

Step	Algorithm: $y := Ax + y$ (A symmetric stored in lower triangular part)
1a	$\{y = \hat{y}$ }
4	$A \rightarrow \left(\begin{array}{c c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right), x \rightarrow \left(\begin{array}{c} x_T \\ x_B \end{array} \right), y \rightarrow \left(\begin{array}{c} y_T \\ y_B \end{array} \right)$ where A_{TL} is 0×0 , x_T has 0 rows, y_T has 0 rows
2	$\left\{ \left(\begin{array}{c} y_T \\ y_B \end{array} \right) = \left(\begin{array}{c} A_{TL}x_T + A_{BL}^T x_B + \hat{y}_T \\ A_{BL}x_T + \hat{y}_B \end{array} \right) \right\}$
3	while $m(A_{TL}) < m(A)$ do
2,3	$\left\{ \left(\begin{array}{c} y_T \\ y_B \end{array} \right) = \left(\begin{array}{c} A_{TL}x_T + A_{BL}^T x_B + \hat{y}_T \\ A_{BL}x_T + \hat{y}_B \end{array} \right) \wedge m(A_{TL}) < m(A) \right\}$
5a	$\left(\begin{array}{c c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right) \rightarrow \left(\begin{array}{c cc} A_{00} & a_{01} & A_{02} \\ \hline a_{10}^T & \alpha_{11} & a_{12}^T \\ A_{20} & a_{21} & A_{22} \end{array} \right), \left(\begin{array}{c} x_T \\ x_B \end{array} \right) \rightarrow \left(\begin{array}{c} x_0 \\ \chi_1 \\ x_2 \end{array} \right), \left(\begin{array}{c} y_T \\ y_B \end{array} \right) \rightarrow \left(\begin{array}{c} y_0 \\ \psi_1 \\ y_2 \end{array} \right)$ where α_{11} is 1×1 , χ_1 has 1 row, ψ_1 has 1 row
6	$\left\{ \left(\begin{array}{c} y_0 \\ \psi_1 \\ y_2 \end{array} \right) = \left(\begin{array}{c} A_{00}x_0 + \chi_1(a_{10}^T)^T + A_{20}^T x_2 + \hat{y}_0 \\ a_{10}^T x_0 + \hat{\psi}_1 \\ A_{20}x_0 + \hat{y}_2 \end{array} \right) \right\}$
8	$\psi_1 := \alpha_{11}\chi_1 + a_{21}^T x_2 + \psi_1$ $y_2 := \chi_1 a_{21} + y_2$
7	$\left\{ \left(\begin{array}{c} y_0 \\ \psi_1 \\ y_2 \end{array} \right) = \left(\begin{array}{c} A_{00}x_0 + \chi_1(a_{10}^T)^T + A_{20}^T x_2 + \hat{y}_0 \\ a_{10}^T x_0 + \alpha_{11}\chi_1 + a_{21}^T x_2 + \hat{\psi}_1 \\ A_{20}x_0 + \chi_1 a_{21} + \hat{y}_2 \end{array} \right) \right\}$
5b	$\left(\begin{array}{c c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right) \leftarrow \left(\begin{array}{c cc} A_{00} & a_{01} & A_{02} \\ \hline a_{10}^T & \alpha_{11} & a_{12}^T \\ A_{20} & a_{21} & A_{22} \end{array} \right), \left(\begin{array}{c} x_T \\ x_B \end{array} \right) \leftarrow \left(\begin{array}{c} x_0 \\ \chi_1 \\ x_2 \end{array} \right), \left(\begin{array}{c} y_T \\ y_B \end{array} \right) \leftarrow \left(\begin{array}{c} y_0 \\ \psi_1 \\ y_2 \end{array} \right)$
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	endwhile
2,3	$\left\{ \left(\begin{array}{c} y_T \\ y_B \end{array} \right) = \left(\begin{array}{c} A_{TL}x_T + A_{BL}^T x_B + \hat{y}_T \\ A_{BL}x_T + \hat{y}_B \end{array} \right) \wedge \neg(m(A_{TL}) < m(A)) \right\}$
1b	$\{y = Ax + \hat{y}$ }

Step	Algorithm: $y := Ax + y$ (A symmetric stored in lower triangular part)
1a	{
4	where
2	{
3	while do
2,3	{ \wedge }
5a	where
6	{
8	
7	{
5b	
2	{
	endwhile
2,3	{ $\wedge \neg($) }
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3	while do
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6	$\left\{ \right\}$
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1b	$\{y = Ax + \hat{y}\}$

	Algorithm: $y := Ax + y$ (A symmetric stored in lower triangular part)
	$A \rightarrow \left(\begin{array}{c c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right), x \rightarrow \left(\begin{array}{c} x_T \\ x_B \end{array} \right), y \rightarrow \left(\begin{array}{c} y_T \\ y_B \end{array} \right)$ <p>where A_{TL} is 0×0, x_T has 0 rows, y_T has 0 rows</p>
	while $m(A_{TL}) < m(A)$ do
	$\left(\begin{array}{c c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right) \rightarrow \left(\begin{array}{c cc} A_{00} & a_{01} & A_{02} \\ \hline a_{10}^T & \alpha_{11} & a_{12}^T \\ A_{20} & a_{21} & A_{22} \end{array} \right), \left(\begin{array}{c} x_T \\ x_B \end{array} \right) \rightarrow \left(\begin{array}{c} x_0 \\ \chi_1 \\ x_2 \end{array} \right), \left(\begin{array}{c} y_T \\ y_B \end{array} \right) \rightarrow \left(\begin{array}{c} y_0 \\ \psi_1 \\ y_2 \end{array} \right)$ <p>where α_{11} is 1×1, χ_1 has 1 row, ψ_1 has 1 row</p>
	$\psi_1 := \alpha_{11}\chi_1 + a_{21}^T x_2 + \psi_1$ $y_2 := \chi_1 a_{21} + y_2$
	$\left(\begin{array}{c c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right) \leftarrow \left(\begin{array}{c cc} A_{00} & a_{01} & A_{02} \\ \hline a_{10}^T & \alpha_{11} & a_{12}^T \\ A_{20} & a_{21} & A_{22} \end{array} \right), \left(\begin{array}{c} x_T \\ x_B \end{array} \right) \leftarrow \left(\begin{array}{c} x_0 \\ \chi_1 \\ x_2 \end{array} \right), \left(\begin{array}{c} y_T \\ y_B \end{array} \right) \leftarrow \left(\begin{array}{c} y_0 \\ \psi_1 \\ y_2 \end{array} \right)$
	endwhile

Algorithm: $y := Ax + y$ (A symmetric stored in lower triangular part)

$$A \rightarrow \left(\begin{array}{c|c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right), x \rightarrow \left(\begin{array}{c} x_T \\ x_B \end{array} \right), y \rightarrow \left(\begin{array}{c} y_T \\ y_B \end{array} \right)$$

where A_{TL} is 0×0 , x_T has 0 rows, y_T has 0 rows

while $m(A_{TL}) < m(A)$ **do**

$$\left(\begin{array}{c|c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right) \rightarrow \left(\begin{array}{c|c} A_{00} & a_{01} \ A_{02} \\ \hline a_{10}^T & \alpha_{11} \ a_{12}^T \\ A_{20} & a_{21} \ A_{22} \end{array} \right), \left(\begin{array}{c} x_T \\ x_B \end{array} \right) \rightarrow \left(\begin{array}{c} x_0 \\ \chi_1 \\ x_2 \end{array} \right), \left(\begin{array}{c} y_T \\ y_B \end{array} \right) \rightarrow \left(\begin{array}{c} y_0 \\ \psi_1 \\ y_2 \end{array} \right)$$

where α_{11} is 1×1 , χ_1 has 1 row, ψ_1 has 1 row

$$\psi_1 := \alpha_{11}\chi_1 + a_{21}^T x_2 + \psi_1$$

$$y_2 := \chi_1 a_{21} + y_2$$

$$\left(\begin{array}{c|c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right) \leftarrow \left(\begin{array}{c|c} A_{00} \ a_{01} & A_{02} \\ \hline a_{10}^T \ \alpha_{11} & a_{12}^T \\ A_{20} \ a_{21} & A_{22} \end{array} \right), \left(\begin{array}{c} x_T \\ x_B \end{array} \right) \leftarrow \left(\begin{array}{c} x_0 \\ \chi_1 \\ x_2 \end{array} \right), \left(\begin{array}{c} y_T \\ y_B \end{array} \right) \leftarrow \left(\begin{array}{c} y_0 \\ \psi_1 \\ y_2 \end{array} \right)$$

endwhile