

Midsem Notes For  
computational intelligence  
PE-1 Artificial Intelligence



20  
30

**VI Semester Re-MidTerm TEST**  
**Artificial Intelligence (PE-I) (CSE\_4053)**

Time Duration: 2 Hours

Date: 12.04.2024

Max marks: 30

| Question No | Topic   | Marks    | BL | CO |
|-------------|---|----------|----|----|
| 1.          | Which type of AI can operate in real time without human intervention and learn from its environment?<br><br>a) Narrow AI<br>b) Reactive AI<br>c) General AI<br>d) Reinforcement Learning Agent  | 0/1<br>1 | 1  | 1  |
| 2.          | Which domain of AI is primarily used in devices like Amazon Alexa or Google Assistant?<br><br>a) Robotics<br>b) Machine Vision<br>✓ c) NLP (Natural Language Processing)<br>d) Expert Systems   | 1/1<br>1 | 2  | 1  |
| 3.          | A problem in a search space is defined by _____.<br><br>a) Initial state<br>✓ b) Initial state and goal state<br>c) Initial state, goal state, and intermediate states<br>d) Sensor inputs  | 0/1<br>1 | 1  | 1  |
| 4.          | If a robot can clean the room by analyzing the layout and learning from mistakes, which AI concept is applied?<br><br>a) General AI<br>b) Supervised Learning<br>✓ c) Reinforcement Learning<br>d) Deep Learning  | 1/1<br>1 | 2  | 3  |
| 5.          | In the context of intelligent agents, what are percept sequences?<br><br>a) Actions performed by the agent<br>b) Goals set by the agent<br>✓ c) Observations received from the environment over time<br>d) Internal states of the agent   | 1/1<br>1 | 2  | 2  |
| 6.          | Reinforcement Learning uses _____.<br><br>a) Decision trees<br>✓ b) Trial and error<br>c) Historical data<br>d) Fixed rules only  | 0/1<br>1 | 2  | 2  |
| 7.          | A self-driving car using AI must decide between stopping for a pedestrian or continuing due to high-speed traffic behind. Which AI technique is most suitable for this scenario?<br><br>a) Supervised Learning<br>b) Rule-based Expert System<br>✓ c) Reinforcement Learning<br>d) General AI | 1/1<br>1 | 2  | 1  |

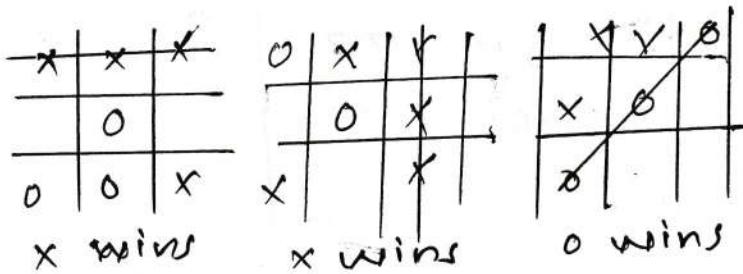
|       |   |     |   |   |
|-------|---|-----|---|---|
| 8.    | What is the main advantage of Reinforcement Learning over Supervised Learning?<br><br>✓ a) It does not need labeled data<br>b) It is faster than supervised learning<br>c) It always gives 100% accurate results<br>d) It does not require large datasets   | 1   | 1 | 1 |
| 9.    | Which of the following is an example of unsupervised learning?<br><br>✓ a) Identifying spam emails from labeled examples<br>✓ b) Grouping customers based on their purchase history<br>c) Training a self-driving car through rewards and penalties<br>d) Translating a document from English to French | 1/1 | 1 | 1 |
| 10.   | Which AI application best represents the use of Computer Vision?<br><br>✓ a) Predicting customer buying behavior<br>✓ b) Detecting objects in surveillance footage<br>c) Recommending movies on Netflix<br>d) Generating human-like text responses  | 1/1 | 2 | 1 |
| 11(a) | Design the specification in terms of PAGE for setting vacuum world agent.   | 5   | 5 | 3 |
| 11(b) | Write in detail about propositional logic and FOPL. Present suitable examples for each. Present a comparative study on these two schemes in not less than four points.  | 5   | 4 | 3 |
| 12(a) | Compare between <i>simple reflex agent</i> and <i>goal-based agent</i> along with neat sketches.  | 5   | 3 | 4 |
| 12(b) | Convert the following expression into clausal form; also, provide the detailed steps with explanation.<br><br>$\exists x \exists w \forall y (\forall z P(f(x, y), w, z) \rightarrow (\exists u Q(w, u) \& \exists v R(y, v)))$   | 5   | 4 | 4 |

Note: BL refers to Bloom's Taxonomy Level.

# Artificial Intelligence.

## Tic-Tac-Toe Game Playing

- It's a paper and pencil game of two players X and O, who chooses to mark a spaces on a grid of  $3 \times 3$ .
- The game is won by player who succeeds in putting three of their marks in a horizontal diagonal line

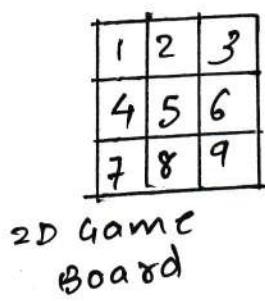


objective: To write a computer program in such way that computer wins most of time.

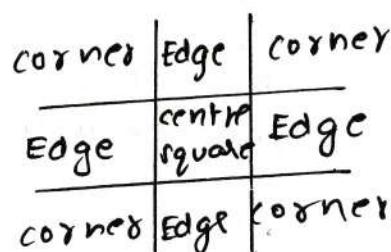
Three approaches

- complexity
- use of Generalization
- clarity of their knowledge
- Extensibility of approach

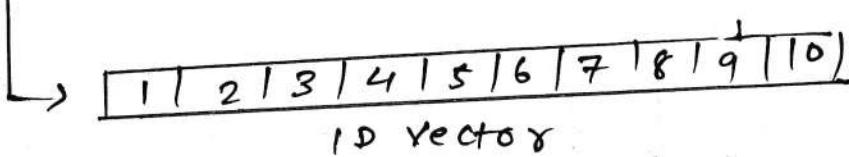
Board Data Structure



The cells could be represented as centre square, corner, edge as below



1 indicating X player move  
2 indicating O player move

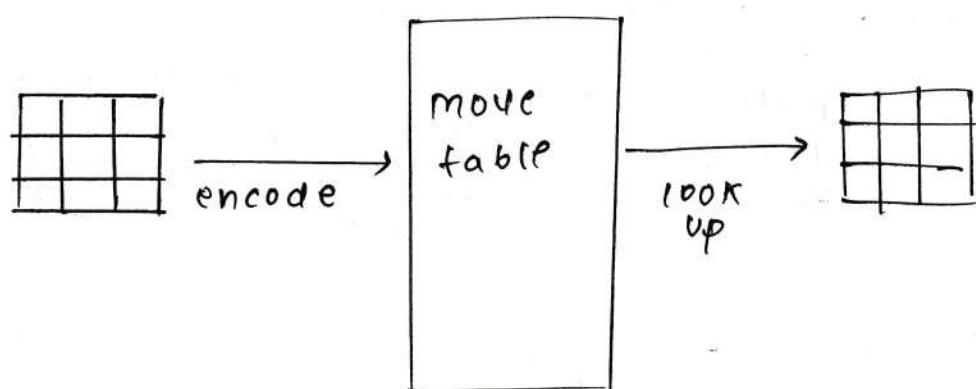


1D Vector

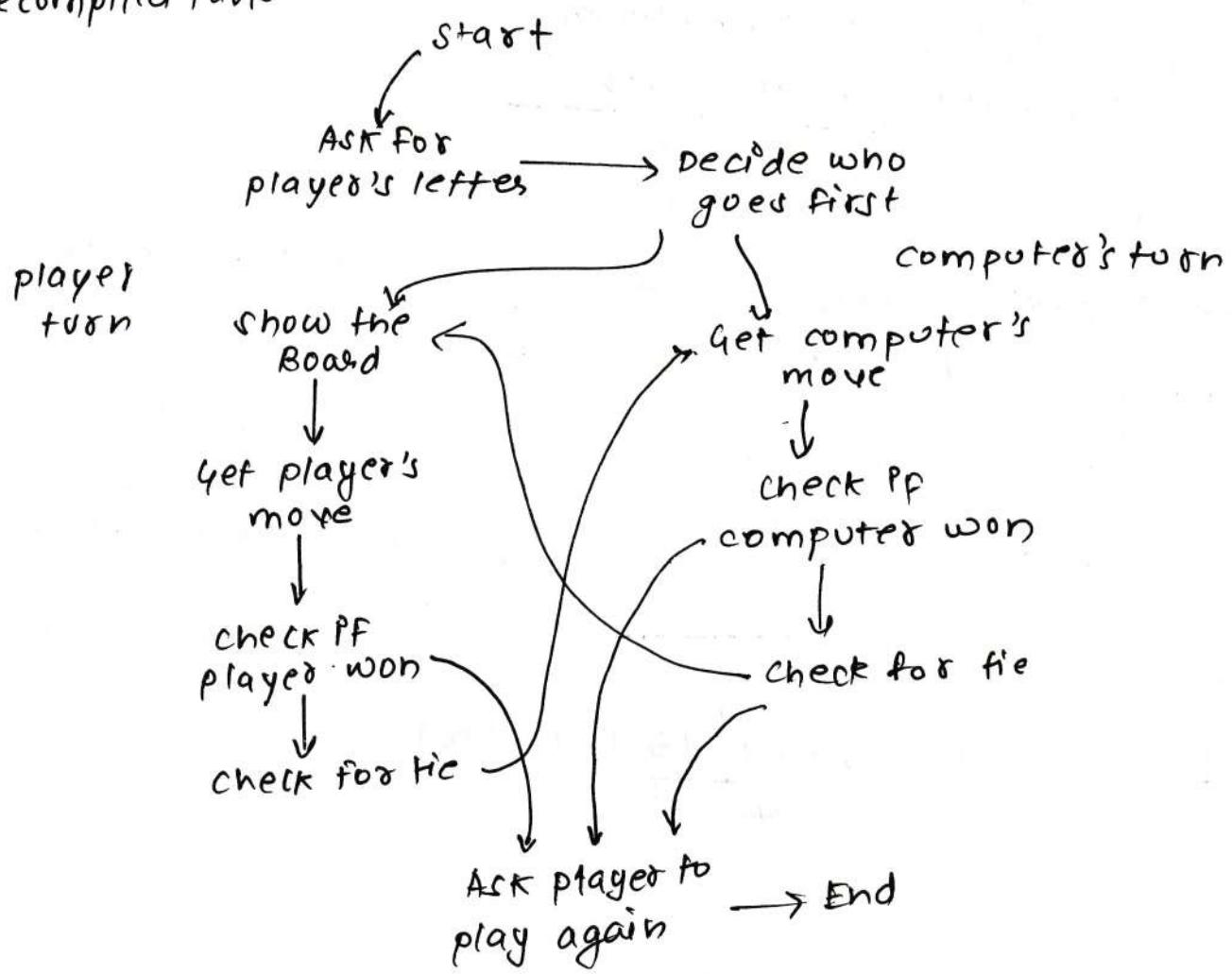
Move Table:  $gt$  is a vector of  $3^9$  elements, each element of which is nine-element vector representing board position

Total of  $3^9 (19683)$  elements in move table

| index | current Board pos | New Board pos |
|-------|-------------------|---------------|
| 0     | 000000000         | 000010000     |
| 1     | 000000001         | 020000001     |
| 2     | 000000002         | 000100002     |
| 3     | 000000010         | 002000010     |



precompiled table



## program 2: Tic Tac Toe Game Playing Magic square

We assign board positions to vector position, sum of all rows and diagonals must be:-

- Algorithm :-

$$15 - (5+4) = 6$$

- First machine will check, chance to win.

$$15 - (4+1) = 10$$

- if the difference is not positive or if it is greater than 9, then original two squares, were not collinear, so it can be ignored

- check if opponent winning block chances of winning

- previous state

|   |   |   |
|---|---|---|
| H |   | C |
|   | C |   |
| H |   |   |

$$\text{diff} = 15 - (5+4) = 6$$

6 is empty, hence computer can't win game

$$\text{diff} = 15 - (8+6) = 1$$

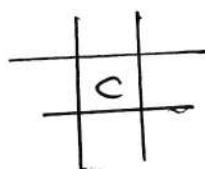
- turn computer (C)

|   |   |   |
|---|---|---|
| H |   | C |
| C | C |   |
| H |   |   |

, is empty, hence human can win the game  
Hence computer it computer - go to 1

### MAGIC SQUARE

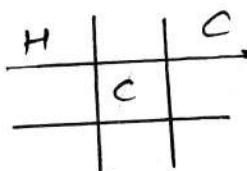
- turn - computer



Turn - Human

|   |   |  |
|---|---|--|
| H |   |  |
|   | C |  |
|   |   |  |

turn computer (C)



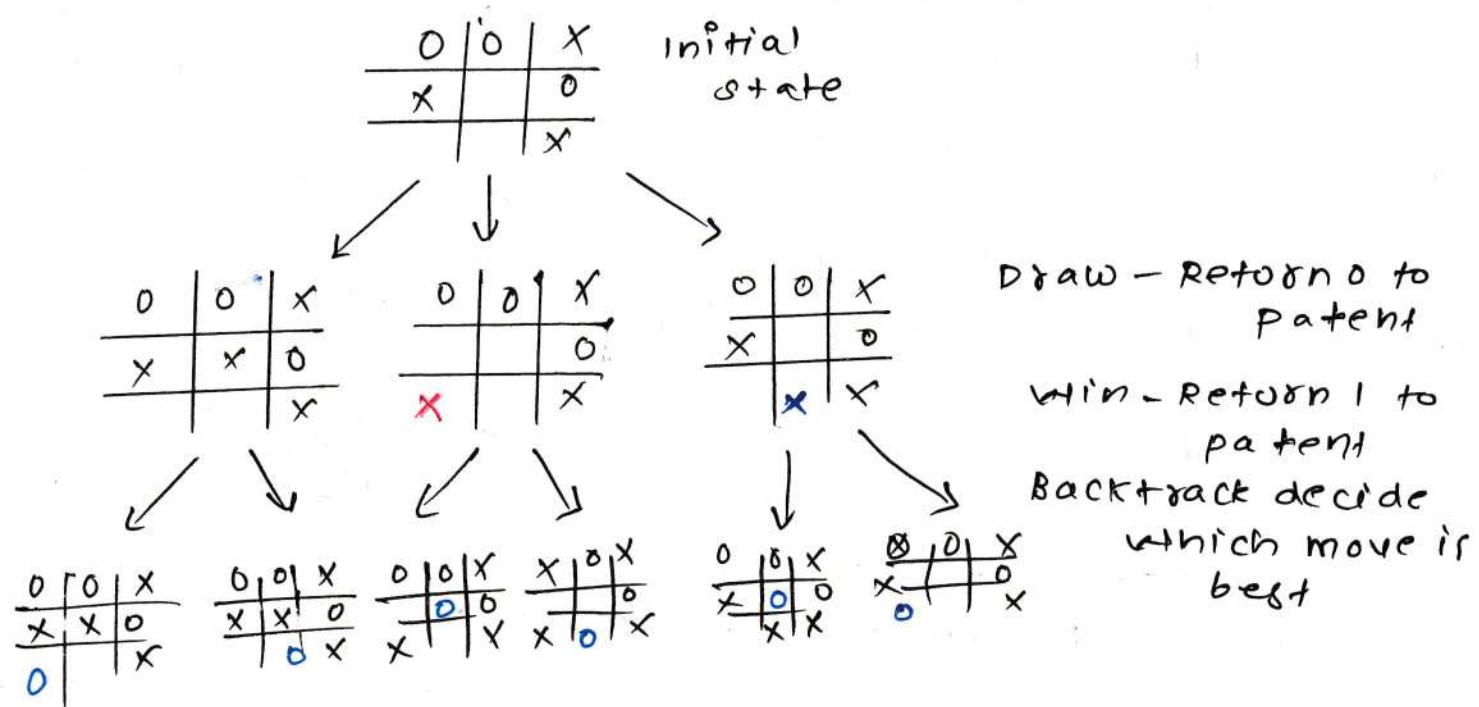
Turn - Human CH

|   |   |   |
|---|---|---|
| H |   | C |
|   | C |   |
| H |   |   |

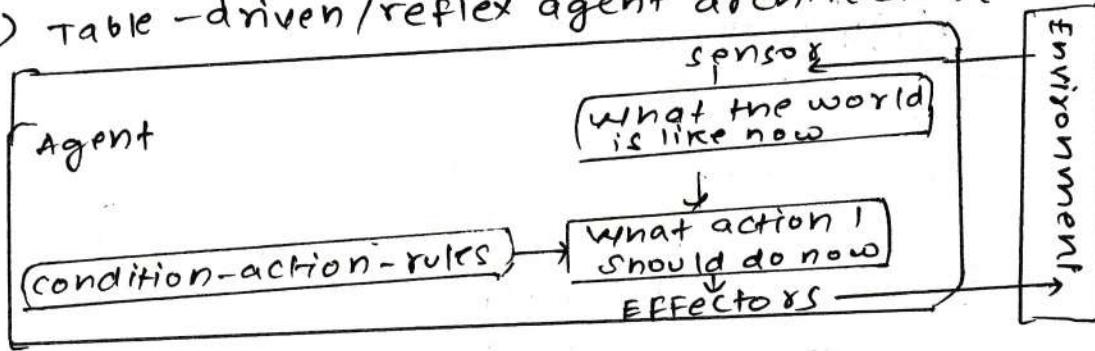
## Tic-Tac-Toe: Game playing - Program 3

### Data structures

- Board position is a structure containing
  - A 9-element array representing the board
  - A list of board positions that could result from next move.
  - A number of rating representing an estimate of how likely the board position is to lead an ultimate win for the player to move



## (0/1) Table-driven/reflex agent architecture



### (0) Table-driven agent

Table lookup of percept-action pairs mapping from every possible perceived state to the optimal Port state

problem

- too big to generate and to store (chess has about  $10^{120}$  states for example)
- no knowledge of non-perceptual parts of the current state
- not adaptive to change in environment; requires entire table to be updated if changes occur.
- looping: can't make actions conditional or previous actions/states.

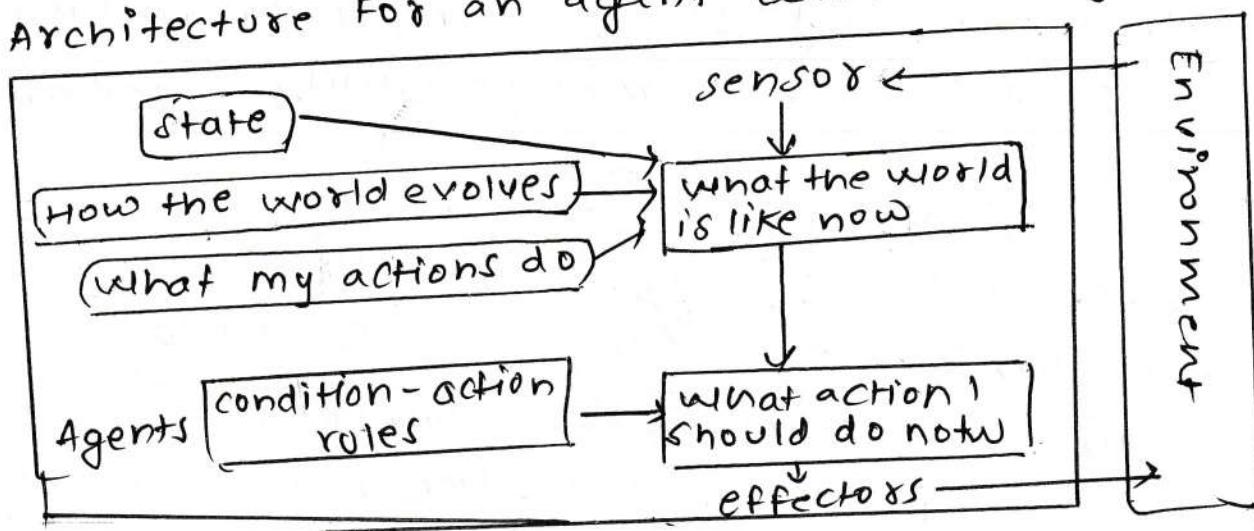
### (1) & simple reflex agents

rule-based reasoning to map from percept to optimal action; each rule handles a collection of perceived states.

problems

same problems as Table driven agen

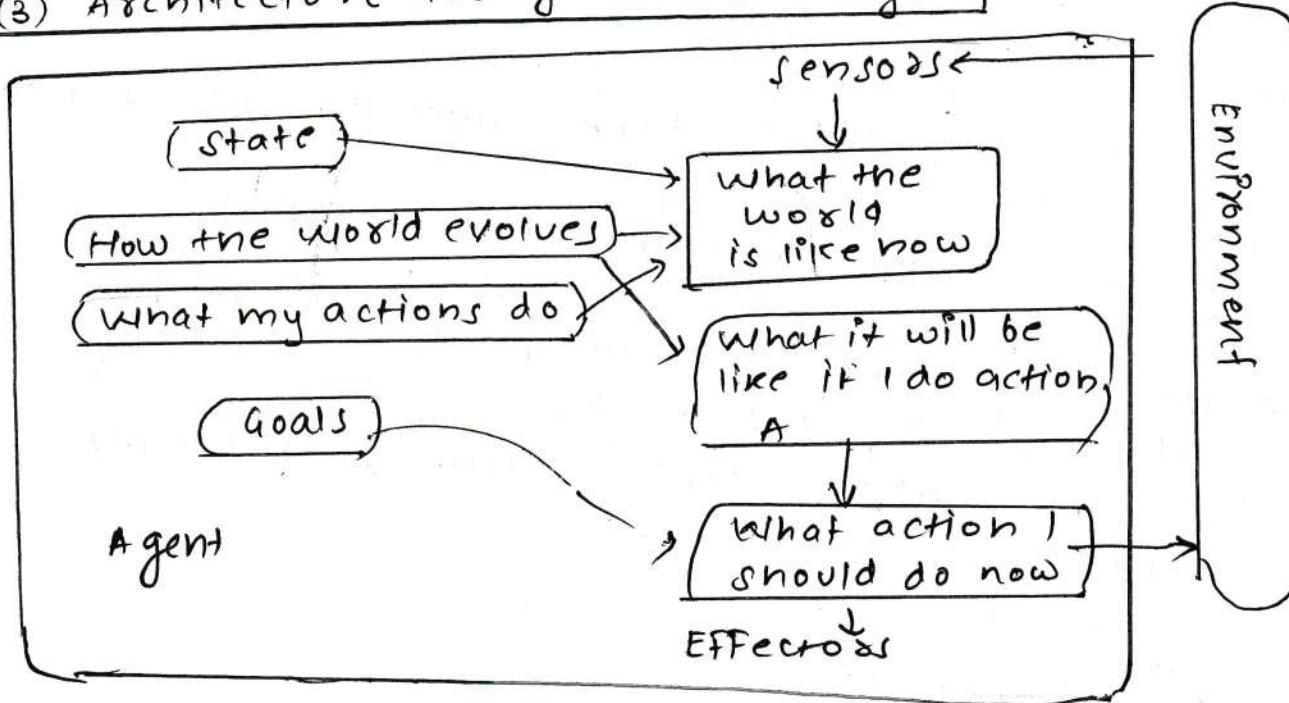
### (2) Architecture for an agent with memory



## (2) Agents with memory

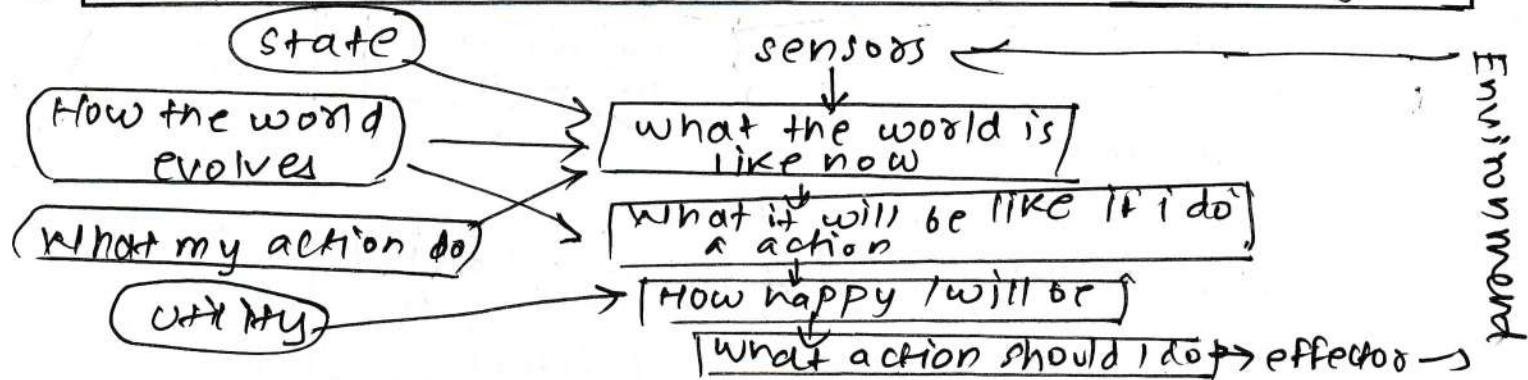
- Encode "internal state" of the world to remember the past as contained in earlier percepts.
- Needed because sensors do not usually give the entire state of the world at each input, so perception of environment is captured over time. "state" is used to encode different "world states" that generate same immediate percept

## (3) Architecture for goal-based agent



- choose actions so as to achieve a (given or computed) goal.
- A goal is a description of desirable situation or state.
- Deliberative instead of reactive.
- May have to consider long sequences of possible actions before deciding if goal is achieved

## (4) Architecture for a complete utility-based agents



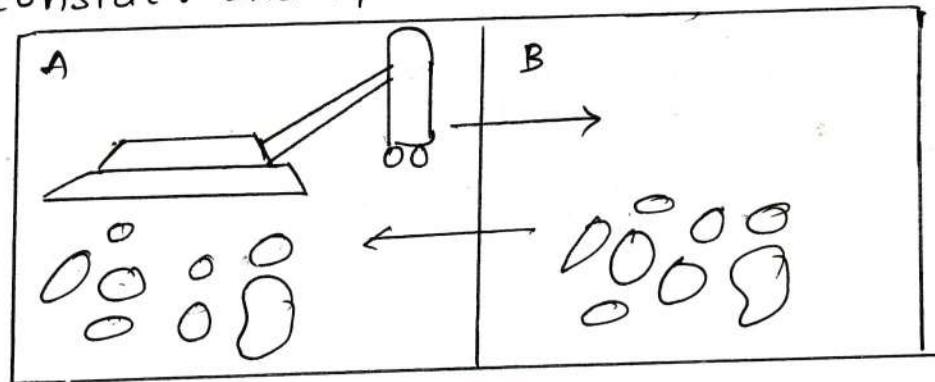
## Module 2: Problem solving by search and Exploration

A problem can be defined formally by six components

- states
- initial state
- actions
- transition model
- goal test
- path cost

**state:** The state is determined by both the agent location and the dirt locations.

consider Example



Goal is that vacuum cleaner has to clean the dirt in both the states

The agent is in one of two locations, each of which might or might not contain dirt

thus there is  $2 \times 2^2 = 8$  possible world states  
A larger Environment has n location has  $n \times 2^n$  states.

1. { $\text{LOC}(A)$ ,  $\text{dirty}(A)$ ,  $\text{dirty}(B)$ }
2. { $\text{LOC}(A)$ ,  $\text{clean}(A)$ ,  $\text{dirty}(B)$ }
3. { $\text{LOC}(A)$ ,  $\text{dirty}(A)$ ,  $\text{clean}(B)$ }

4. { $\text{LOC}(A)$ ,  $\text{clean}(A)$ ,  $\text{clean}(B)$ } Goal state.

5.  $\{ \text{Loc}(B), \text{Dirty}(A), \text{Dirty}(B) \}$

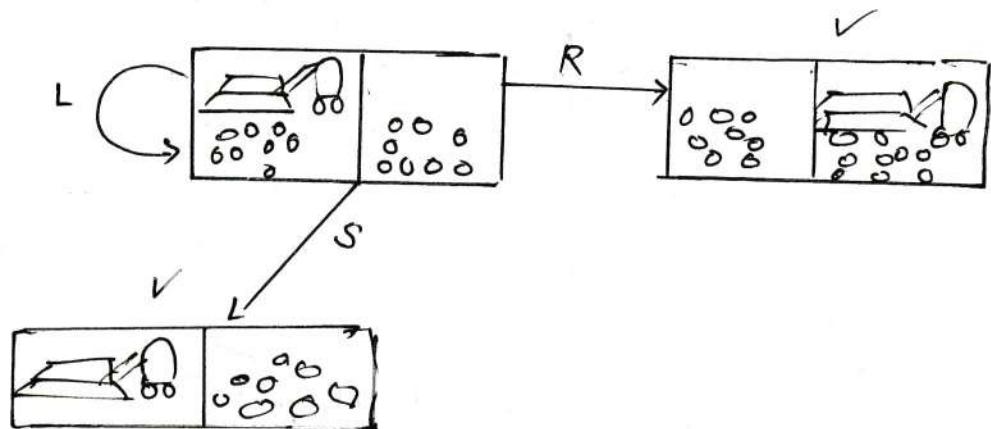
6.  $\{ \text{Loc}(B), \text{Clean}(A), \text{Dirty}(B) \}$

7.  $\{ \text{Loc}(B), \text{Dirty}(A), \text{Clean}(B) \}$

8.  $\{ \text{Loc}(B), \text{Clean}(A), \text{Clean}(B) \}$  ] Goal state

[Action] Three actions : Left, Right, suck

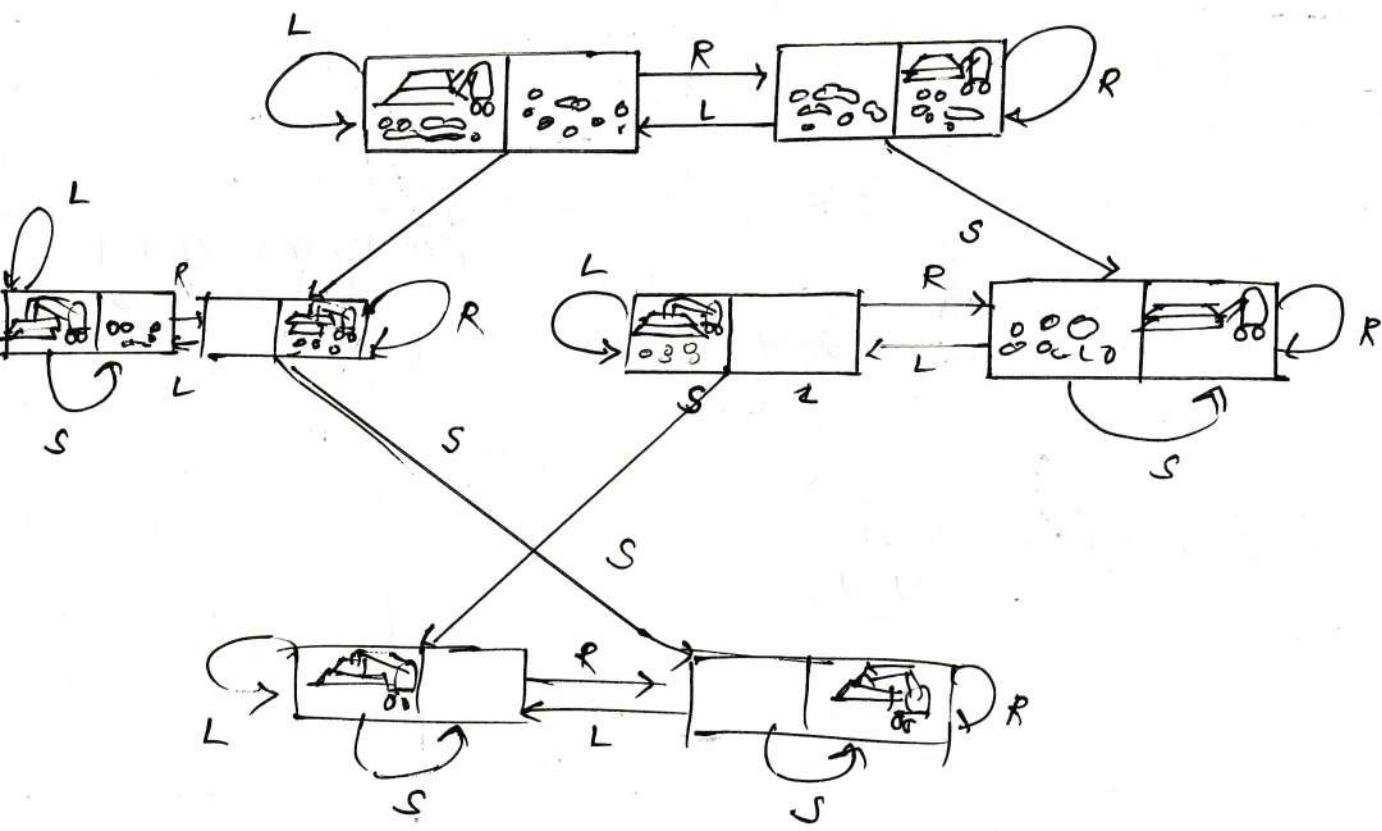
[Transition model] The actions have their expected effects that moving left in the leftmost square, moving right in the rightmost square, & sucking in clean square have no effect



[Goal test] This check whether all squares are clean

[path cost] : Each step cost 1, so cost is number of steps in path.

## Transition Model - vacuum world



States?

actions?

goal & test?

path cost?

## problem solving agent

### problem formulation

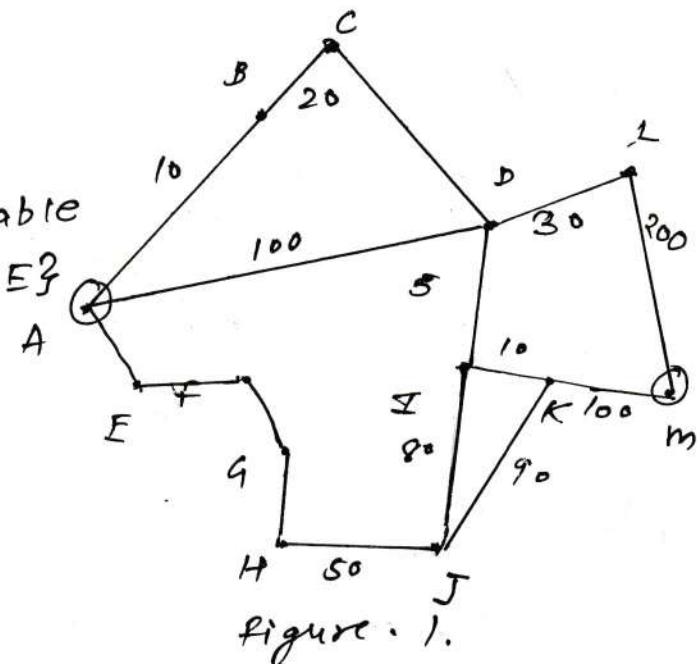
1. Initial state: The initial state is A.
2. Action set: From A the applicable actions are {GO(B,D,E)}

### 3. Successor function:

$$\text{RESULT}(\text{In}(A), \text{GO}(B)) = \text{In}(B)$$

4. Goal state:- The agents goal state is {In(m)}

5. Path cost: Distance between two transition is path cost



RESULT (S, G)

## uninformed searching

1. searching without information (Blind search)

Has informed about only two things

# what is start state

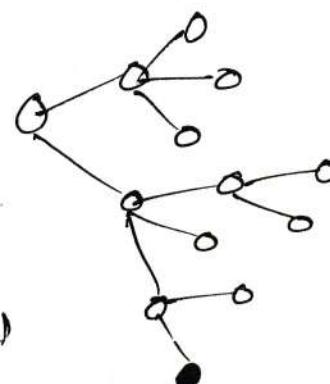
# what is goal state

Doesn't have any guide to take it to goal state

- can distinguish between goal state & Non-goal state

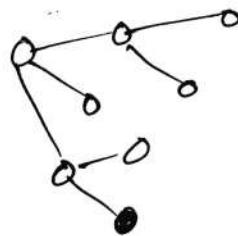
2. More time consumption and high chances of optimal solution

Example: BSF, BFS, DFS, etc.



## Breadth First search.

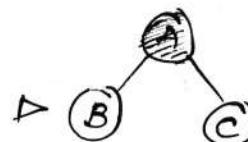
### 1. uninformed search technique



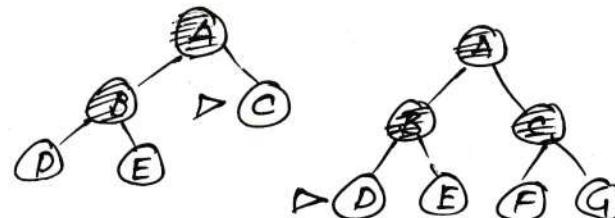
- The root node is expanded first (FIFO)

$\triangleright A$

- All the nodes generated by the root node are then expanded.



- And their successor and so on.



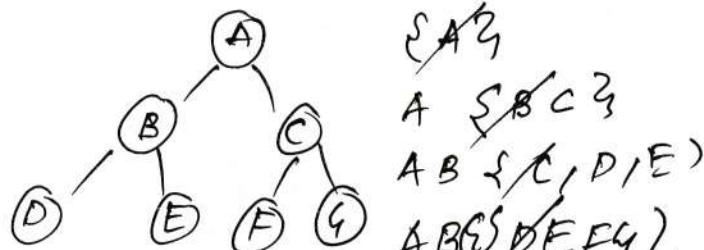
Gives shortest solution.

Time complexity

$$\text{BS} \rightarrow O(V+E)$$

$$\text{AI} \rightarrow O(b^d)$$

### ⑥ Algorithm.



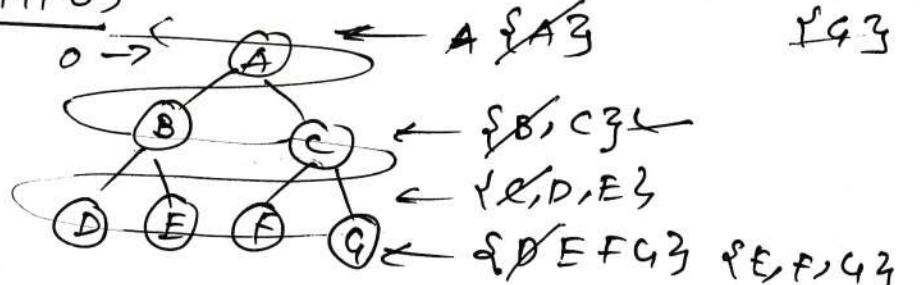
- Entered starting nodes in queue
- If  $\rightarrow$  queue empty return fail and stop
- If  $\rightarrow$  first element in queue is goal node then return success & stop.

Else

- Remove and expand first element in queue and place children nodes at the end of the queue

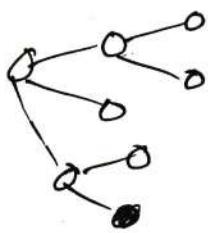
- Goto step (ii) :

Working (FIFO)

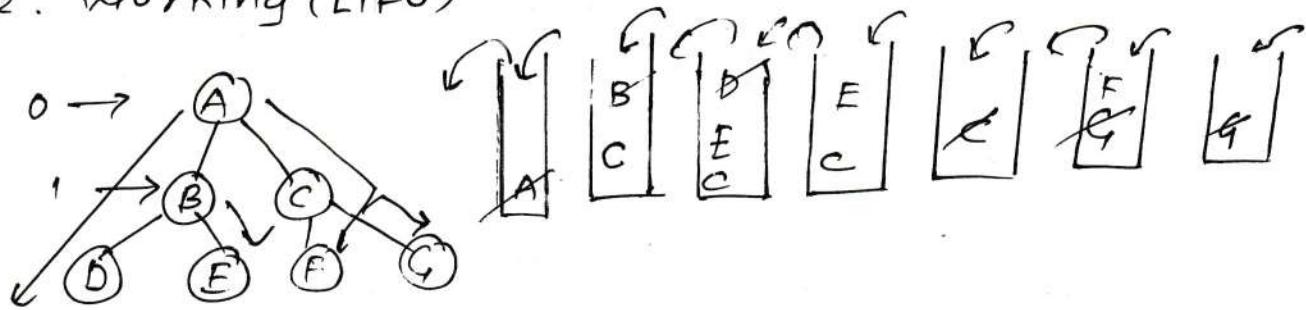


## (Depth First search) (DFS)

### 1. uninformed search techniques



### 2. working (LIFO)



3) works vertically

4) doesn't guarantee a solution always

5) time complexity

DS  $\rightarrow \Theta(V+E)$

AI  $\rightarrow \Theta(b^d)$

6) Algorithm.

1. push the root node in the stack

2. while (stack is not Empty)

    a) pop a node from the stack

        i) if node is a goal node  
            return success

        ii) push all children of node  
            onto the stack

3. return failure.

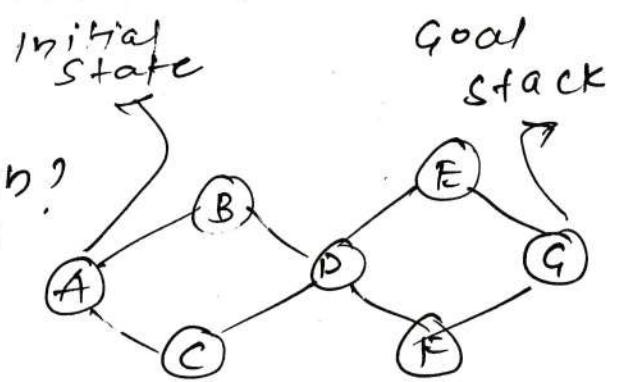
## Bidirectional search

1. What is Bidirectional search?

2. Time complexity:  $2(b^{d/2})$

3. Pros

i) Much EFFICIENT and FAST  
ii) Reduce time requirement  
suppose  $b = 10$   $d = 6$

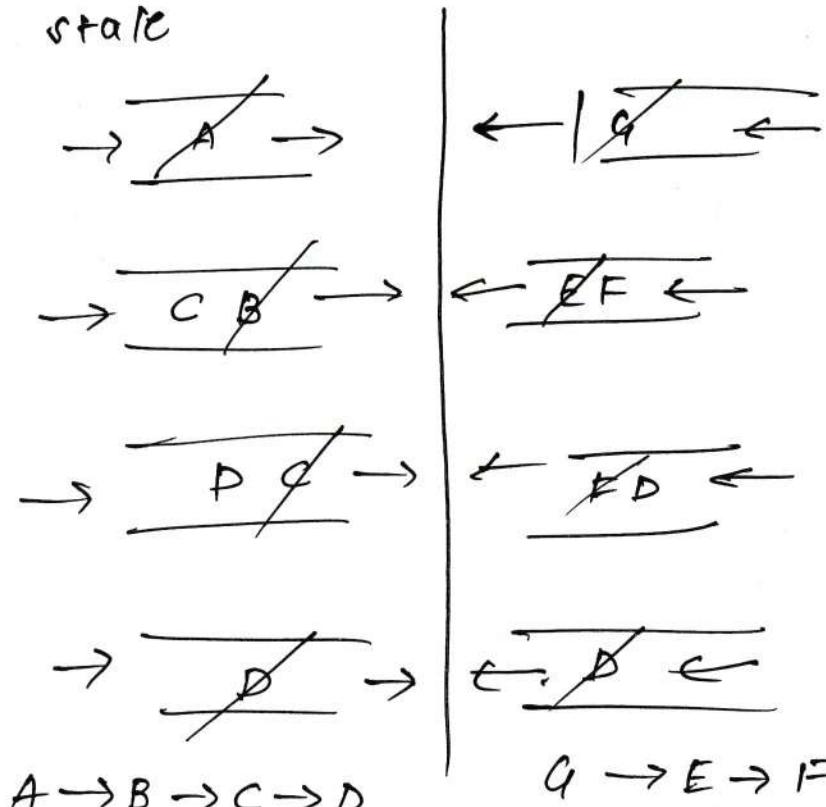
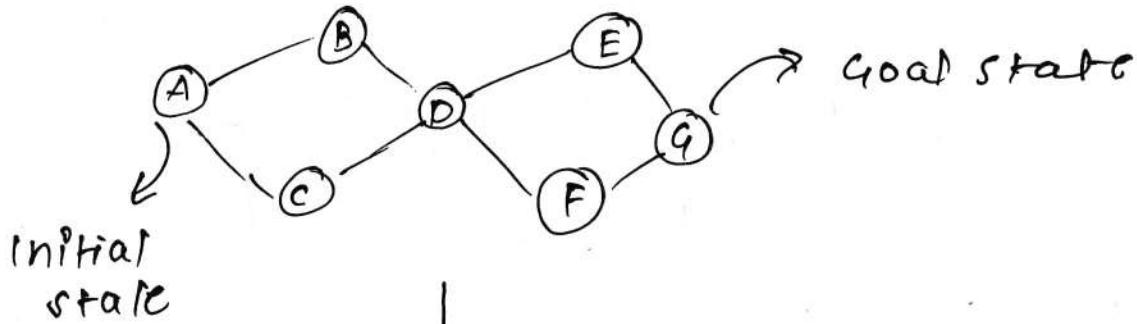


$$B.F.S \therefore 6^d = 10^6 = 1000000 \text{ nodes}$$

$$B.S = 2 \times 10^3 = 2000 \text{ nodes}$$

cons

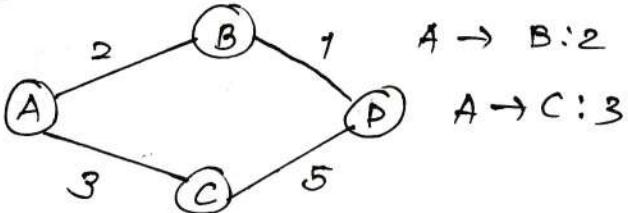
- i) Implementation is difficult
- ii) Goal state must be known in advance



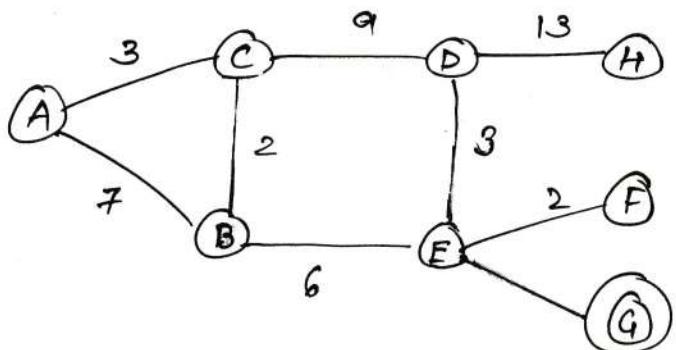
combine both

path  $A \rightarrow B \rightarrow C \rightarrow D \rightarrow F \rightarrow E \Rightarrow G$

## uniform cost search (UCS)



A → B → D path cost: 3



A → C → B → E → G  
3    2    6    1

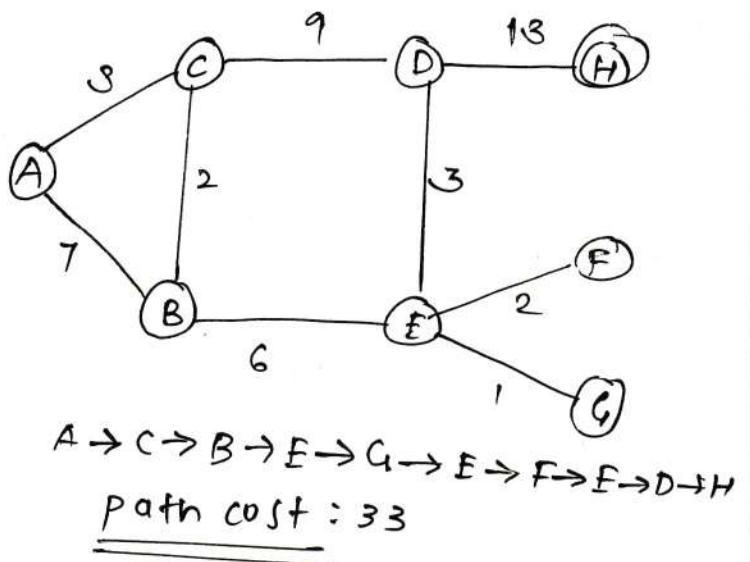
path cost: 12

### Advantages:-

1. Mostly gives optimal solutions

### Disadvantages

1. Can get stuck in an infinite loop.



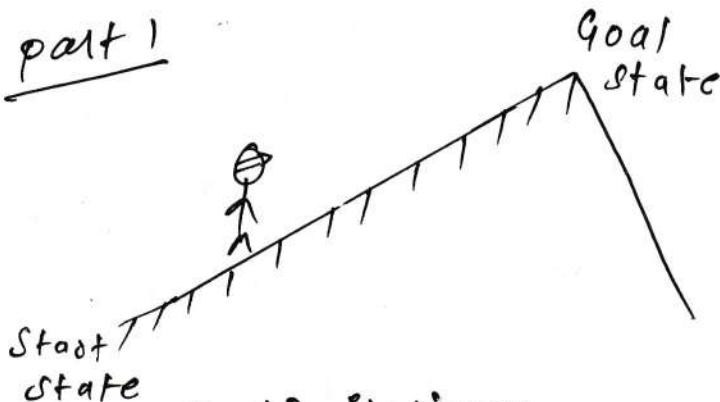
### Features

1. Reaches to Goal node
2. Back Tracking is possible
3. Uses Priority Queue
4. Node Expansion is based on path cost

## Hill climbing Algorithm

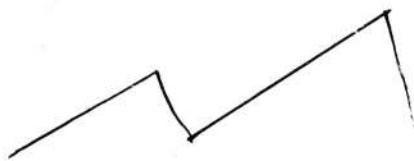
### 1. Introduction

part 1

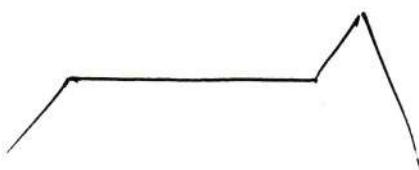


### 2. Limitations

i) Local Maxima



ii) Plateau:-

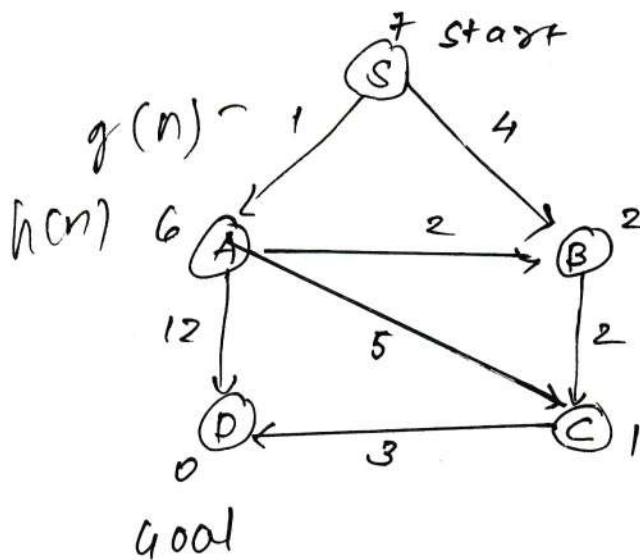


iii) Ridge



part 2

## A\* Algorithm



$S \rightarrow B \rightarrow C$

$$f(n) = g(n) + h(n)$$

$$= 6 + 1$$

$$= 7$$

## A\* Algorithm

$S \rightarrow A$

$$f(n) = g(n) + h(n)$$

$$= 1 + 6$$

$$= 7$$

$S \rightarrow B$

$$f(n) = g(n) + h(n)$$

$$= 4 + 2$$

$$= 6$$

$S \rightarrow A = 7$

$\times S \rightarrow B \Rightarrow 6$

$S \rightarrow B \rightarrow C = 7$

$S \rightarrow B \rightarrow C$ 

$$f(n) = g(n) + h(n)$$

$$= 6 + 1$$

$$= 7$$

 $\times S \rightarrow A \Rightarrow 7$  $\times S \rightarrow B \Rightarrow 6$  $S \rightarrow B \rightarrow C : 7$  $\times S \rightarrow A \rightarrow B = 5$ 

$$S \rightarrow A \rightarrow B \quad f(n) = g(n) + h(n)$$

$$= 3 + 2 = 5$$

 $S \rightarrow A \rightarrow C = 7$  $\cancel{A} \quad S \rightarrow A \rightarrow D \Rightarrow 13$  $S \rightarrow A \rightarrow C$ 

$$f(n) = g(n) + h(n)$$

$$= 6 + 1$$

$$= 7$$

 $S \rightarrow A \rightarrow B \rightarrow C : 6$ 

$$\boxed{\begin{array}{l} \cancel{A} \quad S \rightarrow A \rightarrow B \rightarrow C \rightarrow D = 8 \\ \cancel{A} \quad S \rightarrow B \rightarrow C \rightarrow D \Rightarrow 9 \end{array}}$$

 $S \rightarrow A \rightarrow D$  $S \rightarrow A \rightarrow B \rightarrow C \rightarrow D$ 

$$f(n) = g(n) + h(n)$$

$$= 13 + 0$$

$$= 13$$

$$f(n) = g(n) + h(n)$$

$$= 8 + 0$$

$$= 8$$

 $\cancel{S \rightarrow A \rightarrow B \rightarrow C}$ 

$$f(n) = g(n) + h(n)$$

$$= 5 + 1$$

$$= 6$$

 $S \rightarrow B \rightarrow C \rightarrow D$ 

$$f(n) = g(n) + h(n)$$

$$= 9 + 0$$

$$= 9$$

final path  $S \rightarrow A \rightarrow B \rightarrow C \rightarrow D$

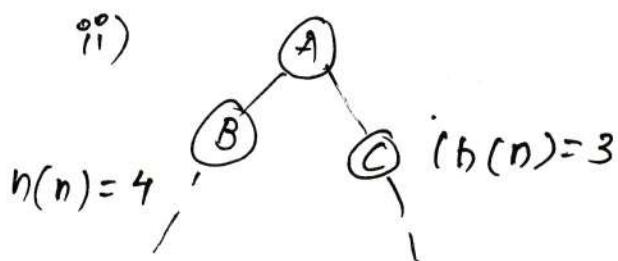
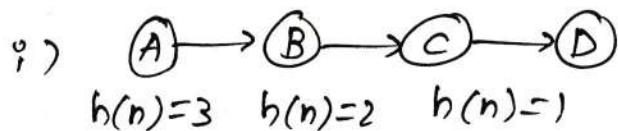
## Heuristic search & Function

1. What is Heuristic search?

→ It tries to optimize a problem with the use of heuristic function.

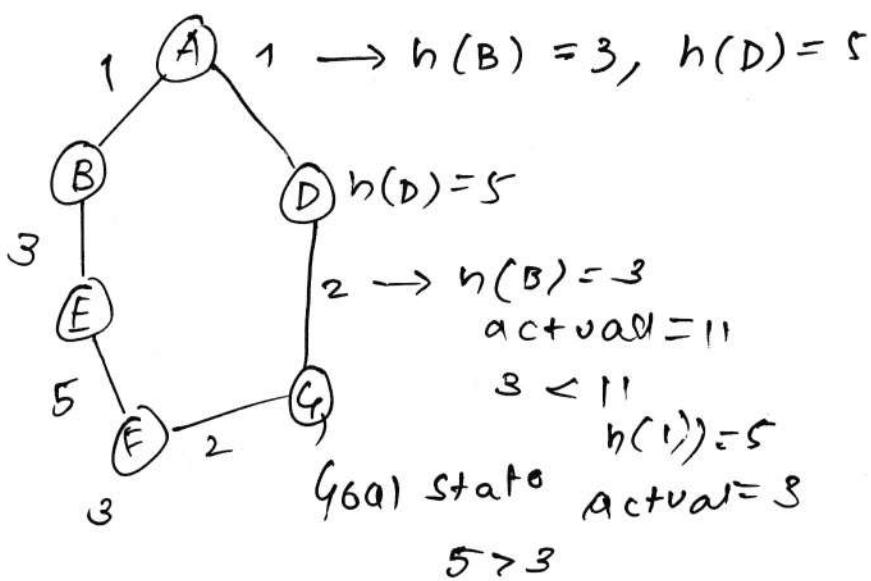
2. What is Heuristic Function?

→ It is a function that gives an estimation of the cost of getting from node  $n$  to the goal node.

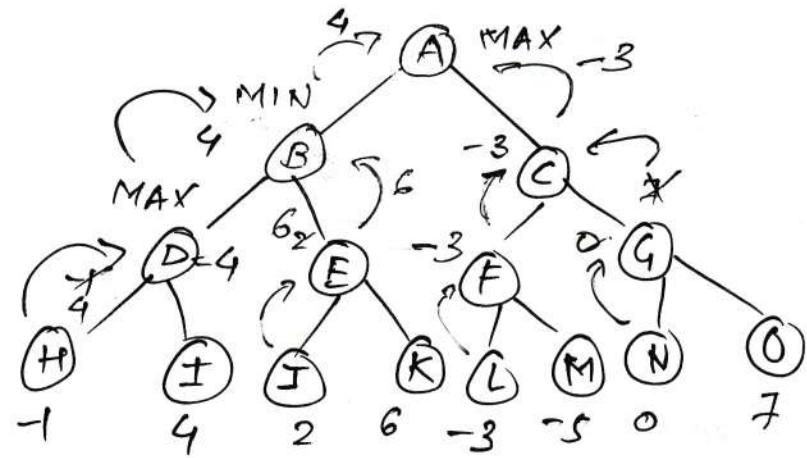


3) Types of Heuristic Function

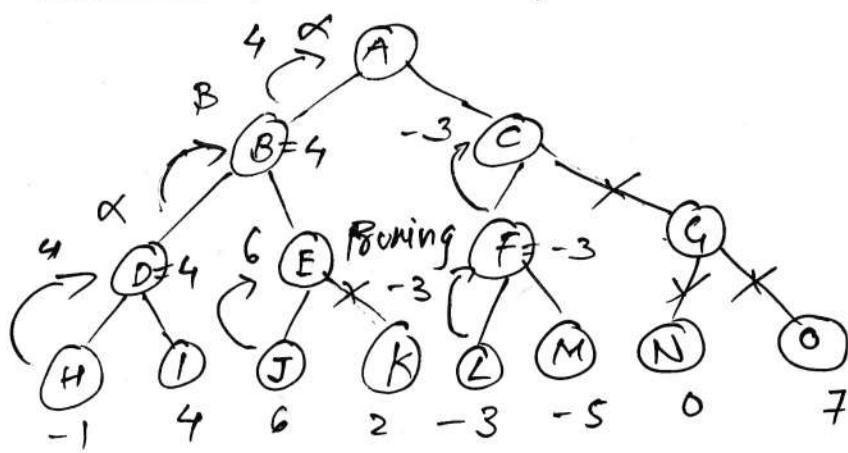
- i) Admissible ( $h(n) \leq h'(n)$ )
- ii) Non-Admissible ( $h(n) > h'(n)$ )



## Min-Max Algorithm



## Alpha-Beta Pruning



## PEAS FOR WUMPUS IN AI

### Environment

A  $4 \times 4$  grid of rooms.

- The agent initially in room square [1,1], Facing toward the right
- Location of wumpus and gold are chosen randomly except the first square [1,1]

### Actions/Accumulators

- The agent can move forward, turn left, by  $90^\circ$  or turn right by  $90^\circ$
- The action Grab can be used to pick up the gold if it is there in same square as agent
- The action Shoot can be used to fire an arrow in a straight line in the direction the agent is facing
- The action Climb can be used to climb out of the cave, but only from square [1,1]

### Sensors The Agent has five sensor :-

- In square containing the wumpus and in the directly (not diagonally) adjacent square, the agent will perceive a Stench.
- In square directly adjacent to a pit, the agent will ~~perceives~~ perceives as Breeze.
- In the square where the gold is, the agent will perceive Glitter.
- When an agent walks into a wall, it will perceive a Bump.

## WUMPUS WORLD

### 1. Introduction:

\* wumpus, stench, Agent, pit, Breeze, gold, Arrow.

### Awards and Punishment

- i) +1000 points if Agent comes out with gold.
- ii) -1 point on agents every Action.
- iii) -10 point if arrow is used.
- iv) -1000 point if agent dies./ or eaten by wumpus or falling into pit

|  |                                 |                 |               |
|--|---------------------------------|-----------------|---------------|
| 4.1<br>Stench  | 4.2                             | 4.3 ~<br>Breeze | 4.4<br>PIT    |
| 3.1<br> Stench | 3.2<br>Breeze<br>Stench<br>Gold | 3.3<br>PIT      | 3.4<br>Breeze |
| 2.1<br>Stench  | 2.2                             | 2.3<br>Breeze   | 2.4           |
| 1.1<br> Start | 1.2<br>Breeze                   | 1.3<br>PIT      | 1.4<br>Breeze |

### P.E.A.S PROPERTIES performance measure

- i) +100

### Environment: i) Empty Room

ii) Room with WUMPUS

iii) stenchy rooms

iv) breezy rooms

v) Room with Gold

vi) Arrow

sensors i) camera, ii) odor sensors iii) audio sensors

Effectors: i) motor to move R, L . ii) Robotic Arm to grab gold

iii) Robotic mechanism to shoot arrow.

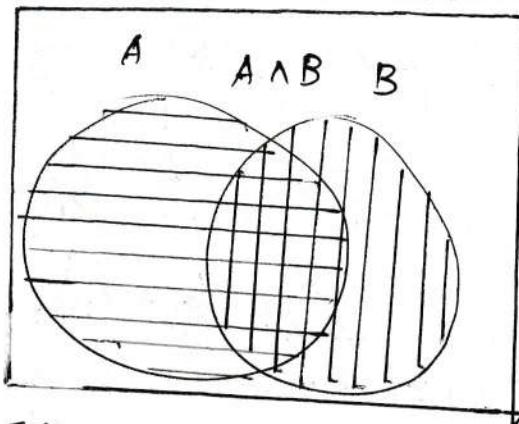
# probabilistic Reasoning

True.

## Axioms of Probability

for any propositions  $A, B$

- $0 \leq P(A) \leq 1$
- $P(\text{True}) = 1$  and  $P(\text{False}) = 0$
- $P(A \vee B) = P(A) + P(B) - P(A \wedge B)$



## Multivalued Random variable

suppose  $A$  can take on more than 2 values  
 $A$  is a random variable with arity  $K$  if it can takes on exactly one value out of  $\{v_1, v_2, \dots, v_K\}$ ,  
 Thus.

$$P(A=v_i \wedge A=v_j) = 0 \text{ if } i \neq j$$

$$P(A=v_1 \vee A=v_2 \vee A=v_K) = 1$$

$$\sum_{j=1}^K P(A=v_j) = 1$$

## conditional probability

conditional probability

$$P(a|b) = \frac{P(a \wedge b)}{P(b)} \quad P(b) > 0$$

product rule gives an alternative

$$P(a \wedge b) = P(a|b) P(b) = P(b|a) P(a)$$

general version holds for whole distribution

$$P(\text{weather, cavity}) = P(\text{Weather} | \text{cavity}) \\ P(\text{cavity})$$

## conditional probability

chain rule is derived by successive application of product rule:-

$$\begin{aligned} P(x_1, \dots, x_n) &= P(x_1, \dots, x_{n-1}) P(x_n | x_1, \dots, x_{n-1}) \\ &= P(x_1, \dots, x_{n-2}) P(x_{n-1} | x_1, \dots, x_{n-2}) P(x_n) \\ &\quad x_1, \dots, x_{n-1}) \\ &= P(x_1) P(x_2 | x_1) P(x_3 | x_1, x_2) \dots P(x_n | x_1, \dots, x_{n-1}) \end{aligned}$$

or  $\prod_{i=1}^n P(x_i | x_1, \dots, x_{i-1})$

## Inference by enumeration

start with the joint probability distribution

|        |               | toothache | $\neg$ toothache |       |              |
|--------|---------------|-----------|------------------|-------|--------------|
|        |               | catch     | $\neg$ catch     | catch | $\neg$ catch |
| cavity | toothache     | 0.108     | 0.012            | 0.072 | 0.008        |
|        | $\neg$ cavity | 0.016     | 0.064            | 0.144 | 0.576        |

$\varphi$  sum the atomic events where it is

$$\text{true } P(\varphi) = \sum_{\omega: \omega \models \varphi} P(\omega)$$

$$P(\text{toothache}) = 0.108 + 0.012 + 0.016$$

conditional probabilities

$$\begin{aligned} P(\neg \text{cavity} | \text{toothache}) &= \frac{P(\neg \text{cavity} \wedge \text{toothache})}{P(\text{toothache})} \\ &= \frac{0.016 + 0.064}{0.108 + 0.012 + 0.016 + 0.064} = 0.4 \end{aligned}$$

## In class exercise

Given the joint distribution shown below and definition  $P(a|b) = \frac{P(a \cap b)}{P(b)}$

$$P(\text{cavity} = \text{True}) = ?$$

$$P(\text{weather} = \text{sunny}) = ?$$

$$P(\text{cavity} = \text{True} | \text{weather} = \text{sunny})$$

$$P(\text{weather}, \text{cav cavity}) = P(\text{weather} | \text{cavity}) \\ P(\text{cavity})$$

|                |  | sunny          |       |      | rainy |      | cloudy |  |
|----------------|--|----------------|-------|------|-------|------|--------|--|
|                |  | cavity = true  | 0.144 | 0.02 | 0.016 | 0.02 |        |  |
|                |  | cavity = false | 0.576 | 0.08 | 0.064 | 0.08 |        |  |
| weather = snow |  |                |       |      |       |      |        |  |

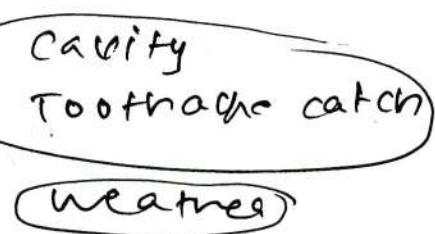
### Independence

A and B are independent iff

$$P(A|B) = P(A) \cdot P(B) \quad \text{or} \quad P(B|A)$$



decomposes into



$$P(\text{Toothache, catch, cavity, weather})$$

$$= P(\text{Toothache, catch, cavity}) P(\text{weather})$$

## Bayes' Rule:

product rule  $P(a \wedge b) = P(a|b)P(b) = P(b|a)P(a)$

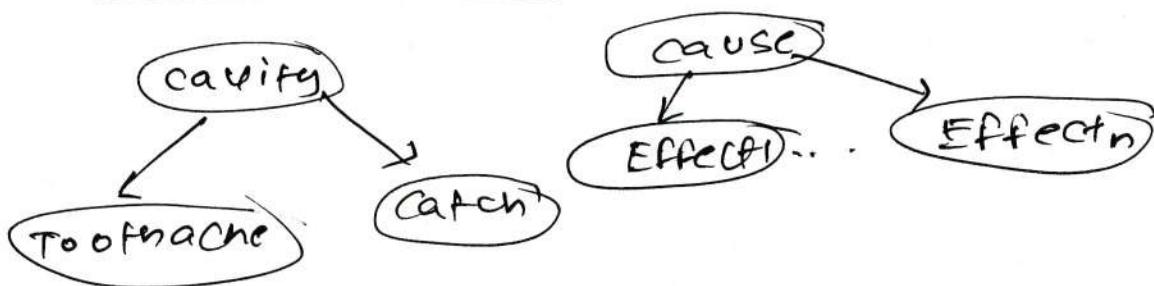
Bayes' Rule  $P(a|b) = P(b|a) \frac{P(a)}{P(b)}$

distribution form

$$P(Y|X) = P(X|Y) \frac{P(Y)}{P(X)} = \alpha P(X|Y)P(Y)$$

$$\begin{aligned}
 & P(\text{Cavity} | \text{toothache} \wedge \text{catch}) \\
 &= \alpha P(\text{toothache} \wedge \text{catch} | \text{cavity}) P(\text{cavity}) \\
 &= \alpha P(\text{toothache} | \text{cavity}) P(\text{catch} | \text{cavity}) P(\text{cavity})
 \end{aligned}$$

## Naive Bayes



conditionally independent

$$P(\text{catch} | \text{toothache}, \text{cavity}) = P(\text{catch} | \text{cavity})$$

$$\begin{aligned}
 P(\text{toothache}, \text{catch} | \text{cavity}) &= P(\text{toothache} | \text{cavity}) \\
 P(\text{catch} | \text{cavity})
 \end{aligned}$$

## Bayesian network

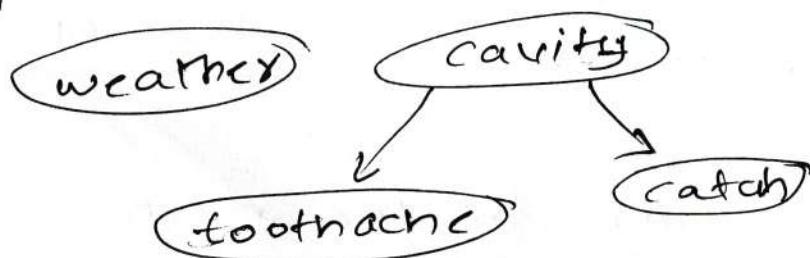
A simple, graph, graphical notation for conditional independence assertions and hence for compact specification of joint distributions.

### Syntax

- a set of nodes, one per variable.
- a directed, acyclic graph (links "directly influences")
- a conditional distribution for each node given its parents:  $P(x_i | \text{parents}(x_i))$ .

### Example

Topology of network encodes conditional independence assertions.



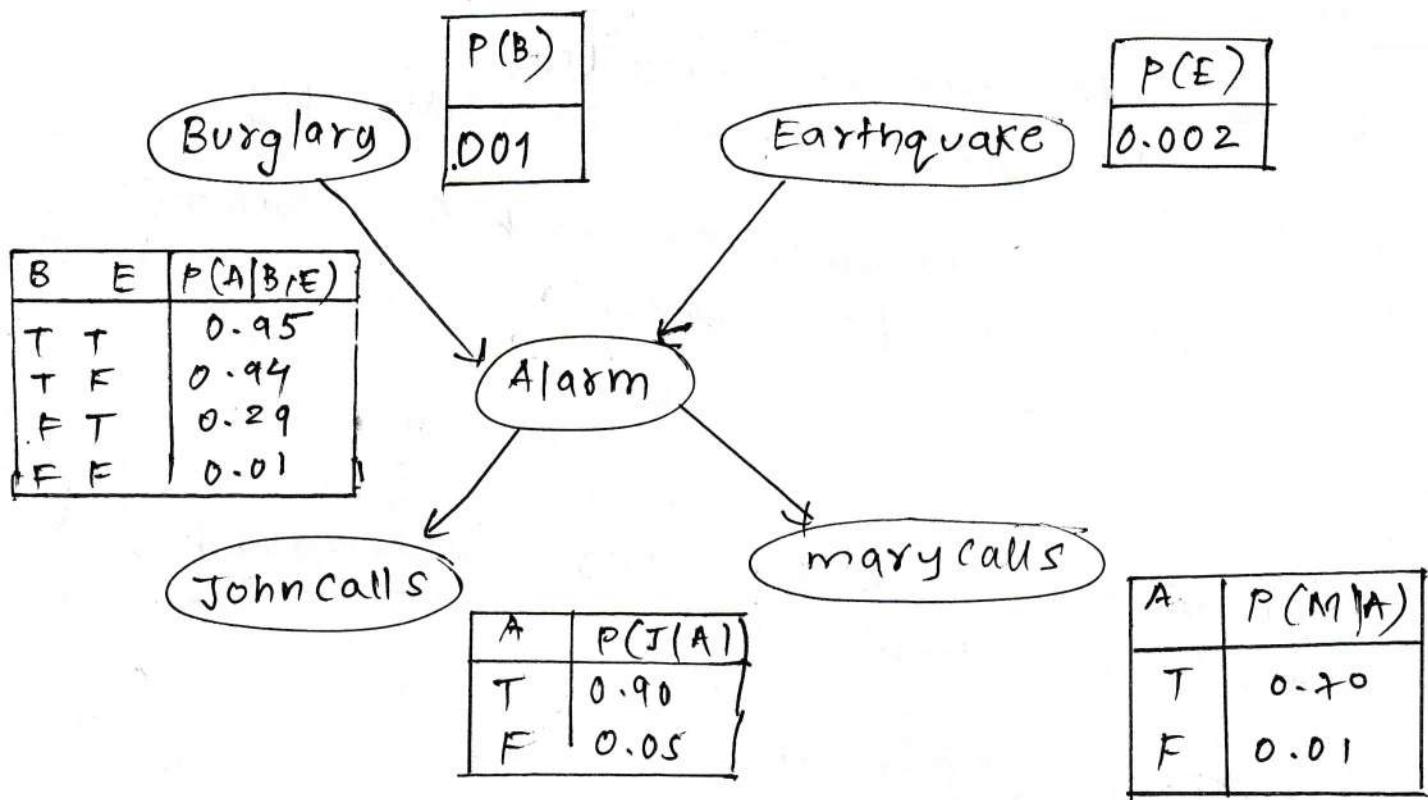
### Example

"I'm at work, neighbor John calls to say my alarm is ringing, but neighbor Mary doesn't. Is there a burglar."

Variables: Burglary, Earthquake, Alarm, JohnCalls, MaryCalls.

Network topology reflects "causal" knowledges:

- A burglar can set the alarm off
- An earthquake can set the alarm off.
- The alarm can cause Mary to call.
- The alarm can cause John to call.



Q1) what is the probability that the alarm has sounded but neither burglary nor an earthquake has occurred and both John and Mary call.

$$\begin{aligned} P(j \wedge m \wedge a \neg b \wedge \neg e) &= P(j|a)P(m|a)P(a \neg b, \neg e)P(\neg b)P(\neg e) \\ &= 0.90 \times 0.70 + 0.001 \times 0.999 \times 0.998 \\ &= 0.00062 \end{aligned}$$

What is the probability that John call?

$$\begin{aligned} &= P(j/a)P(a) + P(j/\neg a)P(\neg a) \\ &= P(j/a) \{ P(a/b, c) * P(b, c) + P(a/\neg b, c) * P(\neg b, c) + \\ &\quad P(a/b, \neg c) * P(b, \neg c) + P(a/\neg b, \neg c) * P(\neg b, \neg c) \} \\ &+ P(j/\neg a) \{ P(\neg a/b, c) * P(b, c) + P(\neg a/\neg b, c) * P(\neg b, c) + \\ &\quad P(\neg a/b, \neg c) * P(b, \neg c) + P(\neg a/\neg b, \neg c) * P(\neg b, \neg c) \} \\ &= 0.96 * 0.00252 + 0.05 * 0.9974 \\ &= \underline{\underline{0.0521}} \end{aligned}$$

Given :-

Let Event 'A' denote falling sick due to flu

Let Event 'B' denote falling sick due to measles  
and no other disease

$$P(A) = ? \quad (R' \text{ Event Rashes})$$

$$P(A) = 0.9 \quad P(R/B) = 0.95 = \frac{0.072}{0.167}$$

$$P(B) = 0.1 \quad P(R/A) = 0.08 \quad P(A/R) = 0.43$$

$$P(R \cap A/R) = \frac{0.08 \times 0.9}{0.95 \times 0.1 + 0.08 \times 0.9}$$

$$P(A/R) = \frac{P(R/A) \cdot P(A)}{P(R/B) \cdot P(B) + P(R/A) \cdot P(A)}$$

$$P(A/R) = 0.072 / 0.072 + 0.095$$

All students are smart

$\forall x : (\text{student}(x) \rightarrow \text{smart}(x))$

There Exist a student

$\exists x : \text{student}(x)$

There Exist a smart student

$\exists x : \text{student}(x) \wedge \text{smart}(x)$

Every student loves some student

$\exists x : \text{student}(x) \wedge \text{Loves} \rightarrow \exists y (\text{student}(y) \wedge \text{loves}(x, y))$

There is a student who is loved by every other student

$\exists x : \text{student}(x) \Rightarrow \exists y : (\text{student}(y) \wedge \neg(x=y) \wedge \text{Lover}(y, x))$

Bill is a student

$\exists x : \text{student}(\text{Bill})$

Bill takes either Analysis or Geometry (not both)

takes(Bill, Analysis)  $\leftrightarrow$  takes(Bill, Geometry)

Bill takes Analysis or Geometry or both

takes(Bill, Analysis)  $\vee$  takes(Bill, Geometry)

Bill takes Analysis and Geometry

takes(Analysis)  $\wedge$  takes(Bill, Analysis)  $\wedge$  takes(Bill, Geometry)

## FIRST ORDER PREDICATE LOGIC (FOPL)

1. All boys like cricket

$$\forall(x): \text{boys}(x) \rightarrow \text{like}(x, \text{cricket})$$

2. Some girls hate football

$$\exists(x): \text{girls}(x) \rightarrow \text{hate}(x, \text{football}) \quad (\text{wrong})$$

$$\exists(x): \text{girls}(x) \wedge \text{hate}(x, \text{Football})$$

2. Some boys like football

$$\exists(x): \text{boys}(x) \wedge \text{like}(x, \text{football})$$

3. All girls love pink

$$\forall(x): \text{girls}(x) \rightarrow \text{love}(x, \text{pink})$$

4. Every person who buys a policy is smart

$$\exists(x) \forall x \forall y: \text{person}(x) \wedge \text{policy}(y) \wedge \text{buys}(x, y) \rightarrow$$

$$\exists(x, y): \text{person}(x) \quad \text{Imp. (example)} \quad \text{smart}(x)$$

6. No person buys expensive policy

$$\nexists \forall x \forall y: \text{person}(x) \wedge \text{policy}(y) \wedge \text{buys}(x, y) \rightarrow$$

$$\neg \text{buys}(x, y) \quad \text{Imp. example}$$

If it is winter, then it will be cool

$\exists x, y : \underline{\text{winter}(x) \wedge \text{cool}(y)} \xrightarrow{\text{Action}} \underline{\text{will be}(x, y)}$

$\exists x, y : \underline{\text{winter}(x) \rightarrow \text{will be}(\text{cool}, x)}$

$\text{winter}(x) \wedge \text{cool}(y) \rightarrow \text{will be}(x, y)$

"The car is either at John's house or at Fred's house if car is not at John house, it must be at Fred's house

$\forall x, \exists y : \underline{\text{Johnhouse}(x), \text{Fredshouse}(y)}$

~~car~~  $\rightarrow \text{isat}(x) \leftrightarrow \text{car} \rightarrow$

$\text{isat}(\text{car}, x) \leftrightarrow \text{isat}(\text{car}, y)$

$\neg (\text{car}, x) \rightarrow \text{isat}(\text{car}, y)$

$\exists x, y : \underline{\text{JohnHouse}(x), \text{Fredhouse}(y)} : \text{isat}(c$

$[\text{isat}(\cancel{\text{car}}, x) \vee \text{isat}(\text{car}, y)] \rightarrow \perp$

$\text{isat}(\text{car}, x) \rightarrow \text{isat}(\text{car}, y)$

Bill does not take Analysis

$\neg \text{take}(\text{Bill}, \text{Analysis})$

No student loves Bill

$\neg \exists x (\text{student}(x) \rightarrow \text{loves}(\text{Bill}, x, \text{Bill}))$

If Bill has at least one sister

$\exists x \text{sister}(x) : \text{sisterof}(x, \text{Bill})$

Bill has no sisters

~~PI~~  
 $\neg \exists x : \text{sister}(x) : \text{sisterof}(x, \text{Bill})$

Bill has at most one sister

\*  $\exists x : \text{Bill sister}(x) :$

$\forall (x) : \text{Bill has at most one sister}$

$\forall (x), \forall (y) : (\text{sisterof}(x, \text{Bill}) \wedge \text{sisterof}(y, \text{Bill}) \Rightarrow x = y)$

Bill has exactly one sister

$\forall x \exists x (\text{sisterof}(x, \text{Bill}) \wedge \forall y (\text{sisterof}(y, \text{Bill}) \Rightarrow x = y))$

if winter

if

## ARTIFICIAL INTELLIGENCE (AI) ASSIGNMENT

Q1) outline the important milestone for the evolution time line of artificial intelligence . What are the latest introduction into the domain of AI ?

A1) MILESTONES IN AI EVOLUTION

1. 1950s - 1960s : Birth of AI - Alan Turing proposed the Turing Test (1950), First AI programs developed (eg: Logic Theorist 1956).
2. 1980s - 90s : rise of expert systems, introduction of neural networks and advancements in machine learning .
3. 2000s - 2010s : Deep learning revolution with algorithms like CNNs and RNNs, rise of AI powered applications (Siri, Google Assistant), AlphaGo defeating human players.
4. 2020s - Present : Generative AI breakthrough (ChatGPT, DALL-E), advancements in AGI research, AI ethics and regulations gaining importance.

LATEST AI Advancement

## - 2024 Highlights

- open AI's sora : AI powered video generation.
- Google's Gemini 1.5: Advanced multimodel AI model.
- xAI's GROK : Elon Musk's AI chatbot

## - Emerging trends

- Multimodel AI (text, image, video integration), AI driven agents, self improving models, advancement in robotics and automation.

Q2) Your AI agent is provided with 2 water jugs  
Q2) of capacity 6L and 8L respectively. Design the  
steps for your agent so that it can successfully  
fill another jug with 4L of water.

→ Given

Jug A: 6L capacity

Jug B: 8L capacity

Goal: measure exactly 4L of water

Rules for AI agent

1. Fill jug A completely:

$$(x, y) \rightarrow (6, y) \text{ if } x < 6$$

2. Fill jug B completely

$$(x, y) \rightarrow (x, 8) \text{ if } y < 8$$

3. Empty the 6L jug on ground:

$$(x, y) \rightarrow (0, y) \text{ if } x > 0$$

4. Empty the 8L jug on ground

$$(x, y) \rightarrow (x, 0) \text{ if } y > 0$$

5. Pour from jug B to jug A until it is full.

$$(x, y) \rightarrow (6, y - (6 - x)) \text{ if } x + y \geq 6 \text{ and } y > 0$$

6. Pour water from jug A to jug B until it is full.

$$(x, y) \rightarrow (x - (8 - y), 8) \text{ if } x + y \geq 8, x > 0$$

7. Pour all water from jug A to jug B

$$(x, y) \rightarrow (0, x + y) \text{ if } x + y \leq 8 \text{ and } x > 0$$

8. Pour all water from jug B to jug A.

$$(x, y) \rightarrow (x + y, 0) \text{ if } x + y \leq 6 \text{ and } y > 0$$

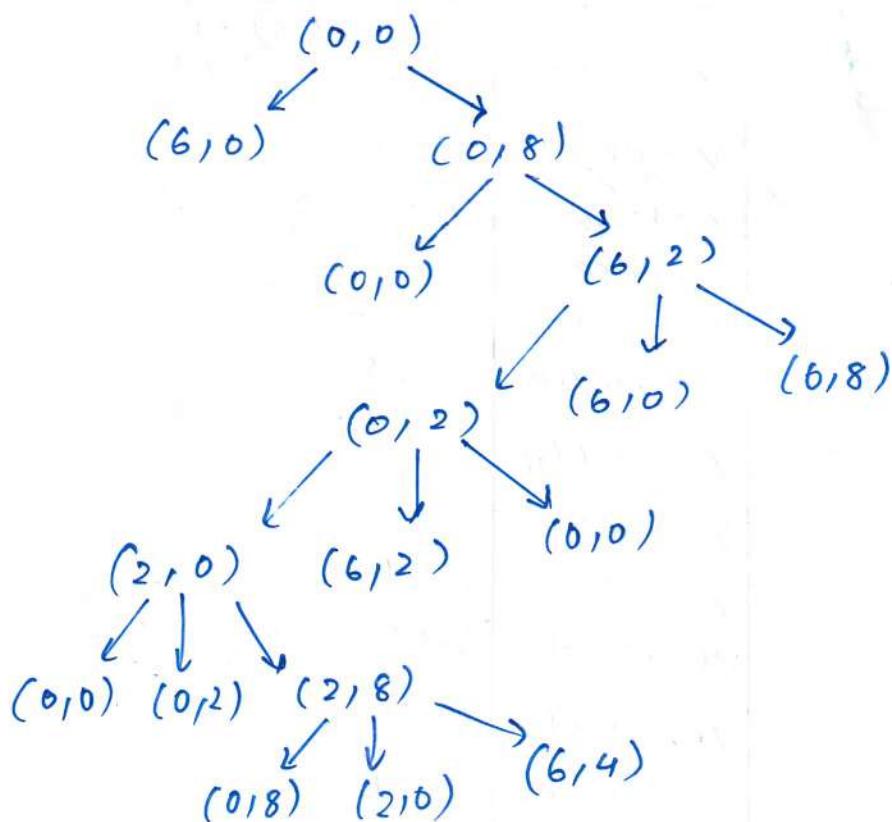
9. If jug B has 4L stop

Goal state:  $(x, 4)$  where  $0 \leq x \leq 6$

roduction for this problem!

| Jug A (6L)          | Jug B (8L) | Rule Applied |
|---------------------|------------|--------------|
| 0                   | 0          |              |
| 0                   | 8          | 2            |
| 6                   | 2          | 5            |
| 0                   | 2          | 3            |
| 2                   | 0          | 8            |
| 2                   | 8          | 2            |
| 6                   | 4          | 5            |
| Goal state Achieved |            |              |

Solution Tree:-



c) determine which species does a flower with sepal length, 5.2, sepal width 3.1 using KNN algorithm. Assume  $K=3$

$$d = \sqrt{(5.3 - 5.2)^2 + (3.7 - 3.1)^2}$$

$$d = \sqrt{(0.1)^2 + (0.36)^2} = 0$$

$$d = \sqrt{0.0001 + 0.1296}$$

$$d = \sqrt{0.1297} =$$

| sepal length | sepal width |
|--------------|-------------|
| 5.2          | 3.1         |

| sepal length | sepal width | species    | Euclidian distance                            |
|--------------|-------------|------------|---|
| 5.3          | 3.7         | setosa     | $\sqrt{(5.2 - 5.3)^2 + (3.7 - 3.1)^2} = 0.61$ |
| 5.1          | 3.8         | setosa     | 0.71  |
| 7.2          | 3.0         | virginica  | 2.00  |
| 5.4          | 3.4         | setosa     | <del>3.00</del> 0.36                          |
| 5.1          | 3.3         | setosa     | 0.22  |
| 5.4          | 3.9         | setosa     | 0.82  |
| 7.4          | 2.8         | virginica  | 2.25  |
| 6.1          | 2.8         | versicolor | 0.45  |
| 7.3          | 2.9         | virginica  | 2.11  |
| 6.0          | 2.7         | versicolor | 0.89  |
| 5.8          | 2.8         | virginica  | 0.67  |
| 6.3          | 2.9         | versicolor | 1.41  |
| 5.1          | 2.5         | versicolor | 0.61  |
| 6.3          | 2.5         | versicolor | 1.28  |
| 5.5          | 2.4         | versicolor | 0.74  |

$(5.1, 3.3)$  — setosa — 0.22

$(5.4, 3.4)$  — setosa — 0.36

$(5.3, 3.7)$  — setosa — 0.61

All 3 nearest neighbors are setosa.

Given below are the initial and final states of an 8 puzzle problem. Find the path and path cost to obtain the solution for this.

$$g(n) = \text{Depth of node}$$

$$\text{and } h(n) = \text{Number of misplaced tiles.}$$

$$f(n) = g(n) + h(n)$$

|   |   |   |
|---|---|---|
| 5 | 1 | 3 |
| 2 |   | 4 |
| 7 | 6 | 8 |

Initial state

|   |   |   |
|---|---|---|
| 4 | 1 | 3 |
| 5 | - | 2 |
| 7 | 6 | 8 |

Final state

$$g(n)$$

$$f(n) = g(n) + h(n)$$

|     |   |     |
|-----|---|-----|
| (5) | 1 | 3   |
| (2) | - | (4) |
| 7   | 6 | 8   |

$$g=0 \quad h=3 \quad f=3$$

INITIAL STATE

|   |   |   |
|---|---|---|
| 5 | 1 | 3 |
| - | 2 | 4 |
| 7 | 6 | 8 |

$$g=1 \quad h=3 \quad f=4$$

|   |   |   |
|---|---|---|
| 5 | 1 | 3 |
| 2 | 4 | - |
| 7 | 6 | 8 |

$$g=1, \quad h=3 \quad f=4$$

|   |   |   |
|---|---|---|
| 5 | - | 3 |
| 2 | 1 | 4 |
| 7 | 6 | 8 |

$$g=1 \quad h=4 \quad f=5$$

|   |   |   |
|---|---|---|
| 5 | 1 | - |
| 2 | 4 | 3 |
| 7 | 6 | 8 |

$$g=2, \quad h=4 \quad f=6$$

|   |   |   |
|---|---|---|
| 5 | - | 1 |
| 2 | 4 | 3 |
| 7 | 6 | 8 |

$$g=3, \quad h=5 \quad f=8$$

|   |   |   |
|---|---|---|
| 5 | 4 | 1 |
| 2 | - | 3 |
| 7 | 6 | 8 |

$$g=4, \quad h=5 \quad f=9$$

|   |   |   |
|---|---|---|
| 4 | 1 | - |
| 5 | 2 | 3 |
| 7 | 6 | 8 |

$$g=8, \quad h=2 \quad f=10$$

|   |   |   |
|---|---|---|
| 4 | - | 1 |
| 5 | 2 | 3 |
| 7 | 6 | 8 |

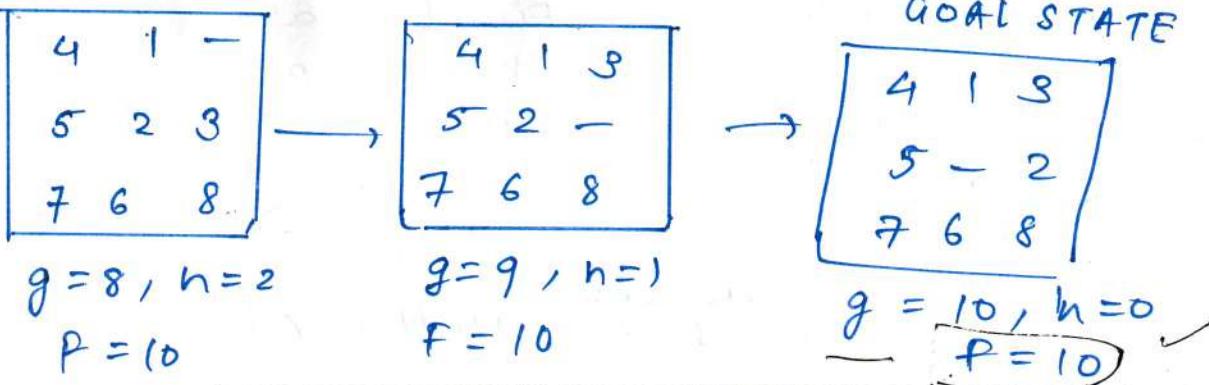
$$g=7, \quad h=3 \quad f=10$$

|   |   |   |
|---|---|---|
| - | 4 | 1 |
| 5 | 2 | 3 |
| 7 | 6 | 8 |

$$g=6, \quad h=4 \quad f=10$$

|   |   |   |
|---|---|---|
| 5 | 4 | 1 |
| - | 2 | 3 |
| 7 | 6 | 8 |

$$g=5, \quad h=5 \quad f=10$$



Final path cost = 10 [Ans]

Q4) Justify the need for conversion to ~~clauses~~ clausal from in KR. convert the following expression into ~~clauses~~ clauses from along with details step

$$\exists x \forall y \forall v (\exists v P(f(x), v) \iff Q(g(y, v) \wedge R(x, v)))$$

A4) In KR (Knowledge representation), it is often necessary to convert logical expression into clausal form, because:

1. standardization.
2. Resolution based Reasoning
3. Eliminating ambiguity
4. Efficiency in computation.
5. Simplifies logical processing.

Given expression:-

$$\begin{aligned} \exists x \forall y \forall v (\exists v P(f(x), v) \iff Q(g(y, v) \wedge R(x, v))) \\ Q(g(y, v)) \iff R(x, v) \end{aligned}$$

Step 1:- Eliminate Biconditional

$$\begin{aligned} \exists x \forall y \forall v (\exists v P(f(x), v) \longrightarrow (Q(g(y, v)) \wedge R(x, v))) \wedge \\ Q(g(y, v)) \wedge R(x, v) \longrightarrow \exists v P(f(x, v)) \end{aligned}$$

Step 2 : Eliminate implications:

$$\exists x \forall y \forall v (\neg \exists u P(f(x), v) \vee (Q(g(y, u)) \wedge R(x, v)) \wedge \\ (\neg (Q(g(y, u)) \wedge R(x, v)) \vee \exists u P(f(x), v)))$$

Step 3 :- move quantifiers outward.

$$\exists x \forall y \forall u \forall v ((\neg (P(f(x), v) \vee Q(g(y, u))) \wedge \neg P(f(x), v) \\ \vee R(x, v)) \wedge (\neg Q(g(y, u)) \vee \neg R(x, v) \vee P(f(x), v)))$$

Step 4 : Distribute quantifiers

$$\exists x \forall y \forall u \forall v ((\neg \neg P(f(x), v) \vee Q(g(y, u)) \wedge \neg P(f(x), v) \\ \vee R(x, v)) \wedge (\neg Q(g(y, u)) \vee \neg R(x, v) \vee P(f(x), v)))$$

Step 5 : Skolemization

$$\forall y \forall u \forall v ((\neg \neg P(f(x), v) \vee Q(g(y, u)) \wedge \neg P(f(x), v) \\ \vee R(c, v)) \wedge (\neg Q(g(y, u)) \vee \neg R(c, v) \vee \\ P(f(c), v)))$$

Step 6 : Distribute conjunction over disjunctions

$$\forall y \forall u \forall v (\neg \neg P(f(c), v) \vee Q(g(y, u))) \wedge \forall y \forall u \forall v \\ (\neg \neg P(f(c), v) \vee R(c, v)) \wedge \forall y \forall u \forall v (\neg Q(g(y, u)) \\ \vee \neg R(c, v) \vee P(f(c), v))$$

Step 7 : convert to clausal form

$$1. \neg \neg P(f(c), v) \vee Q(g(y, u))$$

$$2. \neg \neg P(f(c), v) \vee R(c, v)$$

$$3. \neg Q(g(y, u)) \vee \neg R(c, v) \vee P(f(c), v)$$

$\forall x, y \text{ Add}(x, y) \rightarrow$  greater than  $(x, 0)$

For Every  $x$  and  $y$ , Add  $x$  if  $x+y > 0$  then  
 $x$  is greater than  $0$  | add  $x+y$

$(\neg A \vee \neg B \vee C) \wedge (\neg A \vee B \vee \neg C)$

Step 1 Eliminate biconditionals and implications

Eliminate  $\rightarrow$  replacing  $\alpha \rightarrow \beta$  with  $\neg \alpha \vee \beta$ .

Eliminate  $\leftrightarrow$  replacing  $\alpha \leftrightarrow \beta$  with  $(\alpha \rightarrow \beta) \wedge (\beta \rightarrow \alpha)$

$$\neg(\forall x, p) \equiv \exists x \neg p$$

$$\neg(\exists x, p) \equiv \forall x \neg p$$

$$\neg(\alpha \vee \beta) \equiv \neg \alpha \wedge \neg \beta$$

$$\neg(\alpha \wedge \beta) \equiv \neg \alpha \vee \neg \beta$$

$$\neg \neg \alpha \equiv \alpha$$

Step 2 Skolemization

$$\forall x \text{ person}(x) \Rightarrow \exists y \text{ Heart}(y) \wedge \text{Has}(x, y)$$

$$\forall x \text{ person}(x) \Rightarrow \text{Heart}(\text{H}(x)) \wedge \text{Has}(x, \text{H}(x))$$

$\text{H} \rightarrow$  skolem fn

$\forall x \text{ person}(x)$  becomes  $\text{person}_b(x)$

$$(\alpha \wedge \beta) \vee \gamma \equiv (\alpha \vee \gamma) \wedge (\beta \vee \gamma)$$