

Solution Homework

$$TS1 = \{10, 2, 5, 10, 2, 7\}$$

$$TS2 = \{3, 1, 15, 5, 3, 6\}$$

$$TS3 = \{2, 1, 4, 7, 1, 4\}$$

$$d_{Euc}(TS1, TS2) = 13.3$$

$$d_{Euc}(TS1, TS3) = \underline{9.22}$$

$$d_{Euc}(TS2, TS3) = 11.5$$

TS1 & TS3 most similar

$$d_{Abs}(TS1, TS2) = 25$$

$$d_{Abs}(TS1, TS3) = \underline{17}$$

$$d_{Abs}(TS2, TS3) = 18$$

TS1 & TS3 most similar

$$d_{Inf}(TS1, TS2) = 10$$

$$d_{Inf}(TS1, TS3) = \underline{8}$$

$$d_{Inf}(TS2, TS3) = 11$$

TS1, TS3 most similar

$$d_{edit}(TS1, TS2) = 6$$

$$d_{edit}(TS1, TS3) = 6$$

$$d_{edit}(TS2, TS3) = \underline{5}$$

TS2, TS3 most similar

example of a solution.

new distance: $A = (a_1, \dots, a_6)$, $B = (b_1, \dots, b_6)$

$$d(A, B) = |a_1 - b_1| + \max_{i=2..6} (|a_i - b_i|)$$

$$d(TS1, TS2) = 11$$

$$d(TS2, TS3) = 12$$

$$d(TS1, TS3) = 11$$

Solution Exercise

$$TS1 = \{0, 1, 2, 3, -1, 2, -2\}$$

$$TS2 = \{1, -1, 0.5, 3, -1, 2, 1\}$$

$$TS3 = \{-2, 3, 1, 0, -1, 2, 3\}$$

Euclidean distance:

$$d_{\text{Euc}}(TS1, TS2) = \sqrt{(0-1)^2 + (1+1)^2 + (2+0.5)^2 + (3-3)^2 + (-1+1)^2 + (2-2)^2 + (-2-1)^2} = \\ = \sqrt{1 + 4 + 6.25 + 0 + 0 + 0 + 9} = \sqrt{20.25} = 4.5$$

$$d_{\text{Euc}}(TS2, TS3) = \sqrt{(1+2)^2 + (-1-3)^2 + (-0.5-1)^2 + (3-0)^2 + (-1+1)^2 + (2-2)^2 + (1-3)^2} = \\ = \sqrt{9 + 16 + 2.25 + 9 + 0 + 0 + 4} = \sqrt{40.25} \approx 6.34$$

$$d_{\text{Euc}}(TS1, TS3) = \sqrt{(0+2)^2 + (1-3)^2 + (2-1)^2 + (3-0)^2 + (-1+1)^2 + (2-2)^2 + (-2-3)^2} = \\ = \sqrt{4 + 4 + 1 + 9 + 0 + 0 + 25} = \sqrt{43} \approx 6.56$$

TS1 and TS2 are most similar

Absolute distance:

$$d_{\text{Abs}}(TS1, TS2) = |0-1| + |1+1| + |2+0.5| + |3-3| + |-1+1| + |2-2| + |-2-1| = \\ = 1 + 2 + 2.5 + 0 + 0 + 0 + 3 = 8.5$$

$$d_{\text{Abs}}(TS2, TS3) = |1+2| + |-1-3| + |-0.5-1| + |3-0| + |-1+1| + |2-2| + |1-3| = \\ = 3 + 4 + 1.5 + 3 + 0 + 0 + 2 = 13.5$$

$$d_{\text{Abs}}(TS1, TS3) = |0+2| + |1-3| + |2-1| + |3-0| + |-1+1| + |2-2| + |-2-3| = \\ = 2 + 2 + 1 + 3 + 0 + 0 + 5 = 13$$

Infinity distance:

$$d_{\text{Inf}}(TS1, TS2) = \max(0-1, 1+1, 2+0.5, 3-3, -1+1, 2-2, -2-1) = \\ = \max(1; 2; 2.5; 0; 0; 0; 3) = 3$$

$$d_{\text{Inf}}(TS2, TS3) = \max(1+2, -1-3, -0.5-1, 3-0, -1+1, 2-2, 1-3) = \\ = \max(3; 4; 1.5; 3; 0; 0; 2) = 4$$

$$d_{\text{Inf}}(TS1, TS3) = \max(0+2, 1-3, 2-1, 3-0, -1+1, 2-2, -2-3) = \\ = \max(2; 2; 1; 3; 0; 0; 5) = 5$$