

Код программы

Исходный код 1: Метод отсекающей гиперплоскости

```
1  /*
2  * kelly_cutting_plane.hpp
3  * Kelley's convex cutting plane algorithm.
4  * Vladimir Rutsky <altsysrq@gmail.com>
5  * 27.04.2009
6  */
7
8  #ifndef NUMERIC_KELLEY_CUTTING_PLANE_HPP
9  #define NUMERIC_KELLEY_CUTTING_PLANE_HPP
10
11 #include "numeric_common.hpp"
12
13 #include "linear_problem.hpp"
14 #include "linear_problem_algs.hpp"
15 #include "simplex_alg.hpp"
16
17 #include <vector>
18
19 #include <boost/assert.hpp>
20 #include <boost/concept/assert.hpp>
21 #include <boost/concept_check.hpp>
22
23 namespace numeric
24 {
25     namespace kelly_cutting_plane
26     {
27         // For details see
28         // David G. Luenberger, Yinyu Ye
29         // Linear and Nonlinear Programming, Third Edition
30         // section 14.8 Kelley's convex cutting plane algorithm (p. 463).
31
32         // Finds linear function minimum prefer to convex differentiable constraints.
33         // min  $c^T * x$ ,  $g(x) \leq 0$ 
34         //  $g(x)$  and  $\text{grad } g(x)$  are defined by coordinates through iterators.
35         // Initial constraints and problem formalization is stored in common linear problem
36         // structure,
37         // which is expanded by new constraints along algorithm run.
38         // TODO: Handle more cases, return value should be enumeration of different exit
39         // statuses.
40
41         template< class S, class CLPTraits, class FuncIterator, class GradFuncIterator >
42         inline
43         vector<S>
44         find_min( FuncIterator funcBegin, FuncIterator funcEnd,
45                 GradFuncIterator gradFuncBegin, GradFuncIterator gradFuncEnd,
46                 linear_problem::common_linear_problem<S, CLPTraits> &commonLP )
47         {
48             typedef CLPTraits clp_traits;
49             typedef S scalar_type;
50             typedef vector<scalar_type> vector_type;
51             typedef matrix<scalar_type> matrix_type;
52             typedef zero_matrix<scalar_type> zero_matrix;
53             typedef scalar_traits<scalar_type> scalar_traits_type;
54
55             typedef typename FuncIterator::value_type function_type;
56             typedef typename GradFuncIterator::value_type gradient_function_type;
57
58             typedef linear_problem::common_linear_problem <scalar_type>
59                 common_linear_problem_type;
60             typedef linear_problem::canonical_linear_problem <scalar_type>
61                 canonical_linear_problem_type;
62             typedef typename linear_problem::converter_template_type<scalar_type>::type
63                 converter_type;
64
65             // TODO: Using same type in much places now (like scalar_type).
66             BOOST_CONCEPT_ASSERT(( boost::UnaryFunction<function_type, scalar_type,
67                 vector_type> ));
```

```

61 BOOST_CONCEPT_ASSERT((boost::UnaryFunction<gradient_function_type, vector_type,
62     vector_type>));
63 // TODO: Assert that input constraints are valid (they rise correct LP).
64 BOOST_ASSERT(linear_problem::is_valid(commonLP));
65
66 size_t const n = linear_problem::variables_count(commonLP);
67
68 BOOST_ASSERT(n > 0);
69
70 // Storing constrain function and its gradient.
71 std::vector<function_type> g (funcBegin, funcEnd);
72 std::vector<gradient_function_type> gGrad(gradFuncBegin, gradFuncEnd);
73
74 size_t nIterations(0);
75 size_t const nMaxIterations(1000); // debug
76 while (nIterations < nMaxIterations)
77 {
78     // Solving linear problem.
79     vector_type commonResult;
80     simplex::simplex_result_type const result = solve_by_simplex(commonLP, commonResult
81 );
82     BOOST_ASSERT(result == simplex::srt_min_found); // FIXME: Handle other cases.
83     BOOST_ASSERT(linear_problem::check_linear_problem_solving_correctness(commonLP));
84
85     // Adding new limits to common linear problem according to elements that satisfies
86     //  $g_i(x) > 0$ .
87     bool isInside(true);
88     for (size_t r = 0; r < n; ++r)
89     {
90         scalar_type const gr = g[r](commonResult);
91         if (gr > 0)
92         {
93             isInside = false;
94
95             // Adding new constraint:
96             //  $g[r](commonResult) + grad\ g[r](commonResult) * (x - commonResult) \leq 0$ .
97             // or
98             //  $grad\ g[r](commonResult) * x \leq grad\ g[r](commonResult) * commonResult - g[r]$ 
99             //  $(commonResult)$ .
100
101             size_t const newRows = commonLP.b().size() + 1;
102             BOOST_ASSERT(commonLP.ASign().size() == newRows - 1);
103             BOOST_ASSERT(commonLP.A().size1() == newRows - 1);
104             BOOST_ASSERT(commonLP.A().size2() == n);
105
106             commonLP.b().resize(newRows, true);
107             commonLP.A().resize(newRows, n, true);
108             commonLP.ASign().resize(newRows, true);
109
110             commonLP.ASign()(newRows - 1) = linear_problem::inequality_leq;
111
112             vector_type const grGrad = gGrad[r](commonResult);
113             BOOST_ASSERT(!eq_zero(norm_2(grGrad))); // FIXME: I think this is possible case
114
115             row(commonLP.A(), newRows - 1) = grGrad;
116
117             commonLP.b()(newRows - 1) = inner_prod(grGrad, commonResult) - gr;
118
119             // Assert that builded constraint cuts previosly founded minimum point.
120             BOOST_ASSERT(inner_prod(row(commonLP.A(), newRows - 1), commonResult) >
121                 commonLP.b()(newRows - 1));
122
123             BOOST_ASSERT(linear_problem::assert_valid(commonLP));
124         }
125     }
126
127     if (isInside)
128     {
129         // Founded minimum of linear problem lies inside convex limits, so this is the
130         // answer.

```

```

125         return commonResult;
126     }
127 }
128
129 BOOST_ASSERT(0); // FIXME: Handle different cases.
130 return vector_type(0);
131 }
132 } // End of namespace 'kelley_cutting_plane'.
133 } // End of namespace 'numeric'.
134
135 #endif // NUMERIC_KELLEY_CUTTING_PLANE_HPP

```