

1. Let us consider the training data to be

$$f(x_i, w_i) = \left\{ (x_i, w_i), i=1, \dots, N \right\}$$

Here

x_i = Row

w_i = Height 'H'

Considering training Parameters to be ϕ_0, ϕ_1 , we can use the maximum likelihood estimation & considering further that the data pairs are independent & identically distributed, the equation is.

$$P(w_i | x_i, \theta) = \prod_{i=1}^N \frac{1}{\sqrt{2\pi\sigma^2}} \exp \left\{ -\frac{1}{2} \frac{(w_i - (\phi_0 + \phi_1 x_i))^2}{\sigma^2} \right\}$$

Here the learning parameters $\theta = \{\phi_0, \phi_1, \sigma^2\}$

2. To derive the values of $\{\phi_0, \phi_1, \sigma^2\}$

let

$$L = \frac{1}{\sqrt{2\pi\sigma^2}} \exp \left\{ -\frac{1}{2} \frac{(w_i - (\phi_0 + \phi_1 x_i))^2}{\sigma^2} \right\}$$

as we need to consider derivatives, converting it to logarithmic terms would be easier.

$$L = \operatorname{argmax} \left[\sum_{i=1}^N \left(-\frac{1}{2} \left[N(\log 2\pi) + N \log(\sigma^2) + \sum_{i=1}^N \frac{(w_i - (\phi_0 + \phi_1 x_i))^2}{\sigma^2} \right] \right) \right]$$

Hence taking the derivative of L wrt ϕ_0, ϕ_1 & σ^2 we will find the values.