

C335 Homework #2 Solution

Part I

The result for addition: 110000000011

The result for subtraction: 010100101101

Part II

(1)

$$7\text{ffffffa}(\text{hex}) = 0111\ 1111\ 1111\ 1111\ 1111\ 1111\ 1111\ 1010\ (\text{bin})$$

$$\begin{aligned} 7\text{ffffffa}(\text{hex}) &= 7\text{ffffff}(\text{hex}) - 5\ (\text{dec}) = 2,147,483,647\ (\text{dec}) - 5\ (\text{dec}) \\ &= 2,147,483,642\ (\text{dec}) \end{aligned}$$

(2)

$$1100101011111110111101011001110\ (\text{bin}) = \text{CAFEFACE}(\text{hex})$$

Part III

$$(1) -103(\text{dec}) = 10011001\ (\text{bin}) = 0\text{x}99$$

$$(2) 0\text{xAA} = 10101010\ (\text{bin}) = -86\ (\text{dec})$$

Part IV

(1)

$$\begin{aligned} 4096\ (\text{dec}) &= 2^{12}\ (\text{dec}) \\ &= 0000\ 0000\ 0000\ 0000\ 0001\ 0000\ 0000\ 0000\ (\text{bin}, 2\text{'s complement}) \end{aligned}$$

(2)

$$\begin{aligned} 2047\ (\text{dec}) &= 2048\ (\text{dec}) - 1 \\ &= 2^{11}\ (\text{dec}) - 1 \\ &= 0000\ 0000\ 0000\ 0000\ 1000\ 0000\ 0000\ (\text{bin}) - 1 \\ &= 0000\ 0000\ 0000\ 0000\ 0111\ 1111\ 1111\ 1111\ (\text{bin}) \end{aligned}$$

$$\begin{aligned} -2047\ (\text{dec}) &= (0000\ 0000\ 0000\ 0000\ 0111\ 1111\ 1111\ 1111)' + 1 \\ &= 1111\ 1111\ 1111\ 1111\ 1000\ 0000\ 0000\ (\text{bin}) + 1 \\ &= 1111\ 1111\ 1111\ 1111\ 1000\ 0000\ 0001\ (\text{bin}, 2\text{'s complement}) \end{aligned}$$

(3)

$$\text{X} = 1111\ 1111\ 1111\ 1111\ 1111\ 1111\ 0000\ 0110\ (\text{bin}, 2\text{'s complement})$$

$$\begin{aligned} -\text{X} &= 0000\ 0000\ 0000\ 0000\ 0000\ 0000\ 1111\ 1001\ (\text{bin}) \\ &\quad + 1 \end{aligned}$$

$$= 0000\ 0000\ 0000\ 0000\ 0000\ 0000\ 1111\ 1010\ (\text{bin})$$

$$= 2^8 - 1 - 5 = 256 - 6 = 250\ (\text{dec})$$

$$\text{So X} = -250\ (\text{dec})$$

(4)

$$\text{X} = 1111\ 1111\ 1111\ 1111\ 1111\ 1111\ 1110\ 1111\ (\text{bin}, 2\text{'s complement})$$

$$\begin{aligned} -\text{X} &= 0000\ 0000\ 0000\ 0000\ 0000\ 0000\ 0001\ 0000\ (\text{bin}) \\ &\quad + 1 \end{aligned}$$

$$= 0000\ 0000\ 0000\ 0000\ 0000\ 0000\ 0001\ 0001\ (\text{bin})$$

$$= 16 + 1 = 17\ (\text{dec})$$

$$\text{So X} = -17\ (\text{dec})$$

Part V

```
        add $t0, $zero, $zero      # initialize running sum $t0 = 0
loop:   beq $a1, $zero, finish     # finished when $a1 is 0
        add $t0, $t0, $a0         # compute running sum of $a0
        addi $a1, $a1, -1         # compute this $a1 times
        j loop
finish: addi $t0, $t0, 100         # add 100 to a * b
        add $v0, $t0, $zero       # return a * b + 100
```

The program computes $a * b + 100$.

Part VI

```
        sll $a2, $a2, 2           # max i= 2500 * 4
        sll $a3, $a3, 2           # max j= 2500 * 4
        add $v0, $zero, $zero     # $v0 = 0
        add $t0, $zero, $zero     # i = 0
outer:  add $t4, $a0, $t0          # $t4 = address of array1[i/4]
        lw $t4, 0($t4)            # $t4 = array 1[i]
        add $t1, $zero, $zero     # j = 0
inner:  add $t3, $a1, $t1          # $t3 = address of array2[j/4]
        lw $t3, 0($t3)            # $t3 = array 2[j/4]
        bne $t3, $t4, skip        # if (array 1[i/4] != array 2[j/4]) skip $v0++
        addi $v0, $v0, 1          # $v0++
skip:   addi $t1, $t1, 4           # j = j+4
        bne $t1, $a3, inner       # loop if j != 2500 * 4
        addi $t0, $t0, 4          # i = i+4
        bne $t0, $a2, outer       # loop if i != 2500 * 4
```

The code determines the number of matching elements between the two arrays and returns this number in register \$v0

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Part VII

```
        addi $v0, $zero, -1       # Initialize to avoid counting zero word
loop:   lw, $v1, 0($a0)            # Read next word from source
        addi $v0, $v0, 1          # Increment count words copied
        sw $v1, 0($a1)            # Write to destination
        addi $a0, $a0, 4          # Advance pointer to next source
        addi $a1, $a1, 4          # Advance pointer to next destination
        bne $v1, $zero, loop      # Loop if word copied != zero
```

Bug 1: Count (\$v0) is initialized to zero, not -1 to avoid counting zero word.

Bug 2: Count (\$v0) is not incremented.

Bug 3: Loops if word copied is equal to zero rather than not equal.

Bonus Question

(1) If unsigned:

$$1.1011 \text{ (Bin)} = 1 \times 2^0 + 1 \times 2^{-1} + 0 \times 2^{-2} + 1 \times 2^{-3} + 1 \times 2^{-4} = 1.6875 \text{ (Dec)}$$

If signed, 2's complement:

$$1.1011 \text{ (Bin)} = 1 \times (-2^0) + 1 \times 2^{-1} + 0 \times 2^{-2} + 1 \times 2^{-3} + 1 \times 2^{-4} = -0.3125 \text{ (Dec)}$$

(2) $0.1 \text{ (Bin)} = 0.000110011001100\dots$