

\* 5 large no. of modulation techniques are available

\* Draw backs of Pass band modulation,

\* i) modulator / Demodulator Equipment's design is complex.

\* ii) not suitable for short distance communication

{ we use Base band digital mod techs for short distances}

\* COHERENT BINARY ASK {ON-OFF key}

\* In this method there is only one unit energy ratio & it is switched ON or OFF depending upon the i/p binary sequence.

\* Notes:

ASK is no longer widely used in DC's

Especially in wireless communications, it is an

\* Earliest form of digital modulation used in radio telephony.

\* 27/07/17

$$* c(t) = A \cos(2\pi f_c t)$$

$$P_s = \frac{A^2}{2}$$

$$A = \sqrt{2 P_s}$$

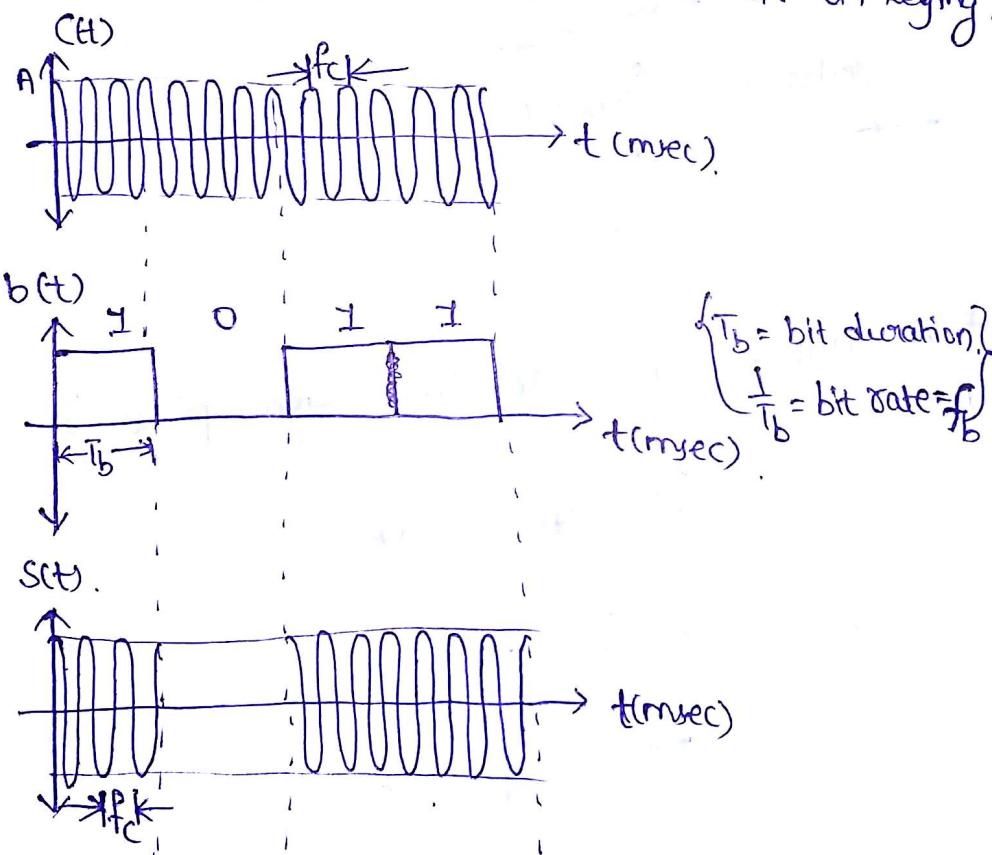
$$\Rightarrow c(t) = \sqrt{2 P_s} \cdot \cos(2\pi f_c t)$$

ASK defined as.

$$s(t) = \begin{cases} \sqrt{2 P_s} \cdot \cos(2\pi f_c t) & ; b_k = 1 \\ 0 & ; b_k = 0 \end{cases} \rightarrow ①$$

\* Hence, Switching ON/OFF of a carrier

⇒ ON-OFF keying.



\* ASK is not used in wireless communications. Especially not used in Satellite Communications because of harmonic distortions

$$* S(t) = \begin{cases} \sqrt{P_s T_b} \cdot \sqrt{\frac{2}{T_b}} \cdot \cos(2\pi f_c t) & ; \text{ if } b_k = 1 \\ 0 & ; \text{ if } b_k = 0 \end{cases} \rightarrow ②$$

$$\Rightarrow S(t) = \begin{cases} \sqrt{P_s T_b} \cdot \phi_i(t) & ; \text{ if } b_k = 1 \\ 0 & ; \text{ if } b_k = 0 \end{cases} \rightarrow ③$$

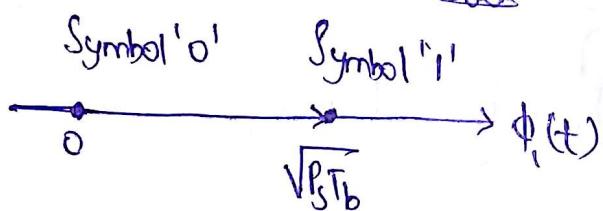
\* General  
the  
Coding  
of

$$\therefore E_b = \cancel{\sqrt{P_s T_b}} \quad \{ \sqrt{P_s T_b} = \sqrt{\text{bit Energy } \{ E_b \}} \}$$

\* This means that there is only one carrier function " $\phi_i(t)$ ".

\* The signal space diagram will have two points on " $\phi_i(t)$ ". One will be at zero & other will be at  $\sqrt{P_s T_b}$ .

\* Straight space representation of ASK:



\* The distance b/w the two signal points is

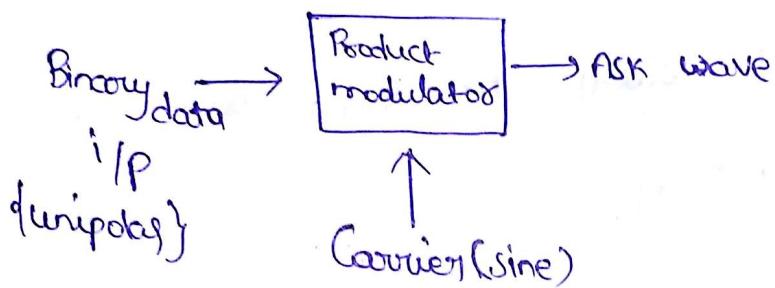
$$d = \sqrt{P_s T_b} - 0$$

$$\Rightarrow d = \sqrt{P_s T_b}$$

$$\Rightarrow d = \sqrt{E_b} \rightarrow ②$$

\* Generation of ASK :-

\* ASK signal may be generated by simply applying the incoming binary data {unipolar} & the sinusoidal carrier to the two i/p's of a product modulator. (i.e., a balanced modulator), the resulting o/p will be an ASK wave form.

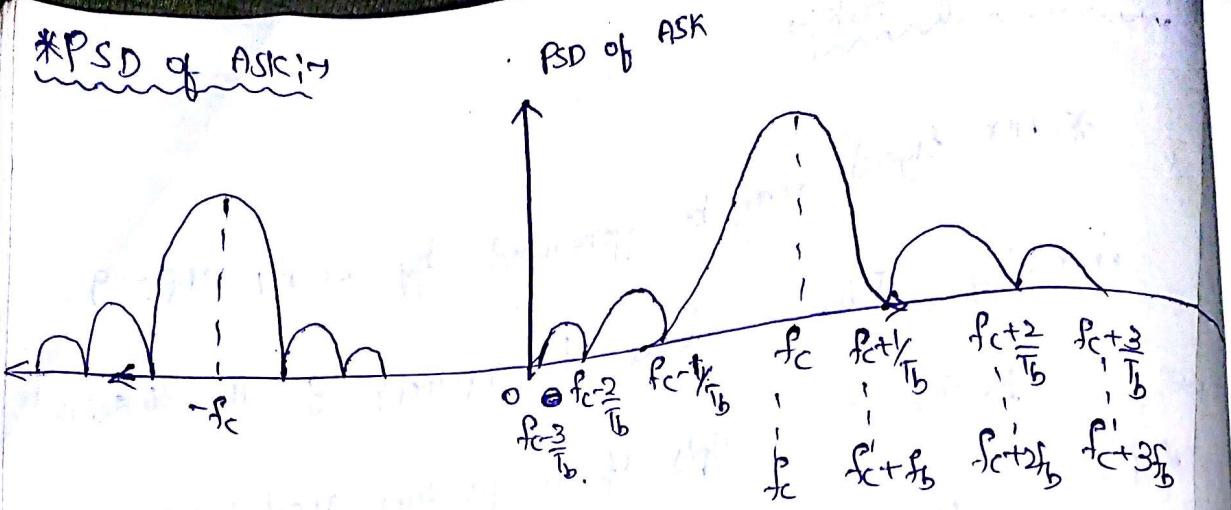


\* The modulation causes a shift of Baseband Signal spectrum

\* The ASK signal is the product of the binary sequence & Carrier signal, cause a power spectral density (PSD) same as that of Baseband & (ON-OFF) signal.

But shifted in freq domain by  $\pm f_c$

\* PSD of ASK :-



PSD of ASK

\* Coherent detection  
ASK  
Signal  
Carrier  
 $\{ \cos(2\pi f_ct) \}$

\* BW of ASK =  $\infty$  {theoretically}

Practically it is not possible. So.

\* The spectrum of ASK signal has infinite BW, if we consider 100% power.

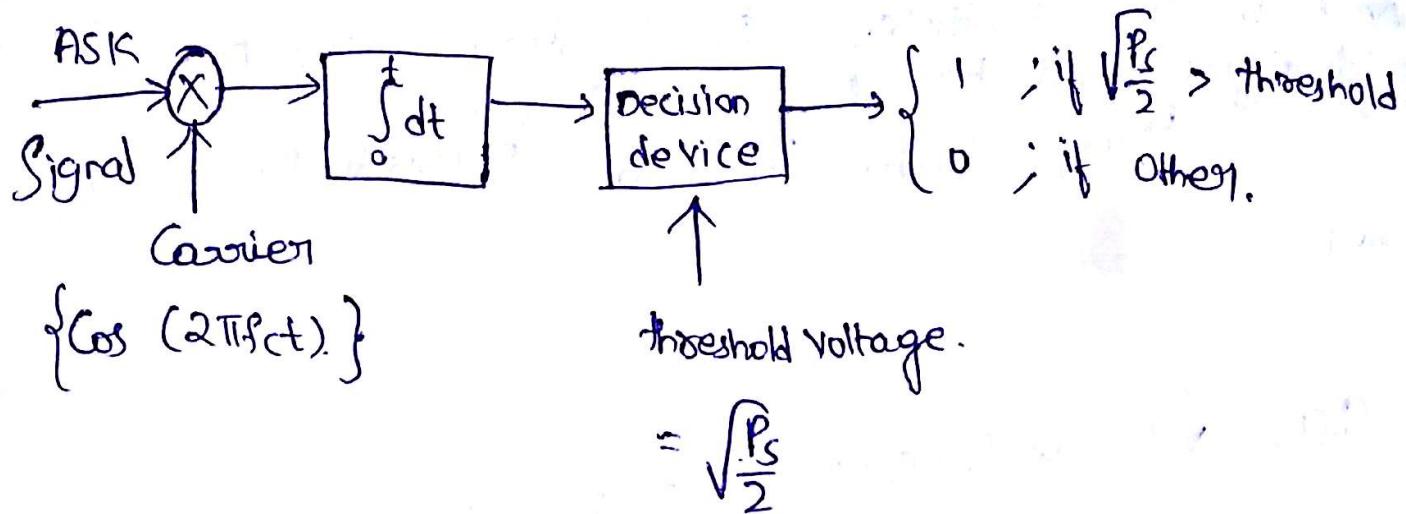
\* However, for practical purpose, BW is defined as the BW of an ideal B.P.F centered at "f\_c". Whole o/p contains about 95% of the total avg Power Content of the ASK signal.

\* Acc to thy

BW of ASK Signal is approximately

$$BW_{ASK} = 3f_b = \frac{3}{T_b}$$

\* Coherent detection of Binary ASK



\* The demodulation of BASK waveform can be achieved with the help of, Coherent detector as shown in the fig above.

\* It consists of Product modulator followed by an Integrator & a decision making device.

\* Integrator operates on the op of the multiplier

\*27 for 2017\*

\*BPSK\*

\*let us assume the carrier as  $s(t) = A \cos(2\pi f_c t)$ ,

- where  $A$  is Peak amplitude, for 1-2 local oscillator power.
- In BPSK, the dissipated would be  $P_s = A^2/2 = A = \sqrt{2P_s}$  modulate the phase of the carrier.

$$S_1(t) = \sqrt{2P_s} \cdot \cos(2\pi f_c t); \text{ for } b_k = 1$$

$$S_2(t) = \sqrt{2P_s} \cdot \cos(2\pi f_c t + \pi); \text{ for } b_k = 0.$$

$$\text{i.e., } S_2(t) = -\sqrt{2P_s} \cos(2\pi f_c t); \text{ for } b_k = 0.$$

$$\Rightarrow s(t) = b(t) \cdot \sqrt{2P_s} \cdot \cos(2\pi f_c t).$$

Where  $b(t) = \begin{cases} 1 & ; b_k = 1 \\ -1 & ; b_k = 0 \end{cases}$

\* Generation of BPSK Signal :-

The BPSK Signal is generated by applying carrier signal of Bi-polar NRZ data sequence to the balanced modulator.

Here, the bipolar signal "b(t)" is applied as a modulating signal to the balanced modulator.

Binary data

$\sqrt{2P_s} = A$

\*

Bipolar  
Signal

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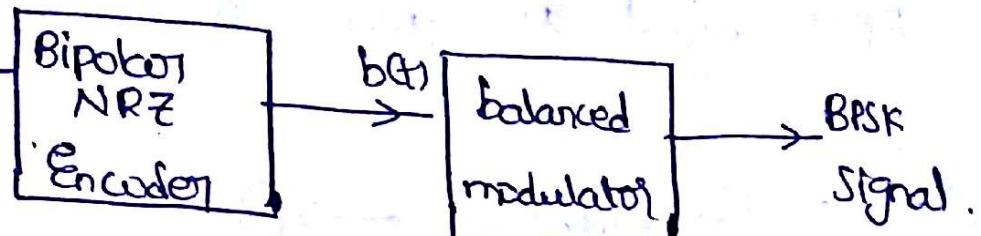
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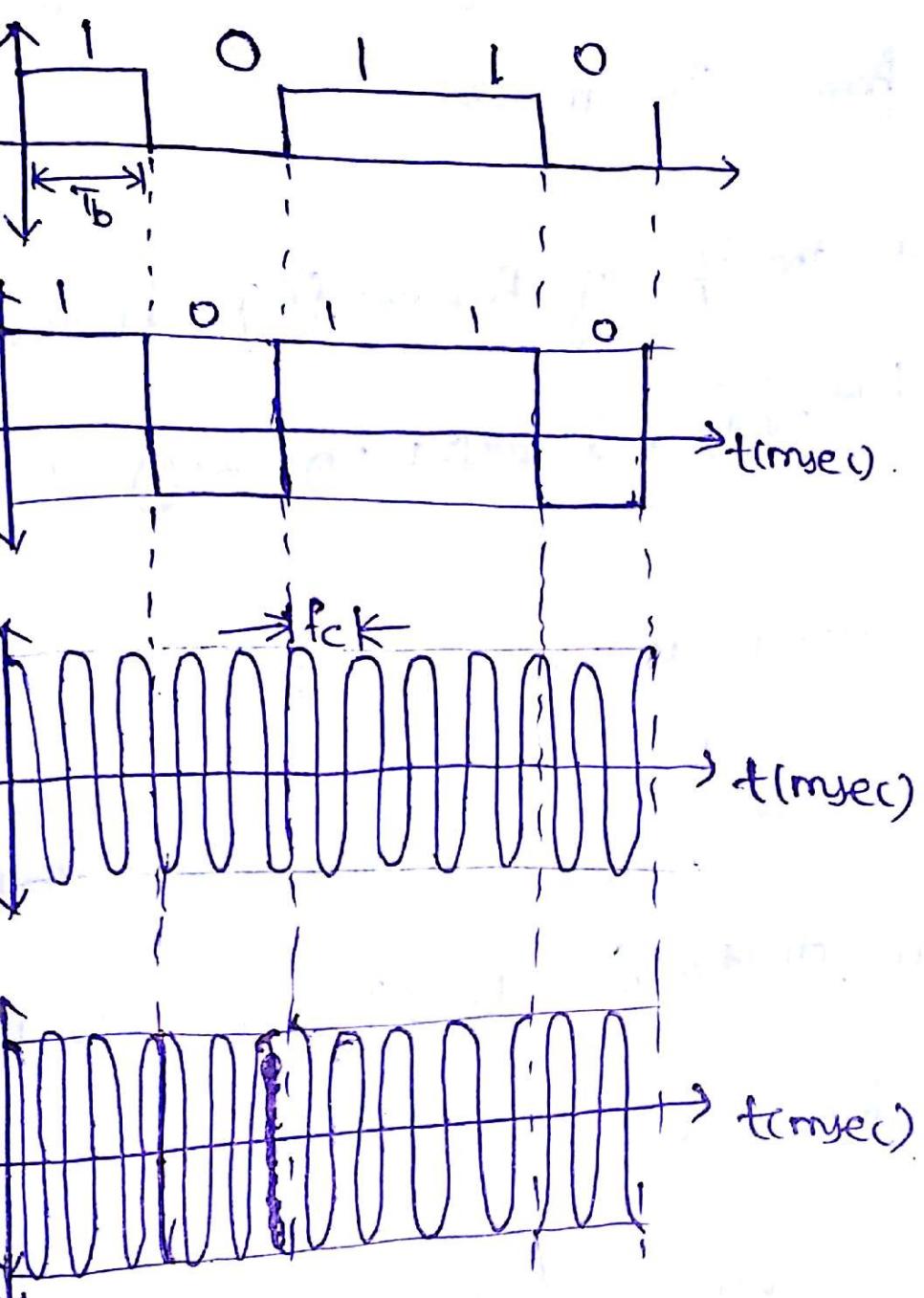
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$$\sqrt{2} P_s \cdot \cos(2\pi f_c t)$$



Method of detection of BPSK Signal: →

\* The transmitted BPSK signal is given as

$$S(t) = b(t) \cdot \sqrt{2P_s} \cdot \cos(2\pi f_c t) \rightarrow ①$$

\* This signal undergoes a phase change " $\theta$ " depending upon the time delay from  $T_R$  to  $R_R$ .

\* ∴ The o/p signal at the i/p of Receiver  $\{R_R\}$  becomes

$$S(t) = b(t) \cdot \sqrt{2P_s} \cdot \cos(2\pi f_c t + \theta) \rightarrow ②$$

\* The local reference carrier is retrieved from the received signal  $\{Eq. ②\}$  by using a square law device & BPF & freq. divider of % by 2, the o/p of the square law device is  $S^2(t)$ .

$$\Rightarrow S^2(t) = \underbrace{(b(t) \cdot \sqrt{2P_s})^2}_{\text{neglect}} \cdot \cos^2(2\pi f_c t + \theta)$$

$$\Rightarrow S^2(t) = \frac{1 + \cos[2(2\pi f_c t + \theta)]}{2} = \frac{1 + \cos[2(\pi f_c t + \theta)]}{2}$$

↑ Neglection is for math  
remove dly BPF

\* The o/p of BPF is

$$\Rightarrow \cos[2(\pi f_c t + \theta)]$$

\* The o/p of freq. divider is  $\cos(2\pi f_c t + \theta)$

\* The o/p of BPF has freq. of  $2f_c$ , hence it should be passed through freq. divider networks, which is of " $\frac{1}{2}$ " type.

\* The freq.  $\downarrow$  o/p signal becomes  $\cos(2\pi f_c t + \theta)$ .

\* The synchronous demodulator multiplies the i/p signal with received carrier.

\* Hence, at the o/p of the multiplier, we get,

$$\Rightarrow b(t) \cdot \sqrt{2P_s} \cdot \cos(2\pi f_c t + \theta) \cdot \cos(2\pi f_c t - \theta)$$

$$\Rightarrow b(t) \sqrt{2P_s} \cdot \cos^2(2\pi f_c t + \theta)$$

$$\Rightarrow b(t) \sqrt{2P_s} \cdot \left[ \frac{1 + \cos[2(2\pi f_c t + \theta)]}{2} \right]$$

$$\Rightarrow b(t) \sqrt{\frac{P_s}{2}} \left\{ 1 + \cos[2(2\pi f_c t + \theta)] \right\}$$

\* Bit synchronizer  
\* This signal is applied to the integrator &

Bit synchronizer

\* The bit sync takes care of starting & ending times of a bit.

\* At the end of the bit duration  $T_B$ , the bit sync closes switch "S" temporarily.

\* This connects the o/p of the integrator to the decision device.

\* Then synch opens switch "S<sub>2</sub>" & "S<sub>1</sub>" is closed temporarily.

\* This results the integrator voltage to a zero value.

then the integrator integrates the next bit.

\* Let us assume one bit period "T<sub>b</sub>". Containing integral number of cycles of carrier

\* This means that phase change occurs in the carrier only at zero crossings.

\* The o/p of the integrator in the k<sup>th</sup> bit interval is

$$\Rightarrow S_0(KT_b) = b(KT_b) \cdot \sqrt{\frac{P_s}{2}} \cdot \int_{(k-1)T_b}^{KT_b} [1 + C_0(2(\pi f t + \theta))] dt$$

$$\Rightarrow S_0(KT_b) = b(KT_b) \cdot \sqrt{\frac{P_s}{2}} \left\{ \int_{(k-1)T_b}^{KT_b} dt + \int_{(k-1)T_b}^{KT_b} C_0(2(\pi f t + \theta)) dt \right\}$$

$$\Rightarrow S_0(KT_b) = b(KT_b) \cdot \sqrt{\frac{P_s}{2}} \cdot [T_b]$$

i.e.,  $S_0(KT_b) = \dots$

\* This signal is applied to a decision making device

which decides whether the received symbol is zero or 1.

\* Constellation Diagram of BPSK:

$$* \text{Eq. of BPSK} \Rightarrow S(t) = b(t) \cdot \sqrt{2P_s} \cdot \cos(2\pi f_c t)$$

$$= b(t) \cdot \sqrt{P_s T_b} \cdot \sqrt{\frac{2}{T_b}} \cdot \cos(2\pi f_c t)$$

$$\text{Let } \phi_1(t) = \sqrt{\frac{2}{T_b}} \cdot \cos(2\pi f_c t),$$

$$\Rightarrow S(t) = b(t) \cdot \sqrt{P_s T_b} \cdot \phi_1(t) \rightarrow ①$$

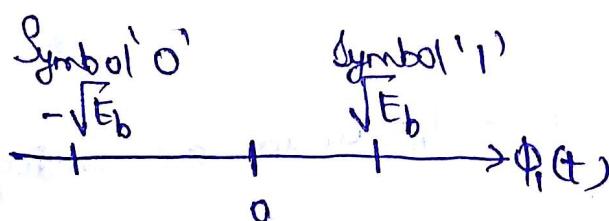
$$E_b = P_s T_b$$

$$\Rightarrow S(t) = b(t) \cdot \sqrt{E_b} \cdot \phi_1(t).$$

{ $b(t)$  can be  $\pm 1$ }

$$\Rightarrow S(t) = \pm \sqrt{E_b} \cdot \phi_1(t)$$

\* They, on the single axis of  $\phi_1(t)$ , there will be two points. One point will be located at " $\sqrt{E_b}$ " & other point will be " $-\sqrt{E_b}$ ".



\* Distance b/w two points is  $\{d\} \cdot 2\sqrt{E_b}$ .

\* Spectrum of BPSK:

\* b(t) is NRZI signal having rectangular pulses of  $\pm V_b$ , assume each pulse is  $\pm \frac{V_b T_b}{2}$  around its centre, then it becomes easy to find FT of such a pulse.

\* The FT of this type of pulse is given as

$$X(f) = V_b T_b \frac{\sin(\pi f T_b)}{\pi f T_b} \rightarrow ①$$

\* for a large number of such "tve" & "-ve" pulses the power spectral density (PSD) is expressed as

$$S(f) = \overline{|X(f)|^2} \rightarrow ②$$

\* Here  $\overline{|X(f)|^2}$  is avg value of  $|X(f)|^2$  to all the pulses of time in b(t).

\*  $T_s$  is symbol duration

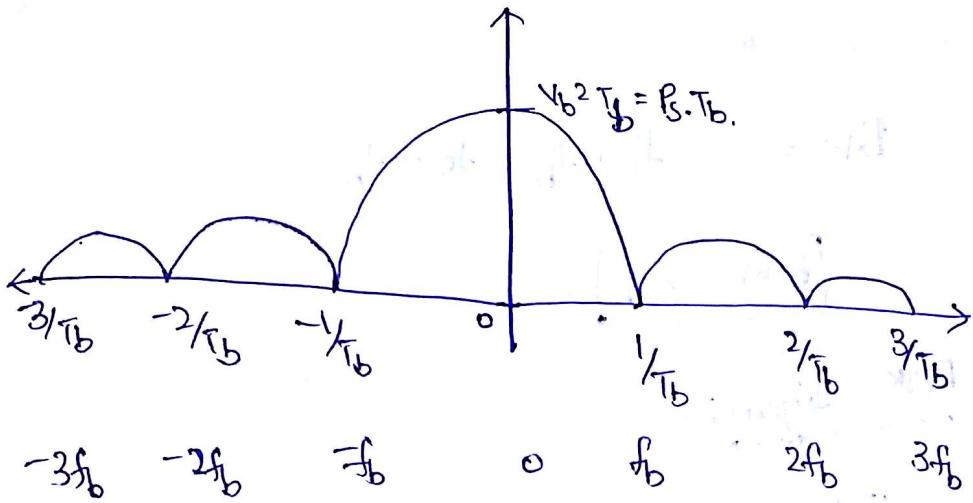
Note:-

\* In BPSK  $T_s = T_b$  as we are sending +1 or -1.

~~By each~~

$$S(f) = \frac{V_b^2 T_b}{2} \left[ \frac{\sin(\pi f T_b)}{\pi f T_b} \right]^2$$

$$\Rightarrow S(f) = \frac{V_b^2 T_b}{2} \left[ \frac{\sin(\pi f T_b)}{\pi f T_b} \right]^2.$$



\* PSD of BPSK signal:

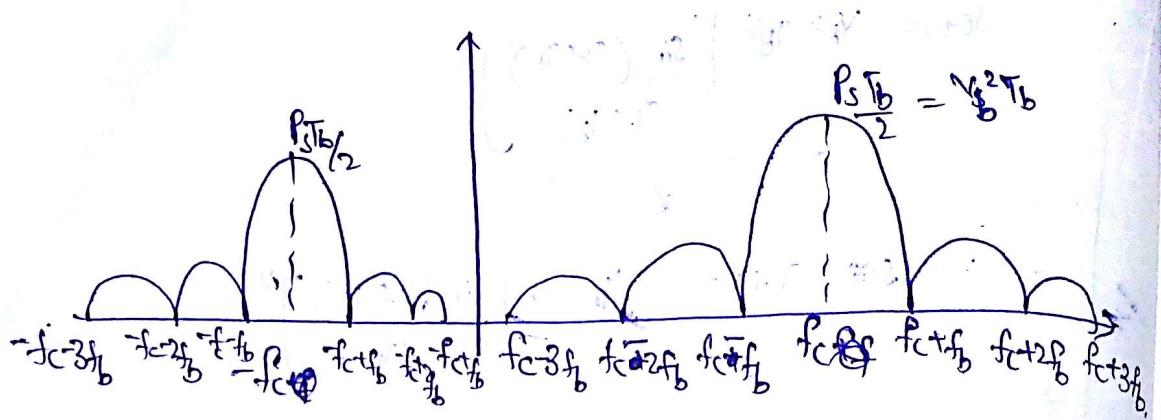
\* The BPSK Signal is generated by modulating a carrier by the base band signal  $b(t)$ .

\* Due to the modulation of the carrier freq "f\_c" the spectral components are translated from,  $f \rightarrow f_c + f$  &  $f_c - f_m$ .

\* The magnitudes of these two components are divided by

half

$$\therefore S_{BPSK}(f) = \frac{V_b^2 T_b}{2} \left[ \left( \frac{\sin(\pi(f_c - f)T_b)}{\pi(f_c - f)T_b} \right)^2 + \left( \frac{\sin(\pi(f_c + f)T_b)}{\pi(f_c + f)T_b} \right)^2 \right]$$



$$B.W = f_c + f_b - f_c + f_b$$

$$B.W = 2f_b$$

\* B.W of BPSK signal :-

If  $\gamma/T_b = f_b$  then the main lobe Extends from  $f_c - \gamma/T_b$  to  $f_c + \gamma/T_b$  & centered at  $f_c$

\* B.W of BPSK =  $2f_b$

Hence, the min B.W of BPSK signal is 2 times of bit rate.

\* Draw backs of BPSK

To generate the carrier in the receiver we start by Squelching

X03-08-12\*

$$b(t) \cdot \sqrt{2} p_s \cos(2\pi f_c t + \theta)$$

\* if the received signal is  $-b(t) \cdot \sqrt{2} p_s \cos(2\pi f_c t + \theta)$ , then  
the square signal remains the same as before.

\* Hence, the received carrier is unchanged even if the IF  
Signal has changed its sign.

∴ it is not possible to determine the received  
Signal is equal to  $b(t)$  or  $-b(t)$ .

this results in ambiguity in the OF Signal

\* This problem can be eliminated by using differential

Phase Shift Keying (DPSK)

\* Other problems of BPSK are ISI & Inter channel

Interference.

\* But these can be minimised by appropriate design of  
Band pass filter in the receiver.

the received

### Q3. Coherent BFSK :-

- \* In BFSK the frequency of the carrier is shifted according to the binary symbol.
- \* Now even, the phase of the carrier is unaffected.
- \* If  $b(t) = 1 \rightarrow$  then  $S_1(t) = \sqrt{2P_s} \cdot \cos[2\pi f_c t + \omega_2 t]$ .
- \* If  $b(t) = 0 \rightarrow$  then  $S_2(t) = \sqrt{2P_s} \cdot \cos[2\pi f_c t - \omega_1 t]$ .
- \* Coder "n" is freq shift
- \* The following conversion table is used to combine the above two FSK equations.

Table I : Conversion table of BFSK.

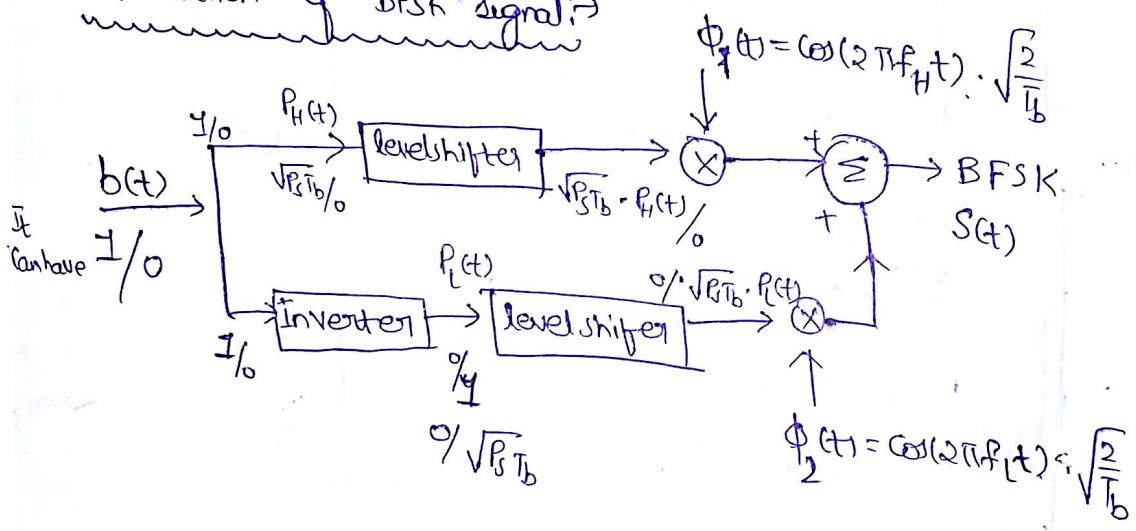
$b(t)$	$d(t)$	$P_H(t)$	$P_L(t)$
$+1V$	$+1V$	$+1V$	$0V$
$0V$	$-1V$	$0$	$+1V$

\* The mark frequency ( $f_M$  or  $f_H$ ) is used for transmission of symbol "1" & space frequency ( $f_S$  or  $f_L$ ) is used for transmission of symbol "0" & are given by

$$* f_M \text{ or } f_H = f_c + \frac{\Omega}{2\pi}$$

$$* f_S \text{ or } f_L = f_c - \frac{\Omega}{2\pi}$$

\* Generation of BFSK signal:



\* The % of the level shifter will be either  $\sqrt{P_{STb}}$   
(if  $b(t) = 1$ ) or 0 (if  $b(t) = 0$ ).

\*  $\Phi_1(t)$  &  $\Phi_2(t)$  are orthogonal signals if are applied to a product modulator.

\* In one bit period " $T_b$ ",  $\Phi_1(t)$  or  $\Phi_2(t)$  have integral no. of cycles.

\* Thus, the modulated signal is having continuous phase.

\* QPSK from both the multipliers are not possible at a time.

Since,  $P_H(t) \oplus P_L(t)$  are complementary to each other.

$\therefore$  If  $P_H(t) = 1$  then QPSK will be only due to upper.

Product modulator (PM) & then lower PM QPSK will be 0.

Since,  $P_L(t) = 0$ .

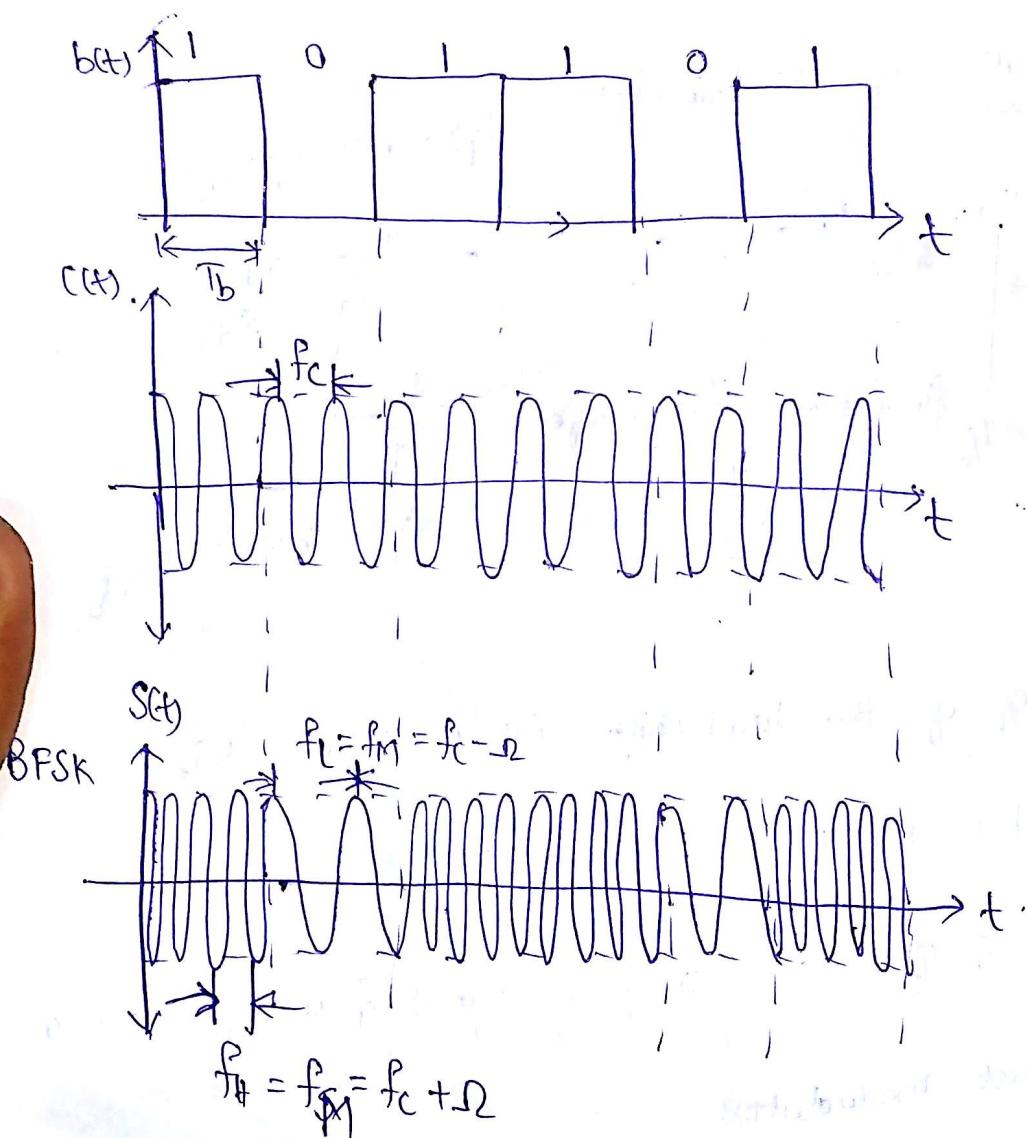


Fig. BFSK WAVEFORMS

\* Spectrum of BFSK \*

\* From the Block diagram of BFSK,  $S(t)$  may be written as

$$S(t) = \sqrt{2P_s} \cdot P_H(t) \cdot \cos(2\pi f_H t).$$

$$\cancel{S(t)} = \sqrt{2P_s} \cdot P_L(t) \cdot \cos(2\pi f_L t). \rightarrow ①$$

\* Now, Consider the Eq of BPSK

$$\underset{\text{BPSK}}{S(t)} = b(t) \cdot \sqrt{2P_s} \cdot \cos(2\pi f_c t).$$

Bipolar

$$\text{Consider } P_H(t) = \frac{1}{2} + \frac{P_H'(t)}{2}; P_L(t) = \frac{1}{2} + \frac{P_L'(t)}{2}$$

\* from ①, ② we get

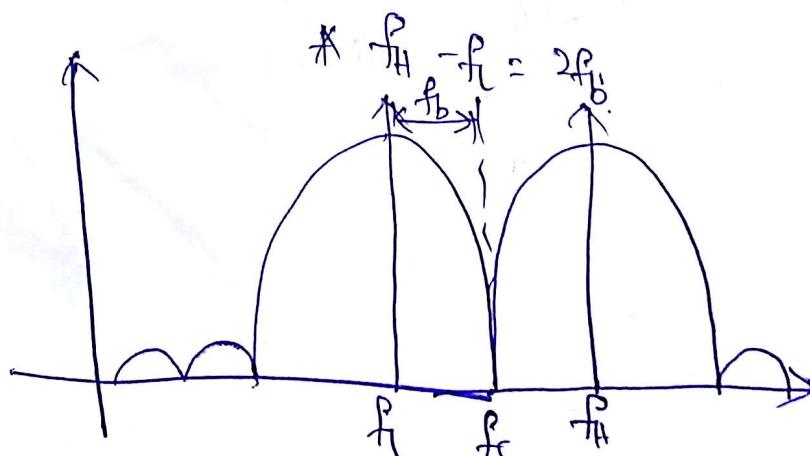
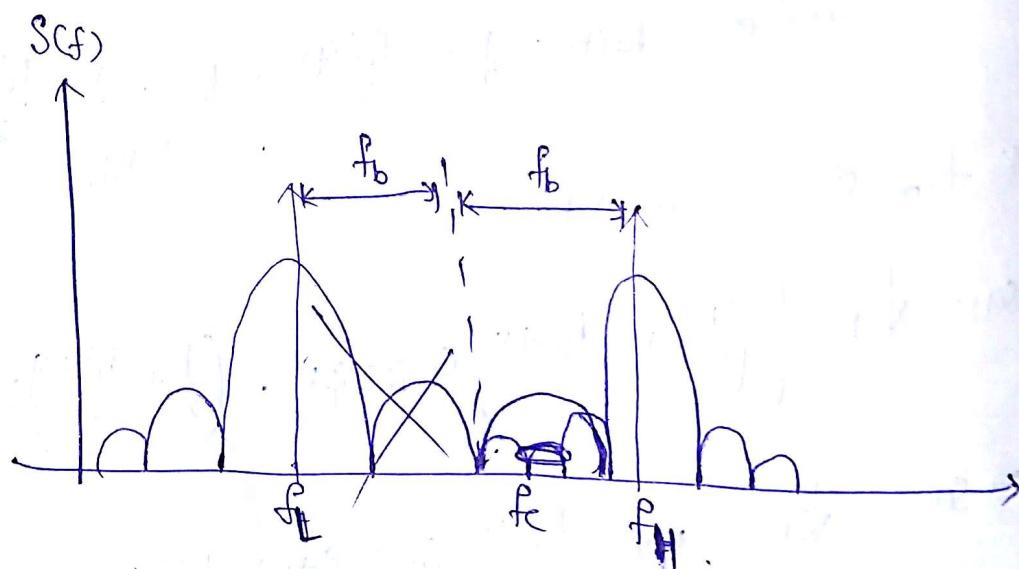
$$\Rightarrow S(t) = \sqrt{2P_s} \left[ \left( \frac{1}{2} + \frac{P_H'(t)}{2} \right) \cos(2\pi f_H t) + \left( \frac{1}{2} + \frac{P_L'(t)}{2} \right) \cos(2\pi f_L t) \right]$$

$$\Rightarrow S(t) = \sqrt{2P_s} \left[ \underbrace{\frac{1}{2} + \frac{P_H'(t)}{2}}_{\cos(2\pi f_H t)} \cos(2\pi f_H t) + \underbrace{\frac{P_L'(t)}{2}}_{\cos(2\pi f_L t)} \cos(2\pi f_L t) \right]$$

$$\frac{\cos(2\pi f_H t) + \cos(2\pi f_L t)}{2}$$

$$S(t) = \sqrt{\frac{P_S}{2}} \cos(2\pi f_H t) + \sqrt{\frac{P_S}{2}} \cos(2\pi f_L t) + \sqrt{\frac{P_S}{2}} P_H^I(t) \cos(2\pi f_H t) \\ + \sqrt{\frac{P_S}{2}} P_L^I(t) \cos(2\pi f_L t)$$

$$S(f) = \sqrt{\frac{P_S}{2}} \left[ d(f - f_H) + d(f + f_H) \right] \\ + \frac{P_S T_b}{2} \left\{ \frac{\sin(\pi f_H T_b)}{\pi f_H T_b} \right\}^2 + \frac{P_S T_b}{2} \left\{ \frac{\sin(\pi f_L T_b)}{\pi f_L T_b} \right\}^2$$



\* B.W of BFSK signal :-

\* from the PSD of BFSK signal.

\* width of one lobe is  $2f_b$ ; the two main lobes  $f_H$  &  $f_L$  are placed such that the total width due to both main lobes is 4 times of  $f_b$ .

$$\text{i.e., } B.W_{\text{BFSK}} = 2f_b + 2f_b = 4f_b$$

$$\Rightarrow \boxed{B.W = 4f_b}$$

\* W.K.T the transmission B.W required for BFSK =  $2f_b$ .

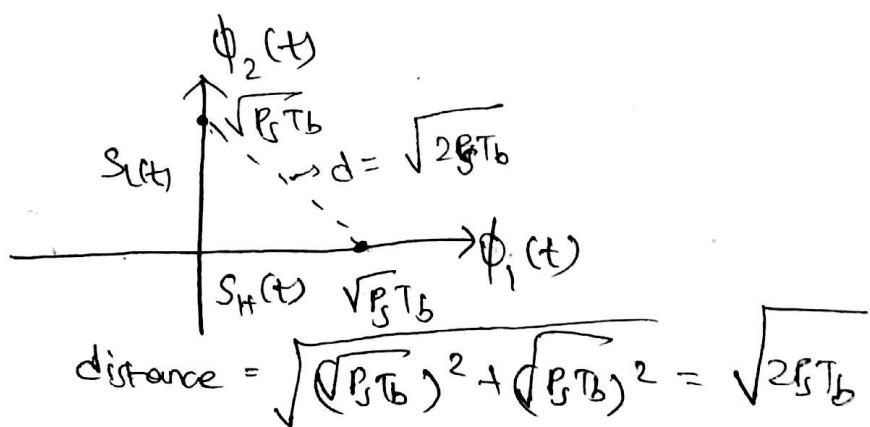
$$\boxed{B.W_{\text{BFSK}} = 2 B.W_{\text{BPSK}}}$$

\* From the block diagram of BFSK generation

$$S_H(t) = \sqrt{P_s T_b} \cdot \sqrt{\frac{2}{T_b}} \cdot \cos(2\pi f_H t) = \sqrt{P_s T_b} \phi_1(t)$$

$$S_L(t) = \sqrt{P_s T_b} \cdot \sqrt{\frac{2}{T_b}} \cos(2\pi f_L t) = \sqrt{P_s T_b} \phi_2(t)$$

$$f_M = f_H = f_C + \frac{f_2 - f_1}{2\pi}; \quad f_S = f_L = f_S - \frac{f_2 - f_1}{2\pi}$$



$$\Rightarrow d = \sqrt{2E_b} \quad \{ E_b = P_s T_b \rightarrow \text{bit energy} \}$$

\* W.K.T

$$d_{BPSK} = \sqrt{E_b}$$

$$\Rightarrow d_{BFSK} < d_{BPSK}$$

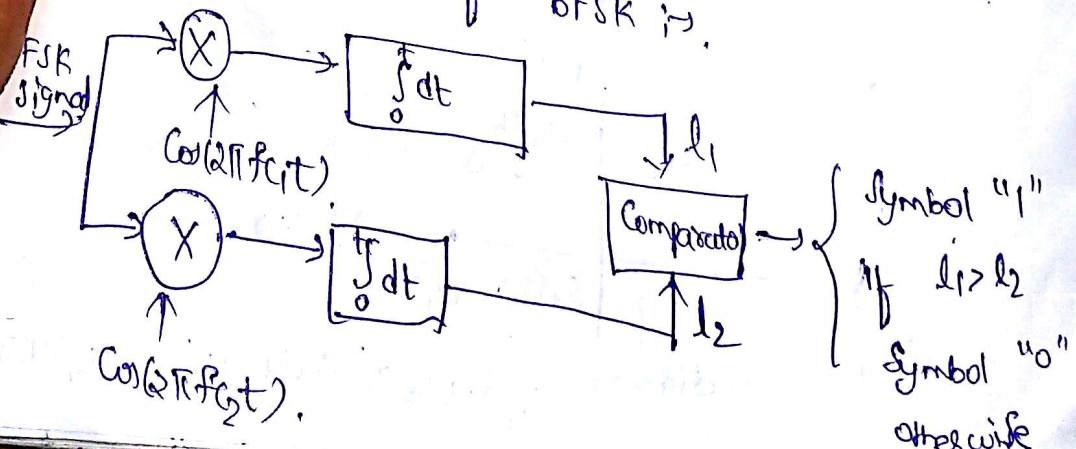
\* Advantages & Disadvantages of BFSK:

→ \* Even though the generation of BFSK is easier but it has disadvantages compared to BPSK.

→ \* BFSK B.W is  $4f_b$  which is twice the B.W of BPSK.

→ \* The distance "d" b/w the signal points is less for BFSK than BPSK. hence, probability of error ( $P_e$ ) or BER (Bit Error Rate) of BFSK is more than BER or  $P_e$  of BPSK.

\* Coherent detection of BFSK is:



	Bn
1	
2	Dif En
3	Pt
4	Sh
5	Pha
6	Pha (Compa Dete dat)
7	

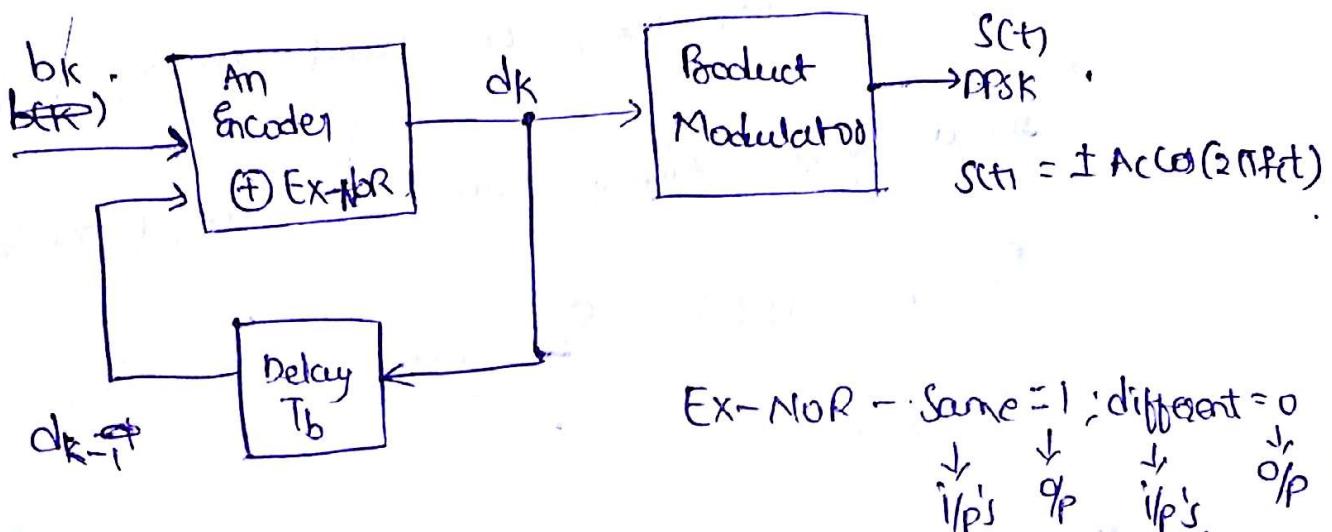
\* 04/08/17 \*

Take Xerox

\* 08/08/17 \*

\* Non-Coherent BPSK : Differential PSK (DPSK)

Generation of DPSK.



Generation of DPSK.

1	Binary data { $b_k$ }		0	0	1.	0	0	1	0	0	1	1
2	Differentially Encoded data { $d_k$ }	1	0	1	1	0	1	1	0	1	1	1
3	Phase of DPSK	0	$\pi$	0	$0$	$\pi$	$0$	$\pi$	0	$\pi$	0	0

- \* In order to eliminate the need for phase synchronization of coherent receiver of "PSK", a differential Encoding system can be used with PSK.
- \* The Binary data is Encoded in terms of signal transition  
Ex:-
  - \* Symbol zero may be used to represent transition in a given binary sequence (w.r.t previous Encoded bit) & symbol 1 to indicate no transition.
- \* This new signalling technique which combines differential Encoding with PSK is known as DPSK.
- \* A Schematic diagram for generation DPSK is shown in figure above.
- \* The binary sequence  $b_k$  is applied to Encoder. The QP of the Encoder is applied to a Product modulator.
- \* The other ip of the Product modulator is a sinusoidal carrier of fixed amplitude ( $A_c$ ) & freq ( $f_c$ ).

- \* The relation between the binary sequence & differentially Encoded version is given in above table for an assumed data sequence of "0010010011".
- \* Assume that Encoding is done in such a way that transition in the binary sequence w.r.t previous encoded bit is represented by a symbol "0" & no transition by symbol "1".
- \* It may be noted that an Extra bit {symbol 1} has been Arbitrarily chosen as an initial bit.
- \* The phase of the generated DPSK signal is shown in 3rd row of the table above.

#### \* Detection of DPSK :-

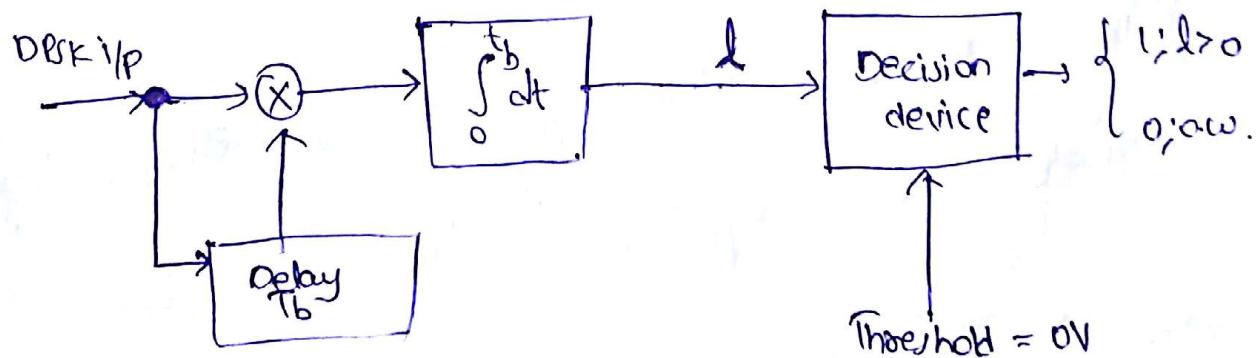


Fig. Receiver for detection of DPSK

A binary data stream "0010010011" needs to be transmitted by using DPSK technique. Prove that the reconstruction of the DPSK signal is independent of the choice of the reference bit {0 or 1}.

(Sol)

Binary data ( $b_k$ )	0	0	1	0	0	1	0	0	1	1
Differentially created ( $d_k$ )	0	1	0	0	1	0	0	1	0	0
Phase of DPSK	$\pi$	0	$\pi$	0	$\pi$	0	$\pi$	$\pi$	$\pi$	$\pi$
Shifted ( $b'_k$ )	0	1	0	0	1	0	0	1	0	0
Shifted ( $d'_k$ )	$\pi$	0	$\pi$	$\pi$	0	$\pi$	$\pi$	0	$\pi$	$\pi$
Phase of Compensation	-	-	+	-	-	+	-	+	+	+
Detected ( $b_k$ )	0	0	1	0	0	1	0	0	1	1

\*10log117\*

\* The received DPSK signal & its delayed signal by " $T_b$ " are applied to the multiplier

\* The delayed received signal is shown in 4<sup>th</sup> row of the table.

\* Assume that the channel noise is absent in the propagation

### Channel

\* The o/p of the difference is proportional to  $\cos \phi$

where, " $\phi$ " is the difference b/w carrier phase angle of the received & delayed DPSK signals measured in the same bit interval.

\* The phase angle of the DPSK signal its delayed

version is shown in 3rd & 5th row respectively.

\* The phase difference b/w the two sequences  $\phi$

Each bit interval is used to determine the sign of the phase Comparator output.

\* When " $\phi = 0$ " the integrated o/p is "tve" & when

" $\phi = \frac{\pi}{2}$  radian" the integrated o/p is "-ve"

\* By comparing the integrated o/p with a decision

-level of zero volt, the decision device

can reconstruct the binary sequence by

assume a symbol zero for -ve integrated o/p &

Symbol 1 for the o/p.

\* The reconstructed binary data is shown in the last row (7th row) of the tabel.

\* Thus, in the absence of channel noise, the receiver can reconstruct the transmitted binary data exactly.

\* Note is

\* The reconstruction is invariant with choice of the initial reference bit "(0 or 1)" in the encoded data.

\* Transmission B.W of DPSK

\* The previous bit is used to decide the phase shift of the next bit

∴ the symbol can said to have 2 bits

Hence, One symbol duration " $T_s$ " is equivalent to 2 bits duration " $T_b$ ".

$$\Rightarrow T_s = 2 T_b$$

\* The transmission B.W is expressed as

\* Hence,

{ Bit

\* Add

\* 1.

\* 2.

\* 2.

\* 3.

$$T_x \times \text{BW} = \frac{2}{T_s} = \frac{2}{2T_b} = \frac{1}{T_b} = f_b = \nu_b$$

$$\Rightarrow \text{BW}_{\text{DPSK}} = f_b \text{ or } \nu_b.$$

$$T_x \text{ BW}_{\text{BPSK}} = 2f_b$$

$$\Rightarrow \boxed{\text{BW}_{\text{DPSK}} = \frac{1}{2}(\text{BW}_{\text{BPSK}})}$$

\* Hence, the min B.W of DPSK signal is Equal to  $f_b$  or  $\nu_b$  { Bit Rate}, the max Base band signal frequency.

\* Advantages of DPSK :-

\*1. DPSK doesn't need carrier at the receiver end.

\*2. This means, that, complicated circuitry for retrieving local carrier reference is not required as in case of BPSK.

\*2. Transmission BW of DPSK is reduced  $\{f_b\}$  compared to BPSK  $\{2f_b\}$

\*3. ~~disa~~

### \* Disadvantages of BPSK :-

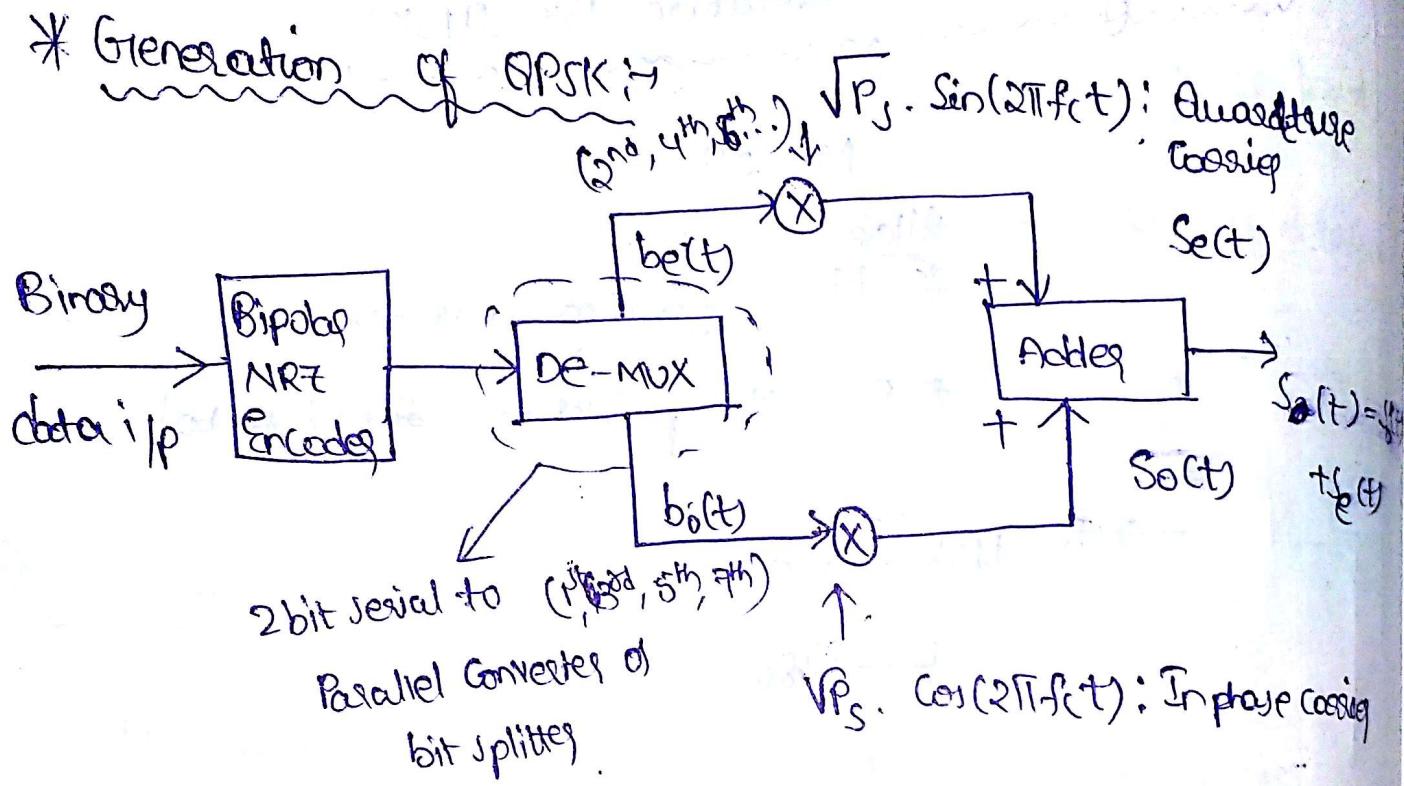
\*1 The "BER" or " $P_e$ " of DPSK is higher than that of BPSK. Because, DPSK uses two successive bits for its reception, Error in the first bit creates Error in the second bit also.. i.e.. Error propagation is more in DPSK. But in BPSK detection of each bit is independent. Hence,  $P_e$  (in BPSK) is less.

\*2. Noise interference is more in DPSK.

### \* DIFFERENTIALLY ENCODED PHASE SHIFT KEYING:- (DEPSK)

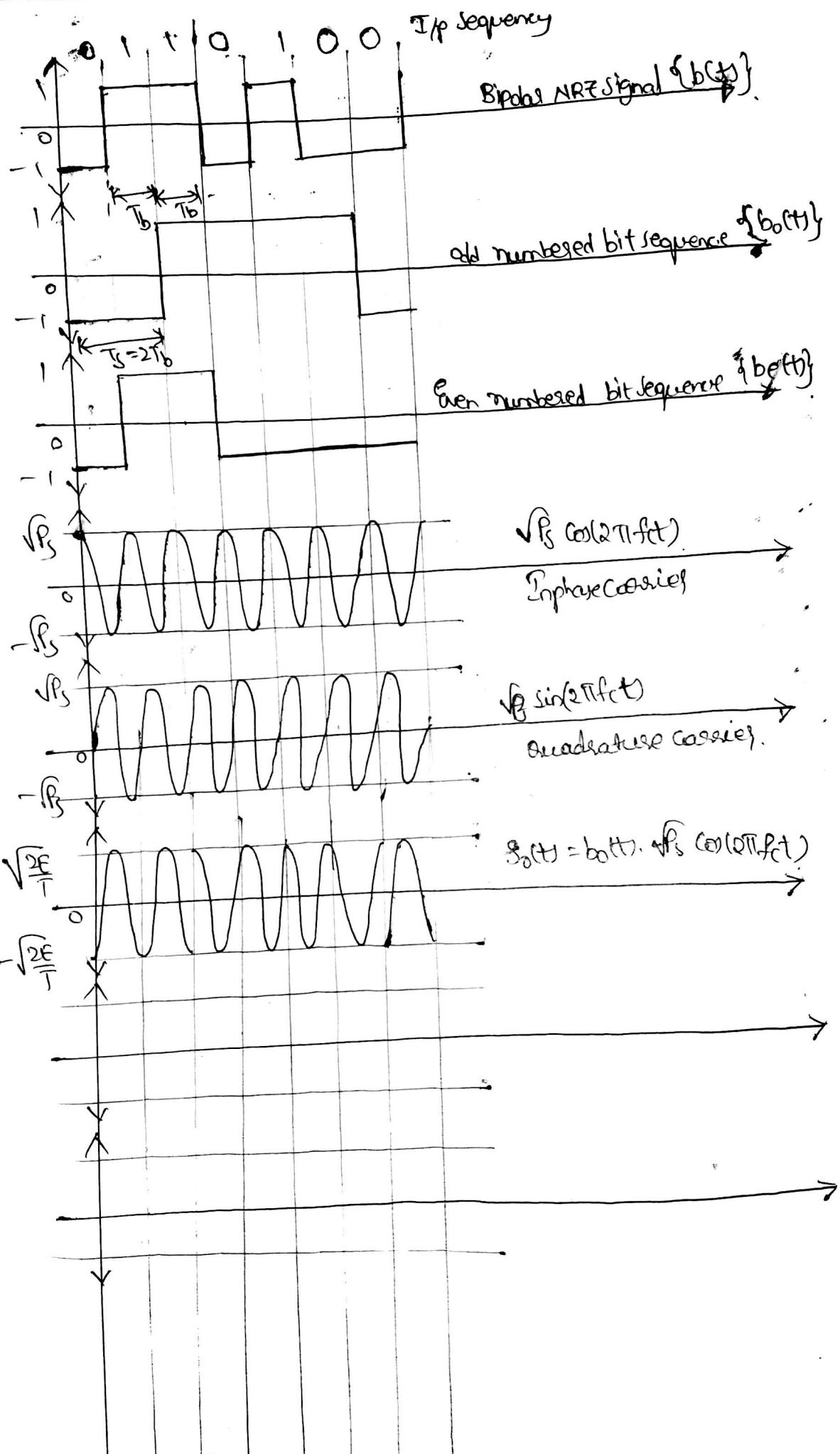
\* In DEPSK the

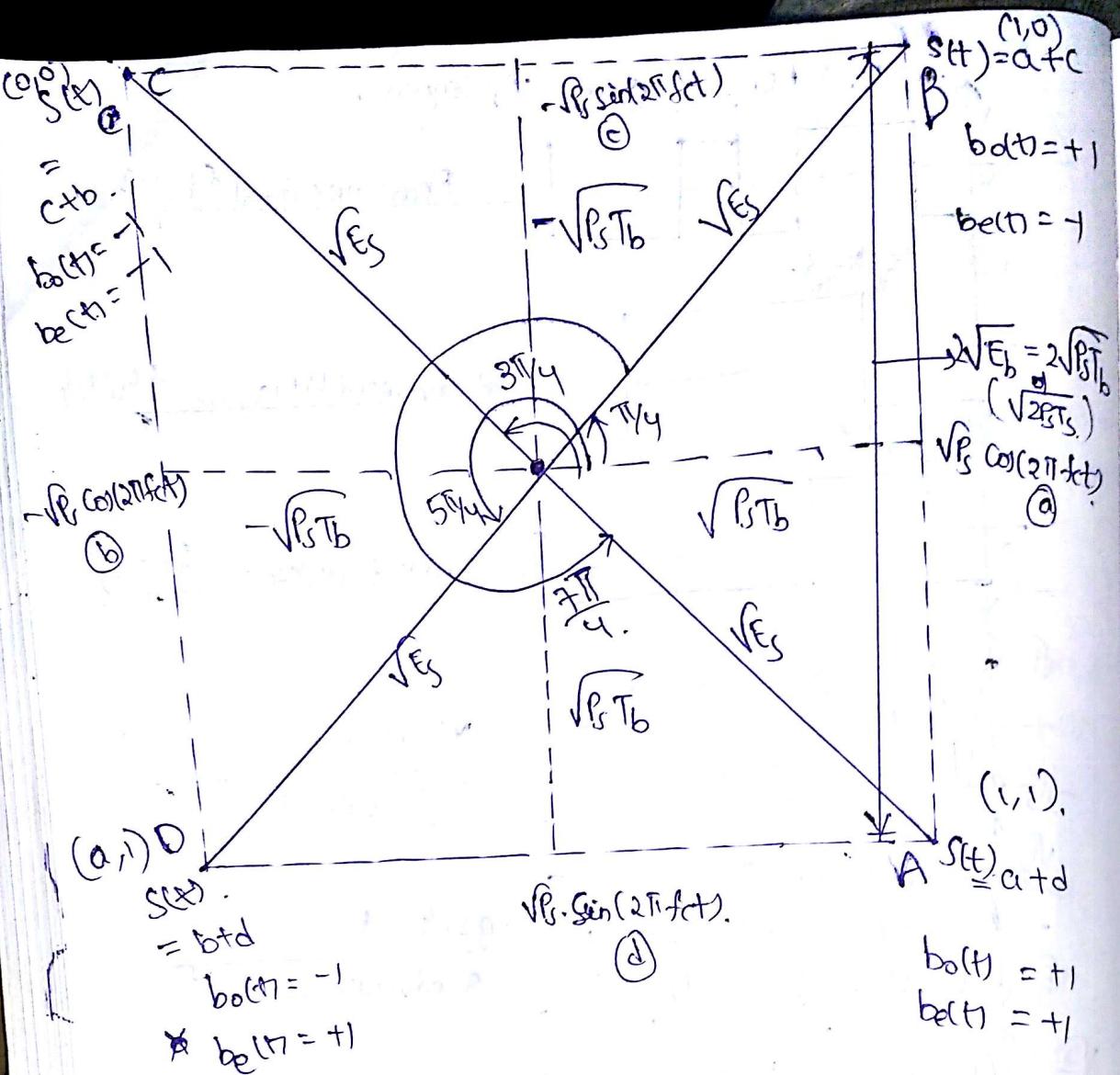
\* There are four symbols & the phase is shifted by  $\frac{2\pi}{4} = \frac{\pi}{2}$   
 $\approx 90^\circ$  for each symbol.



\*  $S_e(t) = b_e(t) \cdot \sqrt{P_s} \cdot \sin(2\pi f_c t)$

\*  $S_o(t) = b_o(t) \cdot \sqrt{P_s} \cdot \cos(2\pi f_c t)$





\* Depending upon the combination of 2 successive bits

the phase shift of the carrier changes.

This means that. A PSK signal may be represented as

$$S(t) = \sqrt{2P_s} \cdot \cos [2\pi f_c t + 2(m+1) \cdot \frac{\pi}{4}] \quad \text{where } m = 0, 1, 2, 3.$$

$$\Rightarrow S(t) = \sqrt{2P_s} \cdot \cos(2\pi f_c t) \cdot \cos[(2m+1)\frac{\pi}{4}]$$

$$= \sqrt{2P_s} \cdot \sin(2\pi f_c t) \cdot \sin[(2m+1)\frac{\pi}{4}]$$

\* From

\* The

$$\Rightarrow S(t) = \left\{ \sqrt{P_s T_s} \cos[(2m+1)\pi f_t t] \right\} \left( \sqrt{\frac{2}{T_s}} \cdot \cos(2\pi f_c t) \right)$$

$\hookrightarrow \phi_1(t)$

$$- \left\{ \sqrt{P_s T_s} \sin[(2m+1)\pi f_t t] \right\} \left( \sqrt{\frac{2}{T_s}} \cdot \sin(2\pi f_c t) \right)$$

$\hookrightarrow \phi_2(t)$

$\phi_1(t), \phi_2(t)$  are orthogonal carriers.

$$\Rightarrow S(t) =$$

\* Let  $b_0(t) = \sqrt{2} \cos[(2m+1)\pi f_t t]$

$$b_e(t) = \sqrt{2} \cdot \sin[(2m+1)\pi f_t t]$$

$$\Rightarrow S(t) = \sqrt{\frac{P_s T_s}{2}} (b_0(t) \cdot \phi_1(t) - b_e(t) \cdot \phi_2(t))$$

$$T_s = 2T_b \Rightarrow T_b = \frac{T_s}{2}$$

$$\therefore S(t) = \sqrt{P_s T_b} \cdot b_0(t) \cdot \phi_1(t) - \sqrt{P_s T_b} b_e(t) \cdot \phi_2(t)$$

$P_s T_b = E_b$  i.e., Bit Energy.

$$\Rightarrow S(t) = \sqrt{E_b} [b_0(t) \cdot \phi_1(t) - b_e(t) \cdot \phi_2(t)]$$

\* From each signal point we obtain two bits.

Ex:- at point "A" (1, 1); pt "B" (+1, 0)

\* The distance any pt from the origin is given as

\* distance OB  $\sqrt{(\sqrt{P_s T_b})^2 + (\sqrt{P_s T_b})^2}$

$$OB = \sqrt{2 P_s T_b}, \quad \left\{ T_b = \frac{T_s}{2} \right\}$$

$$P_s T_s = E_s \Rightarrow \text{Symbol Energy.}$$

$$\Rightarrow OB = \sqrt{E_s} = \sqrt{P_s T_s}$$

\* Hence, the length of each signal pt from te origin is " $\sqrt{E_s}$ "

\* Distance b/w the Signal Points.

\* The ability to determine a bit without error is measured by the distance between two nearest possible signal points in the signal space

\* This distance has .....

\* The distance represents noise immunity of the system.

It shows that noise immunities of BPSK & QPSK are same.

i.e.,  $P_e$  or BER are also same.

\* Spectrum of QPSK Signal:

\* The i/p signal  $b(t)$  is of duration " $T_b$ " {bit duration}

& it is a NRZ Bipolar signal

\* The PSB of such signal is given as

$$S(f) = V_b^2 \cdot T_b \cdot \left[ \frac{\sin(\pi f T_b)}{\pi f T_b} \right]^2$$

$$S(f) = P_s T_b \left[ \frac{\sin(\pi f T_b)}{\pi f T_b} \right]^2 \quad \text{at } R=1 \Omega$$

\*  $b(t)$  signal is divided into  $b_e(t)$  &  $b_o(t)$

with period of " $T_s = 2T_b$ "

\* If we assume symbol 1 & 0 are equi

Probable then PSB's of  $b_e(t)$  &  $b_o(t)$  are given by.

$$S_e(t) = P_s T_s \left[ \frac{\sin(\pi f T_s)}{\pi f T_s} \right]^2$$

$$S_o(t) = P_s T_s \left[ \frac{\sin(\pi f T_s)}{\pi f T_s} \right]^2$$

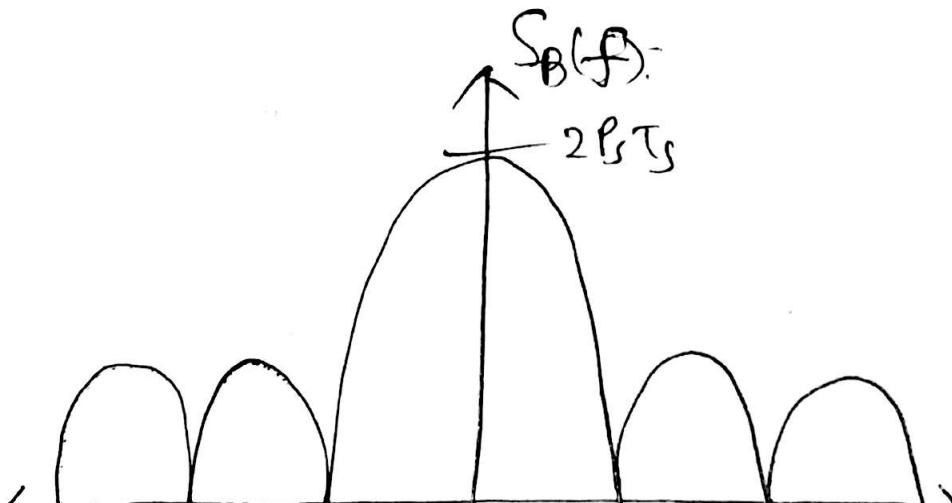
\* Because, Inphase & Quadrature Components are statistically independant the base band ~~PSD~~<sup>PSD</sup> of  $b(t)$  signal is equal to the sum of the individual PSD's of  $b_e(t)$  &  $b_o(t)$

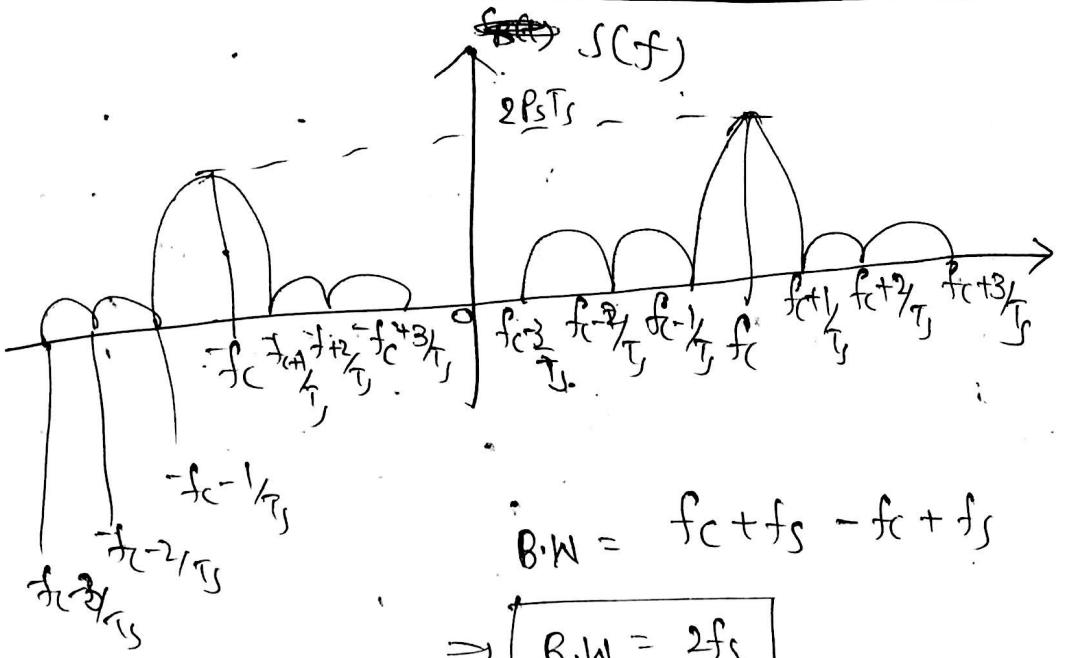
$$\text{i.e., } S_B(f) = S_e(f) + S_o(f).$$

$$\Rightarrow S_B(f) = 2P_s T_s \left[ \frac{\sin(\pi f T_s)}{\pi f T_s} \right]^2$$



PSD of Bipolar NRZ Signal i.e.,  $b(t)$





$$B.W = f_c + f_s - f_c + f_s$$

$$\Rightarrow \boxed{B.W = 2f_s}$$

$$\Rightarrow B.W = \frac{2}{T_b} = \frac{2}{2T_b} = \frac{1}{T_b}$$

$$\Rightarrow \boxed{B.W = f_b}$$

$$B.W_{QPSK} = f_b = \gamma_b.$$

w.r.t.

$$\boxed{B.W_{BPSK} = 2f_b \approx 2\gamma_b}$$

Hence, the transmission B.W of QPSK is  $\frac{1}{2}$  of the

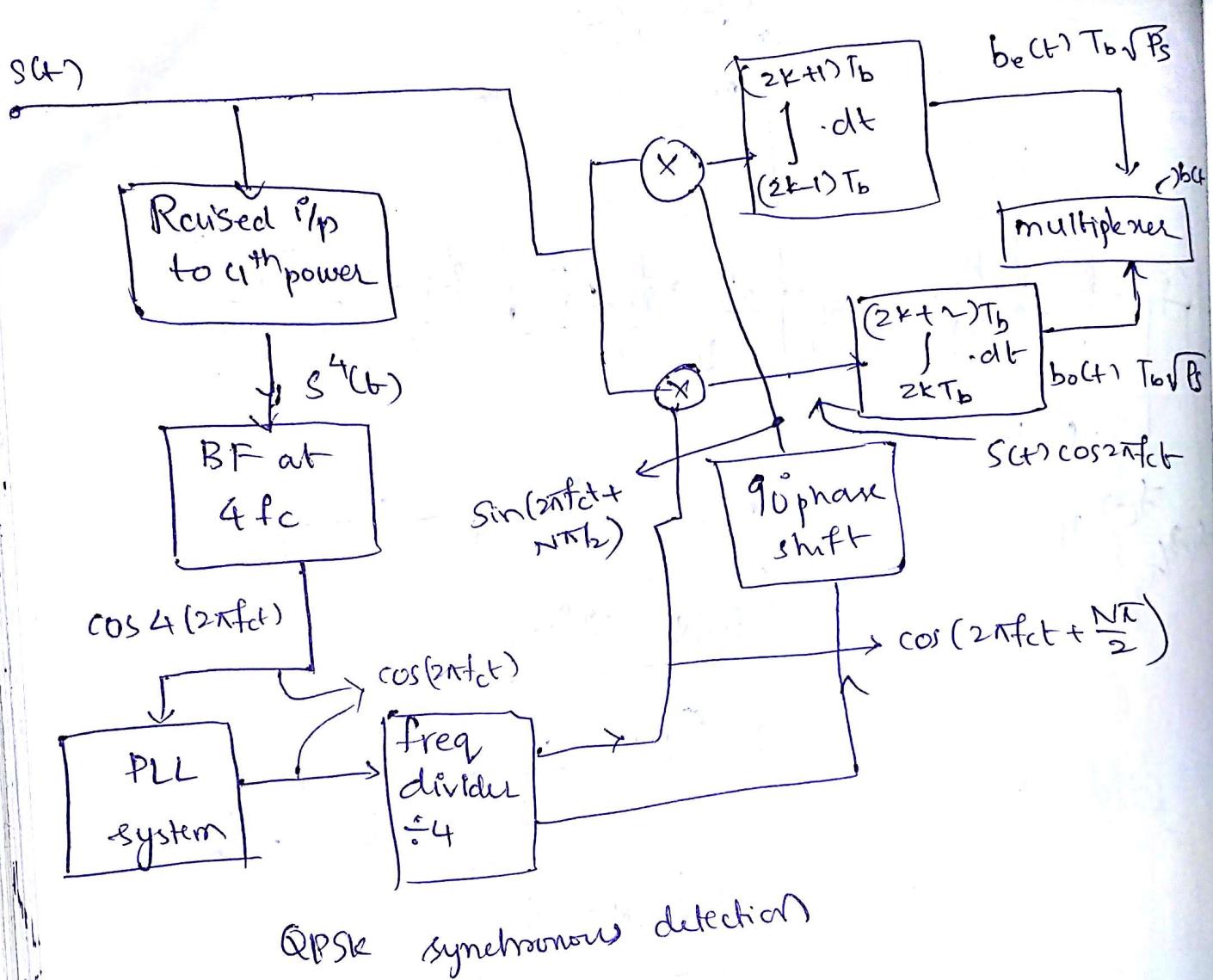
tx B.W of BPSK:

~~$$B.W_{QPSK} = \frac{1}{2} B.W_{BPSK}$$~~

$$\boxed{B.W_{QPSK} = \frac{1}{2} B.W_{BPSK}}$$

$$\text{Similarly } B.W_{8PSK} = \frac{1}{3} B.W_{BPSK}.$$

$$B.W_{16PSK} = \frac{1}{4} B.W_{BPSK}.$$



\* @12/08/17 \*

\* Quadrature amplitude shift keying {QASK}

or

\* Quadrature amplitude Modulation {QAM}