

Calculus, SGA – Open Question: Series, by Magomedov Rustam

$\forall \sum_{n=1}^{\infty} a_n$ that converges, if we expect that the sum of all elements in the sequences converges to 0, then it must hold true that after a while the sum of the sequence of terms will also converge to 0.

Consider the sum of a sequence, defined:

$$\begin{aligned}\sum A_n &= i_1 + i_2 + i_3 + \dots + i_n \mid n = \infty \\ \Rightarrow \sum A_c &= i_c + i_{c+1} + i_{c+2} + \dots + i_{c+n} = A_{c+1} \\ \Rightarrow \text{the relation can be represented as } \sum A_d &= A_{c+1} + a_c \\ \Rightarrow A_n &= A_c = A_d\end{aligned}$$

As the sum of the sequence of terms must converge to 0, $\Rightarrow a_n$ converges to 0 too.
 $\therefore \lim_{x \rightarrow \infty} a_n = 0$