

CCP Fluid Model(II): Model Description & Results

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03/27/2025

CCP Fluid Model(II)

- Fluid electron + nonlinear Poisson-Boltzmann equation (Developed By Shahid).

n_e : Electron Density (x,t)

Γ_e : Electron Flux (x,t)

ϕ : Electric Potential (x,t)

e : Elementary Charge

ϵ_0 : Vacuum Permittivity

n_{io} : Ion Density (x)

R : Reaction Rate (x)

D : Electron Diffusion Coefficient

μ : Electron Mobility Coefficient

m_e : Electron Mass

Governing Equations

$$\left[\begin{array}{l} \frac{\partial n_e}{\partial t} + \frac{\partial \Gamma_e}{\partial x} = R \\ \frac{\partial^2 \phi}{\partial x^2} = -\frac{e}{\epsilon_0} (n_e - n_{io}) \end{array} \right]$$

$$n_{io} = R_0(x_2 - x_1) \sqrt{\frac{m_i}{eT_e}},$$

$$\Gamma_e = \boxed{-D \frac{\partial n_e}{\partial x}} + \boxed{\mu n_e \frac{\partial \phi}{\partial x}}$$

Diffusion Flux

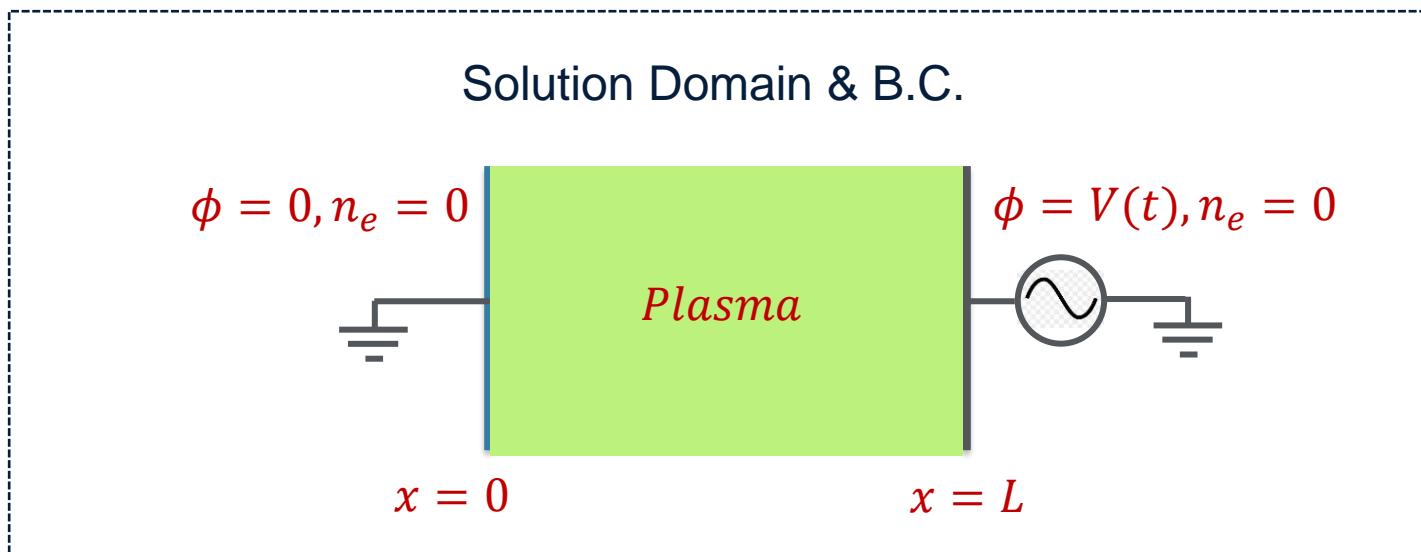
Drift Flux

CCP Fluid Model(II)

$$R(x) = \begin{cases} R_0, & x \in [x_1, x_2] \cup [L - x_2, L - x_1] \\ 0, & \text{otherwise} \end{cases}$$

$$V(t) = V_0 \sin(2\pi ft)$$

$$D = \frac{eT_e}{m_e \vartheta_m} \quad \mu = \frac{e}{m_e \vartheta_m}$$

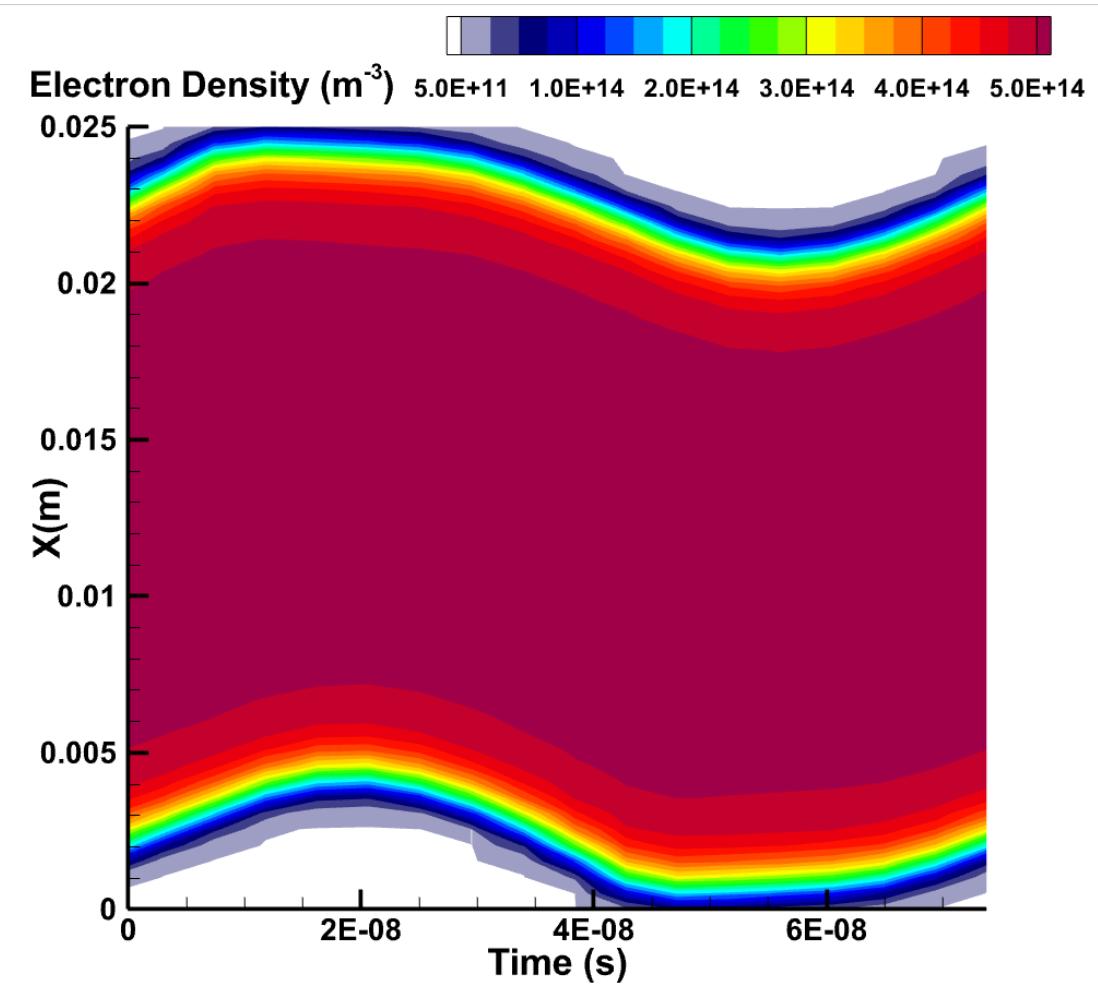
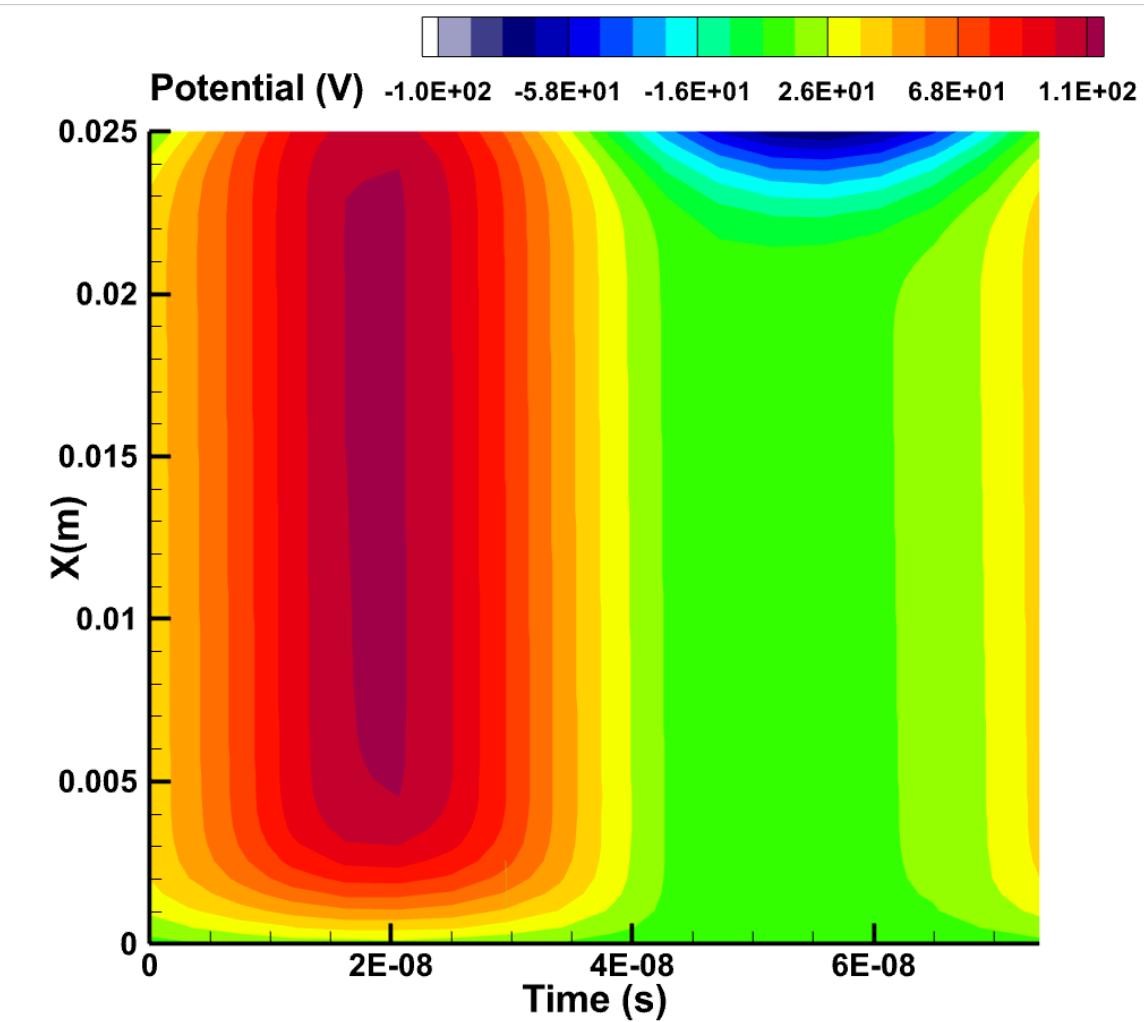


CCP Fluid Model(II)

Input Parameters	Baseline Value (Range (min, max))
Domain Length: L	0.025 m (0.01, 0.035)
Driving Frequency: f	13.56 MHz (1, 40)
Driving Voltage Amplitude: V_0	100 V (100, 300)
Reaction Rate Coefficient: R_0	2.7x10 ²¹ m ⁻³ s ⁻¹ (2.7x10 ¹⁸ , 2.7x10 ²¹)
x_1	0.005 m (0.16L, 0.2L)
x_2	0.01 m (1.5 x_1 , 2 x_1)
Electron Temperature: T_e	3 eV (2, 4)
Ion mass: m_i	40 amu (2, 40)[1 amu = 1.67x10 ⁻²⁷ kg]
Collision Frequency: ϑ_m	1E8 s ⁻¹ (1E7, 1E9)

Constants	Value
e	1.6x10 ⁻¹⁹ C
m_e	9.109x10 ⁻³¹ kg
ϵ_0	8.854x10 ⁻¹² C ² kg ⁻¹ m ⁻³ s ²

Results



$L=0.025\text{m}$, $f=13.56\text{MHz}$, $V=100\text{V}$, $R_0=2.7\text{E}20\text{m}^{-3}\text{s}^{-1}$, $T_e=3.0\text{eV}$

