

C335 Homework #5

Points:	: 40 points
Due Date:	: Mar. 24 th
Submissions:	: For F-2-F students, hardcopy (type or write your solution clearly) For online students, e-copy to Canvas

PART I (8 POINTS)

Assume that X consists of 3 bits, x_2 , x_1 , and x_0 . Write four logic functions that are true if and only if

- (A) X contains only one 0
- (B) X contains an even number of 0s
- (C) X when interpreted as an unsigned binary number is less than 4
- (D) X when interpreted as a signed (two's complement) number is negative

PART II (8 POINTS)

With $x = 01011011$ (bin) and $y = 00001101$ (bin) representing two's complement signed integers, perform, showing all work:

- (A) $x + y$
- (B) $x - y$
- (C) $x * y$
- (D) x/y

PART III (6 POINTS)

Do the unsigned multiply for $0011 * 0111$, using the Multiply Algorithm Version 3 (check the lecture notes). Show the contents of registers for multiplicand (4 bits) and product (8 bits) step by step.

PART IV (6 POINTS)

Do the unsigned multiply for $0011 * 0111$, using the Booth's Algorithm (check the lecture notes). Show the contents of registers for multiplicand (4 bits) and product (8 bits) step by step.

PART V (6 POINTS)

In Lecture Notes c335-ALU-1.pdf, we discussed how we could modify the 4-bit ALU to support detecting overflow but did not give the proof. Now you are expected to prove you can detect overflow by simply check if Carry into MSB \neq Carry out of MSB.

Hint: you could use a table (like a truth table) to list all situations, then identify the cases that cause overflows

PART VI (6 POINTS)

Do necessary modifications on the following 1 bit ALU, then use it to construct a 4-bit ALU that supports the SLT instruction.

Hint: read text appendix **B** section **B.5** to find clue.

