

Step	Algorithm: $A = \hat{A}$
1a	$\{A = \hat{A}$ }
4	$x \rightarrow \begin{pmatrix} x_T \\ x_B \end{pmatrix}, A \rightarrow \begin{pmatrix} A_T \\ A_B \end{pmatrix}$ <p style="text-align: center;">where x_T has 0 rows, A_T has 0 rows</p>
2	$\left\{ \begin{pmatrix} A_T \\ A_B \end{pmatrix} = \begin{pmatrix} x_T y^T + \hat{A}_T \\ \hat{A}_B \end{pmatrix} \right\}$
3	while $m(x_T) < m(x)$ do
2,3	$\left\{ \begin{pmatrix} A_T \\ A_B \end{pmatrix} = \begin{pmatrix} x_T y^T + \hat{A}_T \\ \hat{A}_B \end{pmatrix} \wedge m(x_T) < m(x) \right\}$
5a	$\begin{pmatrix} x_T \\ x_B \end{pmatrix} \rightarrow \begin{pmatrix} x_0 \\ \chi_1 \\ x_2 \end{pmatrix}, \begin{pmatrix} A_T \\ A_B \end{pmatrix} \rightarrow \begin{pmatrix} A_0 \\ a_1^T \\ A_2 \end{pmatrix}$ <p style="text-align: center;">where χ_1 has 1 row, a_1 has 1 row</p>
6	$\left\{ \begin{pmatrix} A_0 \\ a_1^T \\ A_2 \end{pmatrix} = \begin{pmatrix} x_0 y^T + \hat{A}_0 \\ \hat{a}_1^T \\ \hat{A}_2 \end{pmatrix} \right\}$
8	$a_1^T := \chi_1 y^T + a_1^T$
7	$\left\{ \begin{pmatrix} A_0 \\ a_1^T \\ A_2 \end{pmatrix} = \begin{pmatrix} x_0 y^T + \hat{A}_0 \\ \chi_1 y^T + \hat{a}_1^T \\ \hat{A}_2 \end{pmatrix} \right\}$
5b	$\begin{pmatrix} x_T \\ x_B \end{pmatrix} \leftarrow \begin{pmatrix} x_0 \\ \chi_1 \\ x_2 \end{pmatrix}, \begin{pmatrix} A_T \\ A_B \end{pmatrix} \leftarrow \begin{pmatrix} A_0 \\ a_1^T \\ A_2 \end{pmatrix}$
2	$\left\{ \begin{pmatrix} A_T \\ A_B \end{pmatrix} = \begin{pmatrix} x_T y^T + \hat{A}_T \\ \hat{A}_B \end{pmatrix} \right\}$
	endwhile
2,3	$\left\{ \begin{pmatrix} A_T \\ A_B \end{pmatrix} = \begin{pmatrix} x_T y^T + \hat{A}_T \\ \hat{A}_B \end{pmatrix} \wedge \neg(m(x_T) < m(x)) \right\}$
1b	$\{A = x y^T + \hat{A}$ }

Step	Algorithm: $A = \hat{A}$
1a	{
4	
	where
2	{
3	while do
2,3	{ \wedge
5a	
	where
6	{
8	
7	{
5b	
2	{
	endwhile
2,3	{ $\wedge \neg($)
1b	{

Step	Algorithm: $A = \hat{A}$
1a	{ $A = \hat{A}$ }
4	where
2	{
3	while do
2,3	{ \wedge }
5a	where
6	{
8	
7	{
5b	
2	{
	endwhile
2,3	{ $\wedge \neg($) }
1b	{ $A = xy^T + \hat{A}$ }

Step	Algorithm: $A = \hat{A}$
1a	$\{A = \hat{A}$ }
4	
	where
2	$\left\{ \left(\frac{A_T}{A_B} \right) = \left(\frac{x_T y^T + \hat{A}_T}{\hat{A}_B} \right) \right\}$
3	while do
2,3	$\left\{ \left(\frac{A_T}{A_B} \right) = \left(\frac{x_T y^T + \hat{A}_T}{\hat{A}_B} \right) \wedge \right\}$
5a	
	where
6	$\left\{ \right.$
8	
7	$\left\{ \right.$
5b	
2	$\left\{ \left(\frac{A_T}{A_B} \right) = \left(\frac{x_T y^T + \hat{A}_T}{\hat{A}_B} \right) \right\}$
	endwhile
2,3	$\left\{ \left(\frac{A_T}{A_B} \right) = \left(\frac{x_T y^T + \hat{A}_T}{\hat{A}_B} \right) \wedge \neg(\quad) \right\}$
1b	$\{A = xy^T + \hat{A}$ }

Step	Algorithm: $A = \hat{A}$
1a	$\{A = \hat{A}$ }
4	
	where
2	$\left\{ \left(\frac{A_T}{A_B} \right) = \left(\frac{x_T y^T + \hat{A}_T}{\hat{A}_B} \right) \right\}$
3	while $m(x_T) < m(x)$ do
2,3	$\left\{ \left(\frac{A_T}{A_B} \right) = \left(\frac{x_T y^T + \hat{A}_T}{\hat{A}_B} \right) \wedge m(x_T) < m(x) \right\}$
5a	
	where
6	$\left\{ \right\}$
8	
7	$\left\{ \right\}$
5b	
2	$\left\{ \left(\frac{A_T}{A_B} \right) = \left(\frac{x_T y^T + \hat{A}_T}{\hat{A}_B} \right) \right\}$
	endwhile
2,3	$\left\{ \left(\frac{A_T}{A_B} \right) = \left(\frac{x_T y^T + \hat{A}_T}{\hat{A}_B} \right) \wedge \neg(m(x_T) < m(x)) \right\}$
1b	$\{A = xy^T + \hat{A}$ }

Step	Algorithm: $A = \hat{A}$
1a	$\{A = \hat{A}$ }
4	$x \rightarrow \left(\frac{x_T}{x_B} \right), A \rightarrow \left(\frac{A_T}{A_B} \right)$ where x_T has 0 rows, A_T has 0 rows
2	$\left\{ \left(\frac{A_T}{A_B} \right) = \left(\frac{x_T y^T + \hat{A}_T}{\hat{A}_B} \right) \right\}$
3	while $m(x_T) < m(x)$ do
2,3	$\left\{ \left(\frac{A_T}{A_B} \right) = \left(\frac{x_T y^T + \hat{A}_T}{\hat{A}_B} \right) \wedge m(x_T) < m(x) \right\}$
5a	where
6	$\left\{ \right.$
8	
7	$\left\{ \right.$
5b	
2	$\left\{ \left(\frac{A_T}{A_B} \right) = \left(\frac{x_T y^T + \hat{A}_T}{\hat{A}_B} \right) \right\}$
	endwhile
2,3	$\left\{ \left(\frac{A_T}{A_B} \right) = \left(\frac{x_T y^T + \hat{A}_T}{\hat{A}_B} \right) \wedge \neg(m(x_T) < m(x)) \right\}$
1b	$\{A = x y^T + \hat{A}$ }

Step	Algorithm: $A = \hat{A}$
1a	$\{A = \hat{A}$ }
4	$x \rightarrow \begin{pmatrix} x_T \\ x_B \end{pmatrix}, A \rightarrow \begin{pmatrix} A_T \\ A_B \end{pmatrix}$ where x_T has 0 rows, A_T has 0 rows
2	$\left\{ \begin{pmatrix} A_T \\ A_B \end{pmatrix} = \begin{pmatrix} x_T y^T + \hat{A}_T \\ \hat{A}_B \end{pmatrix} \right\}$
3	while $m(x_T) < m(x)$ do
2,3	$\left\{ \begin{pmatrix} A_T \\ A_B \end{pmatrix} = \begin{pmatrix} x_T y^T + \hat{A}_T \\ \hat{A}_B \end{pmatrix} \wedge m(x_T) < m(x) \right\}$
5a	$\begin{pmatrix} x_T \\ x_B \end{pmatrix} \rightarrow \begin{pmatrix} x_0 \\ \chi_1 \\ x_2 \end{pmatrix}, \begin{pmatrix} A_T \\ A_B \end{pmatrix} \rightarrow \begin{pmatrix} A_0 \\ a_1^T \\ A_2 \end{pmatrix}$ where χ_1 has 1 row, a_1 has 1 row
6	$\left\{ \right\}$
8	
7	$\left\{ \right\}$
5b	$\begin{pmatrix} x_T \\ x_B \end{pmatrix} \leftarrow \begin{pmatrix} x_0 \\ \chi_1 \\ x_2 \end{pmatrix}, \begin{pmatrix} A_T \\ A_B \end{pmatrix} \leftarrow \begin{pmatrix} A_0 \\ a_1^T \\ A_2 \end{pmatrix}$
2	$\left\{ \begin{pmatrix} A_T \\ A_B \end{pmatrix} = \begin{pmatrix} x_T y^T + \hat{A}_T \\ \hat{A}_B \end{pmatrix} \right\}$
	endwhile
2,3	$\left\{ \begin{pmatrix} A_T \\ A_B \end{pmatrix} = \begin{pmatrix} x_T y^T + \hat{A}_T \\ \hat{A}_B \end{pmatrix} \wedge \neg(m(x_T) < m(x)) \right\}$
1b	$\{A = x y^T + \hat{A}$ }

Step	Algorithm: $A = \hat{A}$
1a	$\{A = \hat{A}$ }
4	$x \rightarrow \begin{pmatrix} x_T \\ x_B \end{pmatrix}, A \rightarrow \begin{pmatrix} A_T \\ A_B \end{pmatrix}$ where x_T has 0 rows, A_T has 0 rows
2	$\left\{ \begin{pmatrix} A_T \\ A_B \end{pmatrix} = \begin{pmatrix} x_T y^T + \hat{A}_T \\ \hat{A}_B \end{pmatrix} \right\}$
3	while $m(x_T) < m(x)$ do
2,3	$\left\{ \begin{pmatrix} A_T \\ A_B \end{pmatrix} = \begin{pmatrix} x_T y^T + \hat{A}_T \\ \hat{A}_B \end{pmatrix} \wedge m(x_T) < m(x) \right\}$
5a	$\begin{pmatrix} x_T \\ x_B \end{pmatrix} \rightarrow \begin{pmatrix} x_0 \\ \chi_1 \\ x_2 \end{pmatrix}, \begin{pmatrix} A_T \\ A_B \end{pmatrix} \rightarrow \begin{pmatrix} A_0 \\ a_1^T \\ A_2 \end{pmatrix}$ where χ_1 has 1 row, a_1 has 1 row
6	$\left\{ \begin{pmatrix} A_0 \\ a_1^T \\ A_2 \end{pmatrix} = \begin{pmatrix} x_0 y^T + \hat{A}_0 \\ \hat{a}_1^T \\ \hat{A}_2 \end{pmatrix} \right\}$
8	
7	$\left\{ \right\}$
5b	$\begin{pmatrix} x_T \\ x_B \end{pmatrix} \leftarrow \begin{pmatrix} x_0 \\ \chi_1 \\ x_2 \end{pmatrix}, \begin{pmatrix} A_T \\ A_B \end{pmatrix} \leftarrow \begin{pmatrix} A_0 \\ a_1^T \\ A_2 \end{pmatrix}$
2	$\left\{ \begin{pmatrix} A_T \\ A_B \end{pmatrix} = \begin{pmatrix} x_T y^T + \hat{A}_T \\ \hat{A}_B \end{pmatrix} \right\}$
	endwhile
2,3	$\left\{ \begin{pmatrix} A_T \\ A_B \end{pmatrix} = \begin{pmatrix} x_T y^T + \hat{A}_T \\ \hat{A}_B \end{pmatrix} \wedge \neg(m(x_T) < m(x)) \right\}$
1b	$\{A = x y^T + \hat{A}$ }

Step	Algorithm: $A = \hat{A}$
1a	$\{A = \hat{A}$ }
4	$x \rightarrow \begin{pmatrix} x_T \\ x_B \end{pmatrix}, A \rightarrow \begin{pmatrix} A_T \\ A_B \end{pmatrix}$ <p>where x_T has 0 rows, A_T has 0 rows</p>
2	$\left\{ \begin{pmatrix} A_T \\ A_B \end{pmatrix} = \begin{pmatrix} x_T y^T + \hat{A}_T \\ \hat{A}_B \end{pmatrix} \right\}$
3	while $m(x_T) < m(x)$ do
2,3	$\left\{ \begin{pmatrix} A_T \\ A_B \end{pmatrix} = \begin{pmatrix} x_T y^T + \hat{A}_T \\ \hat{A}_B \end{pmatrix} \wedge m(x_T) < m(x) \right\}$
5a	$\begin{pmatrix} x_T \\ x_B \end{pmatrix} \rightarrow \begin{pmatrix} x_0 \\ \chi_1 \\ x_2 \end{pmatrix}, \begin{pmatrix} A_T \\ A_B \end{pmatrix} \rightarrow \begin{pmatrix} A_0 \\ a_1^T \\ A_2 \end{pmatrix}$ <p>where χ_1 has 1 row, a_1 has 1 row</p>
6	$\left\{ \begin{pmatrix} A_0 \\ a_1^T \\ A_2 \end{pmatrix} = \begin{pmatrix} x_0 y^T + \hat{A}_0 \\ \hat{a}_1^T \\ \hat{A}_2 \end{pmatrix} \right\}$
8	
7	$\left\{ \begin{pmatrix} A_0 \\ a_1^T \\ A_2 \end{pmatrix} = \begin{pmatrix} x_0 y^T + \hat{A}_0 \\ \chi_1 y^T + \hat{a}_1^T \\ \hat{A}_2 \end{pmatrix} \right\}$
5b	$\begin{pmatrix} x_T \\ x_B \end{pmatrix} \leftarrow \begin{pmatrix} x_0 \\ \chi_1 \\ x_2 \end{pmatrix}, \begin{pmatrix} A_T \\ A_B \end{pmatrix} \leftarrow \begin{pmatrix} A_0 \\ a_1^T \\ A_2 \end{pmatrix}$
2	$\left\{ \begin{pmatrix} A_T \\ A_B \end{pmatrix} = \begin{pmatrix} x_T y^T + \hat{A}_T \\ \hat{A}_B \end{pmatrix} \right\}$
	endwhile
2,3	$\left\{ \begin{pmatrix} A_T \\ A_B \end{pmatrix} = \begin{pmatrix} x_T y^T + \hat{A}_T \\ \hat{A}_B \end{pmatrix} \wedge \neg(m(x_T) < m(x)) \right\}$
1b	$\{A = x y^T + \hat{A}$ }

Step	Algorithm: $A = \hat{A}$
1a	$\{A = \hat{A}$ }
4	$x \rightarrow \begin{pmatrix} x_T \\ x_B \end{pmatrix}, A \rightarrow \begin{pmatrix} A_T \\ A_B \end{pmatrix}$ <p>where x_T has 0 rows, A_T has 0 rows</p>
2	$\left\{ \begin{pmatrix} A_T \\ A_B \end{pmatrix} = \begin{pmatrix} x_T y^T + \hat{A}_T \\ \hat{A}_B \end{pmatrix} \right\}$
3	while $m(x_T) < m(x)$ do
2,3	$\left\{ \begin{pmatrix} A_T \\ A_B \end{pmatrix} = \begin{pmatrix} x_T y^T + \hat{A}_T \\ \hat{A}_B \end{pmatrix} \wedge m(x_T) < m(x) \right\}$
5a	$\begin{pmatrix} x_T \\ x_B \end{pmatrix} \rightarrow \begin{pmatrix} x_0 \\ \chi_1 \\ x_2 \end{pmatrix}, \begin{pmatrix} A_T \\ A_B \end{pmatrix} \rightarrow \begin{pmatrix} A_0 \\ a_1^T \\ A_2 \end{pmatrix}$ <p>where χ_1 has 1 row, a_1 has 1 row</p>
6	$\left\{ \begin{pmatrix} A_0 \\ a_1^T \\ A_2 \end{pmatrix} = \begin{pmatrix} x_0 y^T + \hat{A}_0 \\ \hat{a}_1^T \\ \hat{A}_2 \end{pmatrix} \right\}$
8	$a_1^T := \chi_1 y^T + a_1^T$
7	$\left\{ \begin{pmatrix} A_0 \\ a_1^T \\ A_2 \end{pmatrix} = \begin{pmatrix} x_0 y^T + \hat{A}_0 \\ \chi_1 y^T + \hat{a}_1^T \\ \hat{A}_2 \end{pmatrix} \right\}$
5b	$\begin{pmatrix} x_T \\ x_B \end{pmatrix} \leftarrow \begin{pmatrix} x_0 \\ \chi_1 \\ x_2 \end{pmatrix}, \begin{pmatrix} A_T \\ A_B \end{pmatrix} \leftarrow \begin{pmatrix} A_0 \\ a_1^T \\ A_2 \end{pmatrix}$
2	$\left\{ \begin{pmatrix} A_T \\ A_B \end{pmatrix} = \begin{pmatrix} x_T y^T + \hat{A}_T \\ \hat{A}_B \end{pmatrix} \right\}$
	endwhile
2,3	$\left\{ \begin{pmatrix} A_T \\ A_B \end{pmatrix} = \begin{pmatrix} x_T y^T + \hat{A}_T \\ \hat{A}_B \end{pmatrix} \wedge \neg(m(x_T) < m(x)) \right\}$
1b	$\{A = x y^T + \hat{A}$ }

	Algorithm: $A = \widehat{A}$
	$x \rightarrow \begin{pmatrix} x_T \\ \frac{x_T}{x_B} \end{pmatrix}, A \rightarrow \begin{pmatrix} A_T \\ \frac{A_T}{A_B} \end{pmatrix}$ <p>where x_T has 0 rows, A_T has 0 rows</p>
	while $m(x_T) < m(x)$ do
	$\begin{pmatrix} x_T \\ \frac{x_T}{x_B} \end{pmatrix} \rightarrow \begin{pmatrix} x_0 \\ \chi_1 \\ x_2 \end{pmatrix}, \begin{pmatrix} A_T \\ \frac{A_T}{A_B} \end{pmatrix} \rightarrow \begin{pmatrix} A_0 \\ a_1^T \\ A_2 \end{pmatrix}$ <p>where χ_1 has 1 row, a_1 has 1 row</p>
	$a_1^T := \chi_1 y^T + a_1^T$
	$\begin{pmatrix} x_T \\ \frac{x_T}{x_B} \end{pmatrix} \leftarrow \begin{pmatrix} x_0 \\ \chi_1 \\ x_2 \end{pmatrix}, \begin{pmatrix} A_T \\ \frac{A_T}{A_B} \end{pmatrix} \leftarrow \begin{pmatrix} A_0 \\ a_1^T \\ A_2 \end{pmatrix}$
	endwhile

Algorithm: $A = \widehat{A}$
$x \rightarrow \begin{pmatrix} x_T \\ \frac{x_T}{x_B} \end{pmatrix}, A \rightarrow \begin{pmatrix} A_T \\ \frac{A_T}{A_B} \end{pmatrix}$ <p>where x_T has 0 rows, A_T has 0 rows</p> <p>while $m(x_T) < m(x)$ do</p> $\begin{pmatrix} x_T \\ \frac{x_T}{x_B} \end{pmatrix} \rightarrow \begin{pmatrix} x_0 \\ \frac{\chi_1}{x_2} \end{pmatrix}, \begin{pmatrix} A_T \\ \frac{A_T}{A_B} \end{pmatrix} \rightarrow \begin{pmatrix} A_0 \\ \frac{a_1^T}{A_2} \end{pmatrix}$ <p>where χ_1 has 1 row, a_1 has 1 row</p>
$a_1^T := \chi_1 y^T + a_1^T$
$\begin{pmatrix} x_T \\ \frac{x_T}{x_B} \end{pmatrix} \leftarrow \begin{pmatrix} x_0 \\ \frac{\chi_1}{x_2} \end{pmatrix}, \begin{pmatrix} A_T \\ \frac{A_T}{A_B} \end{pmatrix} \leftarrow \begin{pmatrix} A_0 \\ \frac{a_1^T}{A_2} \end{pmatrix}$ <p>endwhile</p>