

The birthday paradox can be described as follows:

If 23 persons are chosen at random, then the chances are more than 50% that at least two will have the same birthday!

When they first hear this stated, most persons have trouble believing it and are unconvinced by mathematical proofs¹. The program that you write for this assignment will allow you to test the birthday paradox to see if it is really true. This will be done by simulating birthdays with random numbers between 1 and 365.

Your main program should display a menu that reads as follows:

- 1) Explain birthday paradox
- 2) Check birthday paradox by generating 1000 sets of birthdays
- 3) Display one set of 23 birthdays
- E) Exit

If option 2) is selected, the output would be something like this:

```
Generating 1000 sets of 23 birthdays and checking for matches...
Results : 511 out of 1000 (51.1%) of the sets contained matching birthdays
=====
```

If option 3) is selected, the program will display the results in chronological order with matches indicated. The output should needs to look like this:

```
Here are the results of generating a set of 23 birthdays
=====
January      2      January      5      January      12
January      25     February      3      February      6
February     12     February     17     March          8
April         4      April        12     June           3
June          12     July          3      August         4
September     3      September     9      September     25
(2) October   12     October      16     October       22
December     22
```

Hints and Suggestions

- * A "birthday" can be viewed as a random integer between 1 and 365. Recall that there is function named "rand()" in stdlib that can be used to generate such random numbers. The expression "1 + (rand() % 365)" yields a random number that is between 1 and 365 inclusive. You should use the srand() function, but be *sure to not to call it more than once!*
 - * As a bottom-up exercise, I recommend that you write the following function. *We'll write the algorithm in class.*
- ```
void ConvertDayOfYear (int DayOfYear, // "Converts" a day of the year, such as 32
 int &MonthNumber, // to a MonthNumber, 2 and a DayOfMonth, 1
 int &DayOfMonth)
```
- \* We'll do a top-down design in class that will make your work go more smoothly. The Selection Sort code can be found on website. (also inline function swap is there)
  - \* Very important to look at and follow the algorithm that will be given in class. Write one function at a time!

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<sup>1</sup>It can be shown that in a group of 23, the probability of that *no two persons have the same birthday* is

$$\frac{365 \times 364 \times 363 \times \dots \times (365 - 23 + 1)}{365 \times 365 \times 365 \times \dots \times 365} = \frac{365!}{365^{23} \times 23!}$$