C Milestones

- Originally developed by Dennis Ritchie in early 70s for use with Unix as a general *system programming language*.
- In 1978, Kernighan and Ritchie publish The C Programming Language, popularly known as K&R1. C implementations based on book specification known as K&R1 C.
- 1980 standardization by ANSI and ISO; changes include function prototypes. Known as C89 or C90. K&R2 describes C89.
- 1990s standardization efforts led to C99; changes include variable-length arrays, inline functions.
- 2000's standardization efforts led to C11; changes include multithreading support, anonymous structures and unions, noreturn functions.

Distinguishing Features

- Strongly typed (compiler checks type compatibility) but allows programmer to selectively override type checking.
- Allows programmer to manipulate data at the bit-level.
- Support for directly manipulating memory addresses. This distinguishes C from higher-level programming languages where memory is abstracted out.
- Allows programmer total control over memory allocation.
- Uses a very limited macro system (compile-time text substitution).
- Higher level programming languages are often implemented by being translated into C, at least initially.

Expressions vs Statements

- Expressions return a value which can be stored in a variable. Example of C expressions include arithmetic operators (involving operators like +, -, *, /, %), comparison expressions (with operators like ==, !=, <, <=, >, >=), logical expressions (involving operators like &&, ||, ! with 0 interpreted as false, non-0 as true), bit expressions (involving operators like &, |, ~, >>, <<), assignment expressions (involving operators like =, +=, *=, etc).</p>
- Statements do not have a value. Example of C statements are if, for, while, do, switch.

All programming languages have some kind of expression construct, but not all programming languages have statement constructs.

Data

In any programming language there are two kinds of data:

Primitive Data Data which has no internal structure advertized by the language. In C, this includes various flavors of integers and real numbers as well as pointers (C does also allow getting at the internal structure, but this is a low-level feature).

Composite Data Data which is a collection of other data. In C, this includes arrays (sequence of data of the same type) and structures/unions (collections of data of possibly different types).

Ultimately, all data entities are represented as a sequence of bytes. In C, the number of bytes taken up by any data entity x is given by the expression sizeof(x).

C Integers

Various flavors of integers (in order of non-decreasing size):

```
short At least 2 bytes.
```

int At least 2 bytes, can be 4 or 8 depending on machine.

long At least 4 bytes, can be 8 depending on machine.

long long At least 8 bytes.

- Can have modifier signed or unsigned. Default is signed.
- If unsigned used without a type, then type is int.

Integer Declarations with Initializers

```
//signed by default
short answer = 42;
                               //signed: usually 2 bytes
                              //signed: often 4 bytes
int next = answer + 1;
                          //4 or 8 bytes
long twice = 2 * answer;
long long half = answer/2; //at least 8 bytes
                             //use of a long literal
long value = 99L;
//explicitly declared unsigned
unsigned short s1 = 22;
unsigned short s2 = 1 << 15; //ok
unsigned short s3 = 1 << 16; //may overflow
unsigned u = 99;
                               //type defaults to int
short s4 = 1 << 15:
                                //signed: may overflow
                                //to negative
```

Characters in C

- C does not really support characters or strings.
- A variable declared with type char, is declaring a 1-byte integer.
- If a variable is declared as a char, without a signed or unsigned modifier, then it's signed-ness is undefined.
- C does support character literals enclosed within single quotes.
 These integer value equal to code of character in the local
 character encoding (for example, 'A' has integer value 65 in
 the ASCII encoding).
- Character literals support escapes as in '\n' newline, '\t' tab and '\0' NUL character.
- Since characters are merely integers, arithmetic can be performed with them as in char c; ... c - '0', but the results are not portable in that they may vary with different character encodings.

Char Declarations

Chars are always 1 byte.

C Arrays

- Arrays are a fundamental abstraction in many programming languages which abstract out the random-access property of the main memory in current computer technology.
- In C, arrays are declared using square brackets after the name of the array.

```
int a[3];
int b[] = { 1, 2, 3 };
Employee employees[numEmployees];
```

 A C string is an array of characters terminated by a NUL character '\0'.

```
char hello[] = "hello"; //array of 6 char's
```

C arrays are closely related to pointers (more about that later).



Integer Sum Program

```
In sum.c:
#include <stdio.h>
static int acc = 123;
int main()
  int values[] = { 2, 5, -9, };
  for (int i = 0; i < sizeof(values)/sizeof(values[0]);</pre>
       i++) {
    int value = values[i];
    acc += value;
  printf("%d\n", acc);
  return 0;
```

Integer Sum Program Log

Compiling:

```
$ gcc -g -Wall -std=c11 sum.c -o sum
```

- -g allows debugging compiled program.
- -Wall used for turning on reasonable warnings.
- -std=c11 allows use of C11 features.
- -o sum creates executable in file sum (default is a.out).

Run using:

```
$ ./sum
121
$
```

Integer Sum Program Discussion

- acc is declared outside of any function. It is loosely referred to as a global variable.
- Variables declared outside any function have lifetime equal to that of the entire program.
- If a variable is declared with the static qualifier, then it has lifetime equal to that of the entire program but is visible only to the subsequent code in the same compilation unit (file).
- If a variable is declared with the extern qualifier, then it has lifetime equal to that of the entire program and is visible to the entire program. If there is no static specifier, then the declaration defaults to be extern.
- In current programming practice, global variables are regarded as evil and should be avoided as far as possible. Read-only globals are not as bad as read-write globals.

- Variables declared within a brace-delimited block are visible only within that block and (if there is no static qualifier) retain their value only during a single execution of that block.
- Specifically, variables declared within a function are visible only within that function and (if there is no static qualifier) retain their value only during a single activation of that function.
- These kind of auto-variables are invaluable in implementing recursive functions where multiple activations of a function are alive simultaneously.

```
int factorial(int n) {
   return (n <= 0) ? 1 : n * factorial(n - 1);
}
//factorial(4): n has values 4, 3, 2, 1, 0.</pre>
```

- Usually, best practice is to always provide an initial value for a variable when it is declared.
- Array values[] is initialized with initial values enclosed within braces.
- Could also be declared as int values[3] = { 2, 5, -9 };
 but the size would be redundant.
- Best practice is to omit the size of the array and let it be determined by the length of the initializer.

Since the array values[] has 3 elements, we could have coded the for-loop as:

```
for (int i = 0; i < 3; i++) {
    ...
}</pre>
```

- If we decided to add another element to values[], we would also need to change the loop bound to 4.
- A very important rule in programming is Don't Repeat
 Yourself (DRY). Specifically, you should avoid situations
 where changing one part of a program necessarily requires
 changing another part because the second part depends on the
 first part.

- The use of the complex expression
 sizeof(values)/sizeof(values[0]) avoids a DRY violation.
- The expression sizeof(values) gives the total number of bytes occupied by the values[] array and sizeof(values[0]) gives the total number of bytes occupied by the values[0] element. Hence the quotient gives the number of elements in the values[] array.

Integer Representation

- The C integer types can be regarded as abstract types which
 model a finite subset of the infinite set of all integers. These
 abstract types permits the usual arithmetic operations +, -, *,
 /, %, with results consistent with usual arithmetic (subject to
 size restrictions).
- However, C has operators like bitwise-and &, bitwise-or I, left-shift << and right-shift >> in which the representation of integers is no longer abstract. So it is necessary to understand the internal representation of integers.

Decimal Positional Notation

In positional notation, the value of a digit depends on its position in the number. Specifically, a decimal integer $d_{n-1}d_{n-2}\dots d_1d_0$ represents the number:

$$10^{n-1} \times d_{n-1} + 10^{n-2} \times d_{n-2} + \ldots + 10^1 \times d_1 + 10^0 \times d_0$$

For example,

$$123 == 1 \times 10^2 + 2 \times 10^1 + 3 \times 10^0$$

Positional notation is a big win over additive notations like *Roman numerals* as the value of a represented number increases exponentially with the length of the representation.



Positional Notation for a General Base

For a general base B and digits 0, 1, ..., B-1 in base-B, the value of an n-digit integer $b_{n-1}b_{n-2}...b_1b_0$ in base-B is given by:

$$B^{n-1} \times b_{n-1} + B^{n-2} \times b_{n-2} + \ldots + B^1 \times b_1 + B^0 \times b_0$$

For example, 0x123 (base-16) is

$$1 \times 16^2 + 2 \times 16^1 + 3 \times 16^0$$

which is 291\$, while 0123 (base-8) is

$$1 \times 8^2 + 2 \times 8^1 + 3 \times 8^0$$

which is 83.



Common Bases used in Programming

- Decimal base is almost always the default. Example: 75
- Base-2 binary numbers are commonly used within computers but usually too verbose for human use. Example: 01001011 binary which is 75 decimal. Not in standard C, available as gcc extension 0b01001011.
- Base-16 commonly used as it is easy to convert to/from binary. Digits 0 .. 9 have usual meanings, A .. F (can also be lower-case) represent values 10 .. 15. An example of a C hexadecimal literal is 0x4B (or 0x4b) equal to decimal 75.
- Base-8 was used earlier when word-lengths were multiples of 3 bits (PDP-8: 12-bits) but not popular currently. In C, any integer starting with a leading 0 is octal. For example, C interprets 0113 as an octal literal equal to decimal 75. This can be a gotcha for the unwary.

Representations

Binary	Decimal	Hex	Oct
0000	0	0×0	00
0001	1	0×1	01
0010	2	0×2	02
0011	3	0×3	03
0100	4	0×4	04
0101	5	0×5	05
0110	6	0×6	06
0111	7	0×7	07

Representations Continued

Binary	Decimal	Hex	Oct
1000	8	0x8	010
1001	9	0×9	011
1010	10	0xA	012
1011	11	0xB	013
1100	12	0xC	014
1101	13	0xD	015
1110	14	0×E	016
1111	15	0×F	017

Octal, Hexadecimal Conversions in C

```
In bases.c:
static void
bases(long values[], int nValues)
  for (int i = 0; i < nValues; i++) {</pre>
    long v = values[i];
    printf("number: %ld == 0\%lo == 0X\%lX == 0x\%lx\n",
            v, v, v, v);
```

Octal, Hexadecimal Conversions in C: main()

```
In bases.c:
int
main()
  long values1[] = { 75, 123, 99 };
  long values2[] = { 075, 0x123, 0x99 };
  bases(values1, sizeof(values1)/sizeof(values1[0]));
  bases(values2, sizeof(values2)/sizeof(values2[0]));
  return 0;
```

Octal, Hexadecimal Conversions in C Log

```
$ ./bases
number: 75 == 0113 == 0X4B == 0x4b
number: 123 == 0173 == 0X7B == 0x7b
number: 99 == 0143 == 0X63 == 0x63
number: 61 == 075 == 0X3D == 0x3d
number: 291 == 0443 == 0X123 == 0x123
number: 153 == 0231 == 0X99 == 0x99
$
```

Signed Magnitude Representation of Signed Integers

Signed magnitude representation:

- Integer represented using a single sign bit (0 positive, 1 negative) and an unsigned magnitude.
- +75 has 8-bit signed magnitude representation 01001011; -75 has 8-bit signed magnitude representation 11001011;
- 0 has two representations: +0 00000000 and -0 10000000.
- Not used in practice, but useful when interpreting floating point representation as integers.

Two's Complement Representation

• Two's complement is the representation used currently for representing signed integers. Given bits $b_{n-1}b_{n-2}\dots b_1b_0$, the MSB is used as a sign bit with weight -2^{n-1} . The overall value is:

$$b_{n-1} \times -2^{n-1} + b_{n-2} \times 2^{n-2} \dots b_1 \times 2^1 + b_0 \times 2^0$$

- +75 has 8-bit 2's complement representation 01001011; -75 has 8-bit 2's complement representation 10110101 which is -128 + 53.
- To negate a 2's complement number, form its bit-complement and add 1 to the result. For example, -75 == (~01001011 + 1) == (10110100 + 1) == 10110101.



Two's Complement Examples

Examples of 8-bit 2's complement numbers:

```
1000 0000 == -128

1000 0001 == -127

1000 0010 == -126

1000 0011 == -125

...

1111 1111 == -1

0000 0000 == 0

0000 0001 == 1

...

0111 1111 == 127
```

Output Binary Representation

In out-bits.c:

```
static void out bits(short value, FILE *out)
  fprintf(out, "%d == 0x%x == 0%o == 0b".
          value, value, value):
  int nBits = CHAR_BIT * sizeof(value);
  unsigned mask = 0x1 << (nBits - 1);
  for (int i = 0; i < nBits; i++) {
    char c = (mask & value) ? '1' : '0';
    mask >>= 1:
    fprintf(out, "%c", c):
    if (i % 4 == 3 && i != nBits - 1) fprintf(out, " ");
  fprintf(out, "\n");
```

Output Binary Representation: main()

In out-bits.c:

```
int main()
  short values[] = {
    0, 16, 255, 1<<(sizeof(short)*CHAR_BIT - 2), -1
  };
  for (int i = 0;
       i < sizeof(values)/sizeof(values[0]);</pre>
       i++) {
    out bits(values[i], stdout);
  }
  return 0;
```

Output Binary Representation: Log

Two's Complement Features

- Asymmetric. With n-bits, non-negative numbers range from $0 cdots 2^{n-1} 1$ but the negative numbers range from $-1 cdots -2^{n-1}$. There is no positive counterpart to -2^{n-1} . This can result in subtle bugs.
- Each representable number has a unique representation. No multiple representations for 0. -0 == (0xFFFFFFFF + 1) == 0x00000000°.
- Note that an unsigned n-bit number can represent values in the range $0...2^n-1$. So the largest unsigned number is 1 more than twice the largest positive 2's complement number. This is something to keep in mind when converting between signed and unsigned representation.

C Integer Literals

As discussed previously, integer values can be specified in octal (leading 0), hexadecimal (leading 0x or 0X) or decimal (default). However, that does not say anything about which integer type that literal corresponds to.

- short and char integers always promoted to int integers within expressions. Hence short, char are primarily storage types.
- A literal with 1 or L suffix is a long. Presence of a long literal within an expression will force expression to be evaluated as a long.

C Integer Literals Continued

- A integer literal with a u or U suffix is unsigned. Example 1024U.
- A integer literal with a 11 or LL suffix is long long. Example: 1024LL.
- The size and unsigned suffixes can be combined in either order: 1024UL or 1024Lu are the same.

Bit Operators

- & Bitwise-and of two integers. 0x1234 & 0xF0F0 results in 0x1030.
- | Bitwise-or of two integers. 0x1234 | 0xF0F0 results in 0xF2F4.
- Bitwise-xor of two integers. 0x1234 ^ 0xF0F0 results in 0xE2C4.
- ~ Bitwise complement. ~0x1234 results in 0xEDCB.

Shift Operators

- << i << n is the value of i shifted to the left by n bits with 0 being shifted in from the right. 0x3 << 2 is 0xC. Can be used for multiplying by powers-of-2.
- >> i >> n is the value of i shifted to the right by n bits. If i is unsigned, then 0 is shifted in from the left; otherwise the sign bit is shifted in. Example: OxC >> 2 is Ox3.

Bit and Shift Operator Examples

Assume unsigned int u and bits are numbered starting with LSB being bit 0, next bit being 1, etc.

- Bitwise operators have unintuitive precedence; always parenthesize to avoid ambiguity.
- Non-zero iff bit 0 of u is 0: ((u & 0x1) == 0).
- Non-zero iff bit 2 of u is 1: ((u & 0x4) != 0).
- Set LSB of u to 1 without changing other bits: u |= 0x1.
- Set LSB of u to 0 without changing other bits: u &= ~0x1.
- Value of 2nd hexet (bits 4 7) of u: (u & 0xf0) >> 4 or (u >> 4) & 0x0f.
- Non-zero iff MSB of u is 1: (u & (~Ou >> 1)) != 0. Note u suffix in Ou absolutely necessary.

Counting # of 1s in an int

```
In count-1s-1.c:
int
count ones(unsigned v)
  int ones = 0;
  for (unsigned i = v; i > 0; i >>= 1) {
    if (i & 1) ones++;
  return ones;
```

Counting # of 1s in an int Continued

```
In count-1s-1.c:
int main() {
  unsigned values[] = { 123, 32, 255 };
  for (int i = 0; i < sizeof(values)/sizeof(values[0]);</pre>
       i++) {
    unsigned v = values[i];
    printf("# of ones in u (0xx) is d^n,
           v, v, count ones(v));
  return 0;
```

Counting # of 1s in an int Log

```
$ ./count-1s-1
# of ones in 123 (0x7b) is 6
# of ones in 32 (0x20) is 1
# of ones in 255 (0xff) is 8
$
```

Counting # of 1s in an int Discussion

- The loop starts with i set to the value v within which we want to count the number of 1-bits.
- Basic C does not have boolean type; the value 0 is treated as false, any non-zero value is treated as true. Hence ones is incremented if i & 1 is non-zero; i.e., ones is incremented iff the least-significant bit (LSB) of i is 1.
- After each iteration of the loop, i is shifted to the right by 1
 position. Thus the 1's in i make their way towards the LSB.
- The loop terminates when i is 0; i.e., there are no more 1's to count and ones contains the count of 1's in the original value v.
- The number of iterations in the loop will depend on the position of the leftmost 1 in the original value v.



Counting # of 1s in an int: 2nd Attempt

In count-1s-2.c we reduce number of loop iterations to number of 1's in original value:

```
int
count_ones(unsigned v)
{
   int ones = 0;
   while (v > 0) {
      v &= v - 1;
      ones++;
   }
   return ones;
}
```

Counting # of 1s in an int: 2nd Attempt Discussion

- If v is 101000, then v 1 is 100111. Hence v & (v 1) is 100000. By assigning this back to v, we knock-out the rightmost 1 in v in each loop iteration.
- Since we knock-out the rigthmost 1 in each loop iteration and increment ones on each loop iteration and terminate the loop when no 1's remain in v, at loop termination ones will contain the number of 1's in the original value of v.
- Note that even though the parameter value v is being changed within count_ones(), that change will not be reflected in the caller of count_ones(). That is because when parameters are passed in C, a copy of the actual parameter is passed. This is referred to as call-by-value.

Big Endian versus Little Endian

- In what order are multi-byte quantities (like integers or floats) stored in memory?
- Two common solutions: litte endian versus big endian (details follow). Some machines can choose dynamically ("bi-endian").
- Usually not visible to programmer on an individual machine but is an issue when sending binary data between machines.
- Many current networks mandate big-endian.

Little Endian

Little Endian Least significant byte stored in low address, next least significant byte stored in next higher address, ..., most significant byte stored in high address. For example, if 0x01234567 stored at 0x100:

Address: 0x100 0x101 0x102 0x103 Value: 0x67 0x45 0x23 0x01

Intel machines little endian.

Big Endian

Big Endian Most significant byte stored in low address, next most significant byte stored in next higher address, ..., least significant byte stored in high address. For example, if 0x01234567 stored at 0x100:

Address: 0x100 0x101 0x102 0x103 Value: 0x01 0x23 0x45 0x67

IBM, Sun big endian.

Endian Program

```
In endian.c:
int
main()
  union { //memory for i and bytes overlap
    int i;
    char bytes[sizeof(int)];
  u = \{ 0x123456 \};
  printf("int = 0x%x\n", u.i);
  for (int i = 0; i < sizeof(int); i++) {</pre>
    printf("bytes[%d] at %p is 0x\%02x\n",
            i, &u.bytes[i], u.bytes[i]);
  return 0;
```

Endian Program Log on x86

```
$ ./endian
int = 0x123456
bytes[0] at 0x7fff565cfe00 is 0x56
bytes[1] at 0x7fff565cfe01 is 0x34
bytes[2] at 0x7fff565cfe02 is 0x12
bytes[3] at 0x7fff565cfe03 is 0x00
$
```

Endian Program Log on Sparc

```
bingsuns2% ./endian
int = 0x123456
bytes[0] at ffbff900 is 0x00
bytes[1] at ffbff901 is 0x12
bytes[2] at ffbff902 is 0x34
bytes[3] at ffbff903 is 0x56
bingsuns2%
```

Endian Program Discussion

- The members of a union are assigned at the same memory location. Hence u.i and u.bytes occupy the same memory location. This allows us to look at the individual bytes in inti.
- The & unary operator returns the address of its operand.
 Hence &u.bytes[i] returns the address of the i'th byte.
- Note that for x86, the most significant byte is stored at a higher address than the least significant byte. Hence x86 is a little-endian architecture.
- Note that for sparc, the least significant byte is stored at a higher address than the least significant byte. Hence sparc is a big-endian architecture.

Signed, Unsigned Addition

- The operation of addition is the same for both signed and unsigned numbers with 2's complement.
- Consider 3 bits numbers: Unsigned: 0 to 7; Signed -4 to 3.
- Each following table shows addition of all combinations of a left operand with two right operands.
- Signed result indicated by a signed result in parentheses.
- Overflow indicated by a *.

Signed, Unsigned Addition Tables

Addition table for N + 0b000 and N + 0b001:

Rand1/Rand2	000 = 0 (0)	001 = 1 (+1)
000 = 0 (0)	000 = 0 (0)	001 = 1 (+1)
001 = 1 (+1)	001 = 1 (+1)	010 = 2 (+2)
010 = 2 (+2)	010 = 2 (+2)	011 = 3 (+3)
011 = 3 (+3)	011 = 3 (+3)	$ \ 100 = 4 \ (-4^*) \ $
100 = 4 (-4)	100 = 4 (-4)	101 = 5 (-3)
101 = 5 (-3)	101 = 5 (-3)	110 = 6 (-2)
110 = 6 (-2)	110 = 6 (-2)	111 = 7 (-1)
111 = 7 (-1)	111 = 7 (-1)	$000 = 0^* (0)$

Signed, Unsigned Addition Tables Continued

Addition table for N + 0b010 and N + 0b011:

Rand1/Rand2	010 = 2 (+2)	011 = 3 (+3)
000 = 0 (0)	010 = 2 (+2)	011 = 3 (+3)
001 = 1 (+1)	011 = 3 (+3)	$ 100 = 4 (-4^*) $
010 = 2 (+2)	100 = 4 (-4*)	101 = 5 (-3*)
011 = 3 (+3)	101 = 5 (-3*)	110 = 6 (-2*)
100 = 4 (-4)	110 = 6 (-2)	111 = 7 (-1)
101 = 5 (-3)	$111 = 7 \ (-1)$	$ \ 000 = 0^* \ (\ \ 0) \ $
110 = 6 (-2)	000 = 0*(0)	$ \ 001 = 1^* \ (+1) \ $
111 = 7 (-1)	$001 = 1^* (+1)$	$010 = 2^* (+2)$

Signed, Unsigned Addition Tables Continued

Addition table for N + 0b100 and N + 0b101:

Rand1/Rand2	100 = 4 (-4)	101 = 5 (-3)
000 = 0 (0)	100 = 4 (-4)	101 = 5 (-3)
001 = 1 (+1)	101 = 5 (-3)	110 = 6 (-2)
010 = 2 (+2)	110 = 6 (-2)	$111 = 7 \; (-1)$
011 = 3 (+3)	111 = 7 (-1)	000 = 0*(0)
100 = 4 (-4)	$000 = 0^* (0^*)$	$001 = 1^* (+1^*)$
101 = 5 (-3)	$001 = 1^* (+1^*)$	$010 = 2^* (+2^*)$
110 = 6 (-2)	$010 = 2^* (+2^*)$	$011 = 3^* (+3^*)$
111 = 7 (-1)	$011 = 3^* (+3^*)$	$100 = 4^* (-4)$

Signed, Unsigned Addition Tables Continued

Addition table for N + 0b110 and N + 0b111:

Rand1/Rand2	110 = 6 (-2)	$111 = 7 \ (-1)$
000 = 0 (0)	110 = 6 (-2)	$111 = 7 \ (-1)$
001 = 1 (+1)	111 = 7 (-1)	000 = 0*(0)
010 = 2 (+2)	$000 = 0^* (0)$	$001 = 1^* (+1)$
011 = 3 (+3)	$001 = 1^* (+1)$	$010 = 2^* (+2)$
100 = 4 (-4)	$010 = 2^* (+2^*)$	$011 = 3^* (+3^*)$
101 = 5 (-3)	$011 = 3^* (+3^*)$	$100 = 4^* (-4)$
110 = 6 (-2)	$100 = 4^* (-4)$	$101 = 5^* (-3)$
111 = 7 (-1)	$101 = 5^* (-3)$	$110 = 6^* (-2)$

Typical Ranges for Unsigned Types

_		_+_		+ _	
	# bits	 -+-	Min.	 -	Max Value
i	0	·	^		٠.
ı	8		U	ļ	255
	16		0		65,535
	32		0	l	4,294,967,295
	64	1	0	1	8,446,744,073,709,551,615
_		_+_		.+_	

Typical Ranges for Signed Types

Finding Integer Sizes in C

```
In integer-sizes.c:
#include <stdio.h>
int
main()
  //concatenation of adjacent string literals
  //%Id not portable; modern C allows %zu for sizeof()
  printf("sizeof(char) = %ld, sizeof(short) = %ld, "
          "sizeof(int) = %ld sizeof(long) = %ld, "
          "sizeof(long long) = %ld\n",
          sizeof(char), sizeof(short), sizeof(int),
          sizeof(long), sizeof(long long));
  return 0;
```

Integer Sizes: Edited Log

```
sizeof(char) = 1, sizeof(short) = 2, sizeof(int) = 4
sizeof(long) = 8, sizeof(long long) = 8
```

Powers of ~ 1000

- Since $2^{10} = 1024$ which is close to 1000, $2^{20} = 1,048,576$ which is close to 1,000,000, we can use *kilo* and *mega* notation, but need to distinguish between powers of 1000 and powers of 1024.
- Powers of 1000: normal metric notation: kB, MB, GB, etc.
- Powers of 1024: *IEC units*: KiB, MiB, GiB, etc.
- Write program to show quantities associated with different units.

Kilo Powers Program Log

Note overflow for zetta and yotta.

```
#metric units
$ ./kilo-powers
1000**1 = 1 kilobyte (kB) which is 1000 bytes
1000**2 = 1 megabyte (MB) which is 10000000 bytes
1000**3 = 1 gigabyte (GB) which is 10000000000 bytes
1000**4 = 1 terabyte (TB) which is 1000000000000 bytes
1000**5 = 1 petabyte (PB) which is 100000000000000 bytes
1000**6 = 1 exabyte (EB) which is 10000000000000000 bytes
1000**7 = 1 zettabyte (ZB) which is 3875820019684212736 bytes
1000**8 = 1 yottabyte (YB) which is 2003764205206896640 bytes
```

Kilo Powers Program Log Continued

```
#iec units

1024**1 = 1 kibibyte (KiB) which is 1024 bytes

1024**2 = 1 mebibyte (MiB) which is 1048576 bytes

1024**3 = 1 gibibyte (GiB) which is 1073741824 bytes

1024**4 = 1 tebibyte (TiB) which is 1099511627776 bytes

1024**5 = 1 pebibyte (PiB) which is 1125899906842624 bytes

1024**6 = 1 exbibyte (EiB) which is 1152921504606846976 bytes

1024**7 = 1 zebibyte (ZiB) which is 0 bytes

1024**8 = 1 yobibyte (YiB) which is 0 bytes
```

\$

Kilo Powers Program: Type Declaration

```
In kilo-powers.c:

/** Package unit-name and its abbreviation. */
typedef struct {
   const char *name;
   const char *abbr;
} Unit;
```

Kilo Powers Program: Metric Data

Kilo Powers Program: IEC Data

```
static Unit iecUnits[] = {
    { "kibibyte", "KiB" },
    { "mebibyte", "MiB" },
    { "gibibyte", "GiB" },
    { "tebibyte", "TiB" },
    { "pebibyte", "PiB" },
    { "exbibyte", "EiB" },
    { "zebibyte", "ZiB" },
    { "yobibyte", "YiB" },
};
```

Kilo Powers Program: Guts

```
static void
outUnits(unsigned base, Unit units[], int nUnits,
          FILE *out)
  unsigned long long v = 1;
  for (int i = 0; i < nUnits; i++) {</pre>
    v *= base;
    fprintf(out, "%d**%d = 1 %s (%s) "
             "which is %llu bytes\n",
             base, i + 1, units[i].name,
             units[i].abbr, v);
  fprintf(out, "\n");
```

Kilo Powers Program main() Function

```
int
main()
  outUnits(1000u, metricUnits,
            sizeof(metricUnits)/sizeof(metricUnits[0]),
            stdout);
  outUnits(1024u, iecUnits,
            sizeof(iecUnits)/sizeof(iecUnits[0]),
            stdout);
  return 0;
```

Kilo Powers Program Discussion

- A C struct allows packaging related data together.
- In C, typedef defines a name for some type. So the program uses the name Unit to refer to a particular struct type.
- Note the use of the u suffix on 1000u and 1024u to pass an unsigned base value to outUnits().
- IEC units have not really caught on. In practice, GB may mean "gigabyte" or "gibibyte", depending on context. In commercial contexts, memory sizes are often stated in IEC units, disk sizes in metric units but no guarantees.

Booleans

- Basic C does not have any boolean type.
- C99 introduced stdbool.h header with suitable definitions for true and false.
- Comparison operators <, <=, >, >=, ==, != return result 1 for true and 0 for false.
- Logical operators &&, ||, ! treat 0 as false, all non-0 values as true.
- C has a single falsy value: 0. All values other than 0 are truthy.

Comparing Numeric Expressions in C

An expression which compares two numeric expressions is known as a *relational expression*.

- ==, (!=) Returns 1 iff two expressions are equal (not-equal), 0 otherwise. Do not use with floating point types:
 - Example: if (i != 0) b = x/i;.
 - Watch out for incorrect use of =. For example, if
 (i = 0) b = 1 else b = x/i; will always
 divide by i because of use of = instead of == in
 comparison. Some programmers protect for this
 case by writing if (0 == i) which will cause a
 compilation error if written incorrectly as if (0 =
 i).

Comparing Numeric Expressions in C Continued

- <, (>) Returns 1 iff the left-hand expression is less-than (greater-than) the right-hand expression, 0 otherwise. Example: for (int i = 0; i < 10; i++) { ... }.</p>
- <=, (>=) Returns 1 iff the left-hand expression is less-than-or-equal-to (greater-than-or-equal-to) the right-hand expression, 0 otherwise. **Example:** for (int i = 9; i >= 0; i --) { . . . }.

Can also use on right-hand-side of assignment as in: int aLT10 = (a < 10);.

Short-Circuit Logical Operators

The operators | | (logical-or) and && (logical-and) evaluate operands from left-to-right, but stop ("short-circuit") the evaluation immediately once the result is known for sure; i.e. they may not evaluate their 2nd operand if the result is determined by the value of the first operand.

- $A \mid \mid B \mid$ If expression A evaluates to non-zero, then return 1 without ever evaluating expression B. Otherwise return 0 if B too evaluates to 0, otherwise return 1.
 - Example: In if $(x == 0 | | y/x > 10) \{ \}$, short-circuit property of | | avoids division-by-0 error.

Short-Circuit Logical Operators Continued

- A && B If expression A evaluates to 0, then return 0 without ever evaluating expression B. Otherwise return 1 if B too evaluates to non-zero, otherwise return 0.
 - Example: Search for first element of a[n]
 which is equal to key: for (int i = 0; i < n
 && a[i] != key; i++) { ... }</pre>
 - Note that because of short-circuit evaluation, when i == n code does not examine a[i] at all, thus avoiding an index-out-of-bounds error.

Logical Not

- ! A Return 0 if A is non-zero, 1 when A is 0.
 - Can avoid using ! by applying DeMorgan's law: example, instead of ! ($x <= 10 \mid | y == 5$) use (x > 10 & y != 5), but use ! if it is clearer in a particular context.
 - Idiom !!x can be used to convert from x which may not be strictly 0 or 1 to a strict 0 or 1 value.

Logical Operators versus Bitwise Operators

- Do not confuse bit-wise operators &, |, ^, ~ with logical operators &&, ||, ! which operate on pseudo-boolean values.
- Logical operators && and || have short-circuit semantics and may not evaluate their 2nd operand; bitwise-operators & and | always evaluate both operands.
- Assignment operators &=, |= and ^= refer to the bitwise operators. No assignment operators for logical operators && and ||.

If-then-else Expressions

```
x = (cond) ? expr1 : expr2 equivalent to

if (cond)
    x = expr1
else
    x = expr2;
```

- Note it is possible to chain conditions together as in x = (cond1) ? expr1 : (cond2) ? expr2 : expr3 which is equivalent to x = (cond1) ? expr1 : ((cond2) ? expr2 : expr3), but can easily turn ugly.
- I tend to overuse this in my code compared to normal practice.

Sum of Integer Command-Line Arguments Log

Not particularly robust in checking for errors:

```
$ gcc -g -Wall -Wextra -std=c11 sum-args.c -o sum-args
$ ./sum-args 22 -3 5
24
#silently ignore garbage at end of values
$ ./sum-args 22 -3x 5
24
#silently ignore totally garbage values
$ ./sum-args 22 -3x 5 garbage 3
27
$
```

Sum of Integer Command-Line Arguments

```
In sum-args.c:
```

```
/** Output sum of integer command-line arguments on stdout. */
int
main(int argc, const char *argv[])
  int sum = 0;
  for (int i = 1; i < argc; i++) {
    sum += atoi(argv[i]);
  printf("%d\n", sum);
  return 0;
```

Sum of Integer Command-Line Arguments Discussion

- Recollect that a C string is a array of char terminated by a NUL character '\0'.
- First argument to main() argc gives the number of command-line arguments including the name of the program.
- The notation char *str can be regarded as declaring str to be a string (strictly speaking, is is declaring str to be a pointer to a char).
- Hence const char *argv[] declares argv to be an array of strings; the const means that the strings cannot be changed.

Sum of Integer Command-Line Arguments Discussion Continued

- atoi() is a function declared in included file <stdlib.h>
 which converts a string (which should contain only characters
 corresponding to decimal digits) to the internal representation
 of a C integer.
- \n is an escape sequence used within C-strings to denote a newline character.
- The first argument for printf() should be a C-string denoting a C string. % characters are used as escape sequences within a format string to introduce format specifiers used to print the next corresponding argument.

More Robust Sum Program: Log

```
$ gcc -g -Wall -Wextra -std=c11 robust-sum.c \
      -o robust-sum
$ ./robust-sum 22 -3 5
24
#produce error message for bad arguments
$ ./robust-sum 22 -3x 5
bad argument -3x not integer: ignored
27
#produce error message for bad arguments
$ ./robust-sum 22 -3x 5 garbage 3
bad argument -3x not integer: ignored
bad argument garbage not integer: ignored
30
```

A More Robust Program to Sum Arguments

In robust-sum.c:

```
/** Output sum of integer command-line arguments on stdout. */
int
main(int argc, const char *argv[])
  int sum = 0;
  for (int i = 1; i < argc; i++) {
    char *p;
    int n = strtol(argv[i], &p, 10);
    if (*p == '\0') {
      sum += n;
```

A More Robust Program to Sum Arguments Continued

Arrays

- A C array basically just represents the address of an area of memory; i.e., a C array is basically a pointer.
- It follows that a C array does not track the number of elements it has. The programmer needs to track the number of elements in the array. Some alternatives:
 - Have another variable which explicitly stores the number of elements in the array.
 - Mark the end of the array using some kind of sentinel value;
 i.e. a value which cannot occur as a legal value in the data stored in the array. For example, if an array stores only non-negative integers, then -1 could be used as a sentinel.
 - The number of elements in the array is known ahead of time as some fixed value (like say 27) and all code is written assuming that size. Usually a bad idea.

When Arrays are Pointers

Peter Van Der Linden in Deep C Secrets:

- The use of an array name in an expression (not declaration)
 which is not an operand of sizeof() is treated by the
 compiler as a pointer to the first element of the array.
- A subscript is always equivalent to an offset from a pointer.
- An array name in the declaration of a function parameter is treated by the compiler as a pointer to the first element of the array. This is because arrays are passed by reference for efficiency reasons (all non-array data are passed by value).

Pointers and Arrays

- Only operations for an array are getting its size using sizeof() or obtaining a pointer to element 0 of the array. All other array ops are really pointer ops.
- a[i] is equivalent to *(a + i) which is equivalent to *(i + a) which is equivalent to i[a].
- When used within an expression, an array is equivalent to a pointer to its first element.

Array of char and Pointer to char Are Different

```
o char *msg = "hello";:
    msg: [ ... ] ----> ['h'|'e'|'l'|'l'|'o'|'\0']
```

- sizeof(msg) will be the size of a pointer (i.e. a memory address). Typically, this is 4 or 8.
- To compute the address of msg[i], the compiler will need to produce code to add the value of i to the value stored at memory location msg.

Array of char and Pointer to char Are Different Continued

```
o char msg[] = "hello";
    msg: ['h'|'e'|'l'|'l'|'o'|'\0']
```

- sizeof(msg) will be 6.
- To compute the address of msg[i], the compiler will need to produce code to add the value of i to the address of msg.
- It is wrong to have one file define char msg[] = "hello"; and another file declare extern char *msg; as the compiler will generate different access code.

Multi-Dimensional Arrays

- C has only 1-dimensional arrays.
- Elements of arrays can themselves be arrays, which permits array notation like a[i][j] for multiple dimensions for static and auto (but not dynamically malloc()'d) arrays.
- When declaring (not defining) a multi-dimensional array, first (leftmost) dimension can be unspecified as in a[] [10] [3].
- Impossible to have multi-dimensional array as function parameters without all but the leftmost dimension specified.
 So int a[][] is not allowed as a function parameter.

Declarations versus Definitions

- A declaration provides information about an entity like a variable or function.
- A definition provides a definite value for that entity.
- An entity can have multiple declarations as long as they are consistent.
- There can only be a single definition for an entity.
- Often there is only a single statement which combines both a declaration with a definition.

Declarations vs Definitions Example

Declarations vs Definitions Example

```
//function definition
void quadratic roots(
  //parameter definitions/declarations
  double a, double b, double c,
  double *root1, double *root2)
  double discr; //uninitialized variable definition
  discr = b*b - 4*a*c:
  assert(discr >= 0);
  double sqroot = sqrt(discr); //definition with init
  *root1 = (-b + sqroot) / (2 * a);
  *root2 = (-b - sqroot) / (2 * a);
```

Pointer Sum Annotated Log

```
# 12 + 13 + -12
$ ./ptr-sum 12 13 -0xc
13
$ ./ptr-sum
# 64 + -171 + ** + **
$ ./ptr-sum 0100 -0xAb 12C 099
-107
$
```

Pointer Sum

In ptr-sum.c:

```
/** Sum numeric strings [*start, *end), silently ignoring
 * any strings which are not valid C integer literals.
long
ptr sum(const char **start, const char **end)
  long sum = 0;
  for (const char **p = start; p != end; p++) {
    char *endP;
    long v = strtol(*p, \&endP, 0); //0: c-syntax ints
    if (*endP == ^{\prime}\0') sum += v;
  return sum;
```

Pointer Sum Continued

```
int
main(int argc, const char *argv[])
{
   printf("%ld\n", ptr_sum(&argv[1], &argv[argc]));
   return 0;
}
```

Pointer Sum Discussion

- strtol() needs to return a pointer to the first non-legal character found in the integer string pointed to by its first argument.
- Since return value is being used to return the value of the integer, this pointer must be returned using a function parameter.
- Since the actual arguments passed to a function are copies of the value passed by the caller a function cannot affect the value of a parameter in its caller.
- The only way to have a function return a value via an argument is to have the caller pass a pointer to that value and have the function return the value using the pointer.
- Since strtol() needs to return a pointer via its argument, the second parameter is passed as pointer to a pointer, i.e. &endP.
- Declaration of strtol() is long strtol(const char *str, char **end, int base).

Pointer Sum Discussion Continued

- In ptr_sum(), start is address of first string. Since a string
 has type char *, start is declared char **.
- end is address one past that of the last string; i.e. end is an exclusive limit.
- p is initialized to start of type const char **. Hence *p
 has type const char * which is the string being sent as the
 first argument to strtol()
- p++ will point to next string.
- Since end is an exclusive limit, the loop quits when p == end.

Declaration of Command-Line Arguments in main()

- Typical declaration const char *argv[] for second argument of main(), declares argv to be an array of pointers to constant char (typically, constant strings) with each element containing a command-line argument string.
- argv[1], argv[2] etc. have type of the array element: namely pointer to const char, i.e. const char *; Hence &argv[1] and &argv[2] have type pointer to pointer to const char, i.e. const char **.

Representation of Command-Line Arguments

Given command-line ./ptr-sum 12 13 -0xc, we have argv array as follows:

Standard I/O Example wc(1) Program

Standard I/O Example wc(1) Program

```
void
wc(const char *fName, FILE *f)
  int inWord = 0;
  int nC = 0, nW = 0, nL = 0;
  int c;
  //standard C idiom for reading file while checking EOF
  while ((c = fgetc(f)) != EOF) {
    nC++;
    if (c == '\n') nL++;
    if (isspace(c)) {
      inWord = 0;
```

Standard I/O Example wc(1) Program

}

```
else {
    if (!inWord) nW++;
    inWord = 1;
if (ferror(f)) {
  fprintf(stderr, "i/o error: %s\n",
          strerror(errno));
printf("%*d %*d %*d %s\n", COUNT_CHARS, nL,
       COUNT_CHARS, nW, COUNT_CHARS, nC, fName);
nCTotal += nC; nWTotal += nW; nLTotal += nL;
```

Standard I/O Example wc(1) main() Program

```
int
main(int argc, const char *argv[])
  int i;
  if (argc == 1) {
    wc("", stdin);
  else {
    for (i = 1; i < argc; i++) {
      FILE *in = fopen(argv[i], "r");
      if (!in) {
        fprintf(stderr, "could not read %s: %s\n",
                 argv[i], strerror(errno));
```

Standard I/O Example wc(1) main() Program Continued

```
else {
      wc(argv[i], in);
      fclose(in);
  f(i) = 1; i < argc; i++)
  if (argc > 2) {
    printf("%*d %*d %*d total\n",
           COUNT_CHARS, nLTotal, COUNT_CHARS,
           nWTotal, COUNT_CHARS, nCTotal);
} //else if argc != 1
return 0;
```

wc(1) Log

```
$ which wc
/usr/bin/wc
$ wc wc.c
    62 183 1154 wc.c
$ ./wc wc.c
        183 1154 wc.c
    62
$ wc wc.c buffer.c
    62 183 1154 wc.c
    14 41 278 buffer.c
    76 224 1432 total
$ wc <wc.c
    62
        183
             1154
$ ./wc <wc.c
    62
          183
                1154
$
```

C Character I/O

C Character I/O

- Why do functions on previous slide treat characters as int's rather than char?
- For the output put*() functions, the reason is to do with compatibility with pre-ISO C where all char/'short' arguments were passed as int's.
- But why for input? Couldn't get*() simply return a char?

Signedness of char

- In C, the signedness of a plain char is undefined as on some platforms char may be signed, on others it may be unsigned.
- Can be explicit by declaring signed char or unsigned char.
- get*() functions return EOF on end-of-file or error.
- EOF is typically a negative number, usually -1.
- Hence get*() functions return int.

Record I/O

- Can read/write nRecs records each having size of recSize bytes.
- Can be used for serializing binary data like struct's.
- Simple-minded serialization likely problematic: binary data is inherently unportable (endian and size issues). Serialized pointers are meaningless.

Formatted I/O

- printf(), fprintf(), scanf(), fscanf() and friends.
- Since C cannot change actual parameters, it is necessary that scanf() receive pointers to variables to be changed.

```
int val;
scanf("%d", val); //WRONG
scanf("%d", &val); //correct
```

 Format specifiers for printf() and scanf() bear superficial resemblance but are different.

Character Sets

- A character is an abstract entity representing a symbol used in writing some human language.
- Printed representation is a glyph.
- Represented by an integer code within computers.
- A character set could refer to an abstract set of characters, or a more concrete mapping from some character codes to glyphs.
- Many different character sets.

ASCII

1960s: ASCII is a 7-bit code 0x00 - 0x7F evolved from codes used for telegraph.

- 95 printable characters, 33 control characters.
- 0x00 0x1F Control codes: 0x0a ^J, '\n' line feed; 0x0d ^M, '\r' carriage return; 0x07 ^G, '\a' bell; 0x09, ^I', '\t'' horizontal tab; 0x08, ^H, '\b'' backspace; 0x0c ^L, '\f' form feed; 0x1B ^[escape.
- 0x20(32): space character.
- 0x30 0x39 (48 57): digits.
- 0x41 0x5a (65 90): upper-case alphabet A Z. Get corresponding control-code by stripping off high bit b₆.
- 0x61 0x7a (97 122): lower-case alphabet a z.
- 0x7f: delete character.



ASCII Continued

- Codes not listed above are symbol or punctuation characters.
- Problems with characters like brackets [and], and braces {
 and }, which were difficult to type on some keyboards
 (currently rare). Led to C trigraphs: ??x for alternate
 representation of problematic characters.

8-Bit Character Sets

IBM EBCDIC Used by IBM mainframes. Non-contiguous alphabetic characters. Multiple code pages.

Extended ASCII 1980s, 1990s. Microsoft code pages for different languages; ISO-8859-* for different languages.

8859-1 Latin-1 for Western European languages,

8859-2 Latin-2 for Central European languages, ..,

8859-9 Latin-5 for Turkish. Other 8859-* variants cover most European languages, Arabic, Hebrew,

Thai. Various incompatibilites.

CJK Languages

CJK: Chinese, Japanese and Korean. CJKV: + Vietnamese. Cover main East Asian Languages. Thousands of characters required. 8 bits insufficient.

Two major approaches:

Wide Characters Encode characters using 16-bits (or wider).

Mult-Byte Variable Length Encoding Need escape sequences to shift interpretations. Need to scan string sequentially to interpret escape sequences correctly. Entire string corrupted if a single bit is corrupted. Example: Shift JIS.

Unicode

Unicode universal character set widely used by all modern computer systems to represent international characters.

- Over 1 million code points from 0x000000 to 0x10FFFF.
- Basic Multilingual Plane (BMP): code points less than 0x10000.
- Characters often specified by name or by code-point as U+xxxx.
- Combining characters.
- Can be encoded using a fixed width (UTF-32) or variable width encoding (UTF-16 on windows, UTF-8 on unix and www).

UTF-8 Encoding for Unicode

UTF-8 is a popular variable width encoding for Unicode which is compatible with ASCII. Used widely on WWW.

```
Unicode Range
                         Encoding
U+000000000 - U+0000007F
                           0xxxxxxx
                           110xxxxx 10xxxxxx
U+000000080 - U+00007FF
U+000000800 - U+0000FFFF
                           1110xxxx 10xxxxxx 10xxxxxx
U+000010000 - U+001FFFFF
                           11110xxx 10xxxxxx 10xxxxxx
                                     10xxxxxx
U+000200000 - U+03FFFFF
                           111110xx 10xxxxxx 10xxxxxx
                                     10xxxxxx 10xxxxxx
U+040000000 - U+7FFFFFFF | 11111110x 10xxxxxx 10xxxxxx
                                     10xxxxxx 10xxxxxx
                                     10xxxxxx
```

UTF-8 Encoding for Unicode Continued

- Single byte encodings compatible with ASCII.
- Leading number of 1s in first byte gives # of bytes in multi-byte sequences.
- 4-byte encoding sufficient to represent all Unicode characters up to U+10FFFF.
- Easy to synchronize from middle of string by skipping 10xxxxxx bytes.
- Designed in 1992 by Ken Thompson on a placemat at a New Jersey diner!

UTF-8 with C

- Must set locale appropriately.
- strlen() gives number of bytes, not number of characters.
- Routines in standard library available.

Fractional Binary Numbers

Given a fractional binary number

$$b_m b_{m-1} \dots b_1 b_0 \dots b_{-1} b_{-2} \dots b_{-n-1} b_{-n}$$

By analogy with decimal notation, its value will be given by

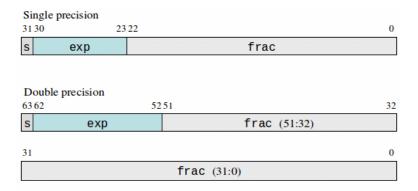
$$\sum_{i=-n}^{m} 2^{i} \times b_{i}$$

So we would have: binary 0.1 representing decimal 0.5, binary 0.01 representing decimal 0.25 and binary 11.101 representing decimal 3.625.

IEEE Floating Point Representation

- Similar to *scientific notation* where a number is represented using a *mantissa* and an *exponent*.
- Floating point representation contains a single sign bit, a k-bit exponent field and a n-bit mantissa or significand fraction field.
- Usually, the exponent is adjusted so that the fraction field is always of the form 1..., i.e. there is always a 1 before the binary point. Hence there is no point in storing it and we say that the fraction field is *normalized*.
- Exponent is stored with a bias.
- Reserve exponent of all 0's and all 1's for exceptional cases.

Floating Point Formats



- Because of normalization, single precision (usually C float's) only store a 23-bit fraction which actually represents 24-bits.
- Again, due to normalization double precision (usually C double's) only store a 52-bit fraction which actually represents 53 bits.

Floating Point Cases

1. Normalized

 $s \neq 0 \& \neq 255 \qquad f$

2. Denormalized



3a. Infinity



3b. NaN



- Denormalized numbers allow graceful underflow.
- ullet Special values of $\pm\infty$ allows saturating arithmetic.

Not-a-Number ('NaN')

When exponent is all 1's and fraction non-zero, we have a NaN.

- NaN indicates an invalid result like 0/0. Can cause an exception ("signalling" NaN) or simply propagates as NaN ("quiet" NaN).
- NaN compares false with anything, including itself.

```
double x = 0/0;
x == x; //evaluates to 0.
x != x; //evaluates to 1.
x < y; //evaluates to 0 for any y.
y < x; //evaluates to 0 for any y.</pre>
```

Floating Point Miscellanea

- Can be sorted by treating bit representation lexicographically or as signed-magnitude integers.
- In C, float literals must have trailing f or F; otherwise literal is treated as a double.
- The value contributed by the last bit in the fraction ("unit in last place") depends on the value of the number.

Floating Point Parameters

- Floating point format characterized by 2 parameters:
 - N total number of bits.
 - k number of exponent bits. Biased by $2^{k-1} 1$.

It follows that number of bits available for storing mantissa is m = N - k - 1.

- IEEE single precision: N=32, k=8, m=32-8-1=23. The exponent bias is $2^{8-1}-1=127$. Normalized exponents in inclusive-range [-126,127].
- IEEE double precision: N=64, k=11, m=64-11-1=52. The exponent bias is $2^{11-1}-1=1023$. Normalized exponents in inclusive-range [-1022,1023].



Floating Point Values

 Given a non-exceptional floating point number (exponent field is not all 0's and not all 1's), it's value is:

$$(-1)^s \times M \times 2^e$$

where s is the value of the sign-bit, M is the value of the mantissa and e is the exponent value (after adjusting by the bias).

- Assuming that the value as an unsigned binary integer of the mantissa field is m', for normalized numbers $M = 1 + m'/2^m$; for denormalized numbers $M = m'/2^m$.
- Assuming that the value as an unsigned binary integer of the exponent field is e', for normalized numbers $e=e'-(2^{k-1}-1)$; for denormalized numbers $e=-(2^{k-1}-2)$.

Floating Point Values Continued

```
Normalized values When 0 < e' < 2^k - 1: M = 1 + m'/2^m and e = e' - (2^{k-1} - 1). Hence value is (-1)^s \times (1 + m'/2^m) \times 2^{e' - (2^{k-1} - 1)}. Denormalized values When e' = 0: M = m'/2^m and e = -(2^{k-1} - 2) and value is (-1)^s \times (m'/2^m) \times 2^{-(2^{k-1} - 2)}. Infinities e' = 2^k - 1, m' = 0. Value is (-1)^s \times \infty. NaN's e' = 2^k - 1, m' \neq 0. Value is NaN.
```

8-Bit Float Values

Following slides list all values for a 7-bit float. Fields from MSB to LSB:

- 1-bit sign
- 3-bit exponent biased by 3.
 - Field value in [1, 6]: exponent value [-2, 3].
 - Field value 0: denormalized: exponent value -2.
 - Field value 7: Exceptional cases: Infinities + NaN.
- 3-bit fraction; for normalized numbers, implicit 1 to left of binary point.

Bits	Exp	Fraction	Value
0 000 000	0	0	$+0.000000(2^{-2}\times(0+0/8))$
0 000 001	0	1	$+0.031250(2^{-2}\times(0+1/8))$
0 000 010	0	2	$+0.062500(2^{-2}\times(0+2/8))$
0 000 011	0	3	$+0.093750(2^{-2}\times(0+3/8))$
0 000 100	0	4	$+0.125000(2^{-2}\times(0+4/8))$
0 000 101	0	5	$+0.156250(2^{-2}\times(0+5/8))$
0 000 110	0	6	$+0.187500(2^{-2}\times(0+6/8))$
0 000 111	0	7	$+0.218750(2^{-2}\times(0+7/8))$

Bits	Exp	Fraction	Value
0 001 000	1	0	$+0.250000(2^{-2}\times(1+0/8))$
0 001 001	1	1	$+0.281250(2^{-2}\times(1+1/8))$
0 001 010	1	2	$+0.312500(2^{-2}\times(1+2/8))$
0 001 011	1	3	$+0.343750(2^{-2}\times(1+3/8))$
0 001 100	1	4	$+0.375000(2^{-2}\times(1+4/8))$
0 001 101	1	5	$+0.406250(2^{-2}\times(1+5/8))$
0 001 110	1	6	$+0.437500(2^{-2}\times(1+6/8))$
0 001 111	1	7	$+0.468750(2^{-2}\times(1+7/8))$

Bits	Exp	Fraction	Value
0 010 000	2	0	$+0.500000(2^{-1} \times (1+0/8))$
0 010 001	2	1	$+0.562500(2^{-1}\times(1+1/8))$
0 010 010	2	2	$+0.625000(2^{-1}\times(1+2/8))$
0 010 011	2	3	$+0.687500(2^{-1}\times(1+3/8))$
0 010 100	2	4	$+0.750000(2^{-1}\times(1+4/8))$
0 010 101	2	5	$+0.812500(2^{-1}\times(1+5/8))$
0 010 110	2	6	$+0.875000(2^{-1}\times(1+6/8))$
0 010 111	2	7	$+0.937500(2^{-1}\times(1+7/8))$

Bits	Exp	Fraction	Value
0 011 000	3	0	$+1.000000(2^0 \times (1+0/8))$
0 011 001	3	1	$ +1.125000(2^0 imes (1+1/8)) $
0 011 010	3	2	$ +1.250000(2^0 \times (1+2/8)) $
0 011 011	3	3	$+1.375000(2^{0} \times (1+3/8))$
0 011 100	3	4	$+1.500000(2^0 \times (1+4/8))$
0 011 101	3	5	$+1.625000(2^0 \times (1+5/8))$
0 011 110	3	6	$+1.750000(2^0 \times (1+6/8))$
0 011 111	3	7	$+1.875000(2^{0} \times (1+7/8))$

Bits	Exp	Fraction	Value
0 100 000	4	0	$+2.000000(2^1 \times (1+0/8))$
0 100 001	4	1	$ +2.250000(2^1 \times (1+1/8)) $
0 100 010	4	2	$+2.500000(2^1 \times (1+2/8))$
0 100 011	4	3	$+2.750000(2^1 \times (1+3/8))$
0 100 100	4	4	$+3.000000(2^1 \times (1+4/8))$
0 100 101	4	5	$+3.250000(2^1 \times (1+5/8))$
0 100 110	4	6	$+3.500000(2^1 \times (1+6/8))$
0 100 111	4	7	$+3.750000(2^1 \times (1+7/8))$

Bits	Exp	Fraction	Value
0 101 000	5	0	$+4.000000(2^2 \times (1+0/8))$
0 101 001	5	1	$+4.500000(2^2 \times (1+1/8))$
0 101 010	5	2	$+5.000000(2^2 \times (1+2/8))$
0 101 011	5	3	$+5.500000(2^2 \times (1+3/8))$
0 101 100	5	4	$+6.000000(2^2 \times (1+4/8))$
0 101 101	5	5	$+6.500000(2^2 \times (1+5/8))$
0 101 110	5	6	$+7.000000(2^2 \times (1+6/8))$
0 101 111	5	7	$+7.500000(2^2 \times (1+7/8))$

Bits	Exp	Fraction	Value
0 110 000	6	0	$+8.000000(2^3 \times (1+0/8))$
0 110 001	6	1	$+9.000000(2^3 \times (1+1/8))$
0 110 010	6	2	$+10.000000(2^3 \times (1+2/8))$
0 110 011	6	3	$+11.000000(2^3 \times (1+3/8))$
0 110 100	6	4	$+12.000000(2^3 \times (1+4/8))$
0 110 101	6	5	$+13.000000(2^3 \times (1+5/8))$
0 110 110	6	6	$+14.000000(2^3 \times (1+6/8))$
0 110 111	6	7	$+15.000000(2^3 \times (1+7/8))$

Bits	Exp	Fraction	Value
0 111 000	7	0	+infinity
0 111 001	7	1	+nan
0 111 010	7	2	+nan
0 111 011	7	3	+nan
0 111 100	7	4	+nan
0 111 101	7	5	+nan
0 111 110	7	6	+nan
0 111 111	7	7	+nan

Bits	Exp	Fraction	Value
1 000 000	0	0	$-0.000000(-2^{-2} \times (0 + 0/8))$
1 000 001	0	1	$\left -0.031250(-2^{-2} \times (0+1/8)) \right $
1 000 010	0	2	$-0.062500(-2^{-2}\times(0+2/8))$
1 000 011	0	3	$-0.093750(-2^{-2}\times(0+3/8))$
1 000 100	0	4	$\left -0.125000(-2^{-2} \times (0 + 4/8)) \right $
1 000 101	0	5	$\left -0.156250(-2^{-2} \times (0+5/8)) \right $
1 000 110	0	6	$\left -0.187500(-2^{-2} \times (0+6/8)) \right $
1 000 111	0	7	$-0.218750(-2^{-2}\times(0+7/8))$

Bits	Exp	Fraction	Value
1 001 000	1	0	$-0.250000(-2^{-2} \times (1+0/8))$
1 001 001	1	1	$-0.281250(-2^{-2}\times(1+1/8))$
1 001 010	1	2	$-0.312500(-2^{-2}\times(1+2/8))$
1 001 011	1	3	$-0.343750(-2^{-2}\times(1+3/8))$
1 001 100	1	4	$-0.375000(-2^{-2}\times(1+4/8))$
1 001 101	1	5	$-0.406250(-2^{-2}\times(1+5/8))$
1 001 110	1	6	$-0.437500(-2^{-2}\times(1+6/8))$
1 001 111	1	7	$-0.468750(-2^{-2}\times(1+7/8))$

Bits	Exp	Fraction	Value
1 010 000	2	0	$-0.500000(-2^{-1} \times (1+0/8))$
1 010 001	2	1	$\left -0.562500(-2^{-1} \times (1+1/8)) \right $
1 010 010	2	2	$-0.625000(-2^{-1}\times(1+2/8))$
1 010 011	2	3	$-0.687500(-2^{-1}\times(1+3/8))$
1 010 100	2	4	$\left -0.750000(-2^{-1} \times (1+4/8)) \right $
1 010 101	2	5	$-0.812500(-2^{-1}\times(1+5/8))$
1 010 110	2	6	$-0.875000(-2^{-1}\times(1+6/8))$
1 010 111	2	7	$-0.937500(-2^{-1}\times(1+7/8))$

Bits	Exp	Fraction	Value
1 011 000	3	0	$-1.000000(-2^0 \times (1+0/8))$
1 011 001	3	1	$-1.125000(-2^0 \times (1+1/8))$
1 011 010	3	2	$-1.250000(-2^0 \times (1+2/8))$
1 011 011	3	3	$-1.375000(-2^0 \times (1+3/8))$
1 011 100	3	4	$-1.500000(-2^0 \times (1+4/8))$
1 011 101	3	5	$-1.625000(-2^0 \times (1+5/8))$
1 011 110	3	6	$-1.750000(-2^0 \times (1+6/8))$
1 011 111	3	7	$-1.875000(-2^0 \times (1+7/8))$

Bits	Exp	Fraction	Value	
1 100 000	4	0	$-2.000000(-2^1 \times (1+0/8))$	
1 100 001	4	1	$-2.250000(-2^1 \times (1+1/8))$	
1 100 010	4	2	$-2.500000(-2^1 \times (1+2/8))$	
1 100 011	4	3	$-2.750000(-2^1 \times (1+3/8))$	
1 100 100	4	4	$-3.000000(-2^1 \times (1+4/8))$	
1 100 101	4	5	$-3.250000(-2^1 \times (1+5/8))$	
1 100 110	4	6	$-3.500000(-2^1 \times (1+6/8))$	
1 100 111	4	7	$-3.750000(-2^1 \times (1+7/8))$	

Bits	Exp	Fraction	Value	
1 101 000	5	0	$-4.000000(-2^2 \times (1+0/8))$	
1 101 001	5	1	$-4.500000(-2^2 \times (1+1/8))$	
1 101 010	5	2	$-5.000000(-2^2 \times (1+2/8))$	
1 101 011	5	3	$-5.500000(-2^2 \times (1+3/8))$	
1 101 100	5	4	$-6.000000(-2^2 \times (1+4/8))$	
1 101 101	5	5	$-6.500000(-2^2 \times (1+5/8))$	
1 101 110	5	6	$-7.000000(-2^2 \times (1+6/8))$	
1 101 111	5	7	$-7.500000(-2^2 \times (1+7/8))$	

Bits	Exp	Fraction	Value	
1 110 000	6	0	$-8.000000(-2^3 \times (1+0/8))$	
1 110 001	6	1	$-9.000000(-2^3 \times (1+1/8))$	
1 110 010	6	2	$-10.000000(-2^3 \times (1+2/8))$	
1 110 011	6	3	$-11.000000(-2^3 \times (1+3/8))$	
1 110 100	6	4	$-12.000000(-2^3 \times (1+4/8))$	
1 110 101	6	5	$-13.000000(-2^3 \times (1+5/8))$	
1 110 110	6	6	$-14.000000(-2^3 \times (1+6/8))$	
1 110 111	6	7	$-15.000000(-2^3 \times (1+7/8))$	

Bits	Exp	Fraction	Value
1 111 000	7	0	—infinity
1 111 001	7	1	— nan
1 111 010	7	2	— nan
1 111 011	7	3	— nan
1 111 100	7	4	— nan
1 111 101	7	5	— nan
1 111 110	7	6	— nan
1 111 111	7	7	— nan

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