaN  NaN
AHD            NaN      NaN  NaN  NaN

```

```
print(df.corr()) #Corelation
```

```

      Unnamed: 0      Age      Sex  ChestPain      RestBP      Chol  \
Unnamed: 0    1.000000 -0.002367 -0.070849      NaN -0.022028 -0.095518

```

Age	-0.002367	1.000000	-0.097542	NaN	0.284946	0.208950
Sex	-0.070849	-0.097542	1.000000	NaN	-0.064456	-0.199915
ChestPain	NaN	NaN	NaN	NaN	NaN	NaN
RestBP	-0.022028	0.284946	-0.064456	NaN	1.000000	0.130120
Chol	-0.095518	0.208950	-0.199915	NaN	0.130120	1.000000
Fbs	-0.039471	0.118530	0.047862	NaN	0.175340	0.009841
RestECG	-0.150232	0.148868	0.021647	NaN	0.146560	0.171043
MaxHR	-0.105488	-0.393806	-0.048663	NaN	-0.045351	-0.003432
ExAng	-0.000402	0.091661	0.146201	NaN	0.064762	0.061310
Oldpeak	-0.120384	0.203805	0.102173	NaN	0.189171	0.046564
Slope	-0.028458	0.161770	0.037533	NaN	0.117382	-0.004062
Ca	0.046938	0.362605	0.093185	NaN	0.098773	0.119000
Thal	NaN	NaN	NaN	NaN	NaN	NaN
AHD	NaN	NaN	NaN	NaN	NaN	NaN

	Fbs	RestECG	MaxHR	ExAng	Oldpeak	Slope	\
Unnamed: 0	-0.039471	-0.150232	-0.105488	-0.000402	-0.120384	-0.028458	
Age	0.118530	0.148868	-0.393806	0.091661	0.203805	0.161770	
Sex	0.047862	0.021647	-0.048663	0.146201	0.102173	0.037533	
ChestPain	NaN	NaN	NaN	NaN	NaN	NaN	
RestBP	0.175340	0.146560	-0.045351	0.064762	0.189171	0.117382	
Chol	0.009841	0.171043	-0.003432	0.061310	0.046564	-0.004062	
Fbs	1.000000	0.069564	-0.007854	0.025665	0.005747	0.059894	
RestECG	0.069564	1.000000	-0.083389	0.084867	0.114133	0.133946	
MaxHR	-0.007854	-0.083389	1.000000	-0.378103	-0.343085	-0.385601	
ExAng	0.025665	0.084867	-0.378103	1.000000	0.288223	0.257748	
Oldpeak	0.005747	0.114133	-0.343085	0.288223	1.000000	0.577537	
Slope	0.059894	0.133946	-0.385601	0.257748	0.577537	1.000000	
Ca	0.145478	0.128343	-0.264246	0.145570	0.295832	0.110119	
Thal	NaN	NaN	NaN	NaN	NaN	NaN	
AHD	NaN	NaN	NaN	NaN	NaN	NaN	

	Ca	Thal	AHD
Unnamed: 0	0.046938	NaN	NaN
Age	0.362605	NaN	NaN
Sex	0.093185	NaN	NaN
ChestPain	NaN	NaN	NaN
RestBP	0.098773	NaN	NaN
Chol	0.119000	NaN	NaN
Fbs	0.145478	NaN	NaN
RestECG	0.128343	NaN	NaN
MaxHR	-0.264246	NaN	NaN
ExAng	0.145570	NaN	NaN
Oldpeak	0.295832	NaN	NaN
Slope	0.110119	NaN	NaN
Ca	1.000000	NaN	NaN
Thal	NaN	NaN	NaN
AHD	NaN	NaN	NaN

```
#e) Perform the data discretization using equi frequency binning method on age attribute
bins = pd.cut(df['Age'], bins=5, labels=False)
df['Age'] = bins
```

```
print(df.head(5))
```

	Unnamed: 0	Age	Sex	ChestPain	RestBP	Chol	Fbs	RestECG	MaxHR	\
0	1	3	1	typical	145	233	1	2	150	
1	2	3	1	asymptomatic	160	286	0	2	108	
2	3	3	1	asymptomatic	120	229	0	2	129	
3	4	0	1	nonanginal	130	250	0	0	187	
4	5	1	0	nontypical	130	204	0	2	172	

	ExAng	Oldpeak	Slope	Ca	Thal	AHD
0	0	2.3	3	0.0	fixed	No
1	1	1.5	2	3.0	normal	Yes
2	1	2.6	2	2.0	reversible	Yes
3	0	3.5	3	0.0	normal	No
4	0	1.4	1	0.0	normal	No

```
#c) How many independent features are present in the given dataset?
features = df.drop(columns=['AHD'])
# Get the number of independent features
independent_features = features.shape[1]
#.shape : returns a tuple representing its dimensions (number of rows, number of columns)
# features.shape[1] : retrieves the number of columns, which corresponds to the number of independent features.
print(independent_features)
```

```

#d)Can we identify unwanted features?
import pandas as pd
# Identify constant value columns
constant_cols = [col for col in df.columns if df[col].nunique() == 1]

# Identify duplicate columns
duplicate_cols = []
for i in range(len(df.columns)):
    col1 = df.columns[i]
    for col2 in df.columns[i+1:]:
        if df[col1].equals(df[col2]):
            duplicate_cols.append(col2)

# Combine all potentially unwanted columns
unwanted_cols = set(constant_cols + duplicate_cols)

print("Potentially unwanted columns:")
print(unwanted_cols)

Potentially unwanted columns:
{'Thal', 'AHD'}

#f) Normalize RestBP, chol, and MaxHR attributes (considering above dataset) using min-max normalization, Z-score normalization, and de
from sklearn.preprocessing import MinMaxScaler, StandardScaler, RobustScaler
# Select attributes to normalize
attributes_to_normalize = ['RestBP', 'Chol', 'MaxHR']

# Min-Max normalization
min_max_scaler = MinMaxScaler()
ans=df[attributes_to_normalize] = min_max_scaler.fit_transform(df[attributes_to_normalize])
print(ans)

[[0.48113208 0.24429224 0.60305344]
 [0.62264151 0.3652968 0.28244275]
 [0.24528302 0.23515982 0.44274809]
 [0.33962264 0.28310502 0.88549618]
 [0.33962264 0.17808219 0.77099237]
 [0.24528302 0.25114155 0.81679389]
 [0.43396226 0.32420091 0.67938931]
 [0.24528302 0.52054795 0.70229008]
 [0.33962264 0.29223744 0.58015267]
 [0.43396226 0.17579909 0.64122137]
 [0.43396226 0.15068493 0.58778626]
 [0.43396226 0.38356164 0.6259542 ]
 [0.33962264 0.29680365 0.54198473]
 [0.24528302 0.31278539 0.77862595]
 [0.73584906 0.16666667 0.69465649]
 [0.52830189 0.09589041 0.78625954]
 [0.1509434 0.23515982 0.74045802]
 [0.43396226 0.25799087 0.67938931]
 [0.33962264 0.34018265 0.51908397]
 [0.33962264 0.3196347 0.76335878]
 [0.1509434 0.19406393 0.55725191]
 [0.52830189 0.35844749 0.69465649]
 [0.24528302 0.36073059 0.67938931]
 [0.35849057 0.22374429 0.77862595]
 [0.33962264 0.1826484 0.46564885]
 [0.24528302 0.21232877 0.66412214]
 [0.24528302 0.48858447 0.77099237]
 [0.52830189 0.2283105 0.32824427]
 [0.52830189 0.27625571 0.76335878]
 [0.1509434 0.09360731 0.32824427]
 [0.43396226 0.25799087 0.61068702]
 [0.21698113 0.23744292 0.67938931]
 [0.43396226 0.47716895 0.66412214]
 [0.38679245 0.24657534 0.6870229 ]
 [0.33962264 0.24429224 0.82442748]
 [0.43396226 0.2283105 0.81679389]
 [0.24528302 0.11643836 0.3740458 ]
 [0.52830189 0.34246575 0.3129771 ]
 [0.35849057 0.51826484 0.46564885]
 [0.52830189 0.26712329 0.50381679]
 [0.52830189 0.2260274 0.32824427]
 [0.43396226 0.16666667 0.81679389]
 [0.62264151 0.40182648 0.69465649]
 [0.52830189 0.19634703 0.65648855]
 [0.33962264 0.46575342 0.7480916 ]
 [0.16981132 0.23744292 0.71755725]
 [0.1509434 0.11187215 0.39694656]
 [0.52830189 0.26712329 0.4351145 ]

```

```
[0.43396226 0.66438356 0.65648855]
[0.33962264 0.16210046 0.61832061]
[0.10377358 0.16438356 0.74045802]
[0.24528302 0.11643836 0.52671756]
[0.16981132 0.37442922 0.6259542 ]
[0.33962264 0.21232877 0.89312977]
[0.33962264 0.28995434 0.55725191]
[0.28301887 0.3196347 0.29007634]
[0.43396226 0.24429224 0.70229008]
[0.1509434 0.10502283 0.66412214]
```

```
# Z-score normalization
```

```
z_score_scaler = StandardScaler()
```

```
ans=df[attributes_to_normalize] = z_score_scaler.fit_transform(df[attributes_to_normalize])
```

```
print(ans)
```

```
[[ 7.57525041e-01 -2.64900304e-01 1.71973294e-02]
 [ 1.61121989e+00 7.60415190e-01 -1.82190531e+00]
 [-6.65299701e-01 -3.42282606e-01 -9.02353991e-01]
 [-9.61698043e-02 6.39744770e-02 1.63735918e+00]
 [-9.61698043e-02 -8.25921990e-01 9.80536808e-01]
 [-6.65299701e-01 -2.06863578e-01 1.24326576e+00]
 [ 4.72960092e-01 4.12194834e-01 4.55078911e-01]
 [-6.65299701e-01 2.07591432e+00 5.86443385e-01]
 [-9.61698043e-02 1.41356778e-01 -1.14167145e-01]
 [ 4.72960092e-01 -8.45267566e-01 2.36138120e-01]
 [ 4.72960092e-01 -1.05806889e+00 -7.03789868e-02]
 [ 4.72960092e-01 9.15179793e-01 1.48561804e-01]
 [-9.61698043e-02 1.80047929e-01 -3.33107936e-01]
 [-6.65299701e-01 3.15466957e-01 1.02432497e+00]
 [ 2.29417576e+00 -9.22649867e-01 5.42655227e-01]
 [ 1.04208999e+00 -1.52236270e+00 1.06811312e+00]
 [-1.23442960e+00 -3.42282606e-01 8.05384176e-01]
 [ 4.72960092e-01 -1.48826852e-01 4.55078911e-01]
 [-9.61698043e-02 5.47613861e-01 -4.64472410e-01]
 [-9.61698043e-02 3.73503683e-01 9.36748650e-01]
 [-1.23442960e+00 -6.90502963e-01 -2.45531619e-01]
 [ 1.04208999e+00 7.02378464e-01 5.42655227e-01]
 [-6.65299701e-01 7.21724040e-01 4.55078911e-01]
 [ 1.76561750e-02 -4.39010483e-01 1.02432497e+00]
 [-9.61698043e-02 -7.87230839e-01 -7.70989517e-01]
 [-6.65299701e-01 -5.35738360e-01 3.67502595e-01]
 [-6.65299701e-01 1.80507626e+00 9.80536808e-01]
 [ 1.04208999e+00 -4.00319332e-01 -1.55917636e+00]
 [ 1.04208999e+00 5.93775086e-03 9.36748650e-01]
 [-1.23442960e+00 -1.54170828e+00 -1.55917636e+00]
 [ 4.72960092e-01 -1.48826852e-01 6.09854876e-02]
 [-8.36038670e-01 -3.22937030e-01 4.55078911e-01]
 [ 4.72960092e-01 1.70834838e+00 3.67502595e-01]
 [ 1.88395144e-01 -2.45554729e-01 4.98867069e-01]
 [-9.61698043e-02 -2.64900304e-01 1.28705392e+00]
 [ 4.72960092e-01 -4.00319332e-01 1.24326576e+00]
 [-6.65299701e-01 -1.34825253e+00 -1.29644741e+00]
 [ 1.04208999e+00 5.66959437e-01 -1.64675268e+00]
 [ 1.76561750e-02 2.05656874e+00 -7.70989517e-01]
 [ 1.04208999e+00 -7.14445506e-02 -5.52048726e-01]
 [ 1.04208999e+00 -4.19664907e-01 -1.55917636e+00]
 [ 4.72960092e-01 -9.22649867e-01 1.24326576e+00]
 [ 1.61121989e+00 1.06994440e+00 5.42655227e-01]
 [ 1.04208999e+00 -6.71157387e-01 3.23714436e-01]
 [-9.61698043e-02 1.61162051e+00 8.49172334e-01]
 [-1.12060362e+00 -3.22937030e-01 6.74019701e-01]
 [-1.23442960e+00 -1.38694368e+00 -1.16508294e+00]
 [ 1.04208999e+00 -7.14445506e-02 -9.46142150e-01]
 [ 4.72960092e-01 3.29468556e+00 3.23714436e-01]
 [-9.61698043e-02 -9.61341018e-01 1.04773646e-01]
 [-1.51899455e+00 -9.41995442e-01 8.05384176e-01]
 [-6.65299701e-01 -1.34825253e+00 -4.20684252e-01]
 [-1.12060362e+00 8.37797492e-01 1.48561804e-01]
 [-9.61698043e-02 -5.35738360e-01 1.68114734e+00]
 [-9.61698043e-02 1.22011203e-01 -2.45531619e-01]
 [-4.37647742e-01 3.73503683e-01 -1.77811715e+00]
 [ 4.72960092e-01 -2.64900304e-01 5.86443385e-01]
 [-1.23442960e+00 -1.44498040e+00 3.67502595e-01]
```

```
# Decimal scaling normalization
```

```
decimal_scaler = RobustScaler()
```

```
ans=df[attributes_to_normalize] = decimal_scaler.fit_transform(df[attributes_to_normalize])
```

```
print(ans)
```

```
[[ 0.75      -0.125      -0.09230769]
 [ 1.5       0.703125   -1.38461538]
 [-0.5      -0.1875     -0.73846154]
```

```

[ 0.      0.140625  1.04615385]
[ 0.     -0.578125  0.58461538]
[-0.5    -0.078125  0.76923077]
[ 0.5     0.421875  0.21538462]
[-0.5     1.765625  0.30769231]
[ 0.      0.203125 -0.18461538]
[ 0.5    -0.59375  0.06153846]
[ 0.5    -0.765625 -0.15384615]
[ 0.5     0.828125  0.      ]
[ 0.      0.234375 -0.33846154]
[-0.5     0.34375  0.61538462]
[ 2.1    -0.65625  0.27692308]
[ 1.     -1.140625  0.64615385]
[-1.     -0.1875   0.46153846]
[ 0.5    -0.03125  0.21538462]
[ 0.      0.53125  -0.43076923]
[ 0.      0.390625  0.55384615]
[-1.     -0.46875  -0.27692308]
[ 1.      0.65625  0.27692308]
[-0.5     0.671875  0.21538462]
[ 0.1    -0.265625  0.61538462]
[ 0.     -0.546875 -0.64615385]
[-0.5    -0.34375  0.15384615]
[-0.5     1.546875  0.58461538]
[ 1.     -0.234375 -1.2      ]
[ 1.      0.09375  0.55384615]
[-1.     -1.15625  -1.2      ]
[ 0.5    -0.03125  -0.06153846]
[-0.65   -0.171875  0.21538462]
[ 0.5     1.46875  0.15384615]
[ 0.25   -0.109375  0.24615385]
[ 0.      -0.125   0.8      ]
[ 0.5    -0.234375  0.76923077]
[-0.5    -1.      -1.01538462]
[ 1.      0.546875 -1.26153846]
[ 0.1     1.75     -0.64615385]
[ 1.      0.03125  -0.49230769]
[ 1.     -0.25     -1.2      ]
[ 0.5    -0.65625  0.76923077]
[ 1.5     0.953125  0.27692308]
[ 1.     -0.453125  0.12307692]
[ 0.      1.390625  0.49230769]
[-0.9    -0.171875  0.36923077]
[-1.     -1.03125  -0.92307692]
[ 1.      0.03125  -0.76923077]
[ 0.5     2.75     0.12307692]
[ 0.     -0.6875   -0.03076923]
[-1.25   -0.671875  0.46153846]
[-0.5    -1.      -0.4      ]
[-0.9     0.765625  0.      ]
[ 0.     -0.34375  1.07692308]
[ 0.      0.1875   -0.27692308]
[-0.3     0.390625 -1.35384615]
[ 0.5    -0.125   0.30769231]
[-1.     -1.078125  0.15384615]

```