

1.5.4 Find the distance from \mathbf{I} to BC .

Solution : We know the value of \mathbf{I} is

$$\mathbf{I} = \frac{1}{\sqrt{37} + 4 + \sqrt{61}} \begin{pmatrix} \sqrt{61} - 16 - 3\sqrt{37} \\ -\sqrt{61} + 24 - 5\sqrt{37} \end{pmatrix} \quad (1)$$

from the problem 1.5.2 . The equation of BC from Problem 1.5.1 is:

$$\mathbf{n}_2^\top \mathbf{x} + 50 = 0 \quad (2)$$

where, $\mathbf{n}_2 = \begin{pmatrix} 11 \\ -1 \end{pmatrix} \Rightarrow \mathbf{n}_2^\top = \begin{pmatrix} 11 & -1 \end{pmatrix}$

Let r be the distance between \mathbf{I} and BC , then

$$r = \frac{|\mathbf{n}_2^\top \mathbf{I} + 50|}{\|\mathbf{n}_2\|} \quad (3)$$

$$r = \frac{\left| \frac{1}{\sqrt{37}+4+\sqrt{61}} \begin{pmatrix} 11 & -1 \end{pmatrix} \begin{pmatrix} \sqrt{61} - 16 - 3\sqrt{37} \\ -\sqrt{61} + 24 - 5\sqrt{37} \end{pmatrix} + 50 \right|}{\sqrt{122}} \quad (4)$$

$$= \frac{\frac{12\sqrt{61}-28\sqrt{37}-200}{\sqrt{37}+4+\sqrt{61}} + 50}{\sqrt{122}} \quad (5)$$

$$= \frac{62\sqrt{61} + 22\sqrt{37}}{\sqrt{122}(\sqrt{37} + 4 + \sqrt{61})} \quad (6)$$

$$= 3.1272 \quad (7)$$