

Cryptography in the Post-Quantum Era

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Abstract—In recent years there has been a surge of interest and development in quantum computing. Quantum computers have the ability to solve complex mathematical problems that classical computers are not able to. This puts modern encryption systems at risk. This report aims to review the concept of "post-quantum cryptography" and what it would look like in the age of large, scalable quantum computers.

Index Terms—Quantum Computing, Cryptography, Public-Key Encryption

I. INTRODUCTION

SINCE the rise of the internet in the 1990's, there has been a very urgent need for cryptography. Cryptography, derived from the Greek word for "hidden" and "writing" has become a staple of every modern technology in use today. It is essential to countless businesses and the security, integrity and confidentiality of our ever-growing online presence as a society. Over the past few decades there have been significant strides made in the cryptography world (such as RSA and AES). Modern encryption algorithms rely on the hardness of solving one of two problems: *Integer Factorization* and the *Discrete Logarithm Problem*. These problems prove to be very difficult to solve modern classical computers as the power and time to solve them is immense. However, a relatively new phenomenon, Quantum-Computers, threaten this security.

Quantum computing began in the early 1980's when a physicist named Paul Benioff proposed a quantum mechanical model of the Turing machine. Richard Feynman, a theoretical physicist later brought up the idea that a quantum computer may be able to perform tasks that a classical computer did not have the capacity for.

This paper aims to review Quantum Computers, how they operate, modern encryption algorithms and how a quantum computer threatens their security.

II. QUANTUM COMPUTERS

Quantum Computers can perform calculations based on the probability an object's state before it's measured. Classical computers encode data in bits. These bits can have either a state of 0 or 1. Quantum computers, on the other hand use *qubits* to perform their calculations. Qubits are undefined properties of a system and have the ability to be in superposition. This means that a qubit can be in both states at the same time. Superposition can be thought of as a spinning coin, as the coin is spinning, it is neither a heads or a tails until it lands. Qubits are plugged into special algorithms that allows them to crunch through a vast number of outcomes simultaneously. To put this into perspective, 1 qubit can be in a superposition of 2 states, 3 qubits can be in a superposition

of 8 states and 50 qubits can be in a superposition of $2^{50} = 1,125,899,906,842,624$ states at once. As of 2019 the most powerful quantum computer is owned by IBM with 53 qubits.

Another phenomenon that makes quantum computing so powerful is *Quantum Entanglement*. Entanglement allows for one or more qubits to become a pair such that a change in one qubit will directly result in a change in the other. This happens, regardless of the distance between them. Quantum Computers can harness the power of entangled qubits in a "daisy chain" leading to exponential increases in computing power and speed.

However Quantum Computers are much more error prone than their classical counterparts due to *decoherence*. Qubits are very susceptible to errors from outside factors such as heat and vibrations. This causes their quantum behaviour to decay and become unreliable. Qubits are very fragile and any noise can cause problems in their superposition. Despite best efforts, researchers have found it difficult to reduce errors due to noise.

There is extensive research being done on Quantum Computers and it won't be long before quantum computers are at a point where they become useful. It is estimated that by 2030 a Quantum computer could be built for a budget of a billion dollars that could crack RSA-2048.

III. CURRENT CRYPTOGRAPHY

Current cryptography techniques can be divided into 2 distinct types: *Symmetric* and *Asymmetric*. These cryptography techniques rely heavily on the hardness of solving problems such as Integer Factorization and the Discrete Logarithm problem.

A. Symmetric

Symmetric-key cryptography algorithms rely on a single key to encrypt and decrypt messages. This key can be shared between two or more users. The plaintext message is entered into a "cipher" that encrypts the message using the key and outputs it as ciphertext. In much the same way, the ciphertext is decrypted using the key and can be converted back to its plaintext form.

Symmetric Cryptography allows for fairly high security with fast speeds, however there is a significant risk of keys being intercepted while they are being distributed.

B. Asymmetric

Also known as public-key cryptography, it makes use of two keys compared to the one in symmetric. The pair of

keys consists of a *public key* and a *private key*. The sender uses the receiver's public key to encrypt a message before sending it. The receiver then decrypts the message using their own related private key. Public-key cryptography is essential to internet applications such as the Secure Socket Layer, Transport Layer Security and HTTPS.

Digital signatures can also be verified using public-key techniques. Digital signatures are a way of validating the integrity of data. A hash of the data to be signed is generated, this hash is then encrypted using the private key. The hash combined with other metadata is then what's known as the digital signature. When the recipient receives the message, it can be verified by running the message through the same hashing algorithm. A match indicates a valid, untampered message.

C. Integer Factorization Problem

D. Discrete Logarithm Problem

E. Current Security

Both symmetric and public-key cryptography are considered to be very secure by today's standards. However this security is threatened as we move towards a reality where Quantum Computers are more powerful. The inherent security of symmetric cryptography is based on the length of the keys used for encryption/decryption. A 128 bit key length would take billions of years to crack on classical hardware. NIST recommends a move to 256 bit key lengths, which are thought to be theoretically resistant to Quantum attacks. The same cannot be said for public-key algorithms such as RSA and Elliptic Curve Cryptography as quantum algorithms such as *Shor's Algorithm* and *Grover's Algorithm* aim to drastically reduce the amount of time it takes to crack them.

IV. SHOR'S ALGORITHM - THIS DEFINITELY NEEDS TO BE BETTER

In 1994, Peter Shor developed a quantum polynomial-time algorithm for integer factorization. This algorithm describes a process for finding factors of a number, even a very large one in a very short amount of time. Integer Factorization serves as the basis for many of the world's currently most secure cryptography algorithms, such as RSA. In layman's terms, Shor's algorithm takes a guess at a number that could share factors with N (but most likely doesn't) and transforms that guess into a much better one that is very likely to be a number that shares factors with N . Shor's algorithm leverages the concept of quantum superposition mentioned earlier to compute factors of these very large numbers at a scale that is unmatched by modern classical computers. In order to compute factors of N

- Consider N , a very large number (eg: An RSA public key)
- In order to crack RSA, we need to find factors of N such that $f(x) = (x^r) \bmod N$.
- Shor's Algorithm shifts the focus to finding period r i.e: $f(x) = f(x + r)$.

- The algorithm uses something known as a *Quantum Fourier Transform* (QFT).
- A quantum computer can be in many states simultaneously, which leads to very fast computing.
- This allows the computer to calculate the period r for all points simultaneously.
- Then the QFT essentially takes these values, transforms them into waves in such a way that they destructively interfere with each other, leaving only the correct value of r .
- This r can then directly be used to solve for a factor of N , thus breaking the encryption.

Shor's algorithm also applies to cryptography schemes that depend on the *Discrete Logarithm Problem*.

V. GROVER'S ALGORITHM

What it works on, how it operates

VI. ALGORITHMS THREATENED BY THE QUANTUM ERA

VII. POST QUANTUM CRYPTOGRAPHY

VIII. CONCLUSION

The conclusion goes here.

APPENDIX A

PROOF OF THE FIRST ZONKLAR EQUATION

Appendix one text goes here.

APPENDIX B

Appendix two text goes here.

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