

| | |
|------|--|
| Step | Algorithm: $y := Ax + y$ |
| 1a | $\{y = \widehat{y}\}$ |
| 4 | $A \rightarrow \left(A_L \left A_R \right. \right), x \rightarrow \left(\frac{x_T}{x_B} \right)$ where A_R has 0 columns, x_B has 0 rows |
| 2 | $\{y = A_R x_B + \widehat{y}\}$ |
| 3 | while $n(A_R) < n(A)$ do |
| 2,3 | $\{y = A_R x_B + \widehat{y} \wedge n(A_R) < n(A)\}$ |
| 5a | $\left(A_L \left A_R \right. \right) \rightarrow \left(A_0 \ a_1 \left A_2 \right. \right), \left(\frac{x_T}{x_B} \right) \rightarrow \left(\frac{x_0}{\chi_1} \right)$ where a_1 has 1 column, χ_1 has 1 row |
| 6 | $\{y = A_2 x_2 + \widehat{y}\}$ |
| 8 | $y := \chi_1 a_1 + y$ |
| 7 | $\{y = \chi_1 a_1 + A_2 x_2 + \widehat{y}\}$ |
| 5b | $A \rightarrow \left(A_L \left A_R \right. \right) \leftarrow \left(A_0 \left a_1 \ A_2 \right. \right), \left(\frac{x_T}{x_B} \right) \leftarrow \left(\frac{x_0}{\chi_1} \right)$ $\left(\frac{x_0}{\chi_1} \right)$ |
| 2 | $\{y = A_R x_B + \widehat{y}\}$ |
| | endwhile |
| 2,3 | $\{y = A_R x_B + \widehat{y} \wedge \neg(n(A_R) < n(A))\}$ |
| 1b | $\{y = Ax + \widehat{y}\}$ |

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| Step | Algorithm: $y := Ax + y$ |
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| 2 | { |
| 3 | while do |
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Algorithm: $y := Ax + y$

$$A \rightarrow \left(A_L \mid A_R \right), x \rightarrow \begin{pmatrix} x_T \\ \frac{x_B}{x_B} \end{pmatrix}$$

where A_R has 0 columns, x_B has 0 rows

while $n(A_R) < n(A)$ **do**

$$\left(A_L \mid A_R \right) \rightarrow \left(A_0 \mid a_1 \mid A_2 \right), \begin{pmatrix} x_T \\ \frac{x_B}{x_B} \end{pmatrix} \rightarrow \begin{pmatrix} x_0 \\ \frac{\chi_1}{x_2} \end{pmatrix}$$

where a_1 has 1 column, χ_1 has 1 row

$$y := \chi_1 a_1 + y$$

$$A \rightarrow \left(A_L \mid A_R \right) \leftarrow \left(A_0 \mid a_1 \mid A_2 \right), \begin{pmatrix} x_T \\ \frac{x_B}{x_B} \end{pmatrix} \leftarrow \begin{pmatrix} \frac{x_0}{\chi_1} \\ x_2 \end{pmatrix}$$

endwhile