

DSCI 318 - Final Project Analysis Report

Russell Whitworth

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Objective

I want to create the best model to predict salary using contract length, team under contract for, and primary position played by a player. I will use backwards selection to create 9 models: full model, model with all three 2 way interactions, three models with two 2-way interactions, three models with a singular two way interaction, and the basic model; and determine the best model using adjusted r-squared.

Data Summary

The dataset used in this project, Major League Baseball Salaries 2021, was collected from USA Today Sports. This dataset details MLB salaries based upon each team's opening day roster at the beginning of the 2021 MLB season. Detailed within the source dataset are the following:

- Name: player name
- Team: team of player
- POS: primary position of player
- Salary: average annual value (AAV) of the contract in USD
- Years: length of current contract in years and the years the contract spans
- Total.Value: total value of the contract in USD

I made the following changes to the dataset outside of R:

- Created Years_Length: extracts the length of current contract in years from Years column
- Changed Salary and Total.Value from strings to numeric values by removing commas

Reading Dataset into R

```
salary <- read.csv("salary.csv")

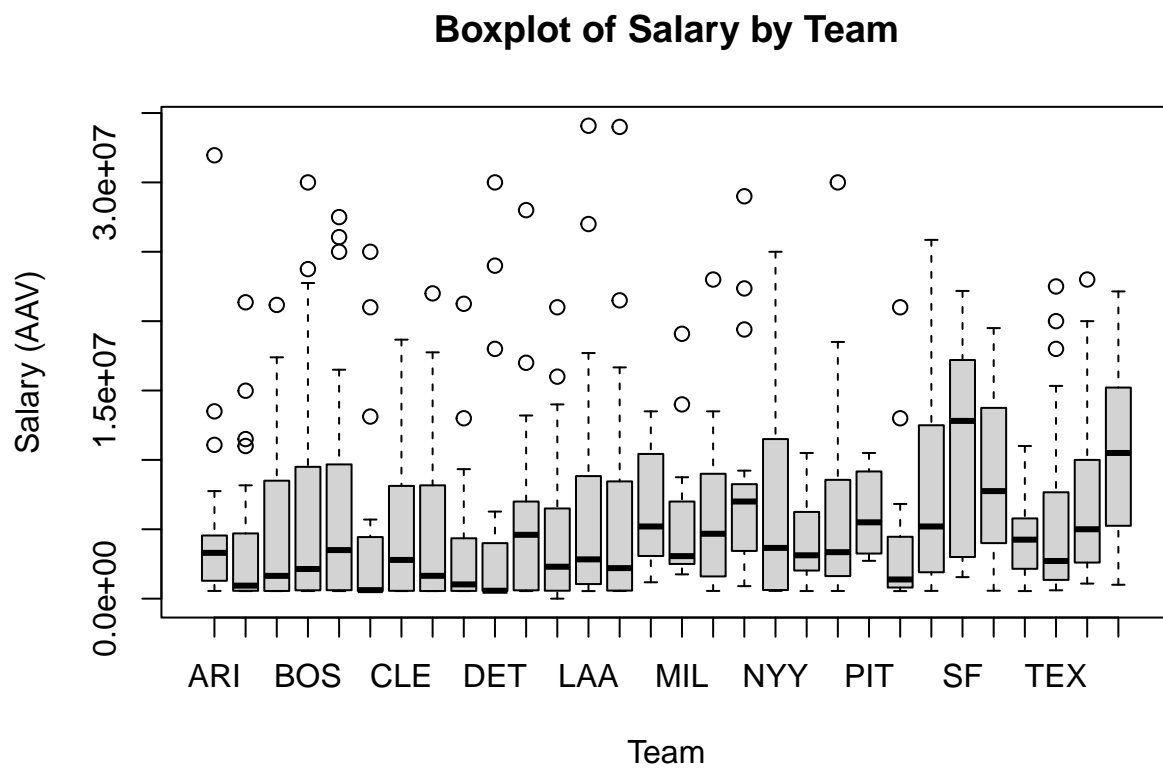
salary <- salary[,c("Team", "POS", "Years_Length", "Salary")]
salary$Team <- as.factor(salary$Team)
salary$POS <- as.factor(salary$POS)
head(salary)
```

```
##   Team POS Years_Length  Salary
## 1  LAA  OF           6 3408333
```

```
## 2  LAD  SP          7 34000000
## 3  ARI  SP          6 31954483
## 4  DET  1B         10 30000000
## 5  BOS  SP          7 30000000
## 6  PHI  SP          3 30000000
```

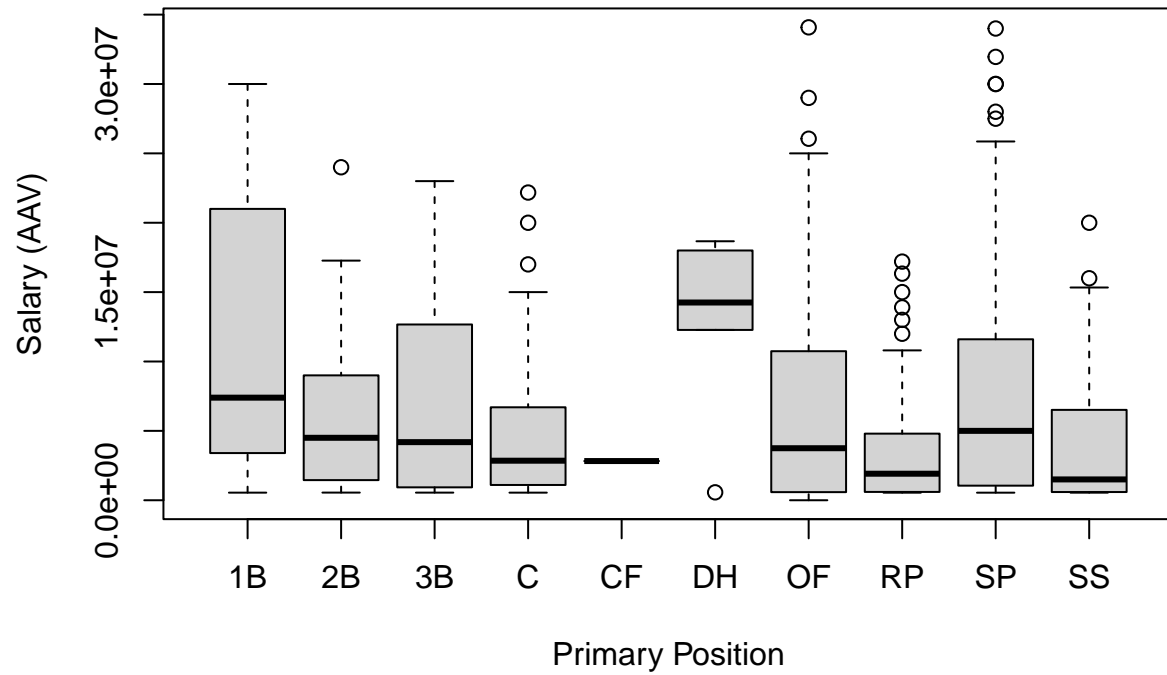
Visualizing the Predictors

```
boxplot(Salary~Team,data=salary, main="Boxplot of Salary by Team",
        xlab="Team", ylab="Salary (AAV)")
```



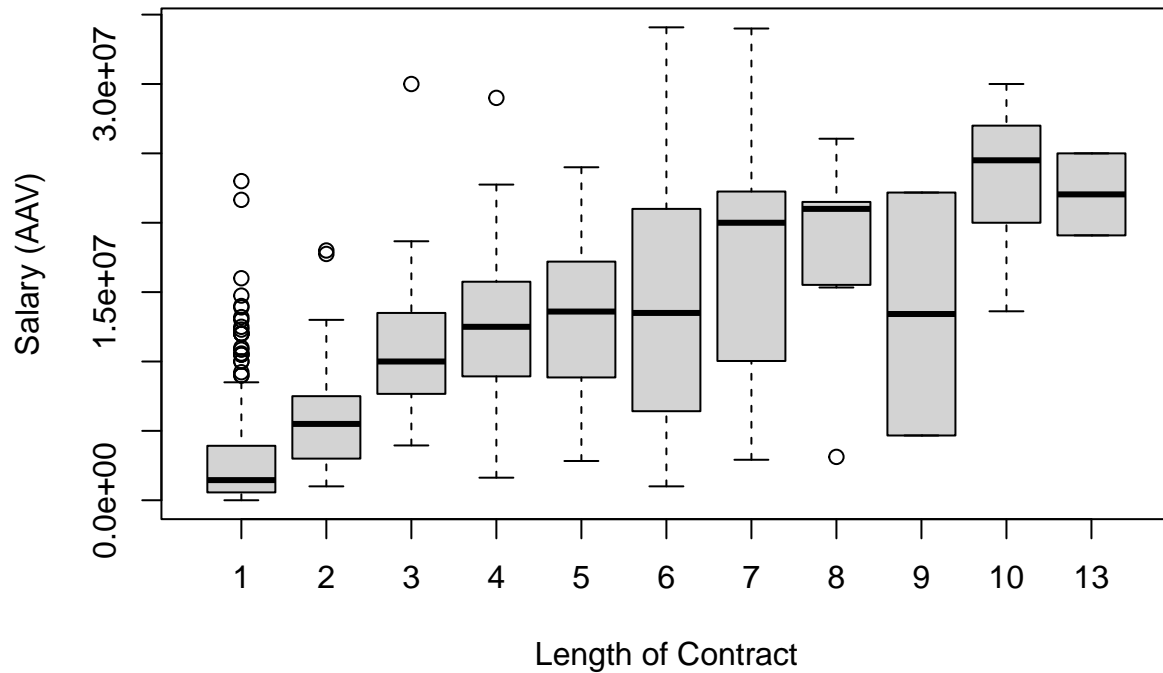
```
boxplot(Salary~POS,data=salary, main="Boxplot of Salary by Position",
        xlab="Primary Position", ylab="Salary (AAV)")
```

Boxplot of Salary by Position



```
boxplot(Salary~Years_Length,data=salary, main="Boxplot of Length of Contract to Predict Salary",  
        xlab="Length of Contract", ylab="Salary (AAV)")
```

Boxplot of Length of Contract to Predict Salary



Models and Diagnosis

Full Model

```
fullmodel.lm <- lm(Salary ~ POS * Team * Years_Length, salary)
fullmodelr2 <- summary(fullmodel.lm)$r.squared
fullmodeladjustedr2 <- summary(fullmodel.lm)$adj.r.squared

# Printing out the first 10 coefficients and r-squared metrics
coef(fullmodel.lm)[0:10]
```

```
## (Intercept)      POS2B      POS3B      POSC      POSCF      POSDH
## -270833.25  7869914.12 21200104.65 -129166.75  2254700.00 12786914.55
##      POSOF      POSRP      POSSP      POSSS
##  2775620.48   -51866.75  -899055.35  -248933.33
```

```
cat("R-Squared:", fullmodelr2, "\nAdjusted R-Squared:", fullmodeladjustedr2)
```

```
## R-Squared: 0.8655051
## Adjusted R-Squared: 0.7179656
```

ANOVA Analysis of Full Model

```
salaryfull.aov <- aov(Salary ~ Team * POS * Years_Length, salary)
summary(salaryfull.aov)
```

```
##              Df      Sum Sq   Mean Sq F value    Pr(>F)
## Team          29 1.962e+15  6.767e+13   5.271 1.54e-14 ***
## POS           9 3.193e+15  3.548e+14  27.638 < 2e-16 ***
## Years_Length  1 1.162e+16  1.162e+16 905.045 < 2e-16 ***
## Team:POS      194 4.531e+15  2.336e+13   1.819 1.58e-06 ***
## Team:Years_Length 29 1.261e+15  4.349e+13   3.388 5.85e-08 ***
## POS:Years_Length 6 3.842e+14  6.403e+13   4.987 6.91e-05 ***
## Team:POS:Years_Length 60 1.751e+15  2.918e+13   2.273 3.31e-06 ***
## Residuals     299 3.838e+15  1.284e+13
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
summaryanova <- summary(salaryfull.aov)[[1]][["Df"]]
df <- summary(salaryfull.aov)[[1]][["F value"]]
colnames(df) <- gsub(" ", ".", colnames(df))

df$FCrit <- with(summaryanova, qf(c(0.05),Df,299,lower.tail=FALSE))
df$IsSignificant <- with(df, ifelse(F.value > FCrit, 1, 0))
df
```

```
##              F.value  FCrit IsSignificant
## Team              5.27 1.5055             1
## POS              27.64 1.9113             1
## Years_Length     905.05 3.8727             1
## Team:POS          1.82 1.2362             1
## Team:Years_Length 3.39 1.5055             1
## POS:Years_Length  4.99 2.1290             1
## Team:POS:Years_Length 2.27 1.3636             1
## Residuals                1.2099
```

Using $\alpha=0.05$, all of the main effects and interactions are significant.

Model with interaction between Team and POS (MODEL 2)

```
salary2.lm <- lm(Salary ~ Team * POS + Years_Length, salary)
model2r2 <- summary(salary2.lm)$r.squared
model2adjustedr2 <- summary(salary2.lm)$adj.r.squared

# Printing out the first 10 coefficients and r-squared metrics
coef(salary2.lm)[0:10]
```

```
## (Intercept)      TeamATL      TeamBAL      TeamBOS      TeamCHC      TeamCIN
##   -957564.3    2013533.8    2043252.9    8083333.5   -9254926.9    960128.3
##      TeamCLE      TeamCOL      TeamCWS      TeamDET
##   3458077.1    4731833.5   11457820.7   5960128.3
```

```
cat("R-Squared:", model2r2, "\nAdjusted R-Squared:", model2adjustedr2)
```

```
## R-Squared: 0.7465167
## Adjusted R-Squared: 0.5966141
```

ANOVA Analysis of Model 2

```
salary2.aov <- aov(Salary ~ Team * POS + Years_Length, salary)
summary(salary2.aov)
```

```
##              Df      Sum Sq   Mean Sq F value    Pr(>F)
## Team          29  1.962e+15  6.767e+13    3.685 2.26e-09 ***
## POS           9   3.193e+15  3.548e+14   19.323 < 2e-16 ***
## Years_Length  1   1.162e+16  1.162e+16  632.779 < 2e-16 ***
## Team:POS      194  4.531e+15  2.336e+13    1.272   0.024 *
## Residuals     394  7.234e+15  1.836e+13
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
summaryanova <- summary(salary2.aov)[[1]][["Df"]]
df <- summary(salary2.aov)[[1]][["F value"]]
colnames(df) <- gsub(" ", ".", colnames(df))

df$FCrit <- with(summaryanova, qf(c(0.05),Df,394,lower.tail=FALSE))
df$IsSignificant <- with(df, ifelse(F.value > FCrit, 1, 0))
df
```

```
##              F.value  FCrit IsSignificant
## Team              3.69 1.4964              1
## POS              19.32 1.9037              1
## Years_Length     632.78 3.8652              1
## Team:POS          1.27 1.2218              1
## Residuals         1.1805
```

Using $\alpha=0.05$, all of the main effects and interactions are significant.

Model with interaction between Team and Years_Length (MODEL 3)

```
salary3.lm <- lm(Salary ~ Team * Years_Length + POS, salary)
model3r2 <- summary(salary3.lm)$r.squared
model3adjustedr2 <- summary(salary3.lm)$adj.r.squared

# Printing out the first 10 coefficients and r-squared metrics
coef(salary3.lm)[0:10]
```

```
## (Intercept)      TeamATL      TeamBAL      TeamBOS      TeamCHC      TeamCIN
##   -572783.1    528833.7   1248098.7   1221269.0    645046.4   -393581.0
##      TeamCLE      TeamCOL      TeamCWS      TeamDET
##   2830320.6  -1541323.2   1139552.2  -555593.5
```

```
cat("R-Squared:", model3r2, "\nAdjusted R-Squared:", model3adjustedr2)
```

```
## R-Squared: 0.641368
## Adjusted R-Squared: 0.597742
```

ANOVA Analysis of Model 3

```
salary3.aov <- aov(Salary ~ Team * Years_Length + POS, salary)
summary(salary3.aov)
```

```
##              Df      Sum Sq   Mean Sq F value    Pr(>F)
## Team          29  1.962e+15  6.767e+13   3.696 8.52e-10 ***
## Years_Length   1  1.399e+16  1.399e+16 764.234 < 2e-16 ***
## POS            9  8.188e+14  9.097e+13   4.968 1.91e-06 ***
## Team:Years_Length 29  1.530e+15  5.277e+13   2.882 1.27e-06 ***
## Residuals     559  1.024e+16  1.831e+13
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
summaryanova <- summary(salary3.aov)[[1]]["Df"]
df <- summary(salary3.aov)[[1]]["F value"]
colnames(df) <- gsub(" ", ".", colnames(df))

df$FCrit <- with(summaryanova, qf(c(0.05),Df,559,lower.tail=FALSE))
df$IsSignificant <- with(df, ifelse(F.value > FCrit, 1, 0))
df
```

```
##              F.value  FCrit IsSignificant
## Team              3.70 1.4879             1
## Years_Length      764.23 3.8581             1
## POS                4.97 1.8966             1
## Team:Years_Length  2.88 1.4879             1
## Residuals          1.1494
```

Using $\alpha=0.05$, all of the main effects and interactions are significant.

Model with interaction between POS and Years_Length (MODEL 4)

```
salary4.lm <- lm(Salary ~ Team + Years_Length * POS, salary)
model4r2 <- summary(salary4.lm)$r.squared
model4adjustedr2 <- summary(salary4.lm)$adj.r.squared

# Printing out the first 10 coefficients and r-squared metrics
coef(salary4.lm)[0:10]
```

```
## (Intercept)      TeamATL      TeamBAL      TeamBOS      TeamCHC      TeamCIN
##    437074.7   -1631698.7    437395.4   1588329.1   179413.7  -2386122.1
##      TeamCLE      TeamCOL      TeamCWS      TeamDET
##   -934227.2    766913.4   -828010.6   -679425.6
```

```
cat("R-Squared:", model4r2, "\nAdjusted R-Squared:", model4adjustedr2)
```

```
## R-Squared: 0.6262689
## Adjusted R-Squared: 0.5959838
```

ANOVA Analysis of Model 4

```
salary4.aov <- aov(Salary ~ Team + Years_Length * POS, salary)
summary(salary4.aov)
```

```
##              Df    Sum Sq   Mean Sq F value    Pr(>F)
## Team          29 1.962e+15 6.767e+13   3.680 9.11e-10 ***
## Years_Length   1 1.399e+16 1.399e+16 760.908 < 2e-16 ***
## POS            9 8.188e+14 9.097e+13   4.947 2.02e-06 ***
## Years_Length:POS 8 1.099e+15 1.374e+14   7.472 1.66e-09 ***
## Residuals     580 1.067e+16 1.839e+13
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
summaryanova <- summary(salary4.aov)[[1]][["Df"]]
df <- summary(salary4.aov)[[1]][["F value"]]
colnames(df) <- gsub(" ", ".", colnames(df))

df$FCrit <- with(summaryanova, qf(c(0.05),Df,580,lower.tail=FALSE))
df$IsSignificant <- with(df, ifelse(F.value > FCrit, 1, 0))
df
```

```
##              F.value  FCrit IsSignificant
## Team              3.68 1.4871             1
## Years_Length      760.91 3.8575             1
## POS                4.95 1.8960             1
## Years_Length:POS   7.47 1.9544             1
## Residuals          1.1465
```

Using $\alpha=0.05$, all of the main effects and interactions are significant.

Model with interactions between Team and POS, Team and Years_Length (MODEL 5)

```
salary5.lm <- lm(Salary ~ Team * Years_Length + Team * POS, salary)
model5r2 <- summary(salary5.lm)$r.squared
model5adjustedr2 <- summary(salary5.lm)$adj.r.squared

# Printing out the first 10 coefficients and r-squared metrics
coef(salary5.lm)[0:10]
```



```
## (Intercept)      TeamATL      TeamBAL      TeamBOS      TeamCHC      TeamCIN
##      -3751571      7085938      2288649      8052445      -17208027      6962419
##      TeamCLE      TeamCOL      TeamCWS      TeamDET
##      7685680      1753559      11825143      -19287679
```

```
cat("R-Squared:", model5r2, "\nAdjusted R-Squared:", model5adjustedr2)
```

```
## R-Squared: 0.7907075
## Adjusted R-Squared: 0.6404756
```

ANOVA Analysis of Model 5

```
salary5.aov <- aov(Salary ~ Team * Years_Length + Team * POS, salary)
summary(salary5.aov)
```

```
##              Df      Sum Sq   Mean Sq F value    Pr(>F)
## Team          29  1.962e+15  6.767e+13   4.135 6.18e-11 ***
## Years_Length   1  1.399e+16  1.399e+16 855.072 < 2e-16 ***
## POS            9  8.188e+14  9.097e+13   5.559 3.41e-07 ***
## Team:Years_Length 29  1.530e+15  5.277e+13   3.224 1.36e-07 ***
## Team:POS       194  4.262e+15  2.197e+13   1.342 0.00851 **
## Residuals     365  5.973e+15  1.636e+13
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
summaryanova <- summary(salary5.aov)[[1]]["Df"]
df <- summary(salary5.aov)[[1]]["F value"]
colnames(df) <- gsub(" ", ".", colnames(df))

df$FCrit <- with(summaryanova, qf(c(0.05), Df, 365, lower.tail=FALSE))
df$IsSignificant <- with(df, ifelse(F.value > FCrit, 1, 0))
df
```

```
##              F.value  FCrit IsSignificant
## Team              4.14  1.4987             1
## Years_Length     855.07  3.8671             1
## POS              5.56  1.9056             1
## Team:Years_Length  3.22  1.4987             1
## Team:POS          1.34  1.2254             1
## Residuals         1.1882
```

Using $\alpha=0.05$, all of the main effects and interactions are significant.

Model with interactions between Team and POS, POS and Years_Length (MODEL 6)

```
salary6.lm <- lm(Salary ~ Team * POS + POS * Years_Length, salary)
model6r2 <- summary(salary6.lm)$r.squared
model6adjustedr2 <- summary(salary6.lm)$adj.r.squared
```

```
# Printing out the first 10 coefficients and r-squared metrics
coef(salary6.lm)[0:10]
```

```
## (Intercept)      TeamATL      TeamBAL      TeamBOS      TeamCHC      TeamCIN
##      -1967894      1339980      1706476      8083333      -10602034      -1397309
##      TeamCLE      TeamCOL      TeamCWS      TeamDET
##      3794854      4731833      12131374      3602691
```

```
cat("R-Squared:", model6r2, "\nAdjusted R-Squared:", model6adjustedr2)
```

```
## R-Squared: 0.7584971
## Adjusted R-Squared: 0.6097363
```

ANOVA Analysis of Model 6

```
salary6.aov <- aov(Salary ~ Team * POS + POS * Years_Length, salary)
summary(salary6.aov)
```

```
##              Df      Sum Sq   Mean Sq F value    Pr(>F)
## Team          29  1.962e+15  6.767e+13    3.809 8.14e-10 ***
## POS           9   3.193e+15  3.548e+14   19.973 < 2e-16 ***
## Years_Length   1   1.162e+16  1.162e+16  654.055 < 2e-16 ***
## Team:POS      194  4.531e+15  2.336e+13    1.315  0.01243 *
## POS:Years_Length  6   3.419e+14  5.699e+13    3.208  0.00437 **
## Residuals     388  6.892e+15  1.776e+13
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
summaryanova <- summary(salary6.aov)[[1]]["Df"]
df <- summary(salary6.aov)[[1]]["F value"]
colnames(df) <- gsub(" ", ".", colnames(df))

df$FCrit <- with(summaryanova, qf(c(0.05),Df,388,lower.tail=FALSE))
df$IsSignificant <- with(df, ifelse(F.value > FCrit, 1, 0))
df
```

```
##              F.value  FCrit IsSignificant
## Team              3.81  1.4968             1
## POS              19.97  1.9040             1
## Years_Length     654.06  3.8655             1
## Team:POS          1.31  1.2225             1
## POS:Years_Length  3.21  2.1220             1
## Residuals         1.1820
```

Using $\alpha=0.05$, all of the main effects and interactions are significant.

Model with interactions between Team and Years_Length, POS and Years_Length (MODEL 7)

```
salary7.lm <- lm(Salary ~ Team * Years_Length + POS * Years_Length, salary)
model7r2 <- summary(salary7.lm)$r.squared
model7adjustedr2 <- summary(salary7.lm)$adj.r.squared

# Printing out the first 10 coefficients and r-squared metrics
coef(salary7.lm)[0:10]
```

```
## (Intercept)      TeamATL      TeamBAL      TeamBOS      TeamCHC      TeamCIN
## -489867.1      262843.2      980122.6      692698.5      312504.1      -530829.3
##      TeamCLE      TeamCOL      TeamCWS      TeamDET
##  2434797.5     -1720381.6      140141.7     -778122.5
```

```
cat("R-Squared:", model7r2, "\nAdjusted R-Squared:", model7adjustedr2)
```

```
## R-Squared: 0.6813752
## Adjusted R-Squared: 0.6374269
```

ANOVA Analysis of Model 7

```
salary7.aov <- aov(Salary ~ Team * Years_Length + POS * Years_Length, salary)
summary(salary7.aov)
```

```
##              Df      Sum Sq   Mean Sq F value    Pr(>F)
## Team          29  1.962e+15  6.767e+13   4.100 2.10e-11 ***
## Years_Length   1  1.399e+16  1.399e+16  847.882 < 2e-16 ***
## POS           9  8.188e+14  9.097e+13   5.512 2.78e-07 ***
## Team:Years_Length 29  1.530e+15  5.277e+13   3.197 8.02e-08 ***
## Years_Length:POS  8  1.142e+15  1.427e+14   8.648 3.80e-11 ***
## Residuals      551  9.093e+15  1.650e+13
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
summaryanova <- summary(salary7.aov)[[1]]["Df"]
df <- summary(salary7.aov)[[1]]["F value"]
colnames(df) <- gsub(" ", ".", colnames(df))

df$FCrit <- with(summaryanova, qf(c(0.05), Df, 551, lower.tail=FALSE))
df$IsSignificant <- with(df, ifelse(F.value > FCrit, 1, 0))
df
```

```
##              F.value  FCrit IsSignificant
## Team              4.10  1.4882             1
## Years_Length      847.88  3.8584             1
## POS               5.51  1.8969             1
## Team:Years_Length  3.20  1.4882             1
## Years_Length:POS   8.65  1.9552             1
## Residuals         1.1506
```

Using alpha=0.05, all of the main effects and interactions are significant.

Model with all three 2-way interactions (MODEL 8)

```
salary8.lm <- lm(Salary ~ Team * Years_Length + Team * POS + POS * Years_Length, salary)
model8r2 <- summary(salary8.lm)$r.squared
model8adjustedr2 <- summary(salary8.lm)$adj.r.squared
```

```
# Printing out the first 10 coefficients and r-squared metrics
coef(salary8.lm)[0:10]
```

```
## (Intercept)      TeamATL      TeamBAL      TeamBOS      TeamCHC      TeamCIN
##      -3642549      7319114      1265031      5750247     -19345669      7516342
##      TeamCLE      TeamCOL      TeamCWS      TeamDET
##      8080056      1035075      11899449     -14106547
```

```
cat("R-Squared:", model8r2, "\nAdjusted R-Squared:", model8adjustedr2)
```

```
## R-Squared: 0.8041679
## Adjusted R-Squared: 0.6579757
```

ANOVA Analysis of Model 8

```
salary8.aov <- aov(Salary ~ Team * Years_Length + Team * POS + POS * Years_Length, salary)
summary(salary8.aov)
```

```
##              Df      Sum Sq   Mean Sq F value    Pr(>F)
## Team          29  1.962e+15  6.767e+13   4.347 1.09e-11 ***
## Years_Length   1  1.399e+16  1.399e+16 898.823 < 2e-16 ***
## POS            9  8.188e+14  9.097e+13   5.843 1.31e-07 ***
## Team:Years_Length 29  1.530e+15  5.277e+13   3.389 3.57e-08 ***
## Team:POS        194  4.262e+15  2.197e+13   1.411 0.002683 **
## Years_Length:POS   6  3.842e+14  6.403e+13   4.113 0.000523 ***
## Residuals       359  5.589e+15  1.557e+13
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
summaryanova <- summary(salary8.aov)[[1]]["Df"]
df <- summary(salary8.aov)[[1]]["F value"]
colnames(df) <- gsub(" ", ".", colnames(df))

df$FCrit <- with(summaryanova, qf(c(0.05),Df,359,lower.tail=FALSE))
df$IsSignificant <- with(df, ifelse(F.value > FCrit, 1, 0))
df
```

```
##              F.value  FCrit IsSignificant
## Team              4.35 1.4992             1
## Years_Length      898.82 3.8675             1
## POS                5.84 1.9060             1
## Team:Years_Length  3.39 1.4992             1
## Team:POS           1.41 1.2263             1
## Years_Length:POS   4.11 2.1239             1
## Residuals         1.1899
```

Using $\alpha=0.05$, all of the main effects and interactions are significant.

Basic Model (Model with no interaction)

```
basic.lm <- lm(Salary ~ Team + Years_Length + POS, salary)
basicr2 <- summary(basic.lm)$r.squared
basicmodeladjustedr2 <- summary(basic.lm)$adj.r.squared

# Printing out the first 10 coefficients and r-squared metrics
coef(basic.lm)[0:10]

## (Intercept)      TeamATL      TeamBAL      TeamBOS      TeamCHC      TeamCIN
##    2262781.8   -1380793.3    292592.4    1558287.4    585835.9   -2540558.9
##      TeamCLE      TeamCOL      TeamCWS      TeamDET
##   -1107425.8    633490.6   -1212937.8   -410530.2

cat("R-Squared:", basicr2, "\nAdjusted R-Squared:", basicmodeladjustedr2)

## R-Squared: 0.587751
## Adjusted R-Squared: 0.560408
```

ANOVA Analysis of Basic Model

```
salarybasic.aov <- aov(Salary ~ Team + Years_Length + POS, salary)
summary(salarybasic.aov)

##              Df      Sum Sq   Mean Sq F value    Pr(>F)
## Team          29  1.962e+15  6.767e+13    3.382 1.36e-08 ***
## Years_Length   1  1.399e+16  1.399e+16  699.329 < 2e-16 ***
## POS            9  8.188e+14  9.097e+13    4.546 8.29e-06 ***
## Residuals     588  1.177e+16  2.001e+13
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

summaryanova <- summary(salarybasic.aov)[[1]][["Df"]]
df <- summary(salarybasic.aov)[[1]][["F value"]]
colnames(df) <- gsub(" ", ".", colnames(df))

df$FCrit <- with(summaryanova, qf(c(0.05),Df,588,lower.tail=FALSE))
df$IsSignificant <- with(df, ifelse(F.value > FCrit, 1, 0))
df

##              F.value  FCrit IsSignificant
## Team              3.38  1.4869             1
## Years_Length     699.33  3.8573             1
## POS              4.55  1.8958             1
## Residuals        1.1454
```

Using $\alpha=0.05$, all of the main effects are significant.

Model Selection

Creating a dataframe to compare model performance

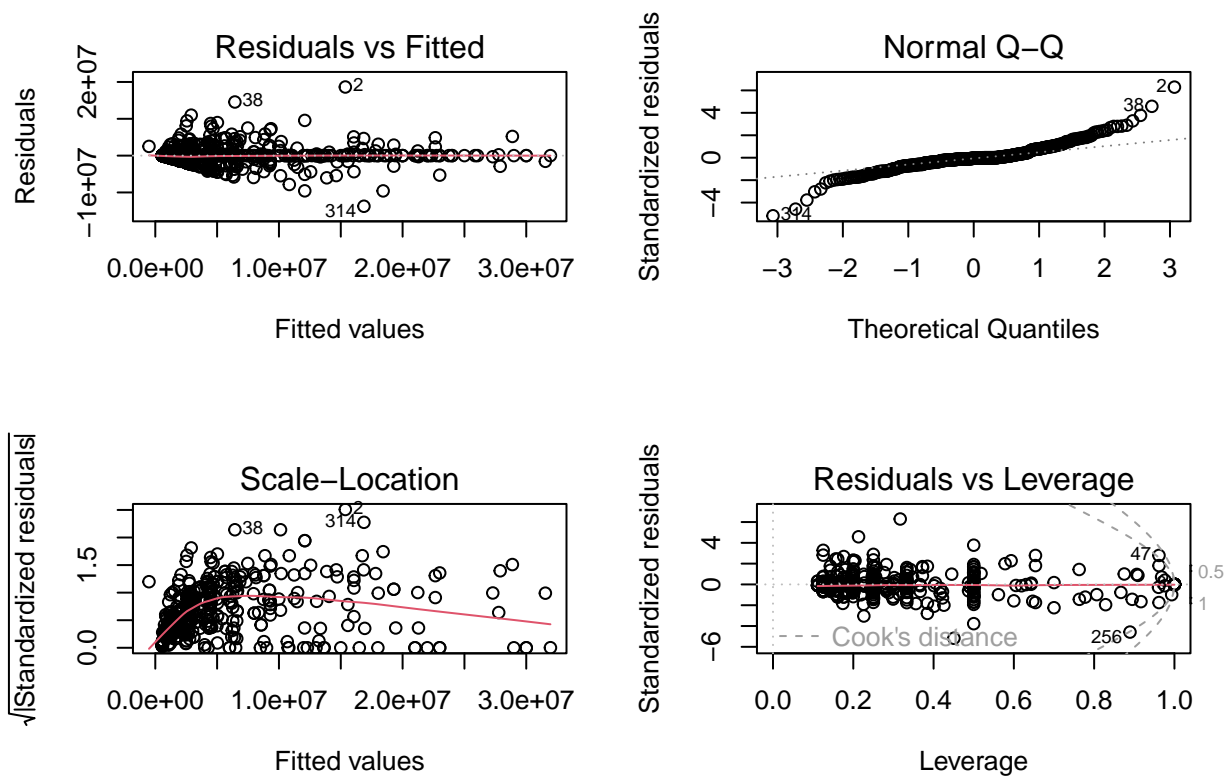
```
Model.Type <- c("Full Model", "Model 2", "Model 3", "Model 4",  
               "Model 5", "Model 6", "Model 7", "Model 8", "Basic Model")  
AdjustedRSquared <- c(fullmodeladjustedr2, model2adjustedr2, model3adjustedr2,  
                      model4adjustedr2, model5adjustedr2, model6adjustedr2,  
                      model7adjustedr2, model8adjustedr2, basicmodeladjustedr2)  
AdjustedRSquared <- round(AdjustedRSquared, digits = 4)  
  
comparisondf <- data.frame(Model.Type, AdjustedRSquared)  
comparisondf <- comparisondf[order(-AdjustedRSquared),]  
comparisondf
```

```
##      Model.Type AdjustedRSquared  
## 1 Full Model      0.7180  
## 8 Model 8         0.6580  
## 5 Model 5         0.6405  
## 7 Model 7         0.6374  
## 6 Model 6         0.6097  
## 3 Model 3         0.5977  
## 2 Model 2         0.5966  
## 4 Model 4         0.5960  
## 9 Basic Model     0.5604
```

The Full Model is the best model as it produces the greatest adjusted r-squared value.

Model Adequacy Checking for Selected Model

```
library(ggplot2)  
opar <- par(mfrow=c(2,2),cex=.8)  
plot(salaryfull.aov)
```



There are no indications of model inadequacy.

Checking Factor Importance

```
noPOS.lm <- lm(Salary ~ Team * Years_Length, salary)
noPOSr2 <- summary(noPOS.lm)$r.squared
noPOSadjustedr2 <- summary(noPOS.lm)$adj.r.squared

cat("R-Squared:", noPOSr2, "\nAdjusted R-Squared:", noPOSadjustedr2)
```

```
## R-Squared: 0.6149549
## Adjusted R-Squared: 0.574959
```

```
noTeam.lm <- lm(Salary ~ POS * Years_Length, salary)
noTeamr2 <- summary(noTeam.lm)$r.squared
noTeamadjustedr2 <- summary(noTeam.lm)$adj.r.squared

cat("R-Squared:", noTeamr2, "\nAdjusted R-Squared:", noTeamadjustedr2)
```

```
## R-Squared: 0.5871265
## Adjusted R-Squared: 0.5749233
```

```
noYears.lm <- lm(Salary ~ Team * POS, salary)
noYearsr2 <- summary(noYears.lm)$r.squared
noYearsadjustedr2 <- summary(noYears.lm)$adj.r.squared

cat("R-Squared:", noYearsr2, "\nAdjusted R-Squared:", noYearsadjustedr2)
```

```
## R-Squared: 0.4631009
## Adjusted R-Squared: 0.1477577
```

Models omitting on factor produce worse adjusted r-squared values than the full model: factors are important.

Conclusion

The best model to predict salary with the predictors Team, POS, and Years_Length is the full model. It produces the best adjusted r-squared value with all of its main effects and interactions significant. Furthermore, I've confirmed that all factors in my full model are important by comparing the adjusted r-squared values of my full model with separate models which omitted one variable.

The full model can be defined by:

$$\text{Salary} = \beta_0 + \text{YearsLength} + \text{Team} + \text{POS} + \text{YearsLength} * \text{Team} + \text{YearsLength} * \text{POS} + \text{Team} * \text{POS} + \text{YearsLength} * \text{Team} * \text{POS}$$