

Step	Algorithm: $y := Ax + y$
1a	$\{y = \hat{y}$ }
4	$A \rightarrow \begin{pmatrix} A_T \\ A_B \end{pmatrix}, y \rightarrow \begin{pmatrix} y_T \\ y_B \end{pmatrix}$ where A_B has 0 rows, y_B has 0 rows
2	$\left\{ \begin{pmatrix} y_T \\ y_B \end{pmatrix} = \begin{pmatrix} \hat{y}_T \\ A_B x + \hat{y}_B \end{pmatrix} \right\}$
3	while $m(A_B) < m(A)$ do
2,3	$\left\{ \begin{pmatrix} y_T \\ y_B \end{pmatrix} = \begin{pmatrix} \hat{y}_T \\ A_B x + \hat{y}_B \end{pmatrix} \wedge m(A_B) < m(A) \right\}$
5a	$\begin{pmatrix} A_T \\ A_B \end{pmatrix} \rightarrow \begin{pmatrix} A_0 \\ a_1^T \\ A_2 \end{pmatrix}, \begin{pmatrix} y_T \\ y_B \end{pmatrix} \rightarrow \begin{pmatrix} y_0 \\ \psi_1 \\ y_2 \end{pmatrix}$ where a_1 has 1 row, ψ_1 has 1 row
6	$\left\{ \begin{pmatrix} y_0 \\ \psi_1 \\ y_2 \end{pmatrix} = \begin{pmatrix} \hat{y}_0 \\ \hat{\psi}_1 \\ A_2 x + \hat{y}_2 \end{pmatrix} \right\}$
8	$\psi_1 := a_1^T x + \psi_1$
7	$\left\{ \begin{pmatrix} y_0 \\ \psi_1 \\ y_2 \end{pmatrix} = \begin{pmatrix} \hat{y}_0 \\ a_1^T x + \hat{\psi}_1 \\ A_2 x + \hat{y}_2 \end{pmatrix} \right\}$
5b	$\begin{pmatrix} A_T \\ A_B \end{pmatrix} \leftarrow \begin{pmatrix} A_0 \\ a_1^T \\ A_2 \end{pmatrix}, \begin{pmatrix} y_T \\ y_B \end{pmatrix} \leftarrow \begin{pmatrix} y_0 \\ \psi_1 \\ y_2 \end{pmatrix}$
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	endwhile
2,3	$\left\{ \begin{pmatrix} y_T \\ y_B \end{pmatrix} = \begin{pmatrix} \hat{y}_T \\ A_B x + \hat{y}_B \end{pmatrix} \wedge \neg(m(A_B) < m(A)) \right\}$
1b	$\{y = Ax + \hat{y}\}$ }

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