

Higher-Ranked Exception Types

Ruud Koot

Department of Computing and Information Sciences, Utrecht University

September 2014

Exception Types

- ▶ In Haskell “types do not lie”:
 - ▶ Functions behave as mathematical function on the domain and range given by their type
 - ▶ Side-effects are made explicit by monadic types
- ▶ Exceptions that may be raised are *not* captured in the type
 - ▶ We would like them to be during program verification
 - ▶ Adding exception types in Haskell are more complicated than in a strict first-order language

Exception Types in Haskell

- ▶ Exception types in Haskell can get complicated because:

Higher-order functions Exceptions raised by higher-order functions depend on the exceptions raised by functional arguments.

Non-strict evaluation Exceptions are not a form of control flow, but are values that can be embedded inside other values.

- ▶ An exception-annotated type for *map* would be:

$$\begin{aligned} \text{map} &: \forall \alpha \beta e_1 e_2 e_3 e_4. \\ &(\alpha^{e_1} \xrightarrow{e_3} \beta^{(e_1 \cup e_2)}) \xrightarrow{\emptyset} [\alpha^{e_1}]^{e_4} \xrightarrow{\emptyset} [\beta^{(e_1 \cup e_2 \cup e_3)}]^{e_4} \\ \text{map} &= \lambda f. \lambda x s. \mathbf{case} \ x s \ \mathbf{of} \\ &\quad [] \quad \mapsto [] \\ &\quad (y : ys) \mapsto f \ y : \text{map} \ f \ ys \end{aligned}$$

Precise Exception Types

- ▶ The exception type above is not a precise as we would like

$$\begin{aligned} \text{map} \ id &: [\alpha^{e_1}]^{e_4} \rightarrow [\alpha^{e_1}]^{e_4} \\ \text{map} \ (\text{const} \ \perp_{\mathbf{E}}) &: [\alpha^{e_1}]^{e_4} \rightarrow [\beta^{(e_1 \cup \{\mathbf{E}\})}]^{e_4} \end{aligned}$$

- ▶ A more appropriate type for *map* (*const* $\perp_{\mathbf{E}}$) would be:

$$\text{map} \ (\text{const} \ \perp_{\mathbf{E}}) : [\alpha^{e_1}]^{e_4} \rightarrow [\beta^{\{\mathbf{E}\}}]^{e_4}$$

- ▶ Exceptional elements in the input list cannot be propagated to the output.

Higher-Ranked Exception Types

- ▶ The problem is that we have already committed the first argument of *map* to be of type

$$\alpha^{e_1} \xrightarrow{e_3} \beta^{(e_1 \cup e_2)}$$

- ▶ It always propagates exceptional values from the input to the output
- ▶ The solution is to move from Hindley–Milner to System F_{ω} , introducing *higher-ranked exception types* and *exception operators*

$$\begin{aligned} \text{map} &: \forall e_2 e_3. (\forall e_1. \alpha^{e_1} \xrightarrow{e_3} \beta^{(e_2 e_1)}) \\ &\rightarrow (\forall e_4 e_5. [\alpha^{e_4}]^{e_5} \rightarrow [\beta^{(e_2 e_4 \cup e_3)}]^{e_5}) \end{aligned}$$

$$\text{id} : \forall e. \alpha^e \xrightarrow{\emptyset} \alpha^e$$

$$\text{const} \ \perp_{\mathbf{E}} : \forall e. \alpha^e \xrightarrow{\emptyset} \beta^{\{\mathbf{E}\}}$$

- ▶ This gives us the desired exception types:

$$\begin{aligned} \text{map} \ id &: \forall e_4 e_5. [\alpha^{e_4}]^{e_5} \rightarrow [\alpha^{e_4}]^{e_5} \\ \text{map} \ (\text{const} \ \perp_{\mathbf{E}}) &: \forall e_4 e_5. [\alpha^{e_4}]^{e_5} \rightarrow [\beta^{\{\mathbf{E}\}}]^{e_5} \end{aligned}$$

Exception Type Inference

- ▶ Higher-ranked exception types are syntactically heavy; we need type inference
- ▶ Type inference is undecidable in System F_{ω} , but exception types piggyback on an underlying type
- ▶ Holdermans and Hage (2010) show that type inference is decidable for a similar higher-ranked annotated type system with type operators

Work-in-Progress

Imprecise exception semantics Haskell has an *imprecise exception semantics*

- ▶ Needed for soundness of various program transformations in an optimizing compiler
- ▶ Not adequately captured by ACI1 constraints; attempt to unification in Boolean rings

Metatheory Is the combined rewrite system of STLC and BR still confluent and normalizing?

- ▶ Needed for decidable exception type equality
- ▶ Hope to use a general result by Breazu-Tannen