

Step	Algorithm: $A := xy^T + A$
1a	$\{A = \widehat{A}$ $\}$
4	$y \rightarrow \begin{pmatrix} y_T \\ \frac{y_T}{y_B} \end{pmatrix}, A \rightarrow \left(A_L \middle A_R \right)$ where y_T has 0 rows, A_L has 0 columns
2	$\left\{ \left(A_L \middle A_R \right) = \left(xy_T^T + \widehat{A}_L \middle \widehat{A}_R \right) \right\}$
3	while $m(y_T) < m(y)$ do
2,3	$\left\{ \left(A_L \middle A_R \right) = \left(xy_T^T + \widehat{A}_L \middle \widehat{A}_R \right) \wedge m(y_T) < m(y) \right\}$
5a	$\begin{pmatrix} y_T \\ \frac{y_T}{y_B} \end{pmatrix} \rightarrow \begin{pmatrix} y_0 \\ \psi_1 \\ y_2 \end{pmatrix}, \left(A_L \middle A_R \right) \rightarrow \left(A_0 \middle a_1 \ A_2 \right)$ where ψ_1 has 1 row, a_1 has 1 column
6	$\left\{ \left(A_0 \ a_1 \ A_2 \right) = \left(xy_0^T + \widehat{A}_0 \ \widehat{a}_1 \ \widehat{A}_2 \right) \right\}$
8	$a_1 := \psi_1 x + a_1$
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5b	$\begin{pmatrix} y_T \\ \frac{y_T}{y_B} \end{pmatrix} \leftarrow \begin{pmatrix} y_0 \\ \psi_1 \\ y_2 \end{pmatrix}, A \rightarrow \left(A_L \middle A_R \right) \leftarrow \left(A_0 \ a_1 \middle A_2 \right)$
2	$\left\{ \left(A_L \middle A_R \right) = \left(xy_T^T + \widehat{A}_L \middle \widehat{A}_R \right) \right\}$
	endwhile
2,3	$\left\{ \left(A_L \middle A_R \right) = \left(xy_T^T + \widehat{A}_L \middle \widehat{A}_R \right) \wedge \neg(m(y_T) < m(y)) \right\}$
1b	$\{A = xy^T + A$ $\}$

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4	where
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3	while do
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	endwhile
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