

Binary Search...

→ How do we calculate upper bound & lower bound in a binary search.

• Upper bound ($> K$)

Suppose we have an array →

l

1	2	4	6	8	10	15
---	---	---	---	---	----	----

 h

and we have value of $K = 7$.

Here, we are supposed to "find the smallest value greater than K "

So, from above array we know that the answer would be "8".

→ Here the 1st way to solve this is →

① $O(n)$ Linear Search + Sorted space (that is our array).

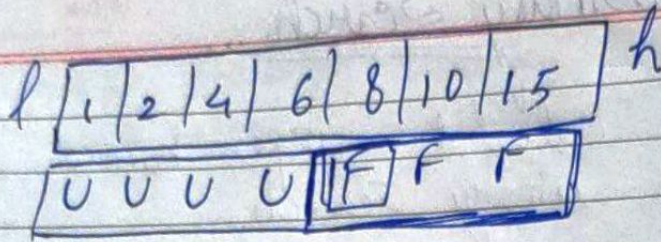
So, we can divide our search space into two zones →

(since, it's upper bound)

(a) values $> K$ → Favorable zone &

(b) values $< K$ → Unfavorable zone.

[Here, $l = \text{low}$, $h = \text{high}$]



→ So, here our answer lies in the second zone, and the first element of our second zone is the answer we wanted.

[Since, we know that if our value lies in the favorable zone,

we add "+1" to our mid value to move to the next index

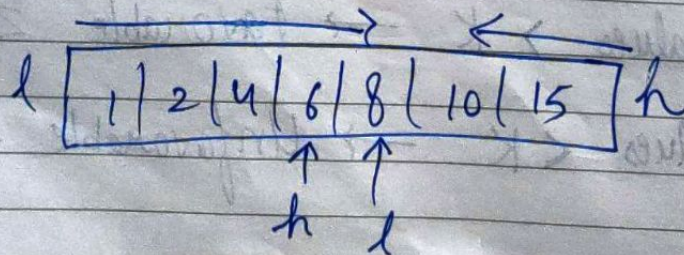
and similarly in case of unfavorable zone

we simply "subtract" "-1" from our mid value to move to the previous index.

So, after all the searching in the end our l will point to the first element of our ~~favorable zone~~ second zone

and h will point towards the last element of our first zone.]

Ex →



$\{(h+1, l)\}$

So, the algo for this or the solⁿ for this would be →

```

while (l <= h)
{
    mid = l + (h - l) / 2;
    if (a[mid] > K)
    {
        h = mid - 1;
    }
    else
    {
        l = mid + 1;
    }
}
return l;

```

→ Lower Bound $\geq K$

if $K = 6$

ans
↓

1	4	5	6	8	10	12
T	T	T	F	F	F	F

So, as we did for the upperbound, in the similar way it will be calculated and the value which we will be returning would be 'l' or 'h+1'.

① Valid Perfect Square →

Given a Positive integer num, write a function which returns True, if num is a perfect square else False.

Ex-① num = 16
Output → True

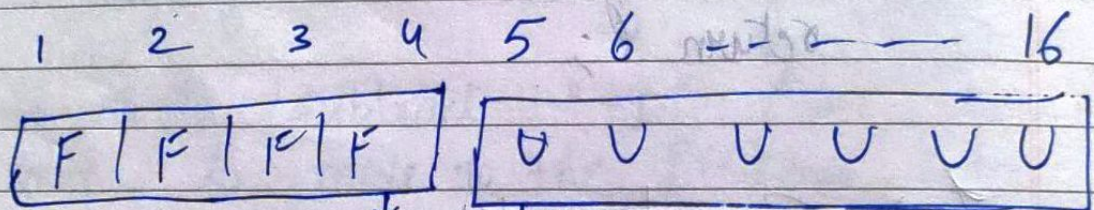
} since, 16 is a perfect square of 4.

② num = 14
Output → False

} since, 14 is not a perfect square of any no.

(ixi) value $\leq K \rightarrow$ Favorable

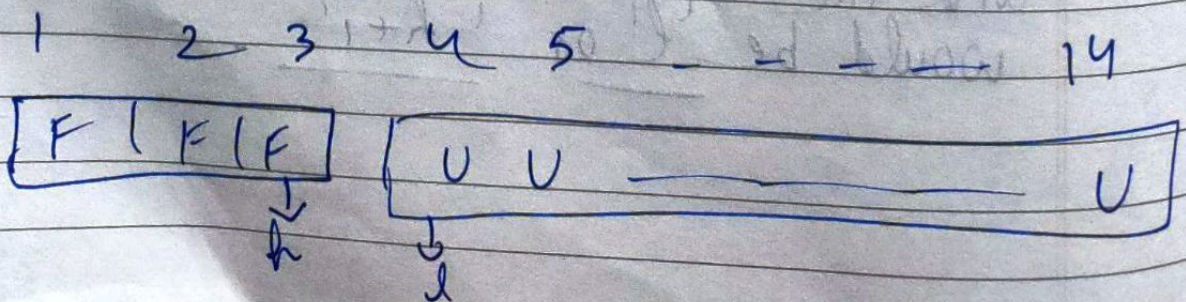
①
So,



for $1 \times 1 = 1 \checkmark \leq K$, $l = mid + 1$
 $2 \times 2 = 4 \leq 11$
 $3 \times 3 = 9$
 $4 \times 4 = 16$ (Terminates here).

return h;

but in 2nd test case →



since $3 \times 3 = 9$ and $4 \times 4 = 16$ \hookrightarrow 14 lies somewhere in between,
so we can't return h ...

So, in order to ~~sat~~ get the correct answer
we will $\text{return, } h \times h == K$

true, else it \downarrow if it is true it will return
will return 0.