

For full credit, you must show all work and circle your final answer.

1

 (2.5 point) Find the Laplace transform of the periodic function below.

$$f(t) = e^t, \quad 0 < t < 1, \text{ and } f(t) \text{ has period } 1.$$

2

(a) (1.5 points) Show that

$$2 \sum_{n=0}^{\infty} a_n x^{n+1} + \sum_{n=1}^{\infty} n b_n x^{n-1} = b_1 + \sum_{n=1}^{\infty} [2a_{n-1} + (n+1)b_{n+1}] x^n$$

(b) (1 points) Given

$$\sin(x) = \sum_{k=0}^{\infty} \frac{(-1)^k}{(2k+1)!} x^{2k+1},$$

find a power series for $\cos(x)$. (Show work, do not simply write an answer.)**University of Florida Honor Code:**

On my honor, I have neither given nor received unauthorized aid in doing this assignment.

Signature