

Step	Algorithm: $A := \text{LU\_UNB\_VAR4}(A)$
1a	$\{A = \hat{A}$
4	$A \rightarrow \left( \begin{array}{c c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right), L \rightarrow \left( \begin{array}{c c} L_{TL} & L_{TR} \\ \hline L_{BL} & L_{BR} \end{array} \right), U \rightarrow \left( \begin{array}{c c} U_{TL} & U_{TR} \\ \hline U_{BL} & U_{BR} \end{array} \right)$ <p>where <math>A_{TL}</math> is <math>0 \times 0</math>, <math>L_{TL}</math> is <math>0 \times 0</math>, <math>U_{TL}</math> is <math>0 \times 0</math></p>
2	$\left\{ \left( \begin{array}{c c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right) = \left( \begin{array}{c c} L \setminus U_{TL} & U_{TR} \\ \hline L_{BL} & \hat{A}_{BR} \end{array} \right) \wedge \frac{L_{TL}U_{TL} = \hat{A}_{TL} \mid L_{TL}U_{TR} = \hat{A}_{TR}}{L_{BL}U_{TL} = \hat{A}_{BL}} \right\}$
3	while $m(A_{TL}) < m(A)$ do
2,3	$\left\{ \begin{array}{l} \left( \begin{array}{c c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right) = \left( \begin{array}{c c} L \setminus U_{TL} & U_{TR} \\ \hline L_{BL} & \hat{A}_{BR} \end{array} \right) \wedge \frac{L_{TL}U_{TL} = \hat{A}_{TL} \mid L_{TL}U_{TR} = \hat{A}_{TR}}{L_{BL}U_{TL} = \hat{A}_{BL}} \wedge m(A_{TL}) < \\ m(A) \end{array} \right\}$
5a	$\left( \begin{array}{c c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right) \rightarrow \left( \begin{array}{c cc} A_{00} & a_{01} & A_{02} \\ \hline a_{10}^T & \alpha_{11} & a_{12}^T \\ A_{20} & a_{21} & A_{22} \end{array} \right), \left( \begin{array}{c c} L_{TL} & L_{TR} \\ \hline L_{BL} & L_{BR} \end{array} \right) \rightarrow \dots, \left( \begin{array}{c c} U_{TL} & U_{TR} \\ \hline U_{BL} & U_{BR} \end{array} \right) \rightarrow \dots$ <p>where <math>\alpha_{11}</math> is <math>1 \times 1</math>, <math>\lambda_{11}</math> is <math>1 \times 1</math>, <math>v_{11}</math> is <math>1 \times 1</math></p>
6	{
8	update line 1 : update line n
7	}
5b	$\left( \begin{array}{c c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right) \leftarrow \left( \begin{array}{c cc} A_{00} & a_{01} & A_{02} \\ \hline a_{10}^T & \alpha_{11} & a_{12}^T \\ A_{20} & a_{21} & A_{22} \end{array} \right), \left( \begin{array}{c c} L_{TL} & L_{TR} \\ \hline L_{BL} & L_{BR} \end{array} \right) \leftarrow \dots, \left( \begin{array}{c c} U_{TL} & U_{TR} \\ \hline U_{BL} & U_{BR} \end{array} \right) \leftarrow \dots$
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	endwhile
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	where
2	{ }
3	while do
2,3	{ } ^
5a	
	where
6	{ }
8	
7	{ }
5b	
2	{ }
	endwhile
2,3	{ } ^ $\neg( \quad )$
1b	{ }

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8	
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2	$\left\{ \left( \begin{array}{c c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right) = \left( \begin{array}{c c} L \setminus U_{TL} & U_{TR} \\ \hline L_{BL} & \hat{A}_{BR} \end{array} \right) \wedge \frac{L_{TL}U_{TL} = \hat{A}_{TL} \mid L_{TL}U_{TR} = \hat{A}_{TR}}{L_{BL}U_{TL} = \hat{A}_{BL}} \right\}$
	endwhile
2,3	$\left\{ \begin{array}{l} \left( \begin{array}{c c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right) = \left( \begin{array}{c c} L \setminus U_{TL} & U_{TR} \\ \hline L_{BL} & \hat{A}_{BR} \end{array} \right) \wedge \frac{L_{TL}U_{TL} = \hat{A}_{TL} \mid L_{TL}U_{TR} = \hat{A}_{TR}}{L_{BL}U_{TL} = \hat{A}_{BL}} \wedge \neg(m(A_{TL}) < \\ m(A) \end{array} \right\}$
1b	$\{A = L \setminus U \wedge LU = \hat{A}$

Step	Algorithm: $A := \text{LU\_UNB\_VAR4}(A)$
1a	$\{A = \hat{A}$
4	$A \rightarrow \left( \begin{array}{c c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right), L \rightarrow \left( \begin{array}{c c} L_{TL} & L_{TR} \\ \hline L_{BL} & L_{BR} \end{array} \right), U \rightarrow \left( \begin{array}{c c} U_{TL} & U_{TR} \\ \hline U_{BL} & U_{BR} \end{array} \right)$ <p>where <math>A_{TL}</math> is <math>0 \times 0</math>, <math>L_{TL}</math> is <math>0 \times 0</math>, <math>U_{TL}</math> is <math>0 \times 0</math></p>
2	$\left\{ \left( \begin{array}{c c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right) = \left( \begin{array}{c c} L \setminus U_{TL} & U_{TR} \\ \hline L_{BL} & \hat{A}_{BR} \end{array} \right) \wedge \frac{L_{TL}U_{TL} = \hat{A}_{TL} \mid L_{TL}U_{TR} = \hat{A}_{TR}}{L_{BL}U_{TL} = \hat{A}_{BL}} \right\}$
3	while $m(A_{TL}) < m(A)$ do
2,3	$\left\{ \begin{array}{c} \left( \begin{array}{c c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right) = \left( \begin{array}{c c} L \setminus U_{TL} & U_{TR} \\ \hline L_{BL} & \hat{A}_{BR} \end{array} \right) \wedge \frac{L_{TL}U_{TL} = \hat{A}_{TL} \mid L_{TL}U_{TR} = \hat{A}_{TR}}{L_{BL}U_{TL} = \hat{A}_{BL}} \wedge m(A_{TL}) < \\ m(A) \end{array} \right\}$
5a	$\left( \begin{array}{c c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right) \rightarrow \left( \begin{array}{c c} A_{00} & a_{01} \mid A_{02} \\ \hline a_{10}^T & \alpha_{11} \mid a_{12}^T \\ A_{20} & a_{21} \mid A_{22} \end{array} \right), \left( \begin{array}{c c} L_{TL} & L_{TR} \\ \hline L_{BL} & L_{BR} \end{array} \right) \rightarrow \dots, \left( \begin{array}{c c} U_{TL} & U_{TR} \\ \hline U_{BL} & U_{BR} \end{array} \right) \rightarrow \dots$ <p>where <math>\alpha_{11}</math> is <math>1 \times 1</math>, <math>\lambda_{11}</math> is <math>1 \times 1</math>, <math>v_{11}</math> is <math>1 \times 1</math></p>
6	{
8	<p>update line 1</p> <p>:</p> <p>update line n</p>
7	{
5b	$\left( \begin{array}{c c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right) \leftarrow \left( \begin{array}{c c} A_{00} & a_{01} \mid A_{02} \\ \hline a_{10}^T & \alpha_{11} \mid a_{12}^T \\ A_{20} & a_{21} \mid A_{22} \end{array} \right), \left( \begin{array}{c c} L_{TL} & L_{TR} \\ \hline L_{BL} & L_{BR} \end{array} \right) \leftarrow \dots, \left( \begin{array}{c c} U_{TL} & U_{TR} \\ \hline U_{BL} & U_{BR} \end{array} \right) \leftarrow \dots$
2	$\left\{ \left( \begin{array}{c c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right) = \left( \begin{array}{c c} L \setminus U_{TL} & U_{TR} \\ \hline L_{BL} & \hat{A}_{BR} \end{array} \right) \wedge \frac{L_{TL}U_{TL} = \hat{A}_{TL} \mid L_{TL}U_{TR} = \hat{A}_{TR}}{L_{BL}U_{TL} = \hat{A}_{BL}} \right\}$
	endwhile
2,3	$\left\{ \begin{array}{c} \left( \begin{array}{c c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right) = \left( \begin{array}{c c} L \setminus U_{TL} & U_{TR} \\ \hline L_{BL} & \hat{A}_{BR} \end{array} \right) \wedge \frac{L_{TL}U_{TL} = \hat{A}_{TL} \mid L_{TL}U_{TR} = \hat{A}_{TR}}{L_{BL}U_{TL} = \hat{A}_{BL}} \wedge \neg(m(A_{TL}) < \\ m(A) \end{array} \right\}$
1b	$\{A = L \setminus U \wedge LU = \hat{A}$

	Algorithm: $A := \text{LU\_UNB\_VAR4}(A)$
	$A \rightarrow \left( \begin{array}{c c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right), L \rightarrow \left( \begin{array}{c c} L_{TL} & L_{TR} \\ \hline L_{BL} & L_{BR} \end{array} \right), U \rightarrow \left( \begin{array}{c c} U_{TL} & U_{TR} \\ \hline U_{BL} & U_{BR} \end{array} \right)$ <p>where <math>A_{TL}</math> is <math>0 \times 0</math>, <math>L_{TL}</math> is <math>0 \times 0</math>, <math>U_{TL}</math> is <math>0 \times 0</math></p>
	while $m(A_{TL}) < m(A)$ do
	$\left( \begin{array}{c c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right) \rightarrow \left( \begin{array}{c c} A_{00} & a_{01} \ A_{02} \\ \hline a_{10}^T & \alpha_{11} \ a_{12}^T \\ \hline A_{20} & a_{21} \ A_{22} \end{array} \right), \left( \begin{array}{c c} L_{TL} & L_{TR} \\ \hline L_{BL} & L_{BR} \end{array} \right) \rightarrow \dots, \left( \begin{array}{c c} U_{TL} & U_{TR} \\ \hline U_{BL} & U_{BR} \end{array} \right) \rightarrow \dots$ <p>where <math>\alpha_{11}</math> is <math>1 \times 1</math>, <math>\lambda_{11}</math> is <math>1 \times 1</math>, <math>v_{11}</math> is <math>1 \times 1</math></p>
	update line 1 : update line n
	$\left( \begin{array}{c c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right) \leftarrow \left( \begin{array}{cc c} A_{00} & a_{01} & A_{02} \\ \hline a_{10}^T & \alpha_{11} & a_{12}^T \\ \hline A_{20} & a_{21} & A_{22} \end{array} \right), \left( \begin{array}{c c} L_{TL} & L_{TR} \\ \hline L_{BL} & L_{BR} \end{array} \right) \leftarrow \dots, \left( \begin{array}{c c} U_{TL} & U_{TR} \\ \hline U_{BL} & U_{BR} \end{array} \right) \leftarrow \dots$
	endwhile

**Algorithm:**  $A := \text{LU\_UNB\_VAR4}(A)$

$$A \rightarrow \left( \begin{array}{c|c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right), L \rightarrow \left( \begin{array}{c|c} L_{TL} & L_{TR} \\ \hline L_{BL} & L_{BR} \end{array} \right), U \rightarrow \left( \begin{array}{c|c} U_{TL} & U_{TR} \\ \hline U_{BL} & U_{BR} \end{array} \right)$$

**where**  $A_{TL}$  is  $0 \times 0$ ,  $L_{TL}$  is  $0 \times 0$ ,  $U_{TL}$  is  $0 \times 0$

**while**  $m(A_{TL}) < m(A)$  **do**

$$\left( \begin{array}{c|c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right) \rightarrow \left( \begin{array}{c|c|c} A_{00} & a_{01} & A_{02} \\ \hline a_{10}^T & \alpha_{11} & a_{12}^T \\ A_{20} & a_{21} & A_{22} \end{array} \right), \left( \begin{array}{c|c} L_{TL} & L_{TR} \\ \hline L_{BL} & L_{BR} \end{array} \right) \rightarrow \dots, \left( \begin{array}{c|c} U_{TL} & U_{TR} \\ \hline U_{BL} & U_{BR} \end{array} \right) \rightarrow \dots$$

**where**  $\alpha_{11}$  is  $1 \times 1$ ,  $\lambda_{11}$  is  $1 \times 1$ ,  $v_{11}$  is  $1 \times 1$

update line 1

:

update line n

$$\left( \begin{array}{c|c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right) \leftarrow \left( \begin{array}{c|c|c} A_{00} & a_{01} & A_{02} \\ \hline a_{10}^T & \alpha_{11} & a_{12}^T \\ A_{20} & a_{21} & A_{22} \end{array} \right), \left( \begin{array}{c|c} L_{TL} & L_{TR} \\ \hline L_{BL} & L_{BR} \end{array} \right) \leftarrow \dots, \left( \begin{array}{c|c} U_{TL} & U_{TR} \\ \hline U_{BL} & U_{BR} \end{array} \right) \leftarrow \dots$$

**endwhile**