

Step	<b>Algorithm:</b> Solve $Lx = y$ overwriting $y$ with $x$ . $L$ is unit lower triangular.
1a	$\{y = \hat{y}\}$
4	$L \rightarrow \left( \begin{array}{c c} L_{TL} & L_{TR} \\ \hline L_{BL} & L_{BR} \end{array} \right), x \rightarrow \left( \begin{array}{c} x_T \\ x_B \end{array} \right), y \rightarrow \left( \begin{array}{c} y_T \\ y_B \end{array} \right)$ <p>where <math>L_{TL}</math> is <math>0 \times 0</math>, <math>x_T</math> has 0 rows, <math>y_T</math> has 0 rows</p>
2	$\left\{ \left( \begin{array}{c} y_T \\ y_B \end{array} \right) = \left( \begin{array}{c} x_T \\ \hat{y}_B \end{array} \right) \wedge L_{TL}x_T = y_T \right\}$
3	<b>while</b> $m(L_{TL}) < m(L)$ <b>do</b>
2,3	$\left\{ \left( \begin{array}{c} y_T \\ y_B \end{array} \right) = \left( \begin{array}{c} x_T \\ \hat{y}_B \end{array} \right) \wedge L_{TL}x_T = y_T \wedge m(L_{TL}) < m(L) \right\}$
5a	$\left( \begin{array}{c c} L_{TL} & L_{TR} \\ \hline L_{BL} & L_{BR} \end{array} \right) \rightarrow \left( \begin{array}{c c c} L_{00} & l_{01} & L_{02} \\ \hline l_{10}^T & \lambda_{11} & l_{12}^T \\ \hline L_{20} & l_{21} & L_{22} \end{array} \right), \left( \begin{array}{c} x_T \\ x_B \end{array} \right) \rightarrow \left( \begin{array}{c} x_0 \\ \chi_1 \\ x_2 \end{array} \right), \left( \begin{array}{c} y_T \\ y_B \end{array} \right) \rightarrow \left( \begin{array}{c} y_0 \\ \psi_1 \\ y_2 \end{array} \right)$ <p>where <math>\lambda_{11}</math> is <math>1 \times 1</math>, <math>\chi_1</math> has 1 row, <math>\psi_1</math> has 1 row</p>
6	$\left\{ \left( \begin{array}{c} y_0 \\ \psi_1 \\ y_2 \end{array} \right) = \left( \begin{array}{c} x_0 \\ \hat{\psi}_1 \\ \hat{y}_2 \end{array} \right) \wedge L_{00}x_0 = \hat{y}_0 \right\}$
8	$\psi_1 := \chi_1 = \hat{\psi}_1 - l_{10}^T x_0 = \psi_1 - l_{10}^T y_0$
7	$\left\{ \left( \begin{array}{c} y_0 \\ \psi_1 \\ y_2 \end{array} \right) = \left( \begin{array}{c} x_0 \\ \chi_1 \\ \hat{y}_2 \end{array} \right) \wedge \begin{array}{l} L_{00}x_0 = \hat{y}_0 \\ l_{10}^T x_0 + \chi_1 = \hat{\psi}_1 \end{array} \quad (\lambda_{11} = 1 \text{ because } L \text{ is unit lower triangular}) \right\}$
5b	$\left( \begin{array}{c c} L_{TL} & L_{TR} \\ \hline L_{BL} & L_{BR} \end{array} \right) \leftarrow \left( \begin{array}{c c c} L_{00} & l_{01} & L_{02} \\ \hline l_{10}^T & \lambda_{11} & l_{12}^T \\ \hline L_{20} & l_{21} & L_{22} \end{array} \right), \left( \begin{array}{c} x_T \\ x_B \end{array} \right) \leftarrow \left( \begin{array}{c} x_0 \\ \chi_1 \\ x_2 \end{array} \right), \left( \begin{array}{c} y_T \\ y_B \end{array} \right) \leftarrow \left( \begin{array}{c} y_0 \\ \psi_1 \\ y_2 \end{array} \right)$
2	$\left\{ \left( \begin{array}{c} y_T \\ y_B \end{array} \right) = \left( \begin{array}{c} x_T \\ \hat{y}_B \end{array} \right) \wedge L_{TL}x_T = y_T \right\}$
	<b>endwhile</b>
2,3	$\left\{ \left( \begin{array}{c} y_T \\ y_B \end{array} \right) = \left( \begin{array}{c} x_T \\ \hat{y}_B \end{array} \right) \wedge L_{TL}x_T = y_T \wedge \neg(m(L_{TL}) < m(L)) \right\}$
1b	$\{y = x \wedge Lx = \hat{y}\}$

Step	Algorithm: Solve $Lx = y$ overwriting $y$ with $x$ . $L$ is unit lower triangular.
1a	{
4	where
2	{
3	while do
2,3	{ $\wedge$ }
5a	where
6	{
8	
7	{
5b	
2	{
	endwhile
2,3	{ $\wedge \neg($ ) }
1b	}

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	where
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3	while do
2,3	$\left\{ \begin{pmatrix} y_T \\ y_B \end{pmatrix} = \begin{pmatrix} x_T \\ \hat{y}_B \end{pmatrix} \wedge L_{TL}x_T = y_T \wedge \right\}$
5a	
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8	
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3	while $m(L_{TL}) < m(L)$ do
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5b	$\left( \begin{array}{c c} L_{TL} & L_{TR} \\ \hline L_{BL} & L_{BR} \end{array} \right) \leftarrow \left( \begin{array}{c c c} L_{00} & l_{01} & L_{02} \\ \hline l_{10}^T & \lambda_{11} & l_{12}^T \\ \hline L_{20} & l_{21} & L_{22} \end{array} \right), \left( \begin{array}{c} x_T \\ x_B \end{array} \right) \leftarrow \left( \begin{array}{c} x_0 \\ \chi_1 \\ x_2 \end{array} \right), \left( \begin{array}{c} y_T \\ y_B \end{array} \right) \leftarrow \left( \begin{array}{c} y_0 \\ \psi_1 \\ y_2 \end{array} \right)$
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2	$\left\{ \left( \begin{array}{c} y_T \\ y_B \end{array} \right) = \left( \begin{array}{c} x_T \\ \hat{y}_B \end{array} \right) \wedge L_{TL}x_T = y_T \right\}$
	<b>endwhile</b>
2,3	$\left\{ \left( \begin{array}{c} y_T \\ y_B \end{array} \right) = \left( \begin{array}{c} x_T \\ \hat{y}_B \end{array} \right) \wedge L_{TL}x_T = y_T \wedge \neg(m(L_{TL}) < m(L)) \right\}$
1b	$\{y = x \wedge Lx = \hat{y}$ }

	<b>Algorithm:</b> Solve $Lx = y$ overwriting $y$ with $x$ . $L$ is unit lower triangular.
	$L \rightarrow \left( \begin{array}{c c} L_{TL} & L_{TR} \\ \hline L_{BL} & L_{BR} \end{array} \right), x \rightarrow \begin{pmatrix} x_T \\ x_B \end{pmatrix}, y \rightarrow \begin{pmatrix} y_T \\ y_B \end{pmatrix}$ <p>where <math>L_{TL}</math> is <math>0 \times 0</math>, <math>x_T</math> has 0 rows, <math>y_T</math> has 0 rows</p>
	<b>while</b> $m(L_{TL}) < m(L)$ <b>do</b>
	$\left( \begin{array}{c c} L_{TL} & L_{TR} \\ \hline L_{BL} & L_{BR} \end{array} \right) \rightarrow \left( \begin{array}{c c c} L_{00} & l_{01} & L_{02} \\ \hline l_{10}^T & \lambda_{11} & l_{12}^T \\ \hline L_{20} & l_{21} & L_{22} \end{array} \right), \begin{pmatrix} x_T \\ x_B \end{pmatrix} \rightarrow \begin{pmatrix} x_0 \\ \chi_1 \\ x_2 \end{pmatrix}, \begin{pmatrix} y_T \\ y_B \end{pmatrix} \rightarrow \begin{pmatrix} y_0 \\ \psi_1 \\ y_2 \end{pmatrix}$ <p>where <math>\lambda_{11}</math> is <math>1 \times 1</math>, <math>\chi_1</math> has 1 row, <math>\psi_1</math> has 1 row</p>
	$\psi_1 := \chi_1 = \hat{\psi}_1 - l_{10}^T x_0 = \psi_1 - l_{10}^T y_0$
	$\left( \begin{array}{c c} L_{TL} & L_{TR} \\ \hline L_{BL} & L_{BR} \end{array} \right) \leftarrow \left( \begin{array}{c c c} L_{00} & l_{01} & L_{02} \\ \hline l_{10}^T & \lambda_{11} & l_{12}^T \\ \hline L_{20} & l_{21} & L_{22} \end{array} \right), \begin{pmatrix} x_T \\ x_B \end{pmatrix} \leftarrow \begin{pmatrix} x_0 \\ \chi_1 \\ x_2 \end{pmatrix}, \begin{pmatrix} y_T \\ y_B \end{pmatrix} \leftarrow \begin{pmatrix} y_0 \\ \psi_1 \\ y_2 \end{pmatrix}$
	<b>endwhile</b>

**Algorithm:** Solve  $Lx = y$  overwriting  $y$  with  $x$ .  $L$  is unit lower triangular.

$$L \rightarrow \left( \begin{array}{c|c} L_{TL} & L_{TR} \\ \hline L_{BL} & L_{BR} \end{array} \right), x \rightarrow \begin{pmatrix} x_T \\ x_B \end{pmatrix}, y \rightarrow \begin{pmatrix} y_T \\ y_B \end{pmatrix}$$

**where**  $L_{TL}$  is  $0 \times 0$ ,  $x_T$  has 0 rows,  $y_T$  has 0 rows

**while**  $m(L_{TL}) < m(L)$  **do**

$$\left( \begin{array}{c|c} L_{TL} & L_{TR} \\ \hline L_{BL} & L_{BR} \end{array} \right) \rightarrow \left( \begin{array}{c|c} L_{00} & l_{01} \ L_{02} \\ \hline l_{10}^T & \lambda_{11} \ l_{12}^T \\ L_{20} & l_{21} \ L_{22} \end{array} \right), \begin{pmatrix} x_T \\ x_B \end{pmatrix} \rightarrow \begin{pmatrix} x_0 \\ \chi_1 \\ x_2 \end{pmatrix}, \begin{pmatrix} y_T \\ y_B \end{pmatrix} \rightarrow \begin{pmatrix} y_0 \\ \psi_1 \\ y_2 \end{pmatrix}$$

**where**  $\lambda_{11}$  is  $1 \times 1$ ,  $\chi_1$  has 1 row,  $\psi_1$  has 1 row

$$\psi_1 := \chi_1 = \hat{\psi}_1 - l_{10}^T x_0 = \psi_1 - l_{10}^T y_0$$

$$\left( \begin{array}{c|c} L_{TL} & L_{TR} \\ \hline L_{BL} & L_{BR} \end{array} \right) \leftarrow \left( \begin{array}{c|c} L_{00} \ l_{01} & L_{02} \\ \hline l_{10}^T \ \lambda_{11} & l_{12}^T \\ L_{20} \ l_{21} & L_{22} \end{array} \right), \begin{pmatrix} x_T \\ x_B \end{pmatrix} \leftarrow \begin{pmatrix} x_0 \\ \chi_1 \\ x_2 \end{pmatrix}, \begin{pmatrix} y_T \\ y_B \end{pmatrix} \leftarrow \begin{pmatrix} y_0 \\ \psi_1 \\ y_2 \end{pmatrix}$$

**endwhile**