1.5.4 Find the distance from  $\mathbf{I}$  to BC.

Solution: We know the value of I is

$$I = \frac{1}{\sqrt{37} + 4 + \sqrt{61}} \begin{pmatrix} \sqrt{61} - 16 - 3\sqrt{37} \\ -\sqrt{61} + 24 - 5\sqrt{37} \end{pmatrix}$$
 (1)

from the problem 1.5.2 . The equation of BC from Problem 1.5.1 is:

$$\mathbf{n}_{\mathbf{2}}^{\top}\mathbf{x} + 50 = 0 \tag{2}$$

where 
$$\mathbf{n}_{\mathbf{2}}^{\top} = \begin{pmatrix} 11 & -1 \end{pmatrix}$$

Let r be the distance between **I** and BC, then

$$r = \frac{\left|\mathbf{n}_{2}^{\top}\mathbf{I} + 50\right|}{\|\mathbf{n}_{2}\|}\tag{3}$$

$$r = \frac{\left|\mathbf{n_2^{\top}I} + 50\right|}{\|\mathbf{n_2}\|}$$

$$r = \frac{\left|\frac{1}{\sqrt{37} + 4 + \sqrt{61}} \left(11 - 1\right) \left(\frac{\sqrt{61} - 16 - 3\sqrt{37}}{-\sqrt{61} + 24 - 5\sqrt{37}}\right) + 50\right|}{\sqrt{122}}$$

$$(4)$$

$$=\frac{\frac{12\sqrt{61}-28\sqrt{37}-200}{\sqrt{37}+4+\sqrt{61}}+50}{\sqrt{122}}\tag{5}$$

$$=\frac{62\sqrt{61}+22\sqrt{37}}{\sqrt{122}(\sqrt{37}+4+\sqrt{61})}\tag{6}$$

$$=3.1272$$
 (7)