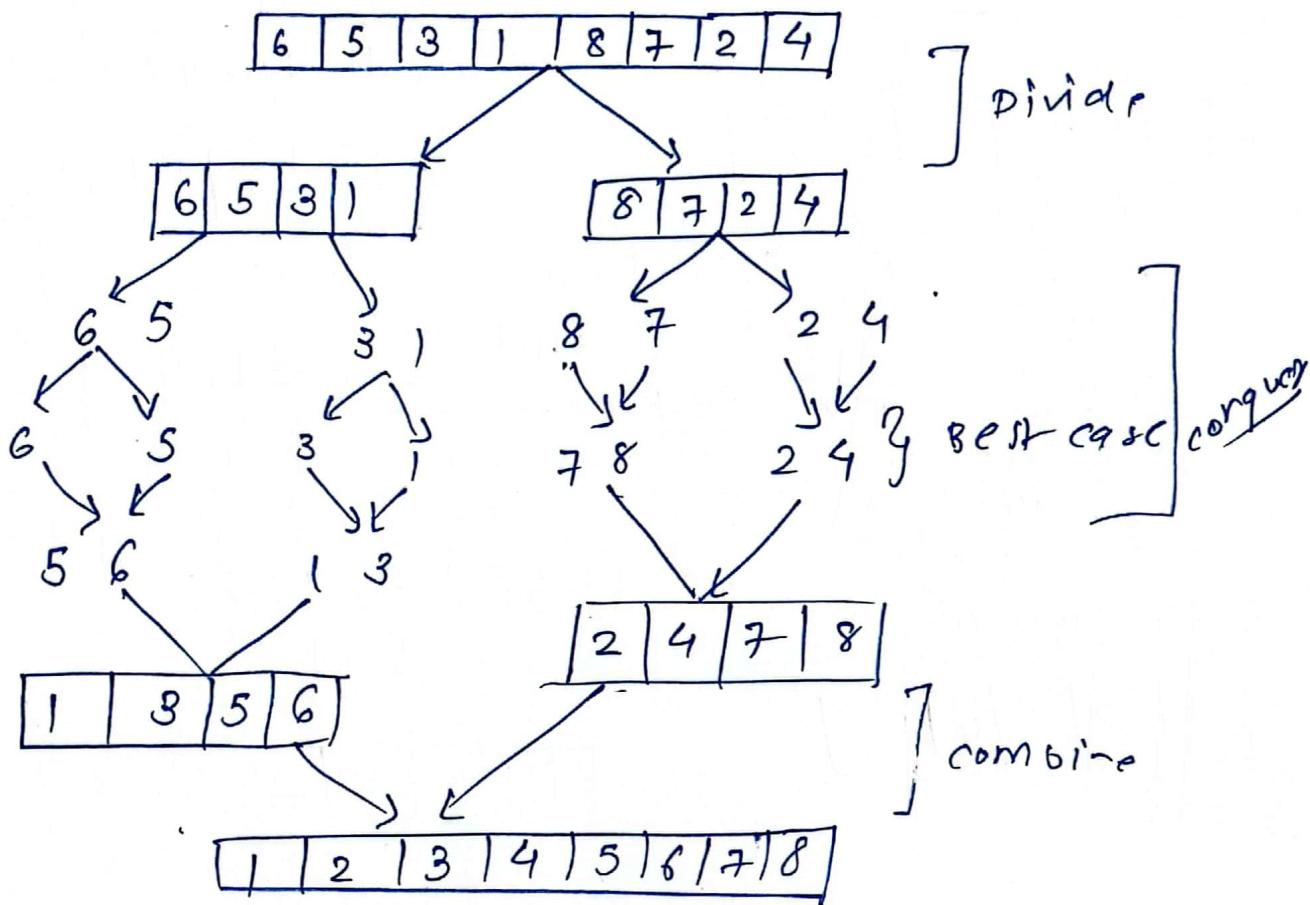
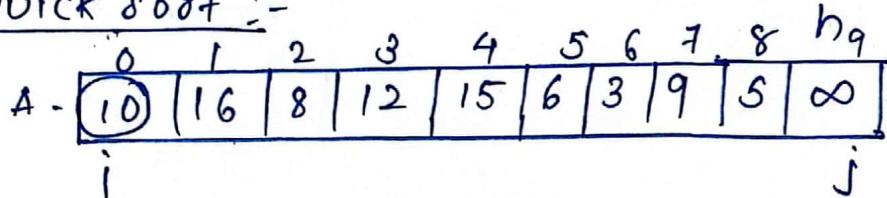


## Divide and conquer:

### Merge sort



### Quick sort :-



$i >$   
 $i > 10$   
 $j < 10$

$(10), 16, 8, 12, 15, 6, 3, 9, 5, \infty \dots$

$10, 5, 8, 12, 15, 6, 3, 9, 16, \infty$

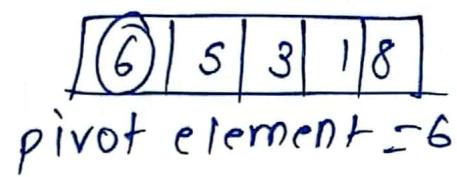
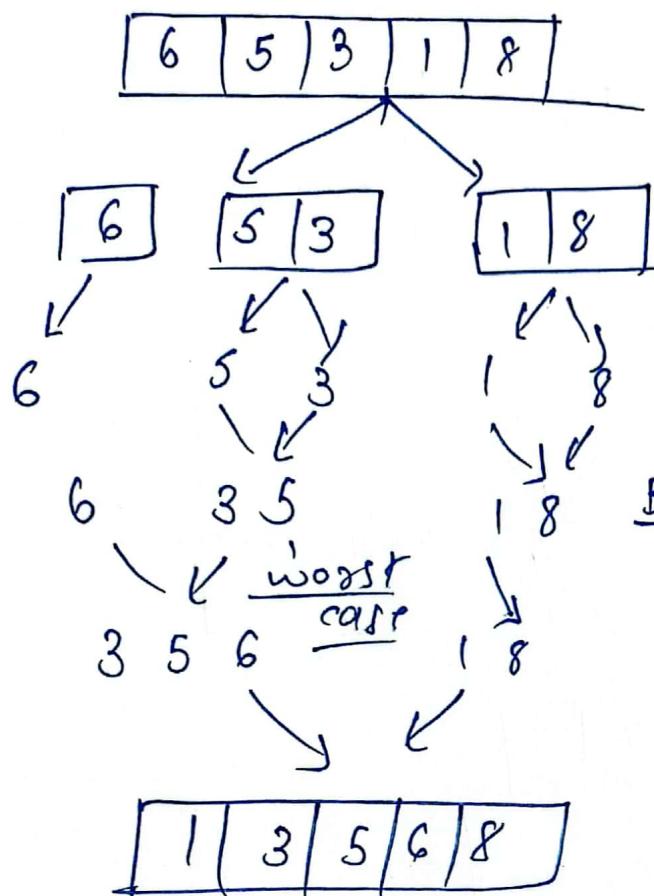
pivot > value  
of pivot

$10, 5, 8, 9, 15, 6, 3, 12, 16$

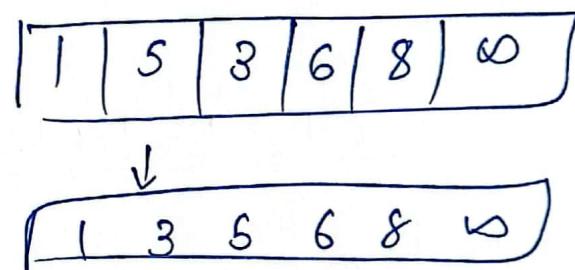
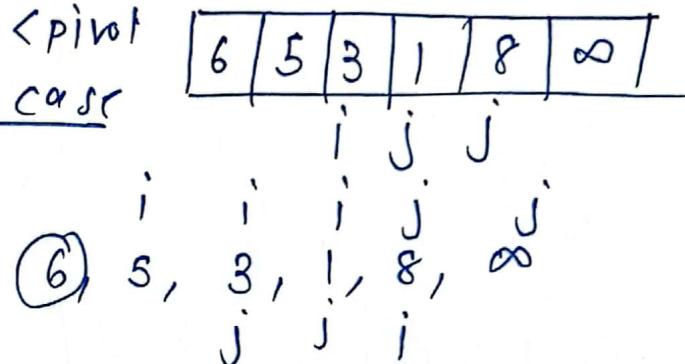
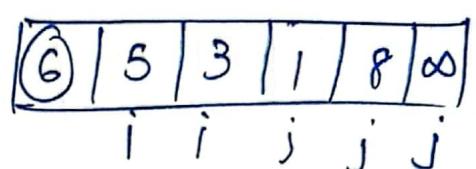
pivot < value  
of  
pivot

$10, 5, 8, 9, 3, 6, 15, 12, 16$

$A = 6 \ 5 \ 3 \ 18$       merge sort      6 pivot? > 6

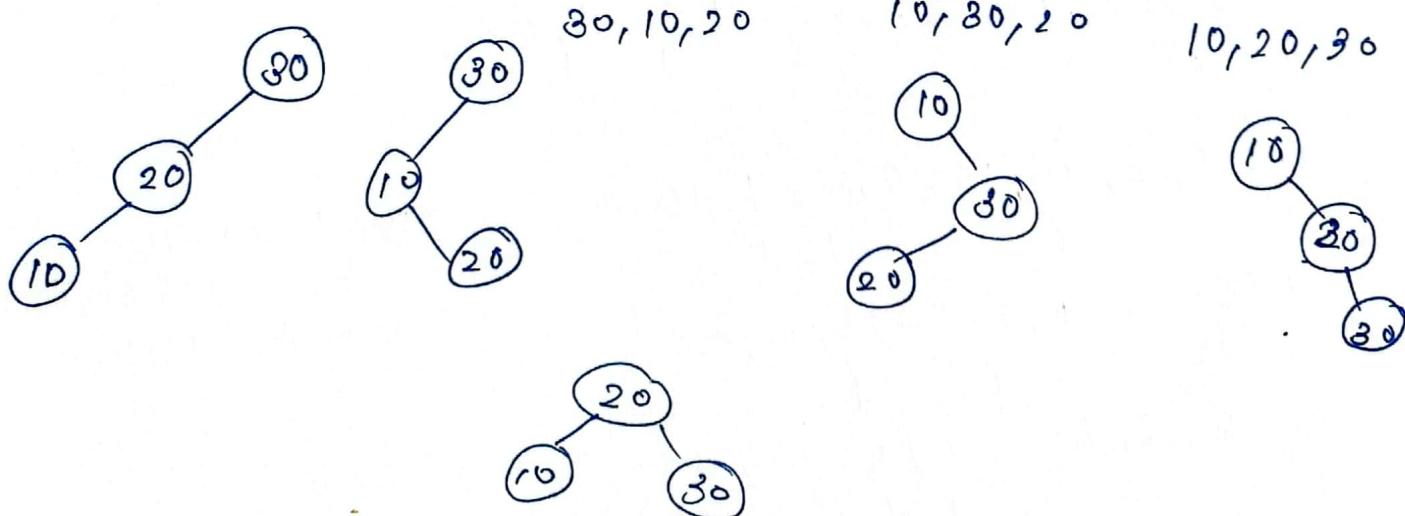


$i > \text{pivot}$   
 $j < \text{pivot}$   
Best case



### AVL Trees

Keys 80, 20, 10



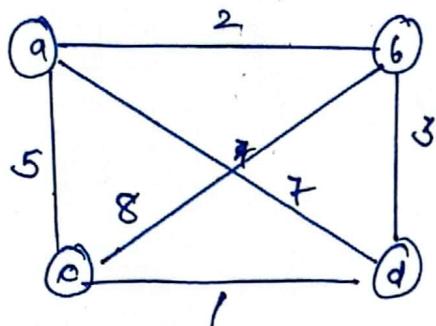
subset	Total weight	Total value	
$\emptyset$	0	0	
[1]	7	42	
[2]	3	12	
[3]	4	40	
[4]	5	25	
$[1, 2]$	10	54	✓
[1, 3]	9	11	Not feasible
[1, 4]	12	11	Not feasible
[2, 3]	5	24	52
[2, 4]	8	37	
[3, 4]	9	52	{ Not feasible }

### Assignment problem

	Job 1	Job 2	Job 3	Job 4
person 1	9	2	7	8
person 2	6	4	3	7
person 3	5	8	1	8
person 4	7	6	9	4

2

## Exhaustive-search



$a \rightarrow d \rightarrow b \rightarrow c \rightarrow a$

$$l = 7 + 3 + 8 + 5 = 23$$

$a \rightarrow d \rightarrow c \rightarrow b \rightarrow a$

$$l = 2 + 1 + 8 + 2 = 13$$

$a \rightarrow b \rightarrow e \rightarrow d \rightarrow a$

$$2 + 8 + 1 + 7 = 18$$

$a \rightarrow b \rightarrow d \rightarrow c \rightarrow a$

$$l = 2 + 3 + 1 + 5 = 11 //$$

optimal

$a \rightarrow c \rightarrow b \rightarrow d \rightarrow a$

$$l = 5 + 8 + 3 + 7 = 23$$

$a \rightarrow c \rightarrow d \rightarrow b \rightarrow a$

$$l = 5 + 1 + 3 + 2 = 11 //$$

optimal

## Knapsack problem using

Exhaustive-Search

Knapsack capacity  $w = 10$

No of items	Weight ( $w_i$ )	Profit ( $v_i$ )
item 1	7	42
item 2	8	12
item 3	4	40
item 4	5	25

$$C = \begin{bmatrix} 9 & 2 & 7 & 8 \\ 6 & 4 & 3 & 7 \\ 5 & 8 & 1 & 8 \\ 7 & 6 & 9 & 4 \end{bmatrix}$$

$$\langle 1 2 8 9 \rangle = 9 + 4 + 1 + 4 = 18$$

$$\langle 1 2 4 3 \rangle = 9 + 4 + 8 + 9 = 30$$

$$\langle 1 8 2 4 \rangle = 9 + 8 + 8 + 4 = 24$$

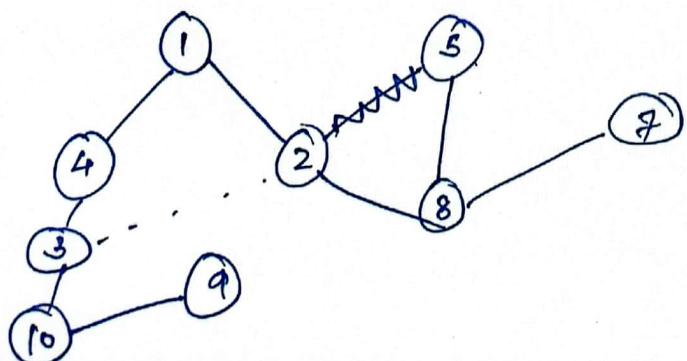
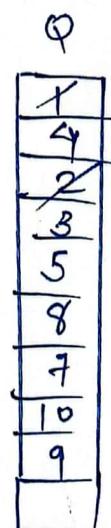
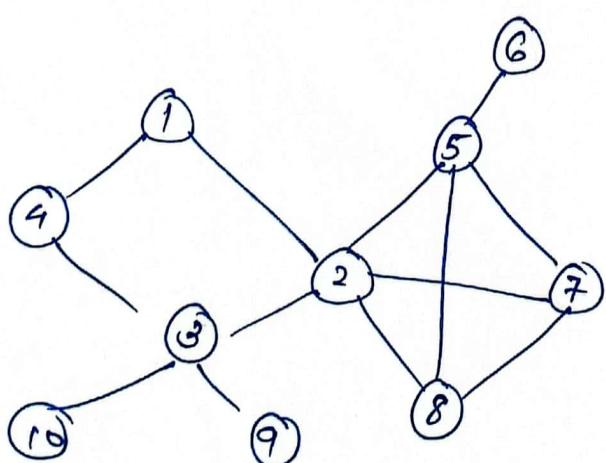
$$\langle 1 3 4 2 \rangle = 9 + 3 + 8 + 1 = 26$$

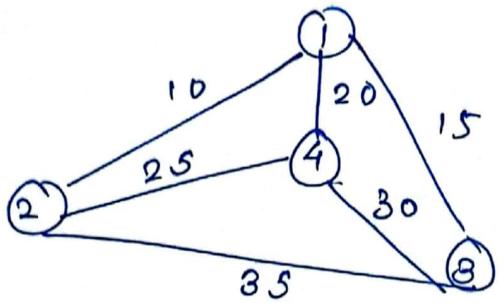
$$\langle 1 4 2 8 \rangle = 9 + 7 + 8 + 9 = 33 \text{ CTC}$$

$$\langle 1 4 3 2 \rangle = 9 + 7 + 1 + 5 = 22$$

(2^n) complexity of time

Breath First search (BFS)





travelling salesman  
problem (TSP)

$$2^4 = 16 \text{ possibl}'y$$

$$\langle 1 \ 2 \ 3 \ 4 \rangle = 10 + 35 + 30$$

$$\langle 1 \ 2 \ 4 \ 3 \rangle = 10 + 25 + 30$$

~~$$\langle 1 \ 3 \ 2 \ 4 \rangle = 15 + 35 + 25$$~~

$$\langle 1 \ 3 \ 4 \ 2 \rangle = 15 + 30 + 25$$

$$\langle 1 \ 4 \ 2 \ 3 \rangle = \langle \dots \text{etc} \dots \rangle \quad \text{find optimal} \\ \langle 1 \ 4 \ 3 \ 2 \rangle \quad 50 |$$

## 0/1 knapsack problem using Bottom up Approach

Items  $n=4$  weights  $w=5$

$$W_1, W_2, W_3, W_4 = \{2, 3, 4, 5\} \quad V_1, V_2, V_3, V_4 = \{3, 4, 5, 6\}$$

(i)	item	weight(w)	value
1		$2 + 3 = 5$	$3 + 4 = 7$
2		3	4
3		4	5
4		5	6

$$T(i, j) = \max(T(i-1, j), (\text{value})_i + T(i-1, j - (\text{weight})_i))$$

weights  $\xrightarrow{j}$

i	0	0	0	0	0	5
1	0	0	3	3	3	3
2	0	0	3	4	4	7
3	0	0	3	4	5	7
4	0	0	3	4	5	7

$$T(1, 1) = \boxed{i=1 \ j=1}$$

$$= \max(T(1-1, 1), \begin{cases} (\text{value})_1 = 3 \\ (\text{weight})_1 = 2 \end{cases})$$

$$T(1, 1) = \max \{ T(0, 1), 3 + T(0, 1-1) \}$$

$$T(1, 1) = \max \{ T(0, 1), 3 + T(0, 1-1) \}$$

$$\max \{ T(0, 1), 3 + T(0, 1-1) \}$$

Step 2 :-

$$T(1, 2) =$$

$$\boxed{i=1, j=2} \quad \begin{cases} (\text{value})_2 = 4 \\ (\text{weight})_2 = 3 \end{cases}$$

$$\max(T(1-1, 2), 4 + T(1-1, 2-1))$$

$$\max(T(1-1, 2), 4) + T(1-1, 2-1)$$

3

### Assignment problem

Jobs J1 J2 J3 J4

person

	J1	J2	J3	J4
a	9	2	7	8
b	6	4	3	7
c	5	8	1	8
d	7	6	9	4

$$L \cdot B = 2 + 3 + 1 + 4 = 10$$

Let's do by

Row-Reduction  
method!

$$L \cdot B = 2 + 3 + 1 + 4 = 10$$

$$a = 1$$

$$a = 2$$

$$a = 3$$

$$a = 4$$

$$9 + 4 + 1 + 4 \\ \hline \approx 18$$

$$2 + \\ 2 + 3 + 1 + 4 \\ \hline$$

$$7 + 3 + 1 + 1 \\ 7 + 4 + 5 + 9 \\ \hline$$

$$8 + 3 + 1 + 6 \\ L \cdot B = 18$$

$$9 + 3 + 1 + 4 \\ L \cdot B = 17$$

$$L \cdot B = 10$$

$$L \cdot B = 20$$

$$a = 2$$

$$b = 1$$

$$b = 3$$

$$b = 1$$

$$6 + 2 + 1 + 4 \\ L \cdot B = 13$$

$$3 + 2 + 5 + 4 \\ L \cdot B = 14$$

$$7 + 2 + 1 + 6 \\ L \cdot B = 17$$

$$1 + 2 + 4 \\ + 4$$

1

$$T(1, 3) = [T(i-1, j), \text{value}_i + T(i-1, j - (\text{weight})_i)]$$

$$T(1, 3) = T(0, 3), (\text{value})_1 + T(0, 3 - (\text{weight})_1)$$

$(\text{value})_1 = 3$
$(\text{weight})_1 = 2$

$$= T(0, 3), 3 + T(0, 3 - 4)$$

$$= T(0, 3), 3 + T(0, 1)$$

$$\max \{ T(0, 3), 3 + T(0, 1) \}$$

$0, 3 + 0$

$$T(1, 4) = T(i, j) \quad \begin{array}{|c|c|} \hline \text{value}_i & \text{weight}_i \\ \hline 3 & 2 \\ \hline \end{array} = 3.$$

$$T(1, 4) = T(1-1, 4), 3 + T(0, 4 - 2)$$

$$\max(T(0, 4), 3 + T(0, 2))$$

$i=1$	$j=5$
-------	-------

$0, 3 + 0$
$T(1, 4) = 3$

$$T(1, 5) = T(1-1, 5), 3 + T(0, 5 - 2)$$

$$T(0, 5), 3 + T(0, 3)$$

$$0, 3 + 0$$

$(\text{value})_2 = 4$	$(\text{weight})_2 = 3$
------------------------	-------------------------

$$T(2, 1) = T(2-1, 1) \quad \boxed{i=2 \ j=1} \quad 4 + T(2-1, 1 - 3)$$

$$T(1, 1) \quad 4 + T(1, -2)$$

$$\max \{ 0, 4 + T(1, -2) \} \quad \text{ignore}$$

$$T(2, 2) \quad [i=2, j=2]$$

$$\begin{cases} (\text{value})_2 = 4 \\ (\text{weight})_2 = 3 \end{cases}$$

$$= \max(2)$$

$$\max(2-1, 2) + 4 + T(2-1, 2-1) \quad \text{ignor}$$

$$\max(1, 2), 4 + T(1, -1)$$

$$\max(3, 4 + T(1, -1))$$

$$= 3$$

$$[i=2, j=3]$$

$$T(2, 3) = \max(2-1, 3) + 4 + T(2-1, 3-3)$$

$$4 + (1, 0)$$

$$3, 0 + 4 + 0$$

$$\max(3, 9) = 9$$

maximum weight that we can put in

$$\text{knapSack} = 7$$

## Sum of subset

$$\delta = \frac{2 \times 2 \times 2 \times 2}{(10, 20, 30, 40)} \quad (2^n)$$

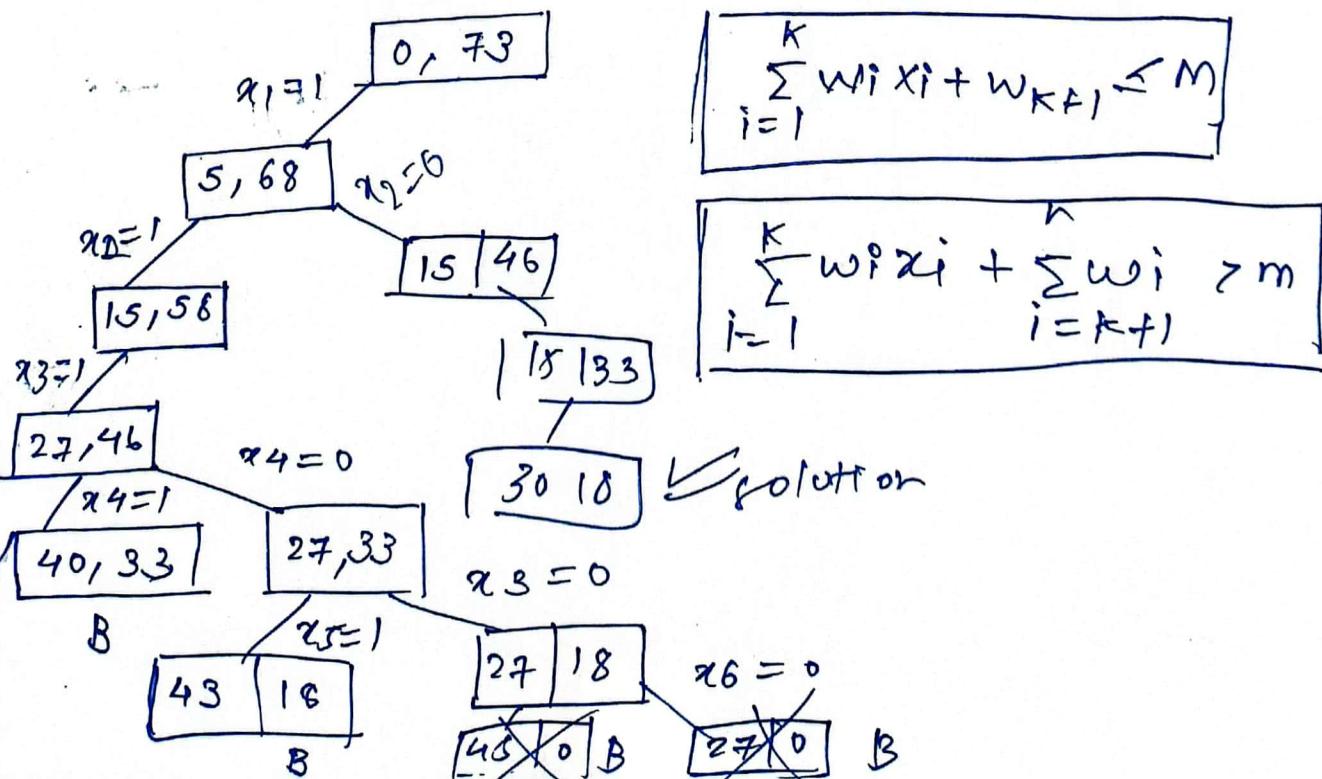
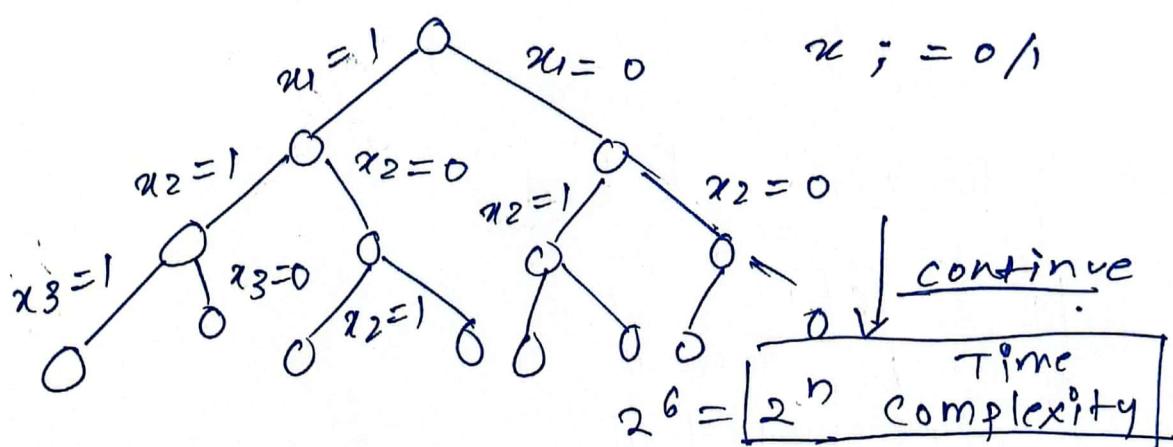
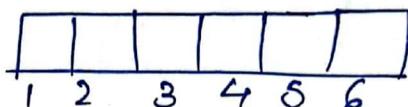
$$SOS(n, m) = \begin{cases} SOS(n-1, m) \\ \text{OR} \\ SOS(n-1, w_n) \end{cases}$$

True  $n=0, m=0$   
 false  $n=0, m \neq 0$   
 True  $n \neq 0, m=0$

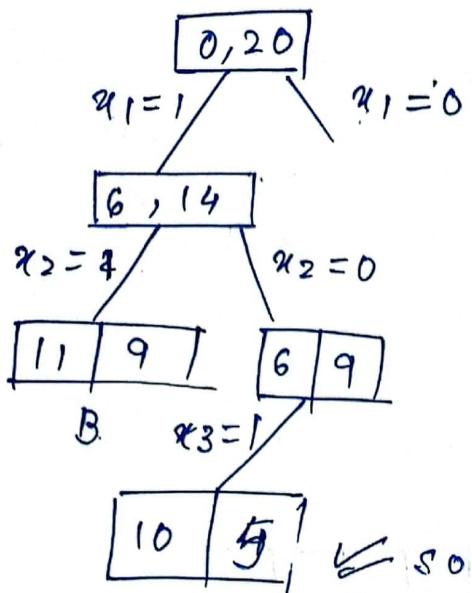
$w_m > m$

$$W[1:6] = \{5, 10, 12, 13, 15, 18\}$$

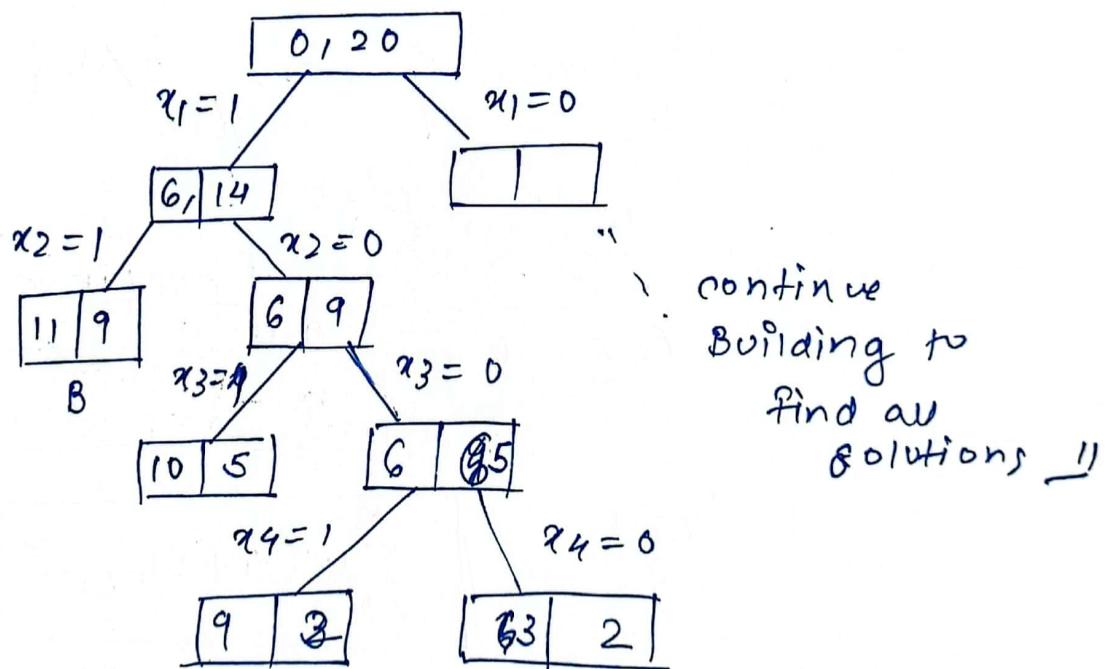
$$n=6 \quad m=30$$

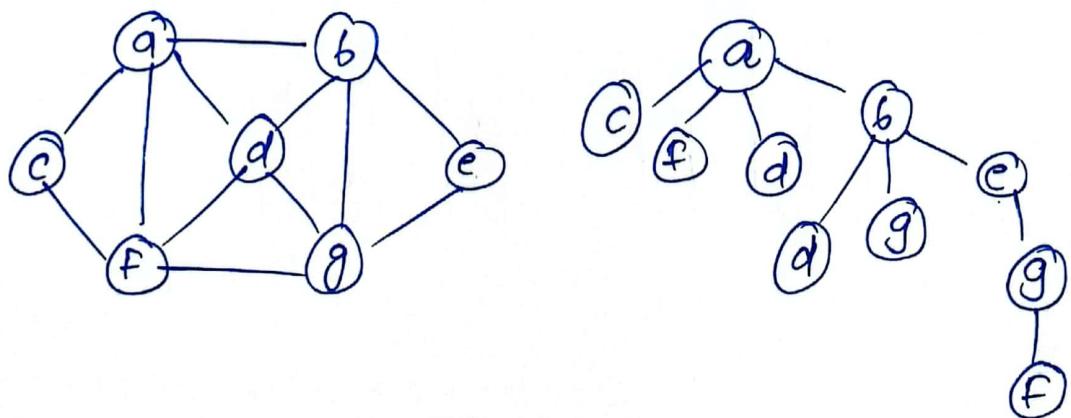
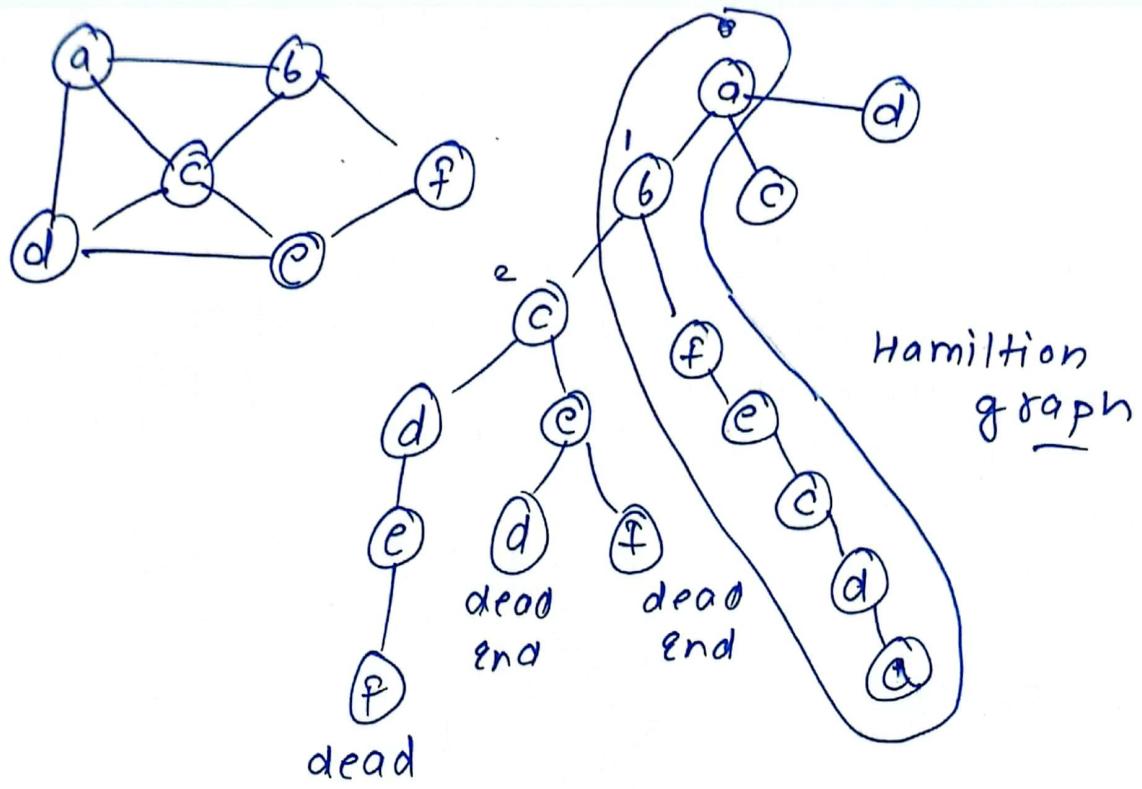


$$A = \{6, 5, 4, 3, 2\} \text{ and } d = 10$$



6	5	4	3	2
$x_1$	$x_2$	$x_3$	$x_4$	$x_5$





## Chapter 12 : coping with Limitation of Algorithm

### A. Backtracking:-

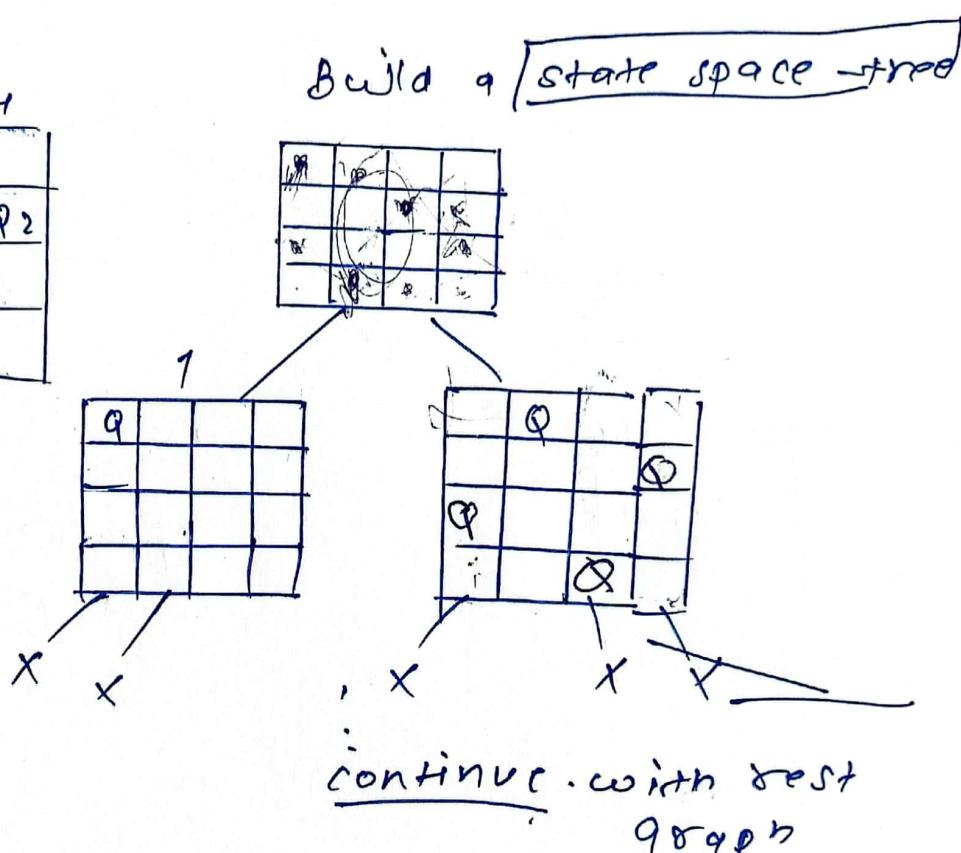
N-Queen's problem :- N queen problem is the classical example of backtracking. N-Queen problem is defined as "given  $N \times N$  chess board. N queens in such a way that NO two queens attack each other.

	1	2	3	4
1	Q1			
2				Q2
3	Q3			
4			Q4	

solution  
OR

	1	2	3	4
1		Q1		
2	Q2			
3			Q3	
4				Q4

solution



### Hamiltonian circuit

#### Hamiltonian Graph

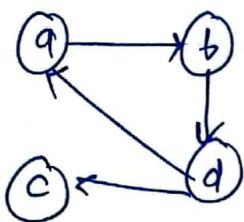
problem is about or concerned finding Hamiltonian circuit in a given graph

Hamiltonian ckt :- defined as a cycle that passes through all vertices of a graph exactly once except starting and ending vertices

## Chp 11 Dynammic programming

### Warshall's and Floyd's algorithm:-

Warshall's algorithm is used to find the transitive closure of a directed graph

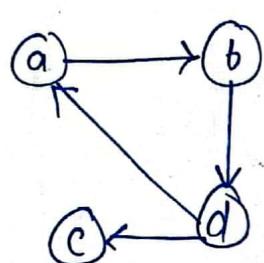


#### Transitive closure

	a	b	c	d
a	1	1	1	0
b	1	1	1	1
c	0	0	0	0
d	1	1	1	1

	a	b	c	d
a	1	1	1	1
b	1	1	1	1
c	0	0	0	0
d	1	1	1	1

#### Dynammic-programming approach



	a	b	c	d
a	0	1	0	0
b	0	0	0	1
c	0	0	0	0
d	1	0	1	0

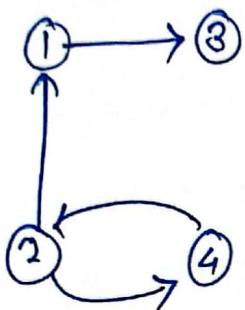
	a	b	c	d
a	0	1	0	0
b	0	0	0	1
c	0	0	0	0
d	1	1	0	0

	a	b	c	d
a	0	1	0	0
b	0	0	0	1
c	0	0	0	0
d	1	1	1	0

	a	b	c	d
a	0	1	0	1
b	0	0	0	1
c	0	0	0	0
d	1	1	1	1

	a	b	c	d
a	0	1	0	1
b	0	0	0	1
c	0	0	0	0
d	1	1	1	1

	a	b	c	d
--	---	---	---	---



$$P = \begin{bmatrix} 1 & 2 & 3 & 4 \\ 1 & 0 & 0 & 1 & 0 \\ 2 & 1 & 0 & 1 & 1 \\ 3 & 0 & 0 & 0 & 0 \\ 4 & 1 & 1 & 1 & 1 \end{bmatrix} = \begin{bmatrix} 0 & 0 & 1 & 0 \\ 1 & 1 & 1 & 1 \\ 0 & 0 & 0 & 0 \\ 1 & 1 & 1 & 1 \end{bmatrix}$$

### Warshall's Algorithm

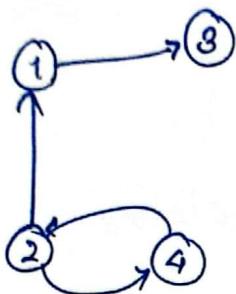
$$P = \begin{bmatrix} 1 & 2 & 3 & 4 \\ 1 & 0 & 0 & 1 & 0 \\ 2 & 1 & 0 & 0 & 1 \\ 3 & 0 & 0 & 0 & 0 \\ 4 & 0 & 1 & 0 & 0 \end{bmatrix}$$

$$R(P) = \begin{bmatrix} 0 & 0 & 1 & 0 \\ 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 1 \\ 0 & 1 & 0 & 1 \end{bmatrix}$$

$$R(1) = \begin{bmatrix} 0 & 0 & 0 & 1 \\ 1 & 0 & 1 & 0 \\ 1 & 1 & 1 & 0 \\ 1 & 1 & 1 & 0 \end{bmatrix}$$

$$R(3) = \begin{bmatrix} 1 & 1 & 1 & 0 \\ 1 & 1 & 1 & 0 \\ 1 & 1 & 1 & 0 \\ 1 & 1 & 1 & 0 \end{bmatrix}$$

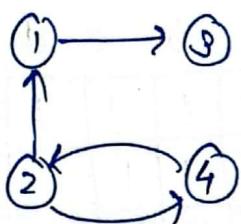
$$R(4) = \begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & & \\ & & & \end{bmatrix}$$



	1	2	3	4
1	0	0	1	0
2	1	1	1	1
3	0	0	0	0
4	1	1	1	1

← Required  
Transitive  
matrix

Apply Warshall's Algorithm



construct  
Adjacency  
matrix

$$\begin{matrix} & \begin{matrix} 1 & 2 & 3 & 4 \end{matrix} \\ \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \end{matrix} & \begin{bmatrix} 0 & 0 & 1 & 0 \\ 1 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix} \end{matrix}$$

$$R(0) = \begin{bmatrix} 0 & 0 & 1 & 0 \\ 1 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix} \Rightarrow \begin{bmatrix} 0 & 0 & 1 & 0 \\ 1 & 0 & 1 & 1 \\ 0 & 1 & 0 & 1 \\ 0 & 1 & 0 & 1 \end{bmatrix}$$

$$R(1) = \begin{bmatrix} 0 & 0 & 1 & 0 \\ 1 & 0 & 1 & 1 \\ 0 & 1 & 0 & 1 \\ 0 & 1 & 0 & 1 \end{bmatrix} \Rightarrow \begin{bmatrix} 0 & 0 & 1 & 0 \\ 1 & 0 & 1 & 1 \\ 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 \end{bmatrix}$$

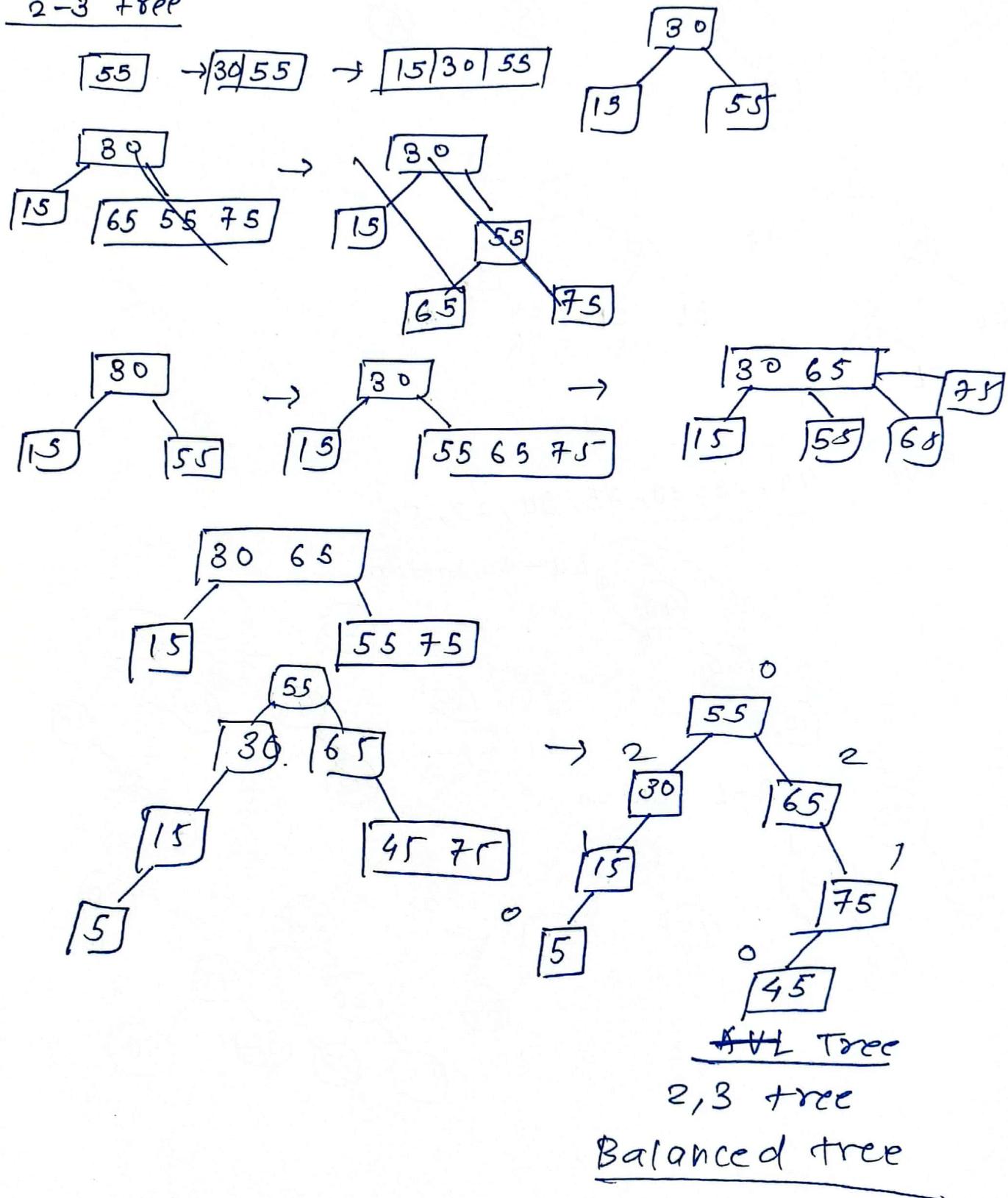
$$= \begin{bmatrix} 0 & 0 & 1 & 0 \\ 1 & 0 & 1 & 1 \\ 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 \end{bmatrix} = \begin{bmatrix} 0 & 0 & 1 & 0 \\ 1 & 0 & 1 & 1 \\ 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} \end{bmatrix}$$

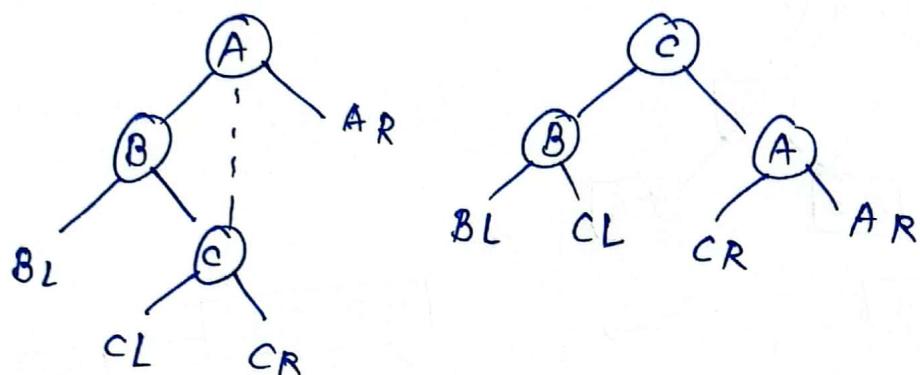
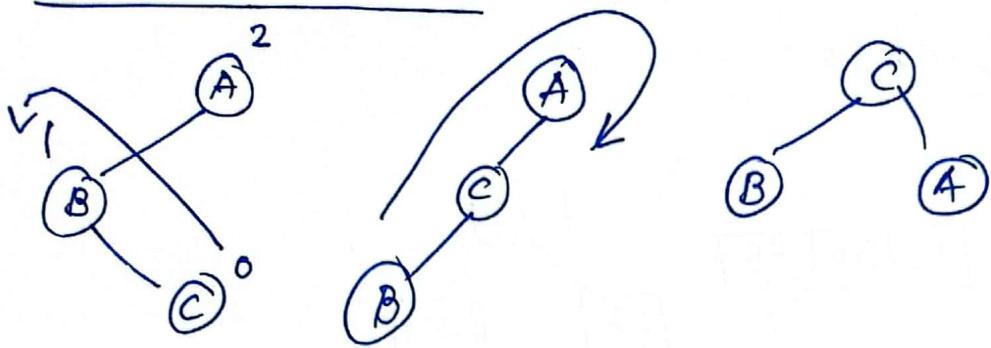
## construction of 2-3 trees

55, 80, 15, 75, 65, 45, 5

### 2-3 tree

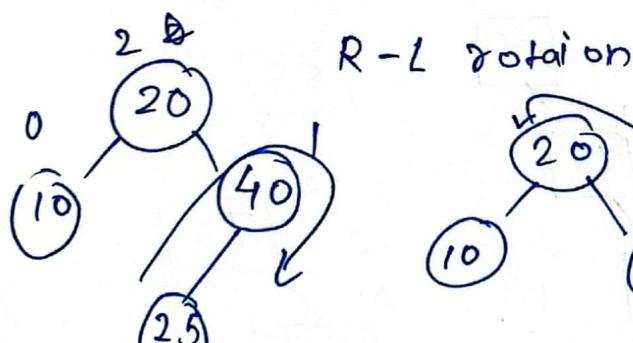
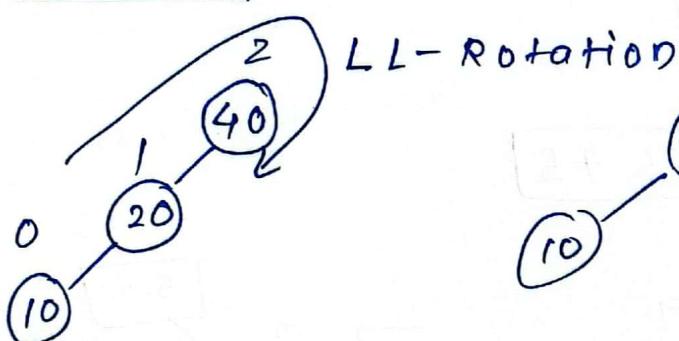


### L-R Rotations

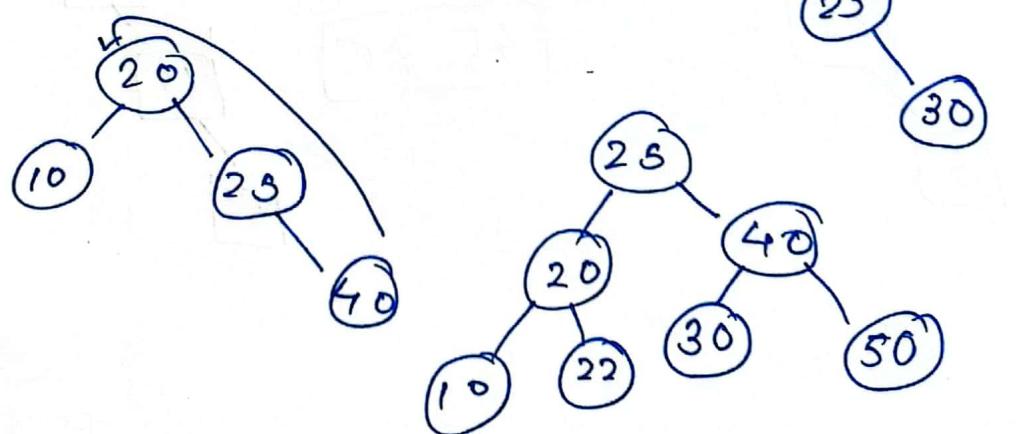


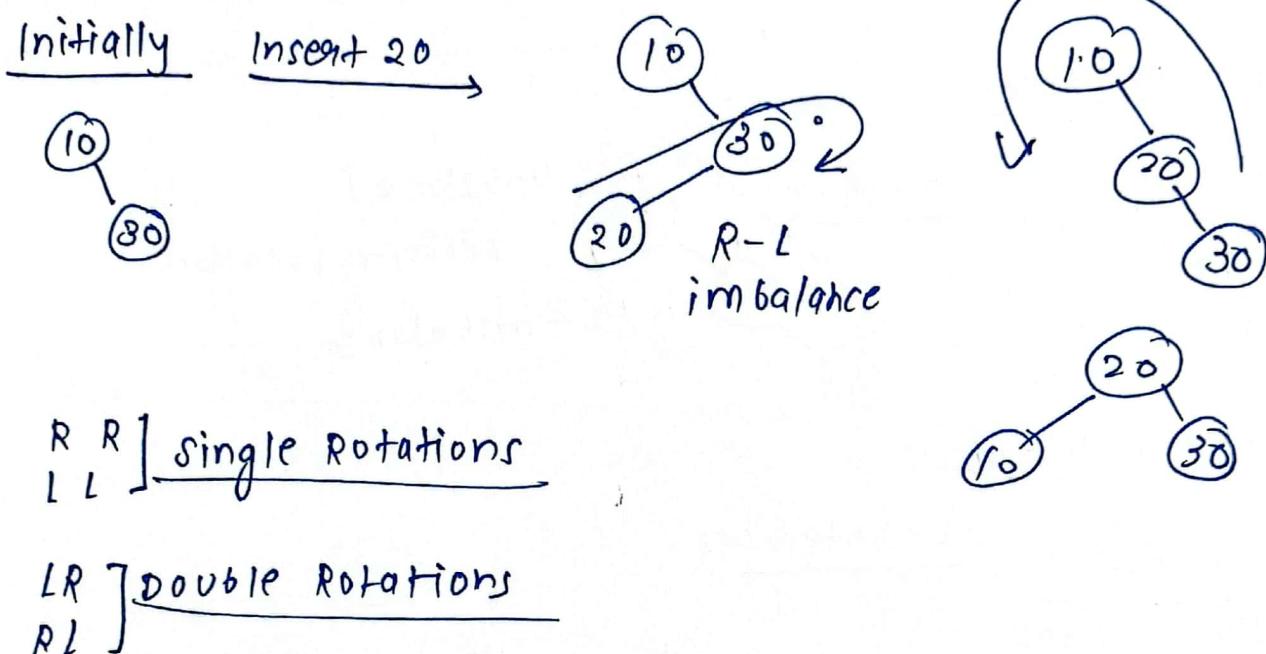
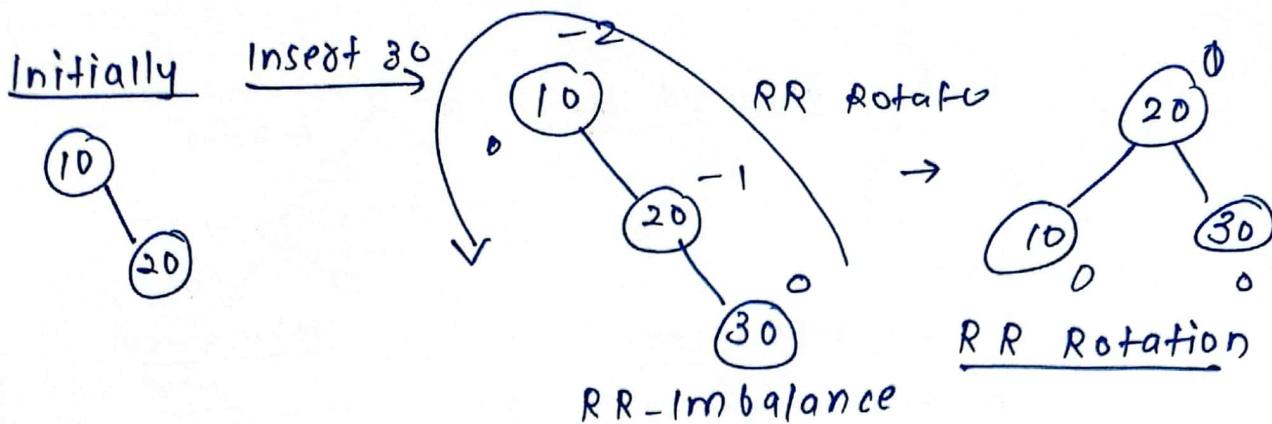
Keys      40, 20, 10, 25, 30, 22, 50

### LL - Rotation



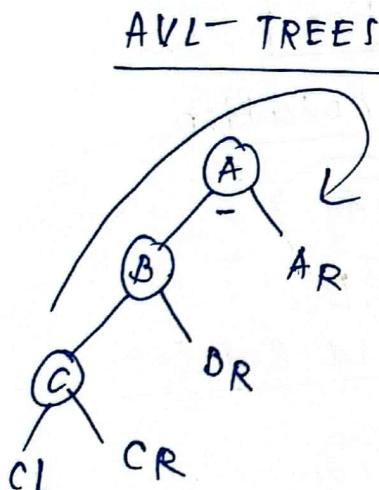
### R-L rotation



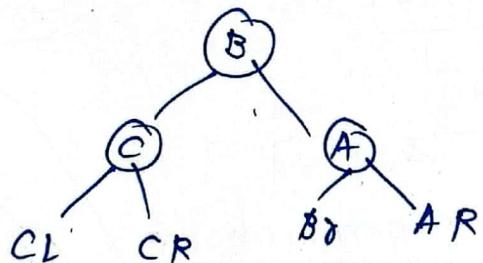


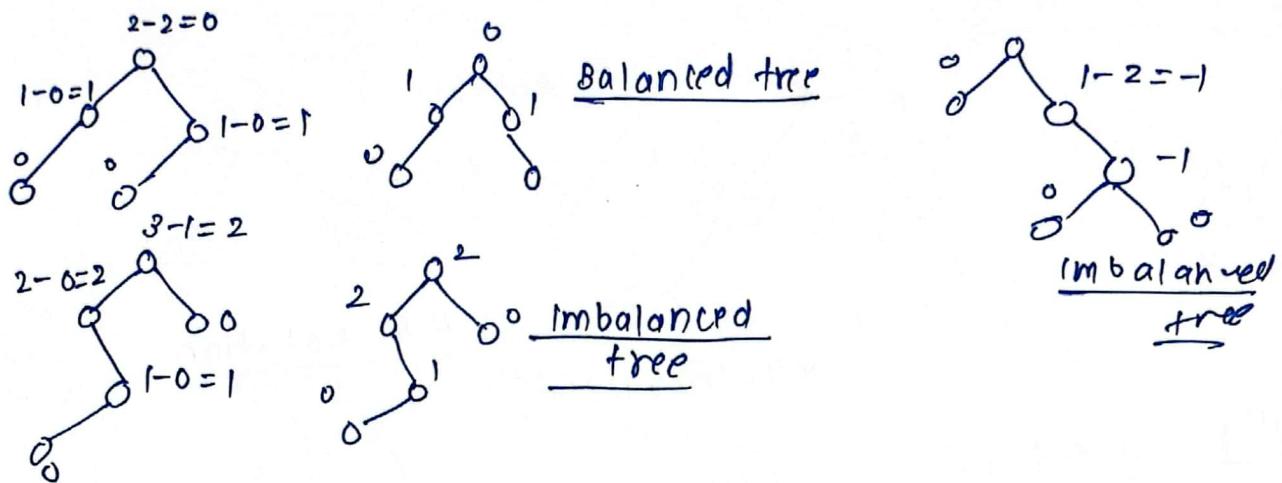
RR ] single Rotations

LR ] double Rotations  
RL ]

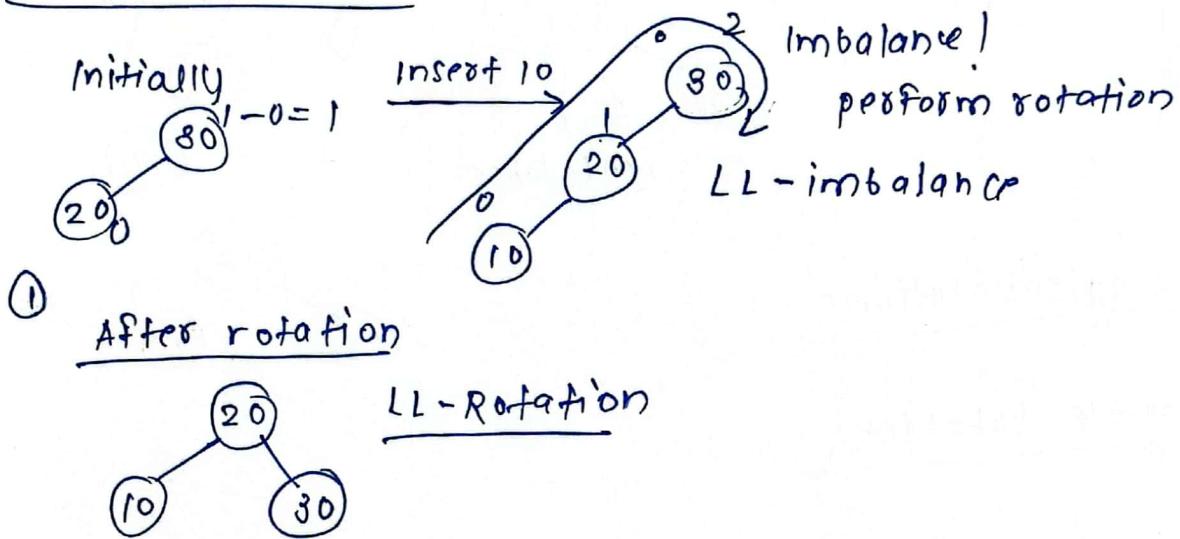


LL - Rotation Formula

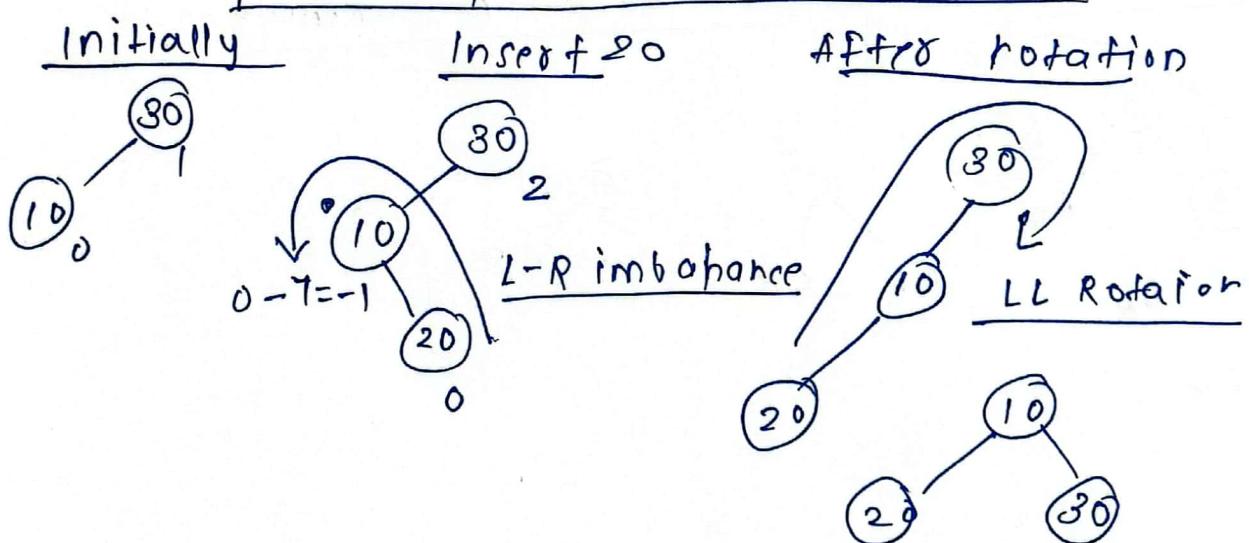




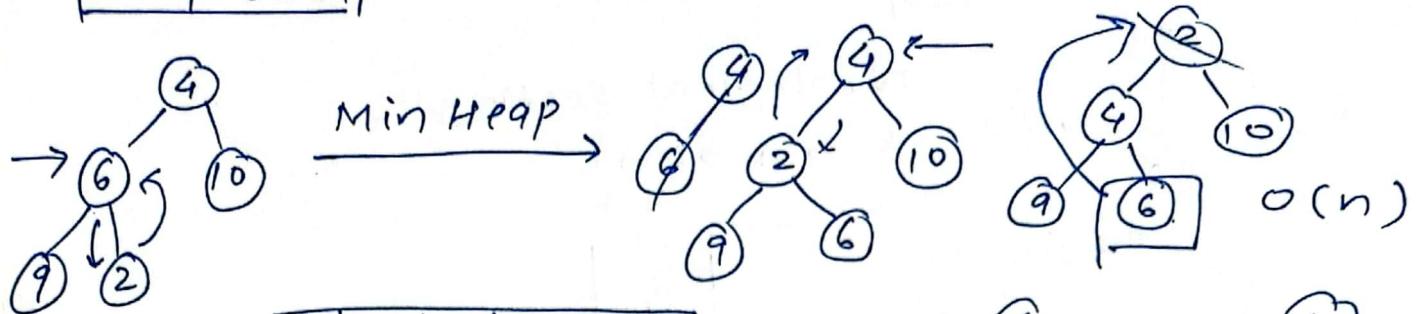
### Rotation of trees



### two-step rotations - LR Rotation



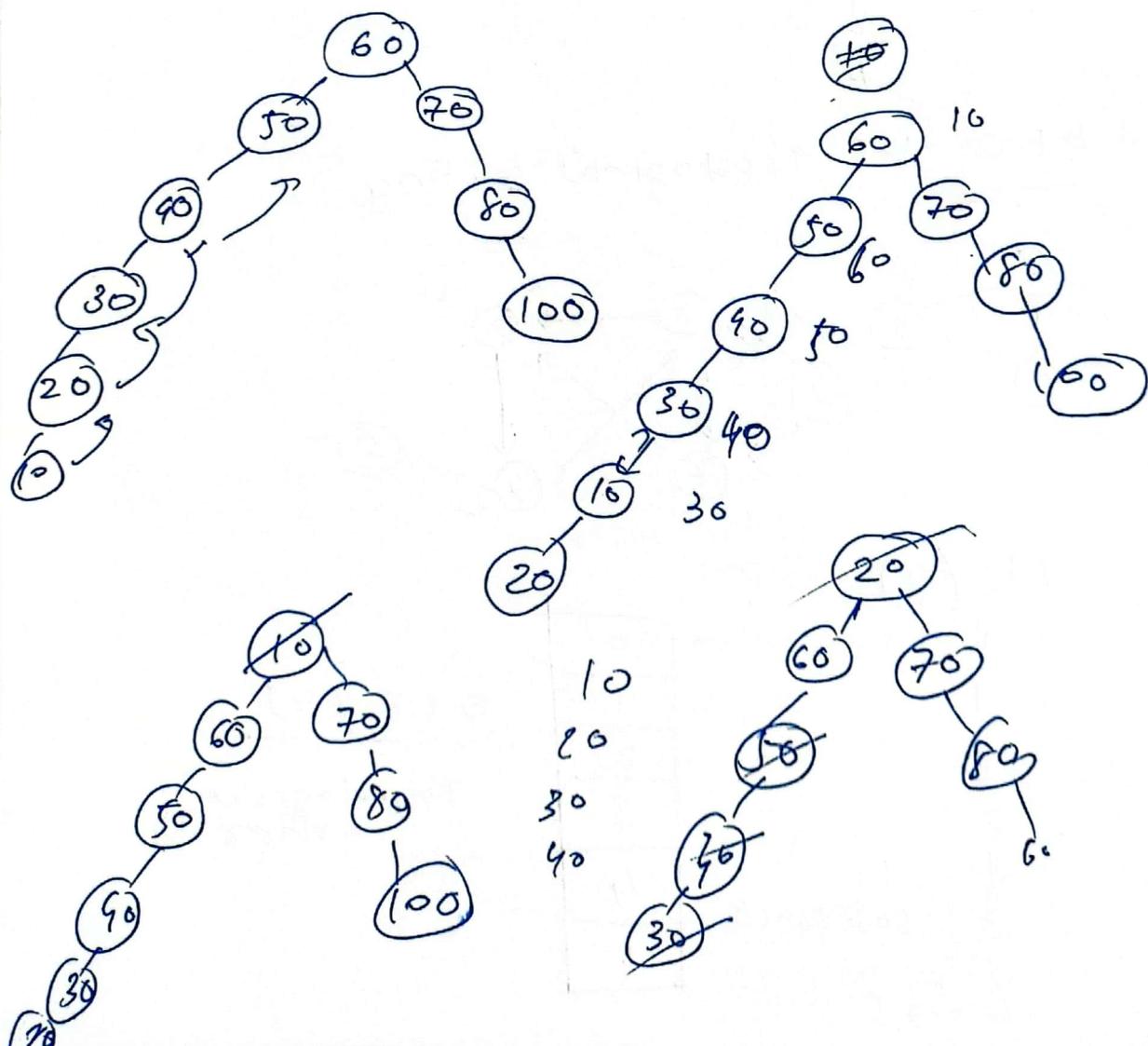
## Heap sort



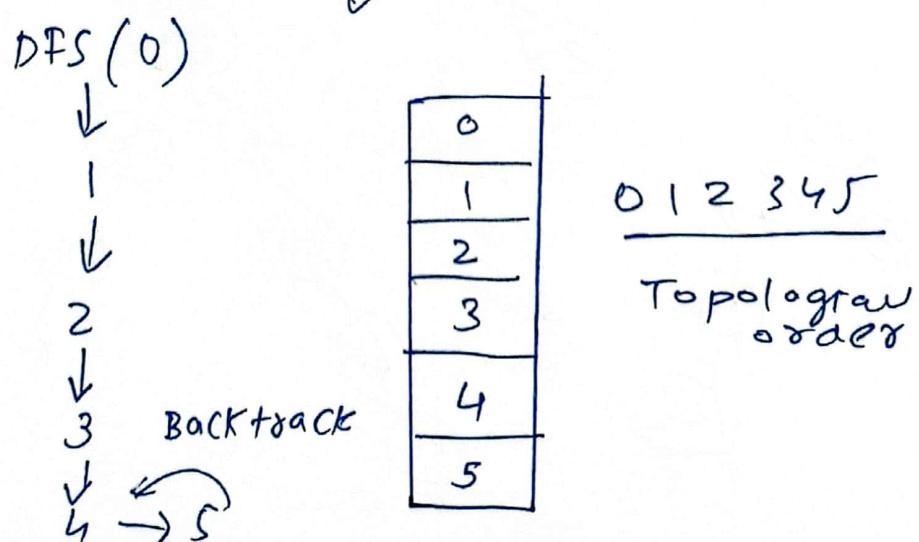
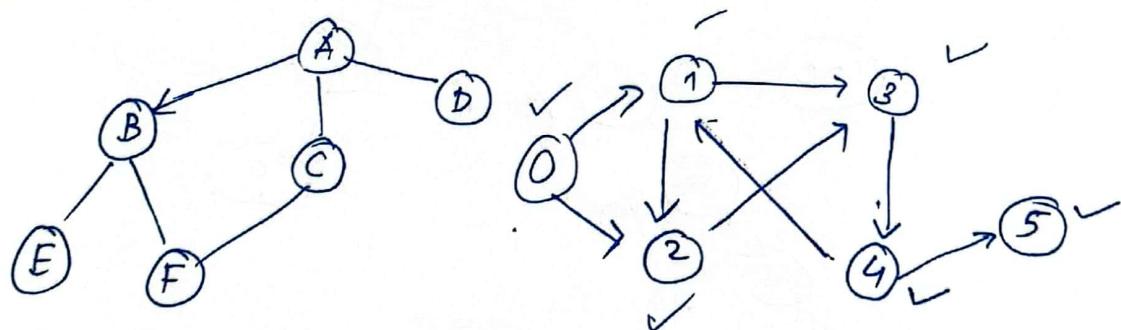
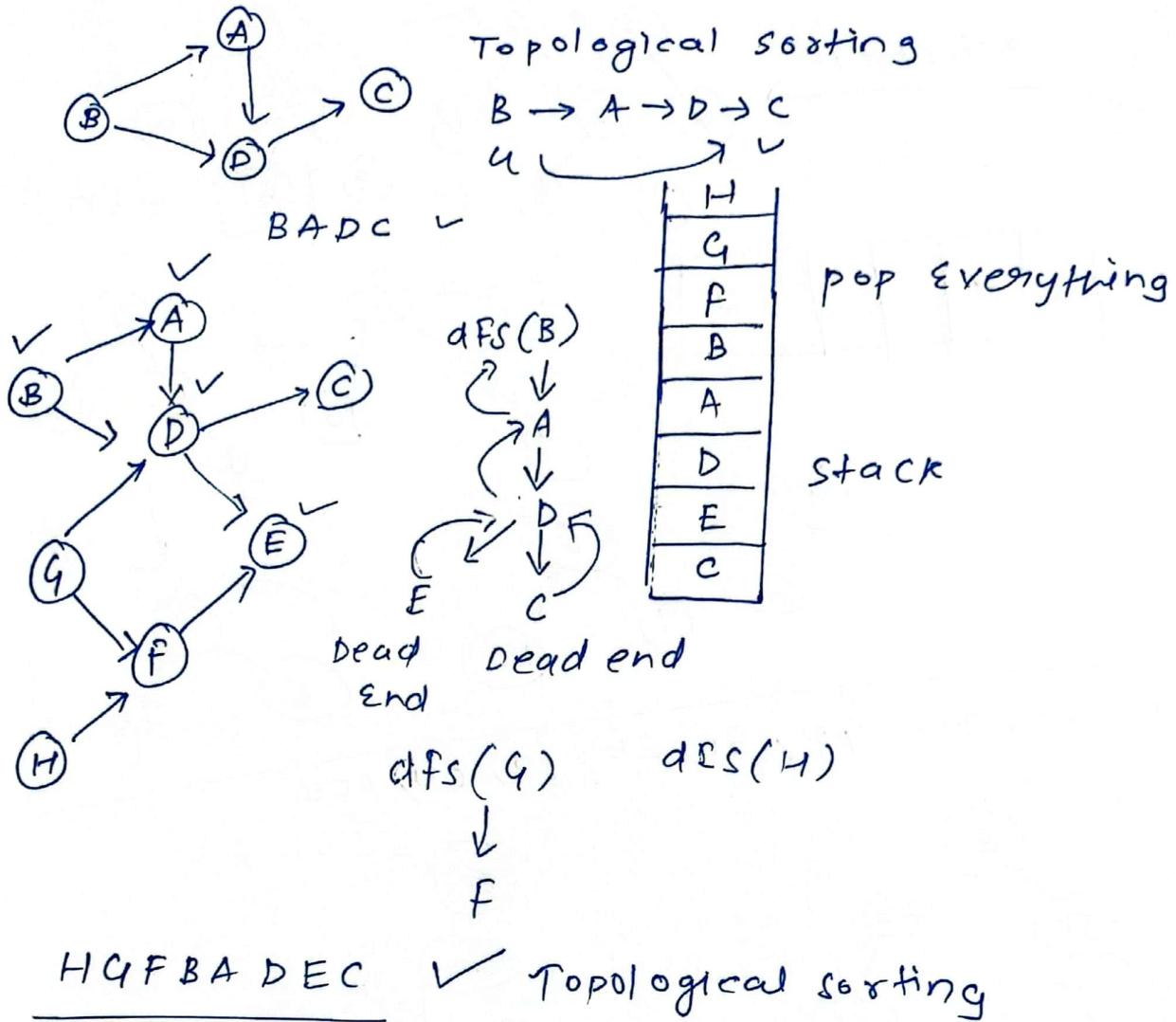
2	4	6	9	10
---	---	---	---	----

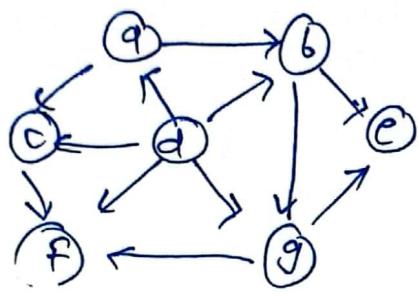
---

50, 60, 70, 90, 30, 20, 10, 80, 100

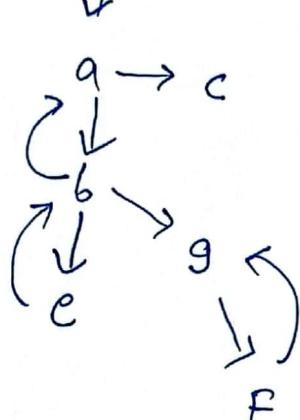


## Topological Sorting

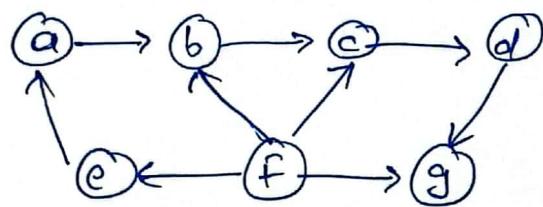
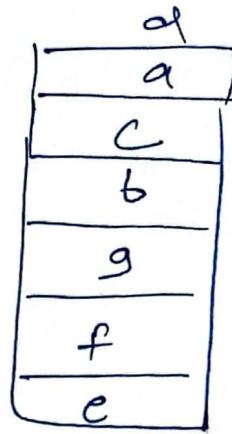




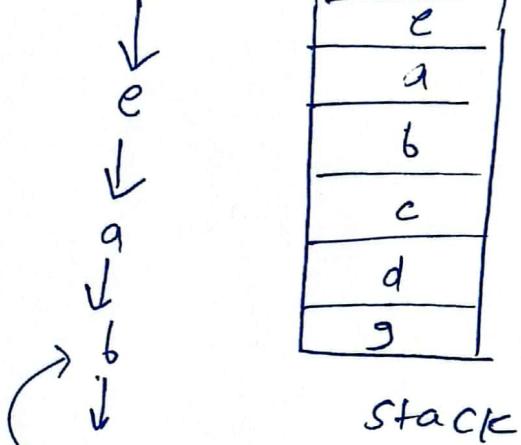
dfs(d)



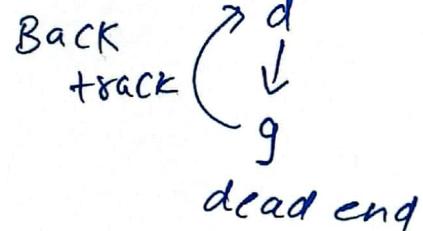
d a c b g f e



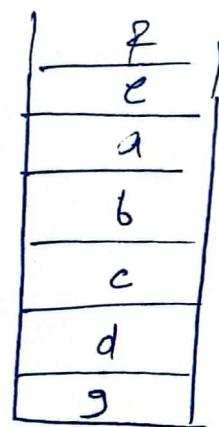
dfs(f)



f e a b c d g Topological sequence

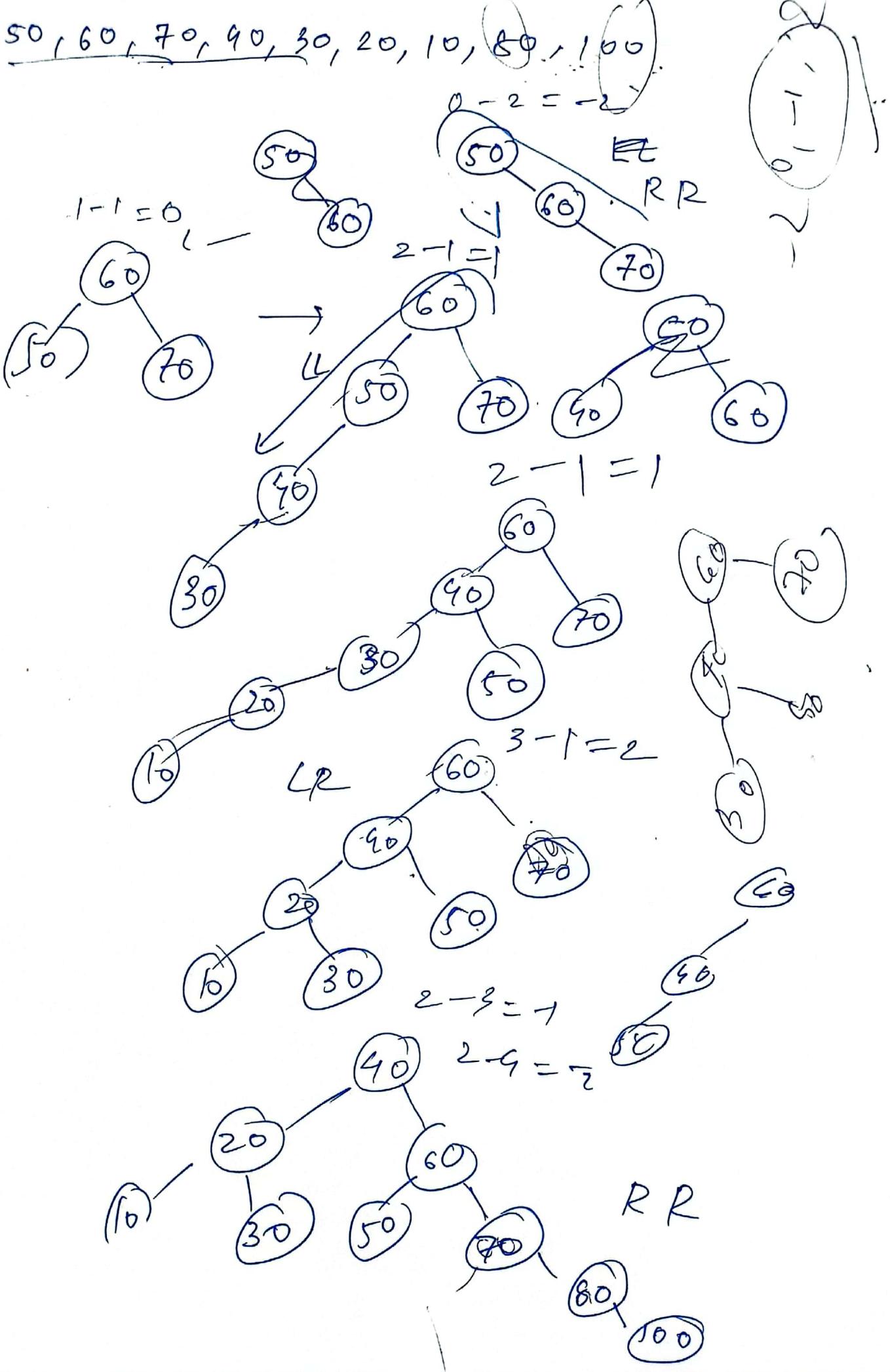


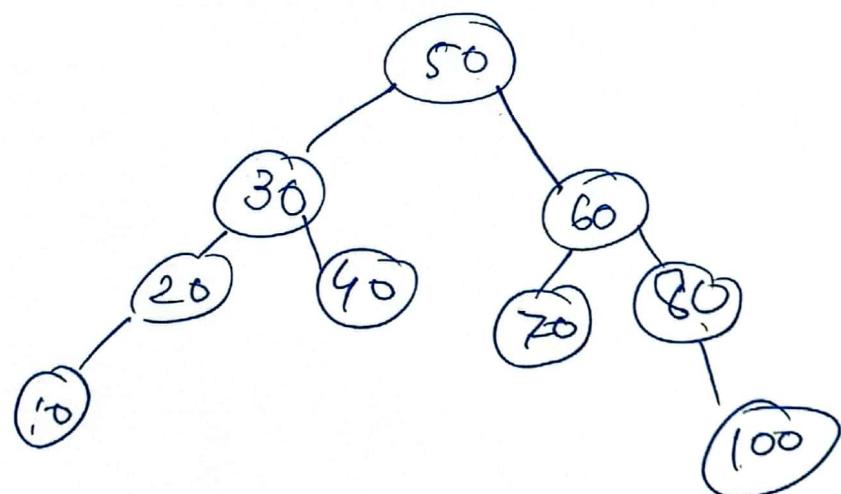
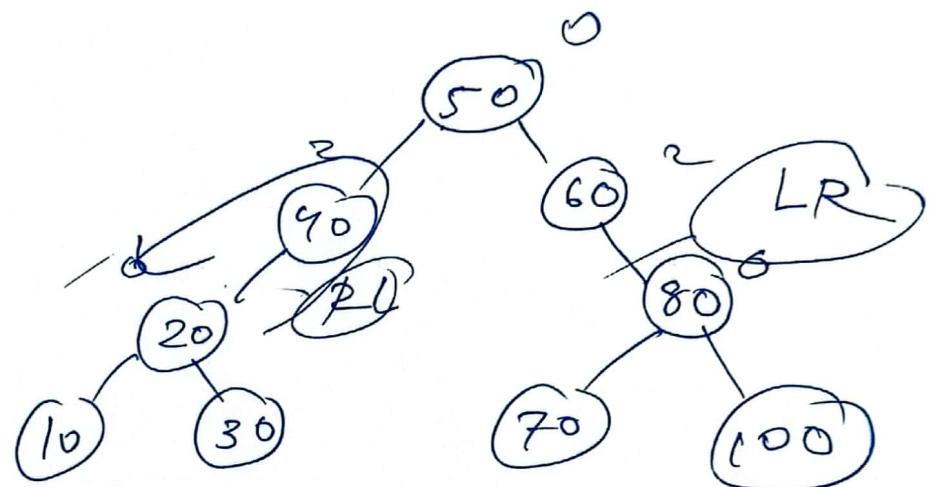
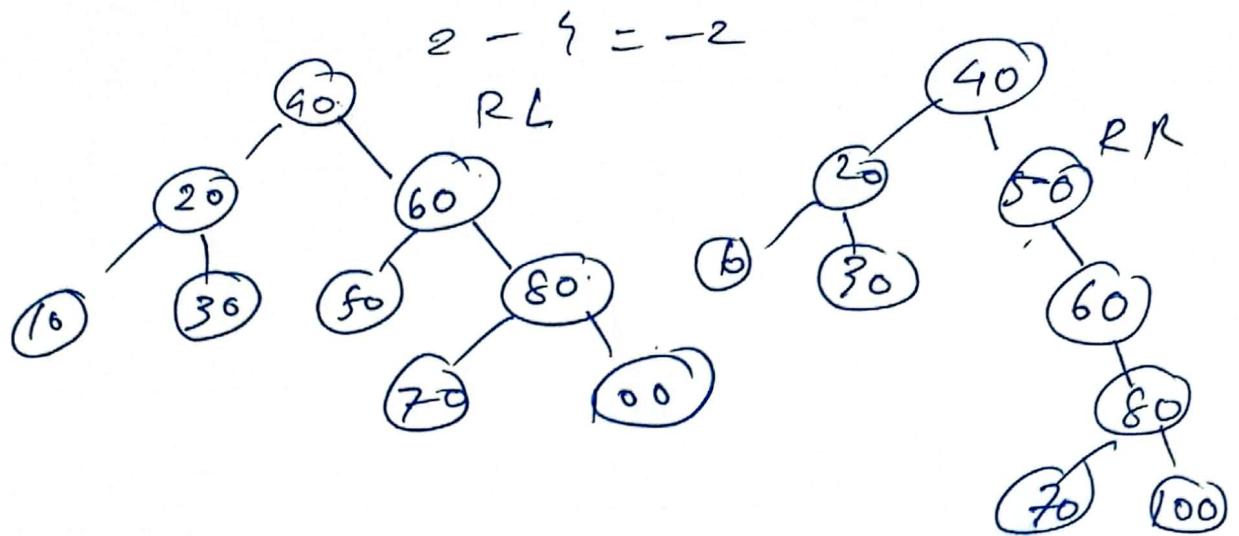
dead end



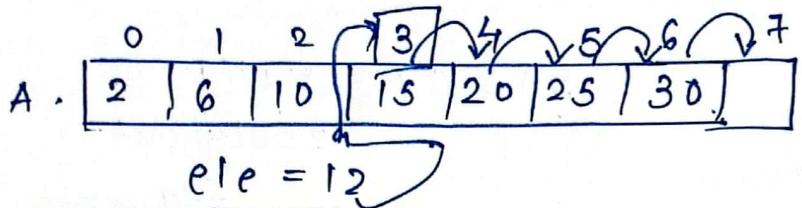
stack

50, 60, 70, 90, 30, 20, 10, 80, 160.





## Chp 3 :- Decrease and conquer



Algorithm

Insertion sort

i) Insert 5 in

8	5	7	3	2	
---	---	---	---	---	--

8	7	3	2	
---	---	---	---	--

5	8	7	3	2	
---	---	---	---	---	--

1st pass

Insert 7

5	8		3	2
---	---	--	---	---

7

2nd pass

5	7	8	3	2
---	---	---	---	---

8
---

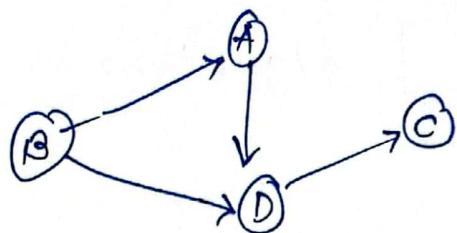
5	7	8	3	2
---	---	---	---	---

IIIrd pass

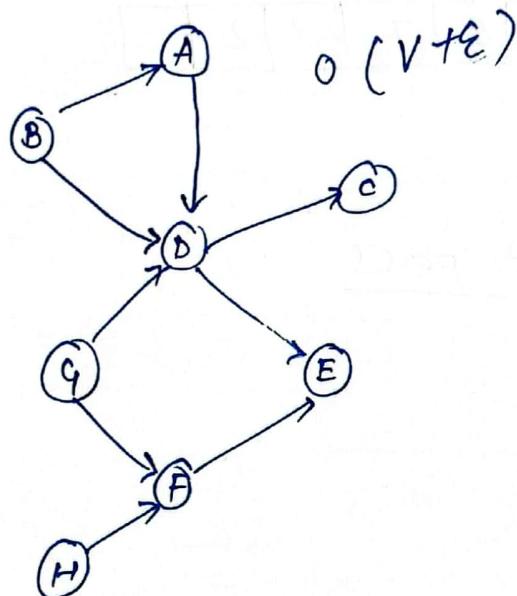
3	5	7	8	2
---	---	---	---	---

2	3	5	7	8
---	---	---	---	---

## Topological order



B A D C ✓ valid  
topological sequence

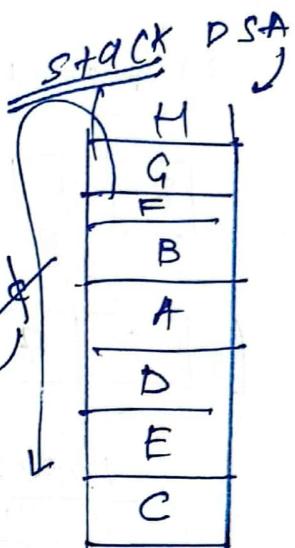


$O(V+E)$

DFS(B)

B → X → D → X → F → X → E → X → C

B A D E C ✓



DFS(A) →

G → F →  
L ↗ ↘

DFS(H)

81 > 92 Yes

$A[9] \geq 70$  ?  $\therefore \text{mid} - 1$

$$\frac{6+9}{2} = \frac{15}{2} = 7$$

Key element is found

Binary searching :-

3	14	12	7	31	139	142	55	70	79	81	85	93	98
0	1	2	3	4	5	6	7	8	9	10	11	12	m

$$\text{mid} = \left( \frac{\text{start} + \text{end}}{2} \right) = \frac{0+12}{2} = 6$$

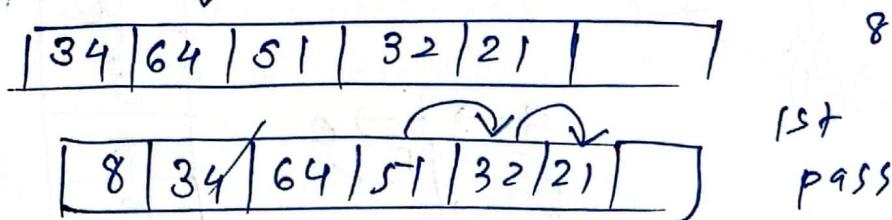
mid > 70 ?

$A[6] > 70$ ? No

$$\frac{6+12}{2} = \frac{18}{2} = 9$$

## Sort using Insertion sort

$$A = \boxed{84 | 8 | 64 | 51 | 32 | 21}$$



$$\boxed{34 | 64 | 51 | 32 | 21} \quad \text{Insert } 8$$

$$\boxed{8 | 34 | 64 | 51 | 32 | 21} \quad \text{2nd pass}$$

$$\boxed{8 | 34 | 51 | 64 | 32 | 21} \quad \text{3rd pass}$$

$$\boxed{8 | 34 | 51 | 32 | 21 | 64} \quad \text{4th pass}$$

$$\boxed{8 | 34 | 32 | 2 | 51 | 64} \quad \text{5th pass}$$

$$\boxed{8 | 32 | 34 | 2 | 51 | 64} \quad \text{6th pass}$$

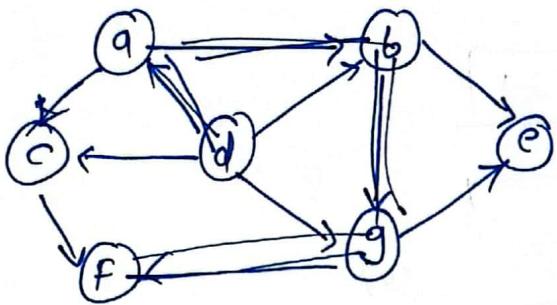
$$\boxed{8 | 32 | 2 | 34 | 51 | 64} \quad A[3] \geq 64 \text{ NO}$$

$A[8] \geq 51 \text{ NO}$

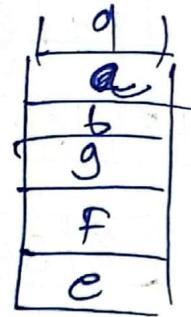
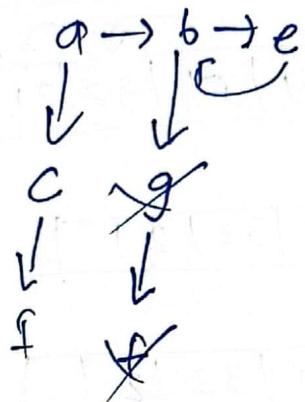
$$\boxed{2 | 8 | 32 | 34 | 51 | 64} \quad \begin{array}{l} \text{result} \\ \text{mid} = \frac{2+8}{2} = 5 \\ \text{key element} = \frac{9+1}{2} = 5 \end{array}$$

$$\text{mid} = \frac{\text{start} + \text{end}}{2} = \frac{0+5}{2} = 2.5 \approx 3$$

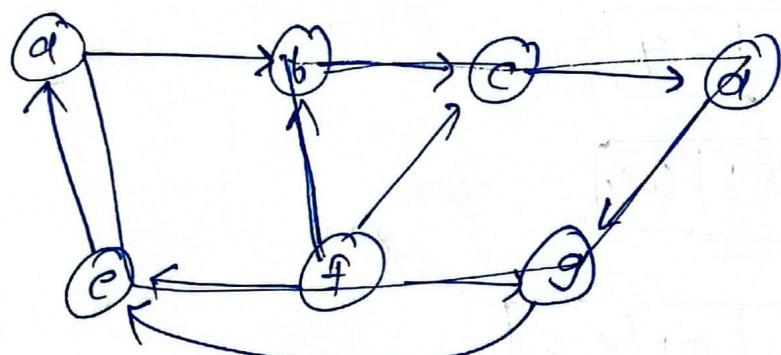
$A[2] > 64 \text{ NO} \quad \checkmark$



$c-f$



a b c g f e

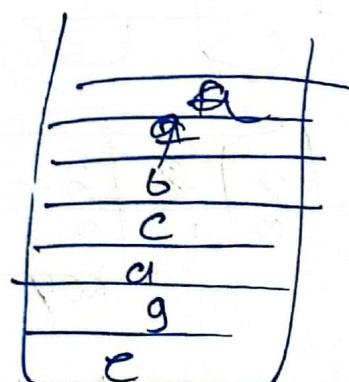
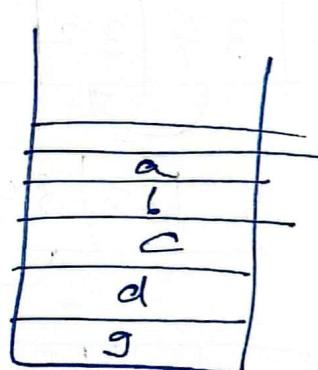


$a \rightarrow b \rightarrow c \rightarrow d \rightarrow g \rightarrow e$

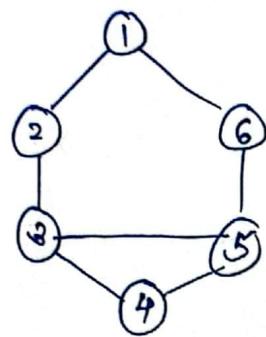
$e-d$

$e-a-b-c-d-g$

$f \rightarrow a \rightarrow b \rightarrow c \rightarrow d \rightarrow g \rightarrow e$



## Greedy technique



$$G = (V, E)$$

$$V = \{1, 2, 3, 4, 5, 6\}$$

$$E = \{(1, 2), (2, 3), (3, 4), \dots\}$$

if ?

N

Minimum cost spanning tree (MST)

## Prims Algorithm

$$V = \{1, 2, 3, 4, 5, 6\}$$

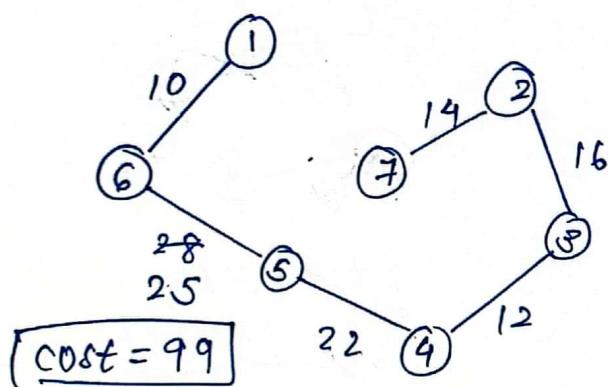
$$|V| = n = 6$$

$$|V| - 1 = 5 \text{ edges}$$

$$|E| = |V| - 1$$

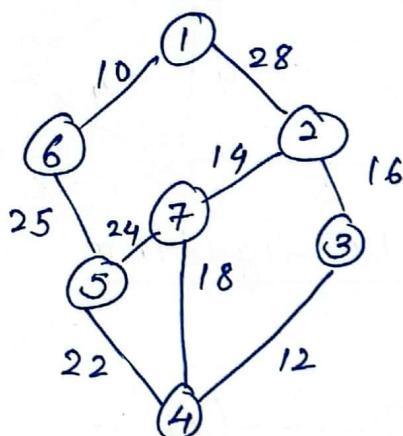
$6^{C_S} = 6$  different spanning trees  
 $7^{C_L}$

Minimum cost spanning tree using Prim's Algorithm



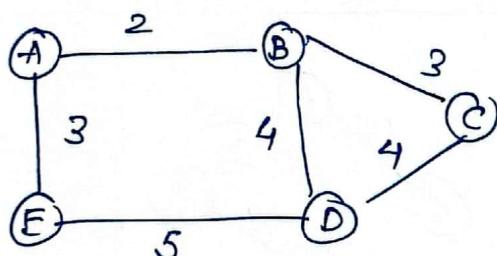
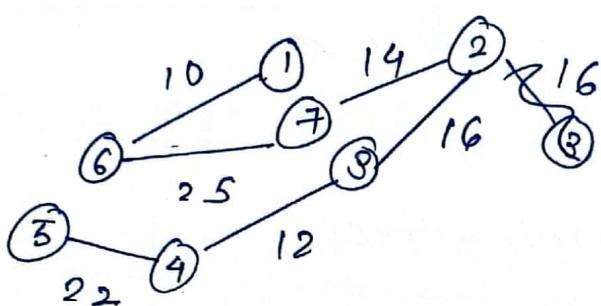
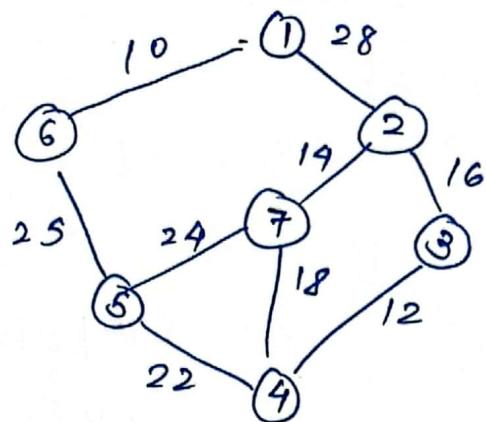
Step 1 :- connect minimum edge possible in graph  
Step 2 :- keep comparing and connecting smallest possible edge for a tree and remember

$$|E| = |V| - 1 \text{ to satisfy cond tree.}$$

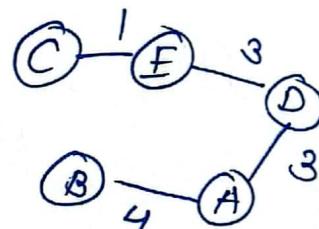
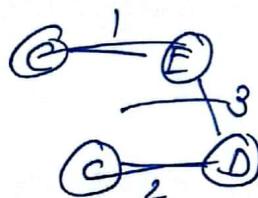
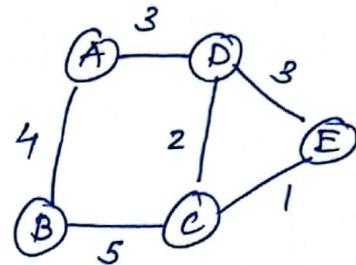


## Kruskals Algorithm

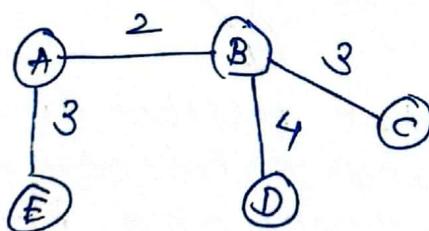
step 1 :-



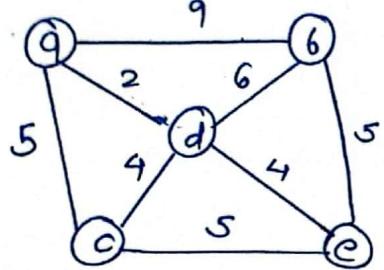
Kruskals algorithm



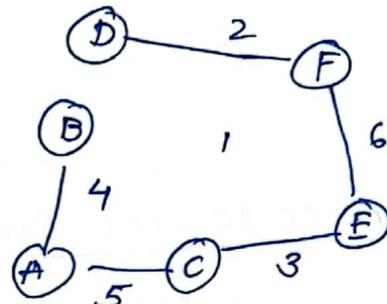
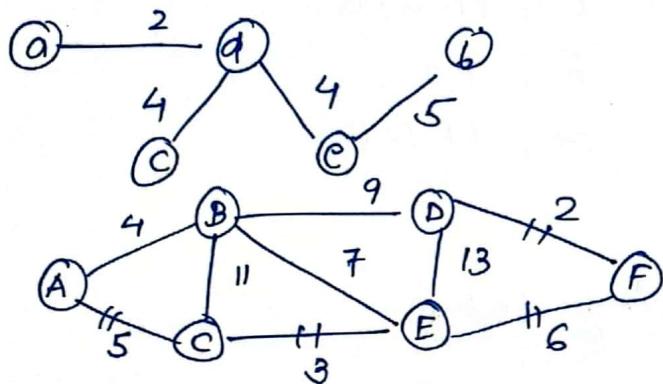
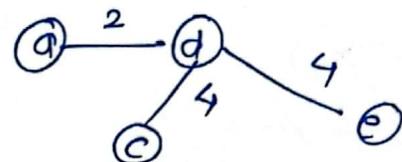
$$1 + 3 + 3 + 4 \\ \underline{11 \text{ cost}}$$



$$2 + \underline{3 + 4 + 3} = 12 \text{ cost}$$

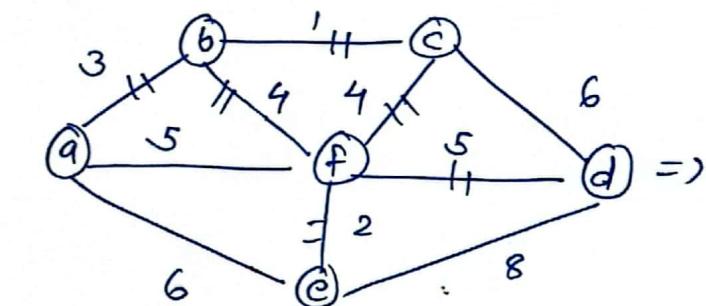


minimum spanning tree using  
prim's algorithm

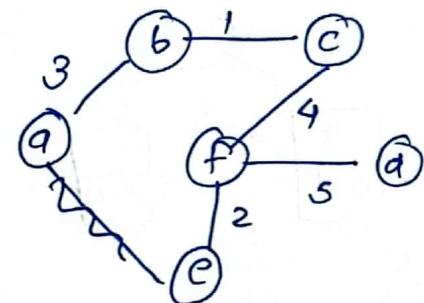


$$2 + 6 + 3 + 5 + 4 \\ = 20$$

Kruskals algorithm



very easy!



$$1 + 3 + 4 + 5 + 2 = 15 \\ \text{cost}$$

Dijkstra's algorithm

## Huffman coding Trees

Message  $\rightarrow$  BECABBDDAE CCABAEDDDCC

length of message = 20

ASCII - 8-bits

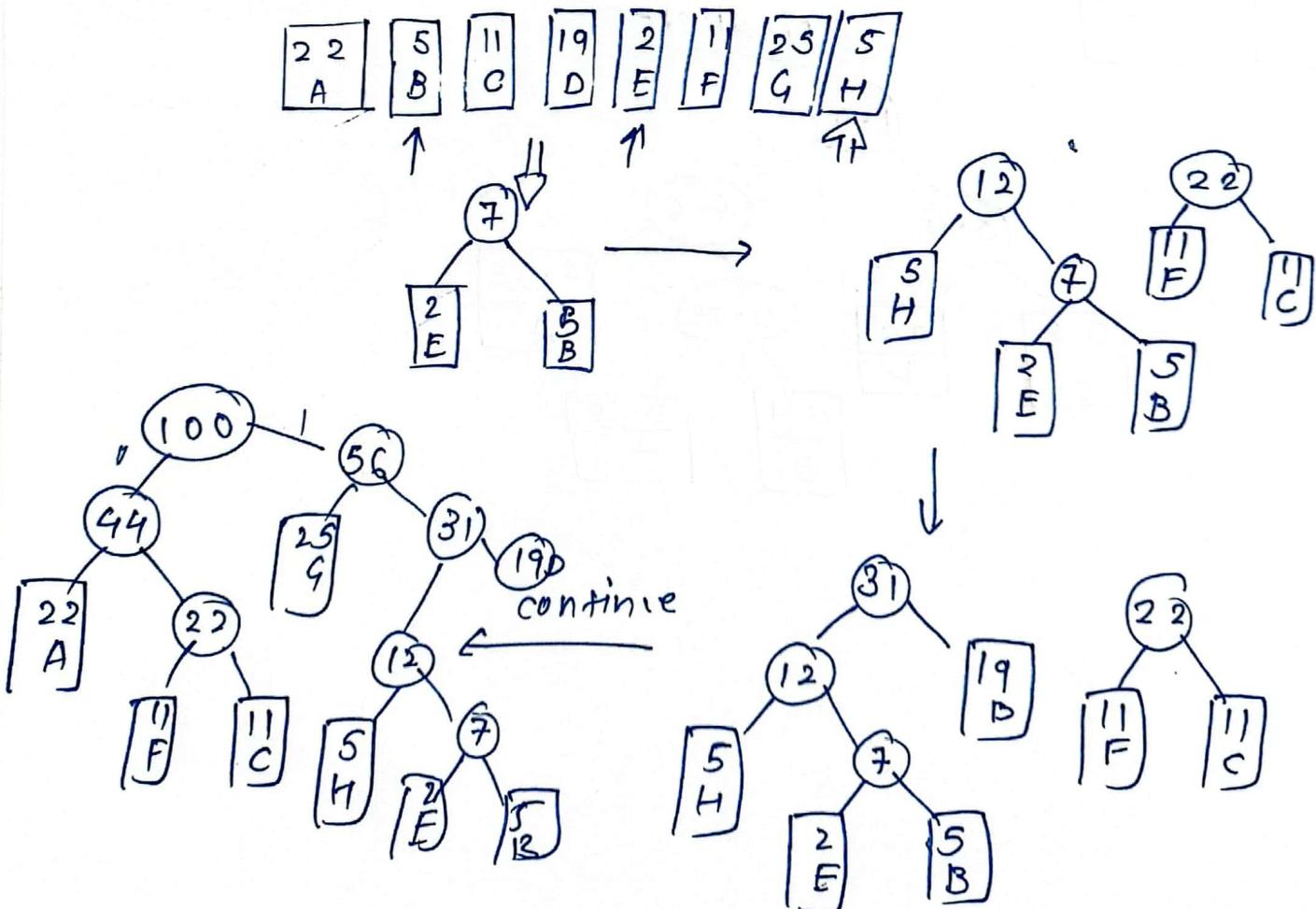
$$8 \times 20 = 160 \text{ BITS}$$

A	65	01000001
B	66	01000010
C	67	:
D	68	:
E	69	:

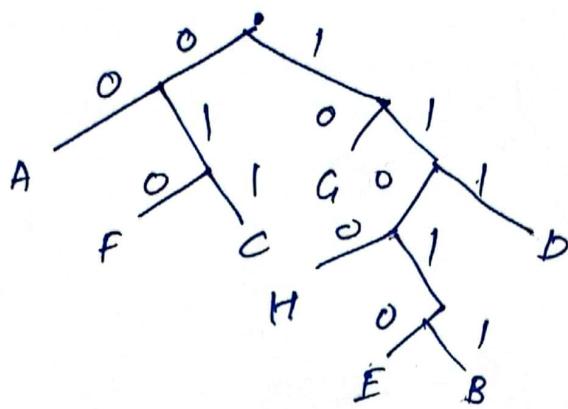
character	count / freq	code,

Suppose A, B, C, D, E, F, G and H are 8 data items and they are assigned weights as

Data Items	A	B	C	D	E	F	G	H
weights	22	5	11	19	2	11	25	5



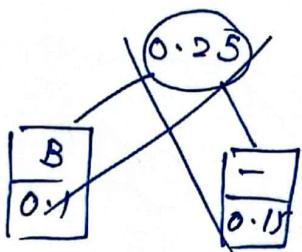
## Huffman Coding



A : 00  
 B : 11011  
 C : 011  
 D : 111  
 E : 11010  
 F : 10  
 G : 1100  
 H : 1100

## Huffman code for following data

symbol	A	B	C	D	-
frequency	0.4	0.1	0.2	0.15	0.15



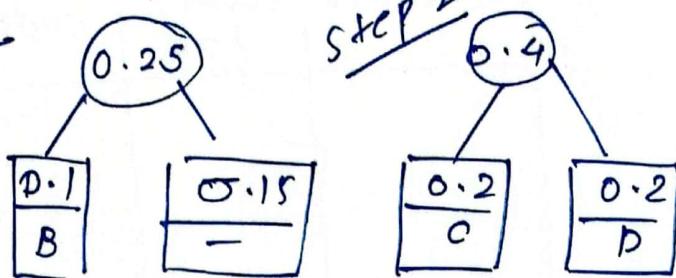
Step 1

## constructing of Huffman coding tree

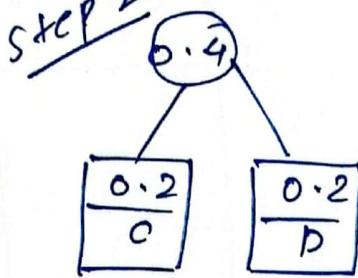
symbol	A	B	C	D	-
frequency	0.35	0.1	0.2	0.2	0.15

Always consider  
2 minimum  
frequencies  
to compare

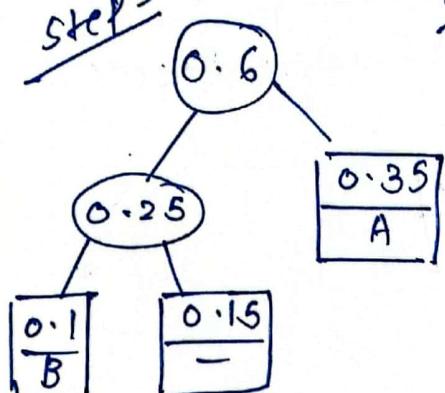
step 1



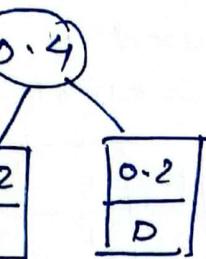
step 2



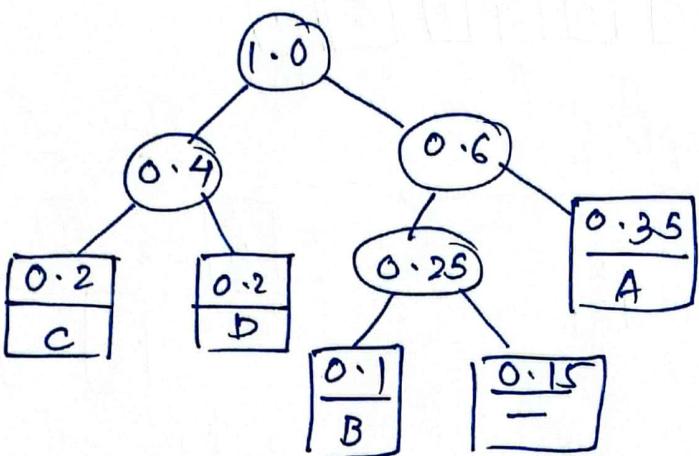
step 3



step 4



final step



## Chp 2: Brute Force Algorithms

### Selection sort algorithm

Sorted - Array

89	45	68	90	29	34	17	↓	min
----	----	----	----	----	----	----	---	-----

Apply selection sort algorithm

17	45	68	90	29	34	89
↑						

swap

Sorted      Unsorted

Noted :- Take the first element and compare it with the smallest (minimum) element of the unsorted array.

17	29	68	90	45	34	89
↓						

swap (minimum)

17	29	34	90	48	68	89
↓						

17	29	34	45	90	68	89
↓						

17	29	34	45	68	90
↓					

17	29	34	45	68	89	90
↓						

Array is sorted !

### Bubble-sort Algorithm

89	45	68	90	29	34	17	)
↑							

compare for min

45	89	68	90	29	34	17
↑	↑					

45	88	89	90	29	34	17
↑	↑	↑	↑			

45 | 68 | 89 | 90 | 29 | 84 | 17 |

45 | 68 | 89 | 29 | 90 | 84 | 17

(45 | 68 | 89 | 29 | 84 | 90 | 17)

45 | 68 | 89 | 29 | 84 | 17 | 90

45 | 68 | 29 | 89 | 34 | 17 | 90

$\therefore [45 | 68 | 29 | 84 | 17 | 89 | 90] \top$

$\therefore 17 | 84 | 4$

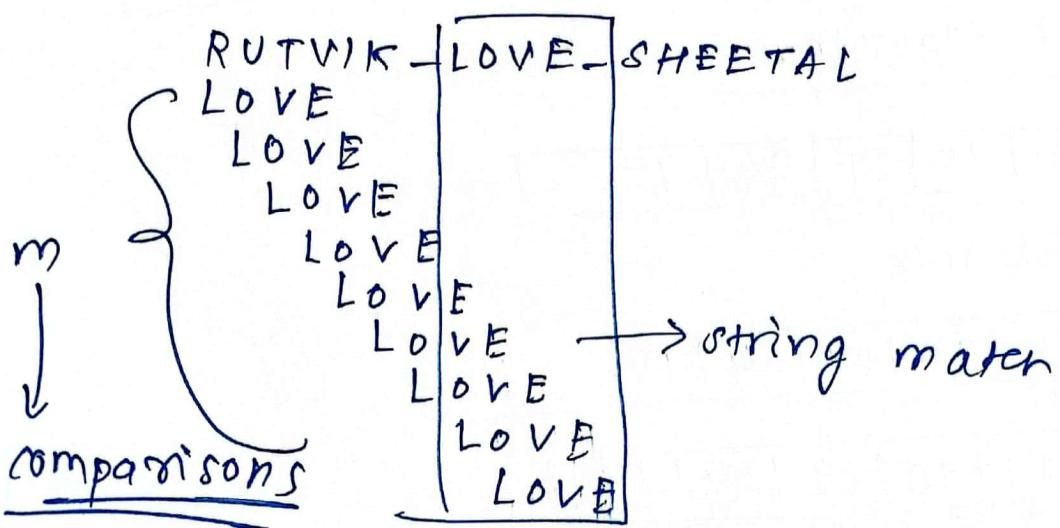
17 | 29 | 34 | 168 | 89 | 90

[17 | 29 | 34 | 45 | 68 | 89 | 90] ← After all comparisons

Brute-force string matching algorithm

Q RUTVIK - LOVE - SHEETAL = T

P = LOVE



## Space and Time - Trade-off

sort-given element using sorting By counting

50, 60, 70, 40, 80, 20, 10, 80, 100

1	1	1	1	1	1	1	1	0	1
10	20	30	40	50	60	70	80	90	100

input size  
A[10 · · · 100]

Traverses  
10, 20, 30, 40, 50, 60, 70, 80, 100

input size  $A[0 \dots 80]$  21, 26, 80, 9, 4, 14, 28, 18, 15, 16, 2, 3, 7

~~2, 3, 4~~ → Traverse from L to R array

2, 3, 4, 7, 9, 10, 14, 15, 18, 21, 26, 28, 36

## Horowitz Algorithm

BANGALORE

## STRING MATCH LORE

## string match table

A	B	C	..	E	..	L	..	O	R	..	Y	Z
4	4	4	-	4	3	2	1	-	4	4		

B A N G A L O R E  
L O R E

string match successful

Boyer Moore Horspool Algorithm for pattern matching.

$T = \text{AINAISESTIZAINAINEN}$

$P = \underline{\text{AINAINEN}}$        $m=8$

Bad match table

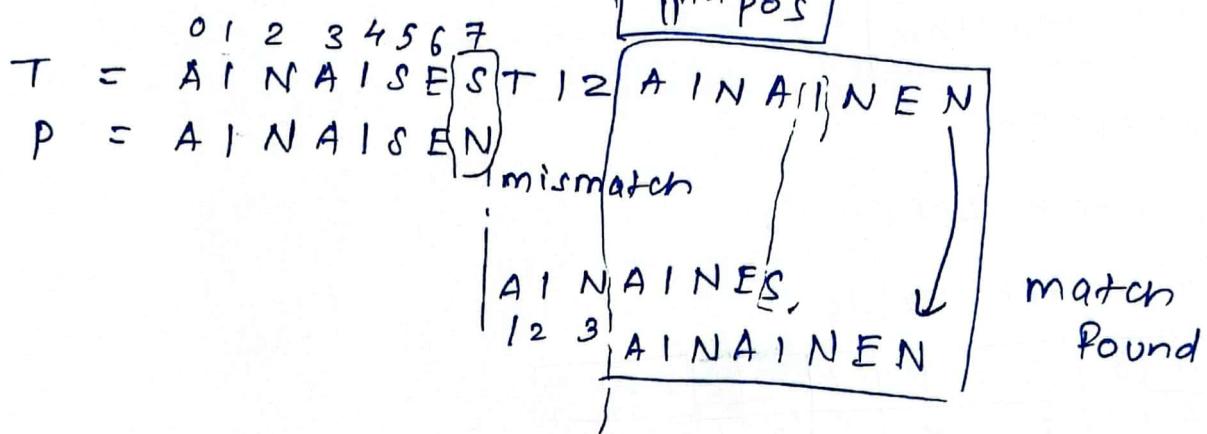
LAST LETTER =  $\star = 8$   
 $m=8=\star$

A	I	E	N	*
4	3	1	8	8

value = length - index - 1      value  $\star =$

$$E = 8 - 6 - 1 = 8 - 4 - 1 = 3$$

$$\begin{matrix} 2-1 \\ = 1 \end{matrix} \quad \begin{matrix} 8-3-1 \\ = 5 \end{matrix}$$



Apply Horspool and boyer-Moore algorithm.

P - NOT

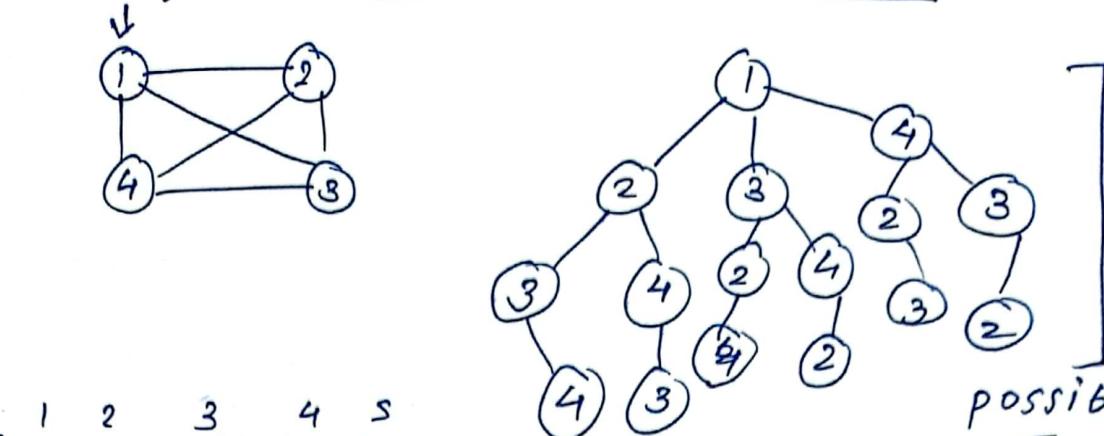
$T = \text{NOBODY-NOTICED-HIM}$

Horspool method

STRING MATCH TABLE

A	B	C	D	.	N	O	T
3	3	3	3		2	1	3

## Traveling-Salesperson Branch-and-Bound

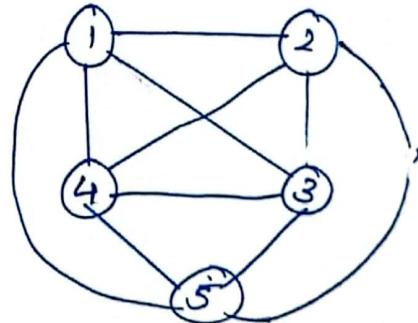
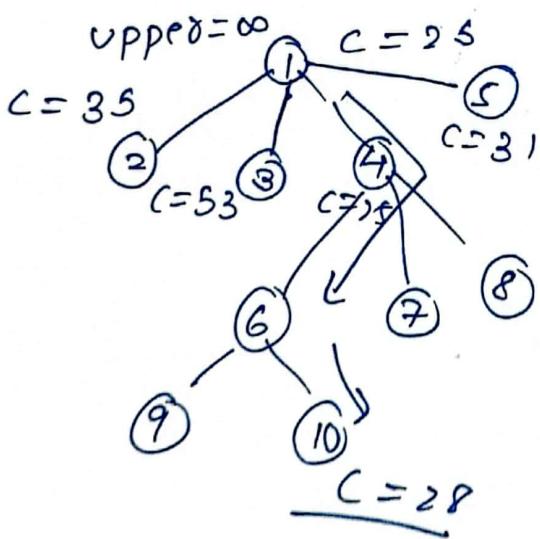


	1	2	3	4	5	
1	$\infty$	20	80	10	11	10
2	15	$\infty$	16	4	2	2
3	3	5	$\infty$	2	4	2
4	19	6	18	$\infty$	3	3
5	16	4	7	16	$\infty$	4
						21

$$\Rightarrow \begin{bmatrix} \infty & 10 & 20 & 0 & 0 \\ 13 & \infty & 14 & 2 & 0 \\ 1 & 3 & \infty & 0 & 2 \\ 16 & 3 & 15 & \infty & 0 \\ 12 & 0 & 3 & 12 & \infty \end{bmatrix} \begin{matrix} T \\ 0 \\ 0 \\ 25 \\ 10 \end{matrix} \quad \begin{matrix} 1 \\ 0 \\ 3 \\ 0 \\ 0 \end{matrix} + \frac{21}{21} = 25$$

	1	2	3	4	5	
1	$\infty$	10	17	0	1	
2	12	$\infty$	11	2	0	
3	0	3	$\infty$	0	2	
4	15	3	12	$\infty$	0	
5	11	0	0	12	$\infty$	

reduced cost = 25



$$C(i, j) + C(R) + R$$