Cı	A1 *(1
Step	Algorithm: $y := Ax + y$
1a	$\{y = \widehat{y}\}$
4	$A \to \left(\frac{A_T}{A_B}\right), y \to \left(\frac{y_T}{y_B}\right)$ where $A_B$ has 0 rows, $y_B$ has 0 rows
2	$\left\{ \left( rac{y_T}{y_B}  ight) = \left( rac{\widehat{y}_T}{A_B x + \widehat{y}_B}  ight)$
3	while $m(A_B) < m(A)$ do
2,3	$\left\{ \left( \frac{y_T}{y_B} \right) = \left( \frac{\widehat{y}_T}{A_B x + \widehat{y}_B} \right) \land m(A_B) < m(A) \right\}$
5a	$ \left(\frac{A_T}{A_B}\right) \to \left(\frac{A_0}{a_1^T}\right),  \left(\frac{y_T}{y_B}\right) \to \left(\frac{y_0}{\psi_1}\right) $ where $a_1$ has 1 row, $\psi_1$ has 1 row
6	$ \left\{ \begin{array}{c} \begin{pmatrix} y_0 \\ \psi_1 \\ y_2 \end{pmatrix} = \begin{pmatrix} \widehat{y}_0 \\ \widehat{\psi}_1 \\ A_2 x + \widehat{y}_2 \end{pmatrix} \right. $
8	$\psi_1 := a_1^T x + \psi_1$
7	$ \left\{ \begin{pmatrix} y_0 \\ \psi_1 \\ y_2 \end{pmatrix} = \begin{pmatrix} \widehat{y}_0 \\ a_1^T x + \widehat{\psi}_1 \\ A_2 x + \widehat{y}_2 \end{pmatrix} \right\} $
5b	$ \left(\frac{A_T}{A_B}\right) \leftarrow \left(\frac{A_0}{a_1^T}\right), \left(\frac{y_T}{y_B}\right) \leftarrow \left(\frac{y_0}{\psi_1}\right) \\ A_2\right) \leftarrow \left(\frac{y_0}{y_2}\right) $
2	$\left\{ \qquad \left( \frac{y_T}{y_B} \right) = \left( \frac{\widehat{y}_T}{A_B x + \widehat{y}_B} \right) \right\}$
	endwhile
2,3	$ \left\{ \left( \frac{y_T}{y_B} \right) = \left( \frac{\widehat{y}_T}{A_B x + \widehat{y}_B} \right) \land \neg (m(A_B) < m(A)) \right\} $
1b	$\{y = Ax + \widehat{y}\}$

Step	Algorithm: $y := Ax + y$
1a	{
4	where
2	
3	while do
2,3	$igg  \left\{ egin{array}{cccccccccccccccccccccccccccccccccccc$
5a	where
6	
8	
7	
5b	
2	
	endwhile
2,3	$\left  \left\{ \begin{array}{c} \\ \\ \end{array} \right. \right. $
1b	{

Step	Algorithm: $y := Ax + y$
1a	$\{y = \widehat{y} $
4	where
2	
3	while do
2,3	
5a	where
6	
8	
7	
5b	
2	
	endwhile
2,3	$\left\{ \begin{array}{c} \wedge \neg ( & ) \\ \end{array} \right.$
1b	$\{y = Ax + \widehat{y}\}$

Step	Algorithm: $y := Ax + y$
1a	$\{y = \widehat{y} \}$
4	where
2	$\left\{ \left( \frac{y_T}{y_B} \right) = \left( \frac{\widehat{y}_T}{A_B x + \widehat{y}_B} \right) \right\}$
3	while do
2,3	$\left\{ \qquad \left(\frac{y_T}{y_B}\right) = \left(\frac{\widehat{y}_T}{A_B x + \widehat{y}_B}\right) \land \qquad \right\}$
5a	where
6	
8	
7	
5b	
2	$\left\{ \qquad \left( \frac{y_T}{y_B} \right) = \left( \frac{\widehat{y}_T}{A_B x + \widehat{y}_B} \right) \right.$
	endwhile
2,3	$\left\{ \left( \frac{y_T}{y_B} \right) = \left( \frac{\widehat{y}_T}{A_B x + \widehat{y}_B} \right) \land \neg ( ) \right\}$
1b	$\{y = Ax + \widehat{y}\}$

Step	Algorithm: $y := Ax + y$
1a	$\{y = \widehat{y} \}$
4	where
2	$\left\{ \left( \frac{y_T}{y_B} \right) = \left( \frac{\widehat{y}_T}{A_B x + \widehat{y}_B} \right) \right\}$
3	while $m(A_B) < m(A)$ do
2,3	$\left\{ \left( \frac{y_T}{y_B} \right) = \left( \frac{\widehat{y}_T}{A_B x + \widehat{y}_B} \right) \wedge m(A_B) < m(A) \right\}$
5a	where
6	
8	
7	
5b	
2	$\left\{ \qquad \left( \frac{y_T}{y_B} \right) = \left( \frac{\widehat{y}_T}{A_B x + \widehat{y}_B} \right) \right.$
	endwhile
2,3	$\left\{ \left( \frac{y_T}{y_B} \right) = \left( \frac{\widehat{y}_T}{A_B x + \widehat{y}_B} \right) \land \neg (m(A_B) < m(A)) \right\}$
1b	$\{y = Ax + \widehat{y}\}$

Step	Algorithm: $y := Ax + y$	
1a	$\{y = \widehat{y}\}$	
4	$A  o \left(\frac{A_T}{A_B}\right), y  o \left(\frac{y_T}{y_B}\right)$	
	where $A_B$ has 0 rows, $y_B$ has 0 rows	7
2	$\left\{ \left( \frac{y_T}{y_B} \right) = \left( \frac{\widehat{y}_T}{A_B x + \widehat{y}_B} \right) \right.$	
3	while $m(A_B) < m(A)$ do	
2,3	$\left\{ \left( \frac{y_T}{y_B} \right) = \left( \frac{\widehat{y}_T}{A_B x + \widehat{y}_B} \right) \land m(A_B) < m(A) \right\}$	
5a		
	where	
6		
8		
		١
7		ļ
		J
5b		
	$y_T$ $\hat{y}_T$	1
2	$\left\{ \begin{array}{c} \left(\frac{y_T}{y_B}\right) = \left(\frac{\widehat{y_T}}{A_B x + \widehat{y}_B}\right) \end{array} \right.$	
	endwhile	
2,3	$\left\{ \left( \frac{y_T}{y_B} \right) = \left( \frac{\widehat{y}_T}{A_B x + \widehat{y}_B} \right) \land \neg (m(A_B) < m(A)) \right\}$	
1b	$\{y = Ax + \widehat{y}\}$	
		_

Step	Algorithm: $y := Ax + y$
1a	$\{y = \widehat{y} \}$
4	$A \to \left(\frac{A_T}{A_B}\right), y \to \left(\frac{y_T}{y_B}\right)$ where $A_B$ has 0 rows, $y_B$ has 0 rows
2	$\left\{ \begin{pmatrix} y_T \\ y_B \end{pmatrix} = \begin{pmatrix} \widehat{y}_T \\ A_B x + \widehat{y}_B \end{pmatrix} \right\}$
3	while $m(A_B) < m(A)$ do
2,3	$\left\{ \left( \frac{y_T}{y_B} \right) = \left( \frac{\widehat{y}_T}{A_B x + \widehat{y}_B} \right) \land m(A_B) < m(A) \right\}$
5a	$ \left(\frac{A_T}{A_B}\right) \to \left(\frac{A_0}{a_1^T}\right), \left(\frac{y_T}{y_B}\right) \to \left(\frac{y_0}{\psi_1}\right) $ where $a_1$ has 1 row, $\psi_1$ has 1 row
6	
8	
7	
5b	$ \left(\frac{A_T}{A_B}\right) \leftarrow \left(\frac{A_0}{a_1^T}\right), \left(\frac{y_T}{y_B}\right) \leftarrow \left(\frac{y_0}{\psi_1}\right) \\ A_2 \qquad \qquad$
2	$\left\{ \qquad \left( \frac{y_T}{y_B} \right) = \left( \frac{\widehat{y}_T}{A_B x + \widehat{y}_B} \right) \right\}$
	endwhile
2,3	$\left\{ \left( \frac{y_T}{y_B} \right) = \left( \frac{\widehat{y}_T}{A_B x + \widehat{y}_B} \right) \land \neg (m(A_B) < m(A)) \right\}$
1b	$\{y = Ax + \widehat{y}\}$

Step	Algorithm: $y := Ax + y$
1a	$\{y = \widehat{y} \}$
4	$A  o \left(\frac{A_T}{A_B}\right), y  o \left(\frac{y_T}{y_B}\right)$
2	where $A_B$ has 0 rows, $y_B$ has 0 rows $ \left\{ \begin{pmatrix} y_T \\ y_B \end{pmatrix} = \begin{pmatrix} \hat{y}_T \\ A_B x + \hat{y}_B \end{pmatrix} \right. $
3	while $m(A_B) < m(A)$ do
2,3	$\left\{ \left( \frac{y_T}{y_B} \right) = \left( \frac{\widehat{y}_T}{A_B x + \widehat{y}_B} \right) \land m(A_B) < m(A) \right\}$
5a	$ \left(\frac{A_T}{A_B}\right) \to \left(\frac{A_0}{a_1^T}\right), \left(\frac{y_T}{y_B}\right) \to \left(\frac{y_0}{\psi_1}\right) $ where $a_1$ has 1 row, $\psi_1$ has 1 row
6	$\left\{ \begin{array}{c} \begin{pmatrix} y_0 \\ \psi_1 \\ y_2 \end{pmatrix} = \begin{pmatrix} \widehat{y}_0 \\ \widehat{\psi}_1 \\ A_2 x + \widehat{y}_2 \end{pmatrix} \right.$
8	
7	
5b	$ \left(\frac{A_T}{A_B}\right) \leftarrow \left(\frac{A_0}{a_1^T}\right), \left(\frac{y_T}{y_B}\right) \leftarrow \left(\frac{y_0}{\psi_1}\right) \\ A_2 \qquad \qquad$
2	$\left\{ \qquad \left( \frac{y_T}{y_B} \right) = \left( \frac{\widehat{y}_T}{A_B x + \widehat{y}_B} \right) \right.$
	endwhile
2,3	$\left\{ \left( \frac{y_T}{y_B} \right) = \left( \frac{\widehat{y}_T}{A_B x + \widehat{y}_B} \right) \land \neg (m(A_B) < m(A)) \right\}$
1b	$\{y = Ax + \widehat{y}\}$

Step	Algorithm: $y := Ax + y$
1a	$\{y = \widehat{y} $
4	$A  o \left(\frac{A_T}{A_B}\right), y  o \left(\frac{y_T}{y_B}\right)$
	where $A_B$ has 0 rows, $y_B$ has 0 rows
2	$\left\{ egin{aligned} \left( rac{y_T}{y_B}  ight) = \left( rac{\widehat{y}_T}{A_B x + \widehat{y}_B}  ight) \end{aligned}  ight.$
3	while $m(A_B) < m(A)$ do
2,3	$\left\{ \left( \frac{y_T}{y_B} \right) = \left( \frac{\widehat{y}_T}{A_B x + \widehat{y}_B} \right) \land m(A_B) < m(A) \right\}$
5a	$ \left(\frac{A_T}{A_B}\right) \to \left(\frac{A_0}{a_1^T}\right), \left(\frac{y_T}{y_B}\right) \to \left(\frac{y_0}{\psi_1}\right) $ where $a_1$ has 1 row, $a_2$ has 1 row.
	where $a_1$ has 1 row, $\psi_1$ has 1 row $( \psi_1 ) \qquad ( \widehat{\psi}_2 ) \qquad ( \widehat{\psi}_3 )$
6	$\left\{egin{array}{c} \left(egin{array}{c} y_0 \ \psi_1 \ y_2 \end{array} ight) = \left(egin{array}{c} \widehat{y}_0 \ \widehat{\psi}_1 \ A_2x + \widehat{y}_2 \end{array} ight) \end{array} ight.$
8	
7	$\left\{ \begin{array}{c} \begin{pmatrix} y_0 \\ \psi_1 \\ y_2 \end{pmatrix} = \begin{pmatrix} \widehat{y}_0 \\ a_1^T x + \widehat{\psi}_1 \\ A_2 x + \widehat{y}_2 \end{pmatrix} \right.$
5b	$ \left(\frac{A_T}{A_B}\right) \leftarrow \left(\frac{A_0}{a_1^T}\right), \left(\frac{y_T}{y_B}\right) \leftarrow \left(\frac{y_0}{\psi_1}\right) \\ A_2 \qquad \qquad$
2	$\left\{ \qquad \left( \frac{y_T}{y_B} \right) = \left( \frac{\widehat{y}_T}{A_B x + \widehat{y}_B} \right) \right.$
	endwhile
2,3	$\left\{ \left( \frac{y_T}{y_B} \right) = \left( \frac{\widehat{y}_T}{A_B x + \widehat{y}_B} \right) \land \neg (m(A_B) < m(A)) \right\}$
1b	$\{y = Ax + \widehat{y}\}$

Step	Algorithm: $y := Ax + y$
1a	$\{y = \widehat{y} $
4	$A  o \left(\frac{A_T}{A_B}\right), y  o \left(\frac{y_T}{y_B}\right)$
	where $A_B$ has 0 rows, $y_B$ has 0 rows
2	$\left\{ egin{aligned} \left( rac{y_T}{y_B}  ight) = \left( rac{\widehat{y}_T}{A_B x + \widehat{y}_B}  ight) \end{aligned}  ight.$
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2,3	$\left\{ \left( \frac{y_T}{y_B} \right) = \left( \frac{\widehat{y}_T}{A_B x + \widehat{y}_B} \right) \land m(A_B) < m(A) \right\}$
5a	$\left(\frac{A_T}{A_B}\right) \to \left(\frac{A_0}{a_1^T}\right), \left(\frac{y_T}{y_B}\right) \to \left(\frac{y_0}{\psi_1}\right)$
	where $a_1$ has 1 row, $\psi_1$ has 1 row
6	$\left\{egin{array}{c} \left(egin{array}{c} y_0 \ \psi_1 \ y_2 \end{array} ight) = \left(egin{array}{c} \widehat{y}_0 \ \widehat{\psi}_1 \ A_2x + \widehat{y}_2 \end{array} ight) \end{array} ight.$
8	$\psi_1 := a_1^T x + \psi_1$
7	$\left\{ \begin{array}{c} \begin{pmatrix} y_0 \\ \psi_1 \\ y_2 \end{pmatrix} = \begin{pmatrix} \widehat{y}_0 \\ a_1^T x + \widehat{\psi}_1 \\ A_2 x + \widehat{y}_2 \end{pmatrix} \right.$
5b	$ \left(\frac{A_T}{A_B}\right) \leftarrow \left(\frac{A_0}{a_1^T}\right), \left(\frac{y_T}{y_B}\right) \leftarrow \left(\frac{y_0}{\psi_1}\right) \\ A_2 \qquad \qquad$
2	$\left\{ \qquad \left( \frac{y_T}{y_B} \right) = \left( \frac{\widehat{y}_T}{A_B x + \widehat{y}_B} \right) \right.$
	endwhile
2,3	$\left\{ \left( \frac{y_T}{y_B} \right) = \left( \frac{\widehat{y}_T}{A_B x + \widehat{y}_B} \right) \land \neg (m(A_B) < m(A)) \right\}$
1b	$\{y = Ax + \widehat{y}\}$

Algorithm: $y := Ax + y$
$A \to \left(\frac{A_T}{A_B}\right), y \to \left(\frac{y_T}{y_B}\right)$ where $A_B$ has 0 rows, $y_B$ has 0 rows
while $m(A_B) < m(A)$ do
$ \left(\frac{A_T}{A_B}\right) \to \left(\frac{A_0}{a_1^T}\right), \left(\frac{y_T}{y_B}\right) \to \left(\frac{y_0}{\psi_1}\right) $ where $a_1$ has 1 row, $\psi_1$ has 1 row
$\psi_1 := a_1^T x + \psi_1$
$ \left(\frac{A_T}{A_B}\right) \leftarrow \left(\frac{A_0}{a_1^T}\right), \left(\frac{y_T}{y_B}\right) \leftarrow \left(\frac{y_0}{\psi_1}\right) \\ A_2\right) \leftarrow \left(\frac{y_0}{\psi_1}\right) $
endwhile

Algorithm: y := Ax + y

$$A \to \left(\frac{A_T}{A_B}\right), y \to \left(\frac{y_T}{y_B}\right)$$

where  $A_B$  has 0 rows,  $y_B$  has 0 rows while  $m(A_B) < m(A)$  do

$$\left(\frac{A_T}{A_B}\right) \to \left(\frac{A_0}{a_1^T}\right), \left(\frac{y_T}{y_B}\right) \to \left(\frac{y_0}{y_2}\right)$$

where  $a_1$  has 1 row,  $\psi_1$  has 1 row

$$\psi_1 := a_1^T x + \psi_1$$

$$\left(\frac{A_T}{A_B}\right) \leftarrow \left(\frac{A_0}{a_1^T}\right), \left(\frac{y_T}{y_B}\right) \leftarrow \left(\frac{y_0}{\psi_1}\right) \\
A_2$$

endwhile