

# Multiclass object detection: nested cascades and coupled components in multiclass classifiers

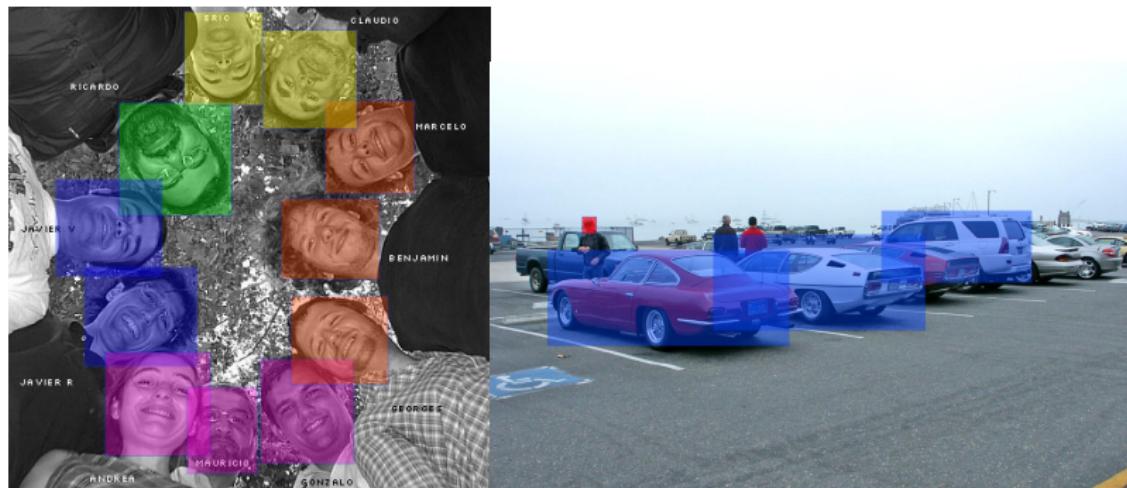
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UPF  
September 9, 2008

# Multiclass Object detection

**Object detection:** For a given set of object classes, to find, if any, the instances of these classes appearing on the image.



## 1 Introduction

- Motivation
- Cascade classifiers

## 2 Nested Cascade of Boosted Classifier

- Adaboost
- Nested Cascade Classifiers

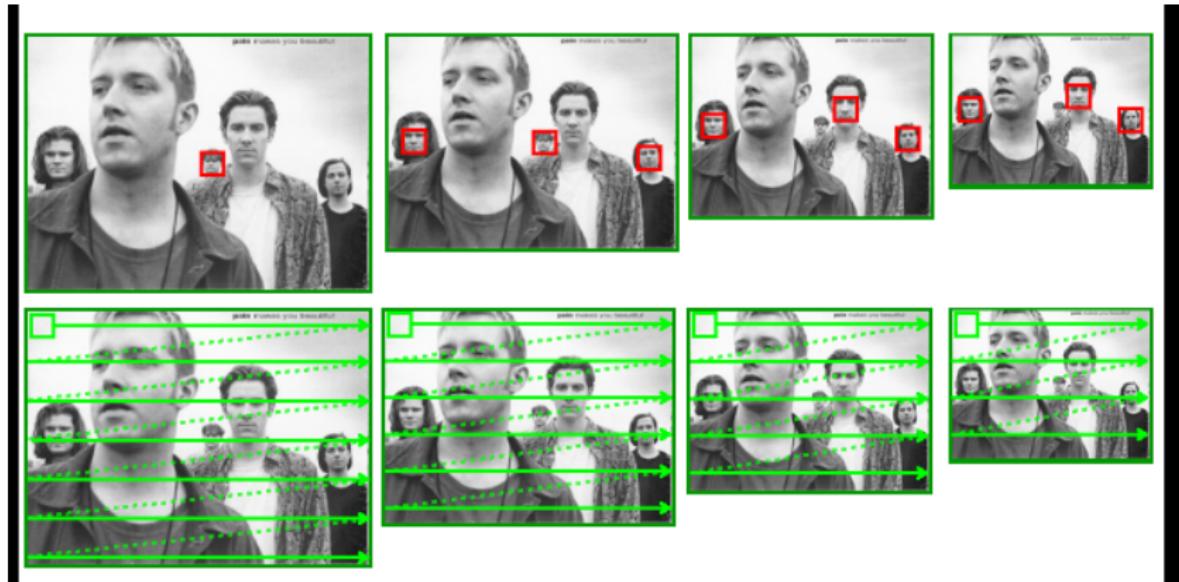
## 3 Multiclass Object Detection

- A multiclass extension of Adaboost
- Weak classifier
- Training procedures

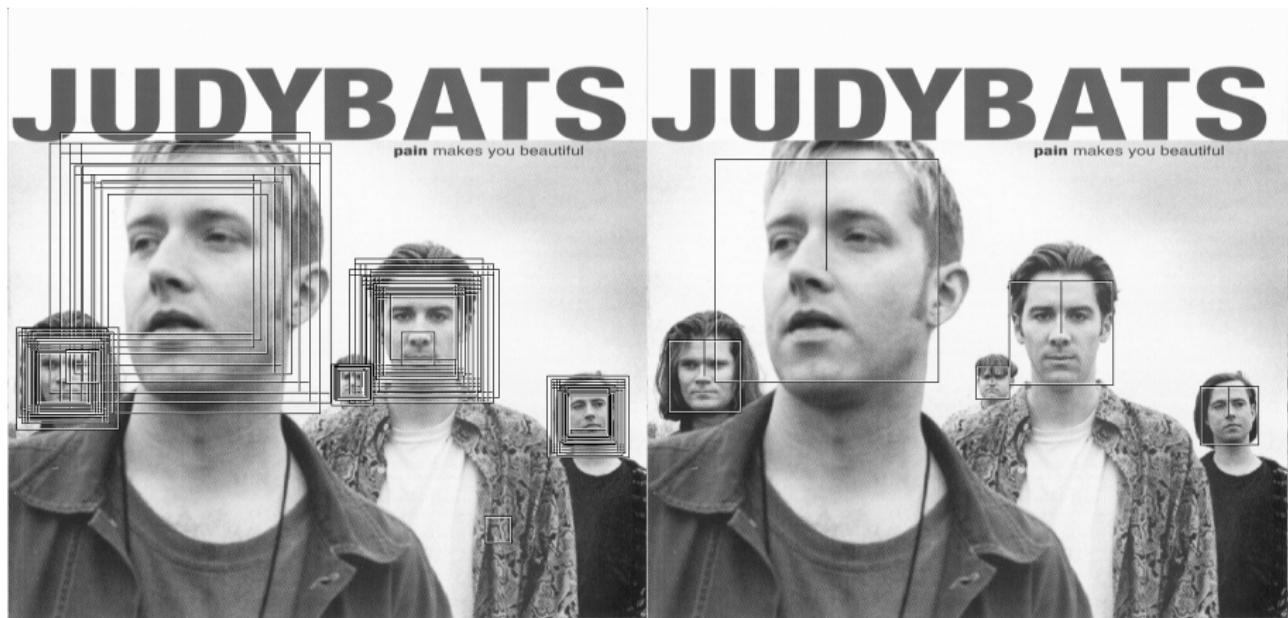
## 4 Results, and future work

- Experiment set up
- Example results and Comments
- Future work

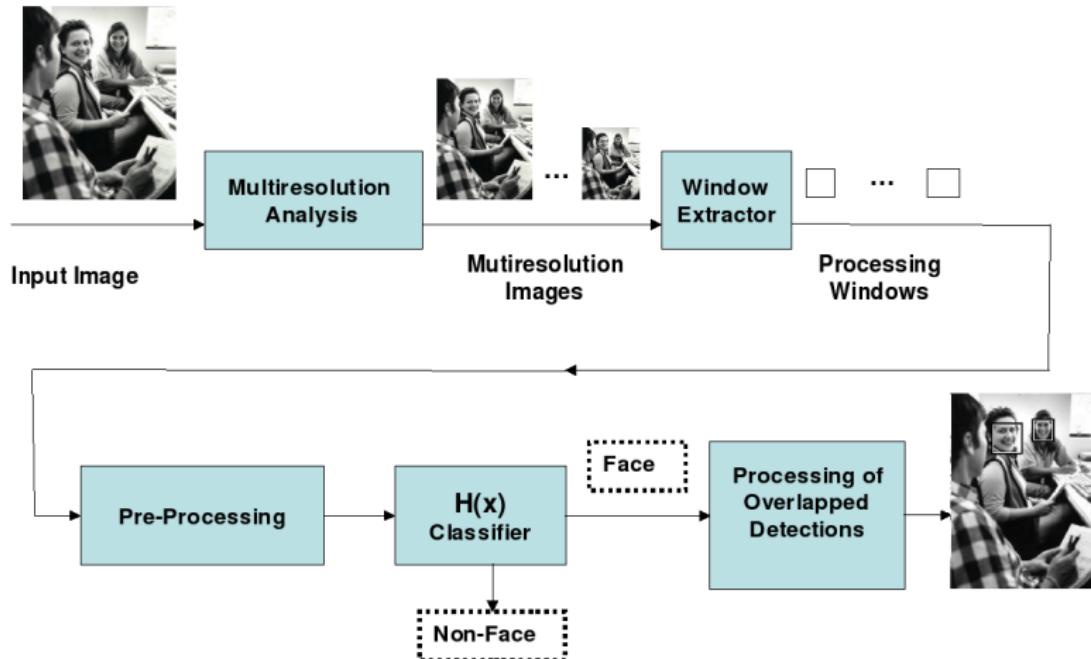
# Multiscale search



# Multiscale search



# Detection Architecture



# What do we want from Multiclass object detector?

## Use

- High accuracy
  - ▶ high detection rate ( $> 99.9\%$ )
  - ▶ low false positive rate ( $< 10^{-6}$ )
- Fast detection
- Robustness to noise, illumination, etc.

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- Fast training
- Good results when trained using small training sets

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## Scalability with the number of classes

- Training time
- Detection time
- Accuracy

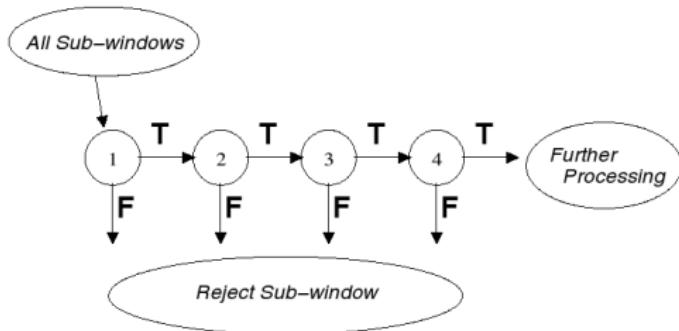
# Cascade classifiers [Viola and Jones 2001]

- Very asymmetric problem
- In an image, most windows correspond to the background
- Most non-object windows are very different from object windows

→ Average processing time depends mainly on the processing time of non-object windows



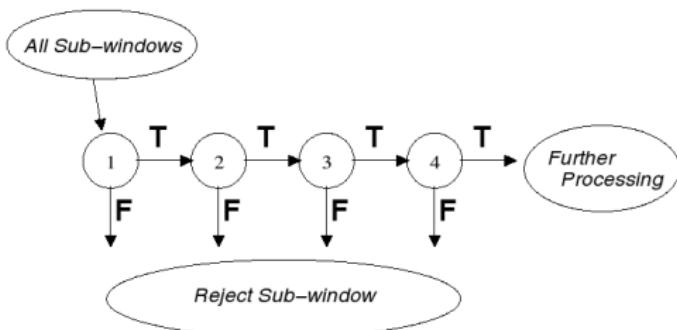
# Cascade classifiers [Viola and Jones 2001]



## Asymmetric problem

- Coarse-to-Fine approach:
  - Reduce the (negative) hypothesis space incrementally.
- Efficient way of organizing object detection
  - there are more non-object than object windows.
- First layers must be very fast

# Cascade classifiers [Viola and Jones 2001]



## Asymmetric problem

- Layers must have high true positive rates (e.g.):  
→ if  $d_i = 0.999, n = 10, D = \prod_{i=1}^n \simeq 0.99$   
and low false positive rates (e.g.):  
→ if  $f_i = 0.2, n = 10, F = \prod_{i=1}^n \simeq 10^{-6}$
- First layers are easier to be trained, complexity of the problem increases as we move through the cascade

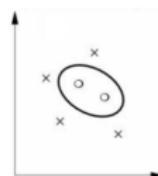
# Adaboost (two-class case)

## Classification: Basic concepts

Using a training set  $S = \{(x_i, y_i)\}_{i=1,\dots,m}, y_i \in \{-1, 1\}$

build a classifier  $H(x) : \mathbb{R}^n \rightarrow \mathbb{R}$

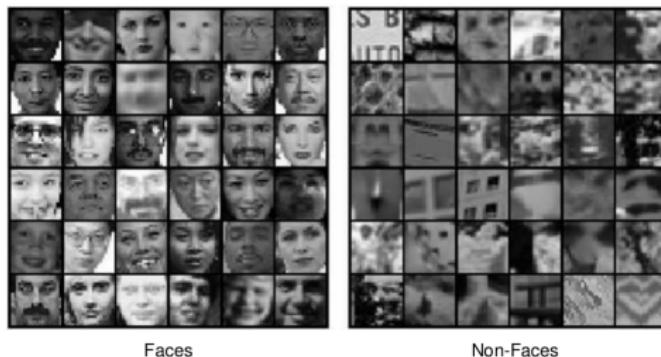
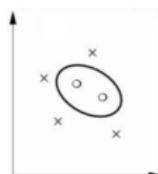
such that  $\text{Prob}(\text{sign}(H(x)) \neq y)$  is small



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Images from: Ce Liu & Huena-Yeung Shum. 2003

# Adaboost (two-class problem)

## Adaboost: Main ideas

- Build **additive** model:  $H(x) = \sum_{t=0}^T h_t(x)$
- Add terms to sum iteratively
- Drive focus to wrongly classified examples
- Basically we will minimize  $E_{x \sim S}[\exp(-yH(x))]$  iteratively

Note: The classification is correct  $\iff$  the margin  $yH(x) \geq 0$

# Features

Associate a weak classifier to a feature

$$H(x) = \sum_{t=0}^T h_t(x) = \sum_{t=0}^T h_t(f_t(x))$$

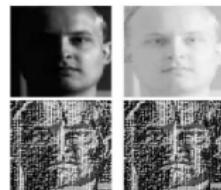
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Associate a weak classifier to a feature

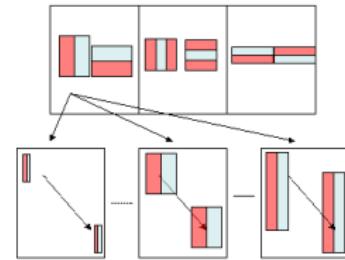
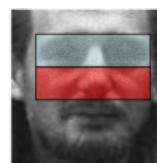
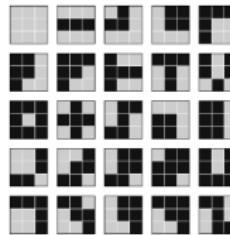
$$H(x) = \sum_{t=0}^T h_t(x) = \sum_{t=0}^T h_t(f_t(x))$$

## Examples of feature sets

- Modified Local Binary Patterns (mLBP) [Froba et al 2004]
  - ▶ Well suited for face detection
  - ▶ Invariant to linear contrast changes
- Haar-like wavelets [Viola and Jones 2001]
  - ▶ Well suited for frontal face detection,
  - ▶ Very fast evaluation using the Integral Image



|       |       |       |
|-------|-------|-------|
| $y_1$ | $y_2$ | $y_3$ |
| $y_4$ | $x$   | $y_5$ |
| $y_6$ | $y_7$ | $y_8$ |



# Adaboost

- Input: Training set  $S = \{(x_i, y_i)\}_{i=1,\dots,m}$
- Initialize Weights:  $w_i(0) = 1, i = 1, \dots, m$
- For  $t = 0, \dots, T$ 
  - ▶ Normalized weights  $\{w_i(t)\}_{i=1,\dots,m}$  such that they add to one
  - ▶ Select  $h_t \in \mathbf{H}$  (and  $f_t \in \mathbf{F}$ ), such that

$$Z_t = \sum_{i=1}^m w_i(t) \exp(-y_i h_t(f_t(x_i)))$$

is minimized

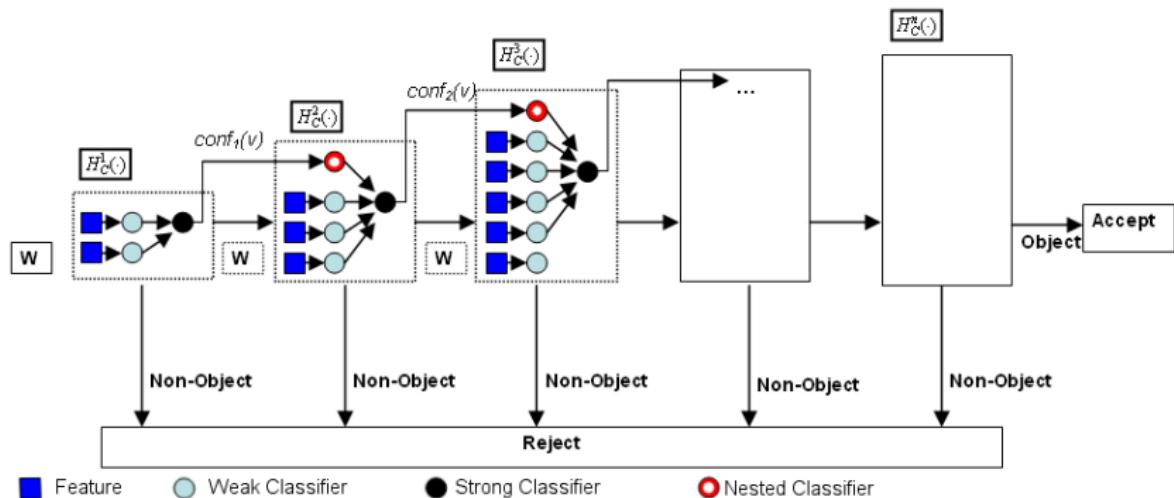
- ▶ Update weights:  $w_i(t+1) = w_i(t) \exp(-y_i, h_t(f_t(x_i)))$
- Return:

$$H(x) = \sum_{t=0}^T h_t(f_t(x))$$

# Nested Cascade

- Allows to reuse information
- Faster and more robust than the non-nested case

$$H^k(x) = \sum_{t=0}^{T_k} h_t^k(f_t(x)) + H^{k-1}(x), k > 1$$



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# Multiclass Object Detection: Related work

- Multiple cascades [Wu & al 2004, Schneiderman 2004]  
→ Frontal faces, rotated faces, cars, traffic signs, etc.
- View estimation followed by multiple cascades [Jones & Viola 2003]  
→ Frontal and rotated faces.
- Tree of boosted cascades (Floatboost) [Li et al 2004 ; Ong & Bowden 2004]  
→ Faces, hands.
- Coarse-to-fine [Fleuret & Geman 2001; Amit et al. 2004; Gangaputra & Geman 2006]  
→ Faces, Numbers and Letters.
- Sharing of weak classifiers among classes (**Jointboost**) [Torralba et al. 2004]  
→ frontal faces, cars, persons, keyboards, telephones, etc.
- Vectorized Adaboost and tree structure (**Vector Boosting**) [Huang et al 2007]  
→ Faces at multiple rotations.

# Extending the classifier to the multiclass case

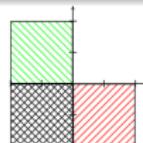
## Desired requirements/properties

- The classifier should scale well with the number of classes  
Accuracy, robustness, processing time
- The training time should scale well with the number of classes.
- Good results should be obtained using small training sets.
- Fast evaluation
  - ▶ Reuse of feature and classifier evaluations

# Multiclass formulation

## Multiclass

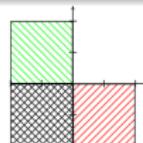
$$\vec{H}(x) = \sum_{t=0}^T \vec{h}_t(\vec{f}_t(x))$$



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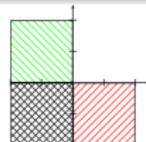
## Feature sharing

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## Notation

$$H(x, c) = \sum_{t=0}^T h_t(f_t(x), c), c = 1, \dots, M$$

# Multiclass formulation

## One case

- Training example:  $(x_i, y_i)$ ,  $y_i \in \{-1, 1\}$  represents the target halfspace
- $yH(x) \geq 0$  if  $H(x)$  is in the correct half space

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## Multiclass case

- Training example:  $(x_i, \mathbf{V}_i)$ , The vector set  $\mathbf{V}_i$  represents the target sub space defined as the intersection of halfspaces
- An object instance  $x_i$  (belonging to class  $C_m$ ) is classified correctly
  - ▶ iff  $\forall \vec{V} \in \mathbf{V}_m, \vec{V} \cdot \vec{H}(x) \geq 0$  (Vector Boosting, [Huang et al 2007])

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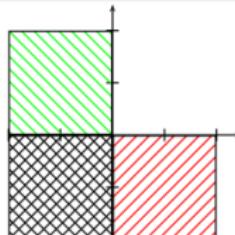
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(iff  $\forall \vec{V} \in \mathbf{V}_m, Q(\vec{V}, \vec{H}(x)) \geq 0$ ) (Generalized Multiclass Adaboost)

# Objective space

Example 1: 2 objects classes and a non-object class

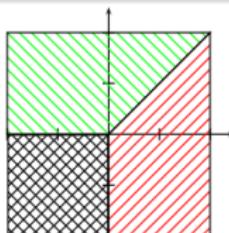


Disjoint and non overlapping

| Class      | Vectors            | Objective region | Region on figure |
|------------|--------------------|------------------|------------------|
| Object 1   | $(+1, 0); (0, -1)$ | $x > 0, y < 0$   | Red              |
| Object 2   | $(-1, 0); (0, +1)$ | $x < 0, y > 0$   | Green            |
| Non Object | $(-1, 0); (0, -1)$ | $x < 0, y < 0$   | Dashed Grey      |

# Objective space

Example 2: 2 objects classes and a non-object class

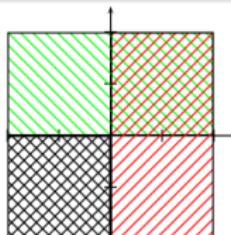


Joint boundary

| Class      | Vectors             | Objective region | Region on figure |
|------------|---------------------|------------------|------------------|
| Object 1   | $(+1, 0); (+1, -1)$ | $x > 0, x > y$   | Red              |
| Object 2   | $(-1, 0); (-1, +1)$ | $y > 0, y > x$   | Green            |
| Non Object | $(-1, 0); (0, -1)$  | $x < 0, y < 0$   | Dashed Grey      |

# Objective space

Example 3: 2 objects classes and a non-object class



## Ovelapping

| Class      | Vectors            | Objective region | Region on figure |
|------------|--------------------|------------------|------------------|
| Object 1   | $(1, 0);$          | $x > 0$          | Red              |
| Object 2   | $(0, 1);$          | $y > 0$          | Green            |
| Non Object | $(-1, 0); (0, -1)$ | $x < 0, y < 0$   | Dashed Grey      |

# Generalized Adaboost

- Training set  $S = \{(x_i, \mathbf{V}_i)\}_{i=1,\dots,m}$
- $\mathbf{V}_i = \{\vec{V}_i^j\}_j$  is a vector/parameter set representing the objective region associated to the example  $x_i$
- Initialize Weights:  $w_{i,j}(0) = 1$
- For  $t = 0, \dots, T$ 
  - ① Normalized weights  $\{w_{i,j}(t)\}_{i,j}$  so that they add to one
  - ② Select  $\vec{h}_t$  and  $f_t$ , such that  $Z_t$  is minimized, with

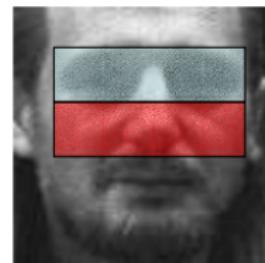
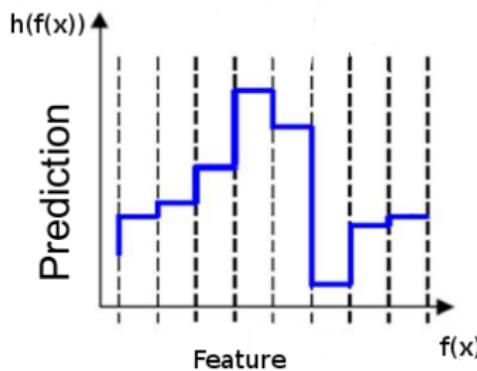
$$Z_t = \sum_{i=1}^m \sum_{j: V_i^j \in \mathbf{V}_i} w_{i,j}(t) \exp \left( -Q \left( \vec{V}_i^j, \vec{h}_t(f_t(x_i)) \right) \right)$$

- ③ Update weights:  $w_{i,j}(t+1) = w_{i,j}(t) \exp \left( -Q \left( \vec{V}_i^j, \vec{h}_t(f_t(x_i)) \right) \right)$
- return  $\vec{H}(x) = \sum_t \vec{h}_t(f_t(x))$

# Domain Partitioning (one-class case)

## Domain Partitioning weak classifiers [Shapire and Singer 1999]

- Fast evaluation thanks to the use of look up tables:  $O(1)$ .
- Well fitted for different types of features (e.g, rectangular features and mLBP).



$$H(x) = \sum_{t=0}^T h_t(f_t(x))$$

# Possible outputs of the weak classifier $\vec{h}_k$

- Independent classifiers [Huang et al 2007]

$$H(x, c) = \sum_{t=1}^T h_t(f_t(x), c)$$

- Joint classifiers (Similar to [Torralba et al 2007])

$$H(x, c) = \sum_{t=1}^T \beta_t^c h_t(f_t(x)), \beta_t^c \in \{0, 1\}$$

- Coupled classifiers (Proposed)

$$H(x, c) = \sum_{t=1}^T \gamma_t^c h_t(f_t(x)), \gamma_t^c \in \mathbb{R}$$

# Possible outputs of the weak classifier $\vec{h}_k$

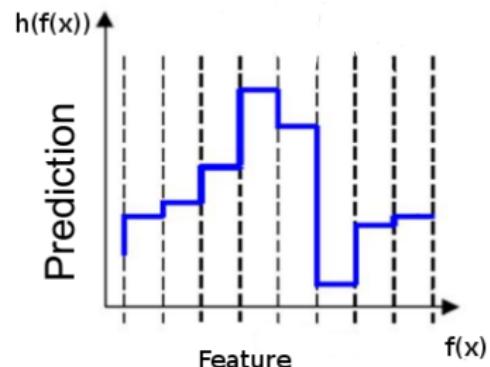
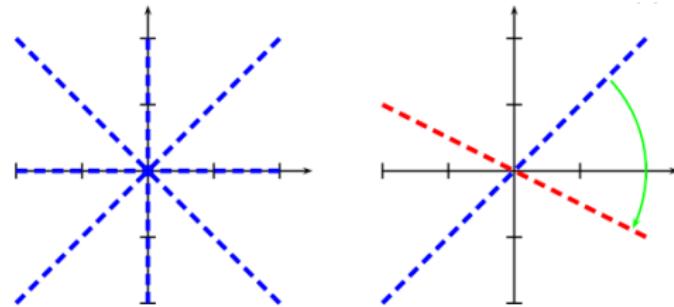


Figure: Left: Joint, Center: Coupled (Proposed), Right: domain partitioning

# Optimization problem

| Method      | Problem                                                                                                   | Solution | N. of Prob. | N. of Variables | Order $O()$     |
|-------------|-----------------------------------------------------------------------------------------------------------|----------|-------------|-----------------|-----------------|
| Adaboost    | $\min_{c_j} \sum_j w_+^j e^{-c_j} + w_-^j e^{+c_j}$                                                       | Analitic | $J$         | $J$             | $N + J$         |
| Joint       | $\min_{c_j, b_m \in \{0,1\}} \sum_{j,m} w_+^{j,m} e^{-\beta_m c_j} + w_-^{j,m} e^{\beta_m c_j}$           | Analytic | $2^M$       | $J(+M)$         | $N + J2^M$      |
| Independent | $\min_{c_j, m} \sum_m \sum_j w_+^{j,m} e^{-c_{j,m}} + w_-^{j,m} e^{c_{j,m}}$                              | Analytic | $J$         | $JM$            | $N + JM$        |
| Coupled     | $\min_{c_j, \gamma_m \in \mathbb{R}} \sum_{j,m} w_+^{j,m} e^{-\gamma_m c_j} + w_-^{j,m} e^{\gamma_m c_j}$ | Newton * | 1           | $J + M$         | $N + (J + M)^2$ |

Weak classifier: domain partitioning ( $J$  bins);  $M$  classes;  $N$  training examples

# Train Nested Cascade

**Input:** Positive Training Set  $S = \{(x_i, \vec{V}_i)\}_{i=1,\dots,m}$

**Input:** Bootstrapp Set  $B$

**Input:** Min true positive rate per node  $D$

**Input:** Max false positive rate per node  $F$  and max false positive of the cascade

$F_C$

1:  $k = 1, F_k = 1, H \leftarrow 0, S_{B_0} = B$

2: **while**  $F_k > F_C$  **do**

3:    $S_{B_k} = \text{Bootstrapp}(S_{B_{k-1}}, \vec{H}, M)$

4:    $[\vec{H}_k] = \text{TrainLayer}(S \otimes S_{B_k}, \vec{H}, F, D)$

5:    $\vec{H} \leftarrow \vec{H} \cup \vec{H}_k$

6:    $F_k \leftarrow \text{Evaluate current cascade } \vec{H}$

7:    $k \leftarrow k + 1$

8: **end while**

**Output:** Trained cascade  $\vec{H}$

# *Bootstrapp*( $B, H, M$ )

**Input:** Boostrapp Set  $B$

**Input:** Classifier  $\vec{H}$

```
1:  $S = \emptyset, i = 0$ 
2: while  $i < M$  do
3:    $x \leftarrow$  sample  $S_B$ 
4:   if  $H(x) > 0$  then
5:      $S \leftarrow S \cup x$ 
6:    $i \leftarrow i + 1$ 
7: end if
8: end while
```

**Output:**  $S$

# Train Layer

**Input:** Training Set  $S = \{(x_i, \vec{e}_i)\}_{i=1,\dots,m}$

**Input:** Already trained cascade  $\vec{H}$

- 1: Init:  $t \leftarrow 0, w_0(i) \leftarrow \exp(-\vec{e}_i \cdot \vec{H}(x_i)), F_0 \leftarrow 1, \vec{H}_0 \leftarrow \vec{H}_0, m_0 \leftarrow m$
- 2: **while**  $F_t > F$  **do**
- 3:   Normalize the weights  $\{w_t(i)\}_{i=1,\dots,m_t}$  s.t they add to one
- 4:   **Select**  $\vec{h}_t(\cdot)$  s.t  $Z_t = \sum_i w_t(i) \exp\left(-\vec{e}_i \cdot \vec{h}_t(x_i)\right)$  is minimized
- 5:   Set  $\vec{H}_t \leftarrow \vec{H}_{t-1} + \vec{h}_t$
- 6:   Update weights:  $w_{t+1}(i) = w_t(i) \exp(-\vec{e}_i \cdot \vec{h}_t(f_t(x_i)))$
- 7:   Set threshold for  $\vec{H}_t$  such that  $D_t > D$  and evaluate current false positive rate  $F_t$
- 8:    $t \leftarrow t + 1$
- 9: **end while**

**Output:**  $\vec{H}(\cdot) = \sum_{t=1}^T \vec{h}_t(\cdot), \vec{h}_t(\cdot) = \vec{\beta}_t h_t(f_t(\cdot))$

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- Nested Cascade Classifiers

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# Experiments

## In plane Rotated Faces

- Nested Cascade
- Rectangular and mLBP features
- Vectorized weak classifiers trained with :
  - ▶ Independent classifiers:  $H(x, c) = \sum_{t=1}^T h_t(f_t(x), c)$
  - ▶ Joint classifiers:  $H(x, c) = \sum_{t=1}^T \beta_t^c h_t(f_t(x)), \beta_{c,t} \in \{0, 1\}$
  - ▶ Coupled classifiers:  $H(x, c) = \sum_{t=1}^T \gamma_t^c h_t(f_t(x)), \gamma_{c,t} \in \mathbb{R}$

## 4-classes case

- Number of classes ( $n$ )
  - ▶ 1 class: Frontal faces without in plane rotation
  - ▶ 2 classes: 0 and 180 degrees of in plane rotation
  - ▶ 4 classes: 0, 90, 180 and 270 degrees of in plane rotation
  - ▶ 8 classes: 0, 45, 90, 135, 180, 225, 270 and 315 degrees
- Number of training examples. Positives:  $n * 5000$ , Negative:  $n * 5000$



# 1-class

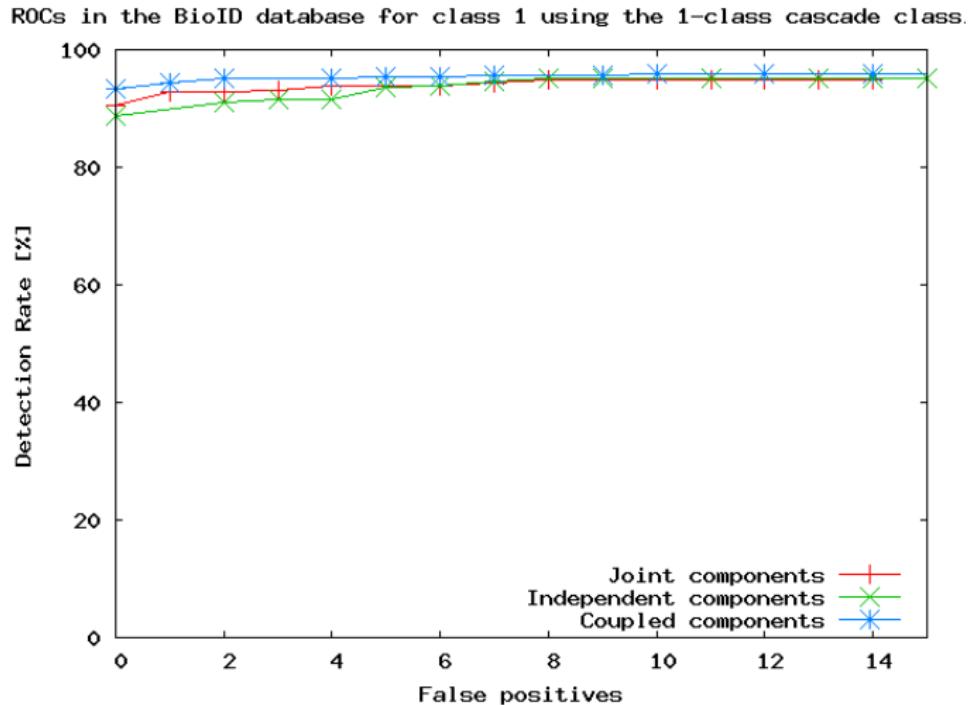


Figure: ROCs of the 1-class cascade used for detecting faces of class 1

## 2-classes

ROCs in the BioID database for class 1 using the 2-classes cascade clas:

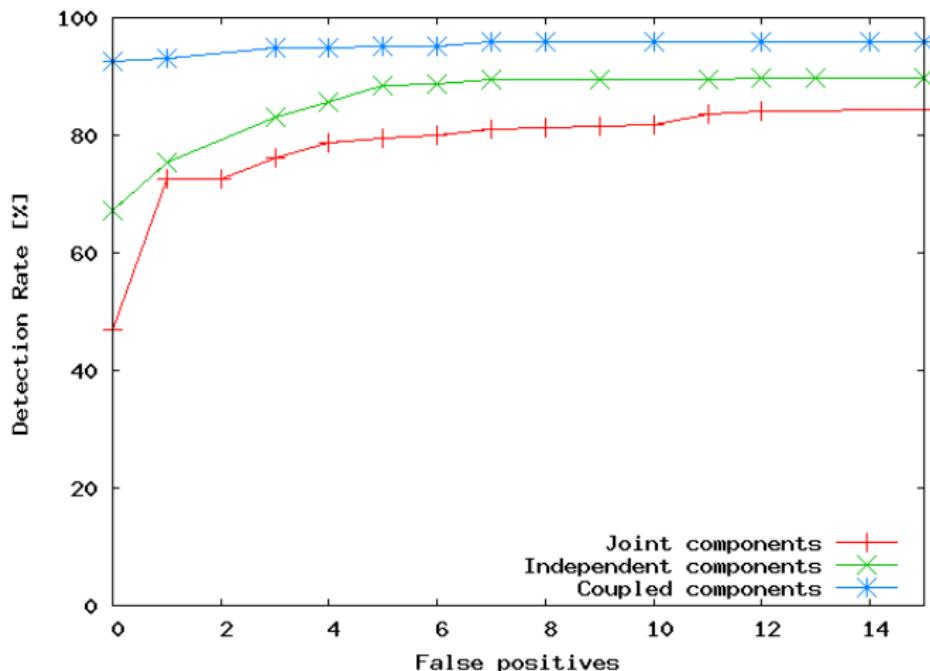


Figure: ROCs of the 2-classes cascade used for detecting faces of class 1

## 4-classes

ROCs in the BioID database for class 1 using the 4-classes cascade clas:

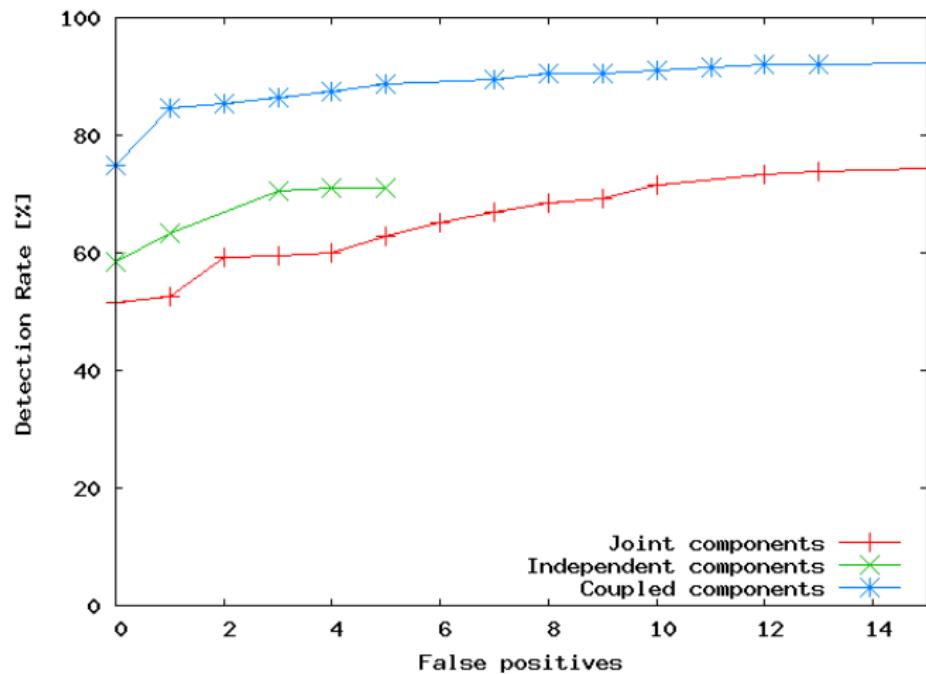


Figure: ROCs of the 4-classes cascade used for detecting faces of class 1

## 8-classes

ROCs in the BioID database for class 1 using the 8-classes cascade clas:

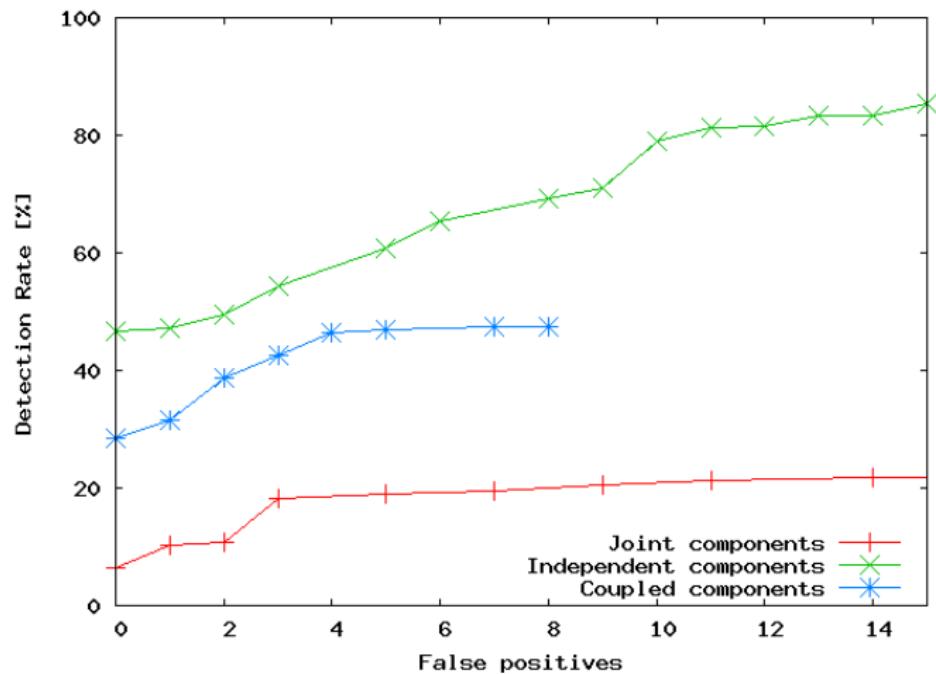


Figure: ROCs of the 8-classes cascade used for detecting faces of class 1

# Comparision

Table: Detection rate [%] for 5 false positives.

| Weak classifier's<br>training method | Number of classes |              |              |              |
|--------------------------------------|-------------------|--------------|--------------|--------------|
|                                      | 1                 | 2            | 4            | 8            |
| Independent                          | 93.56             | 88.36        | 71.07        | <b>60.88</b> |
| Jointly trained                      | 93.82             | 79.55        | 62.72        | 18.94        |
| Coupled                              | <b>95.27</b>      | <b>95.07</b> | <b>88.63</b> | 46.94        |

# Processing time

Table: Average processing time [sec] for a 384x286 pixels image

| Weak classifier's training method | Number of classes |      |      |      |
|-----------------------------------|-------------------|------|------|------|
|                                   | 1                 | 2    | 4    | 8    |
| Independent                       | 0.33              | 0.38 | 0.53 | 6.39 |
| Jointly trained                   | 0.33              | 0.52 | 1.33 | 0.95 |
| Coupled                           | 0.31              | 0.95 | 3.49 | 5.09 |

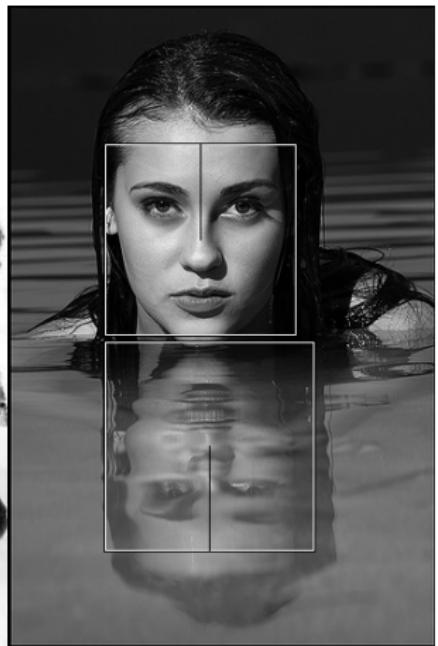
Table: Number of weak classifiers at the first layer of the cascade

| Weak classifier training's method | Number of classes |    |    |    |
|-----------------------------------|-------------------|----|----|----|
|                                   | 1                 | 2  | 4  | 8  |
| Independent                       | 12                | 10 | 8  | 28 |
| Jointly trained                   | 12                | 9  | 7  | 9  |
| Coupled                           | 9                 | 11 | 17 | 24 |

# 1-class case



## 4-classes case



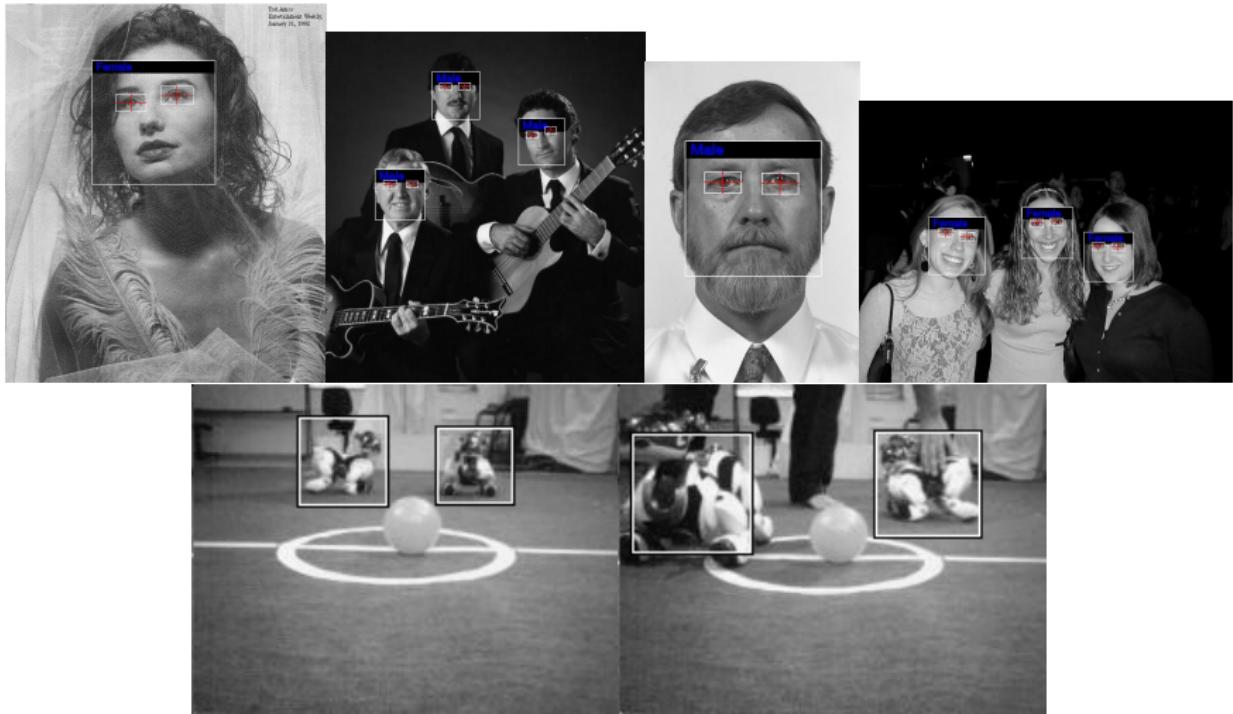
## 4-classes case



## 4-classes case



# 1-class case



# Results

## Training time

### 1-class

- Independent: 2.6 hours
- Joint: 2.6 hours
- Coupled: 2.6 hours

### 8-classes

- Independent: 37 hours
- Joint: 72.6 hours
- Coupled: 34.3 hours

# Summary

## Main proposed ideas

- Multiclass nested cascade
- Generalized version of Vector Boosting
- Use of coupled components
- Multiclass extention of bootstrapping

# Conclusions

## Features

- Using the right features is essential, in particular if the system will share features and classifier parameters

## Nested Cascade

- Number of weak classifiers in the first layer is almost the same for the three variants
- Number of weak classifiers in the first layer grows logarithmically with the number of classes
- Number of layers in the cascade does not grow with the number of classes

# Conclusions

## Vectorized weak classifiers

- Independent components:

- ▶ Reasonable results overall, but only the best in the case of 8-classes.
- ▶ It works well even when the classes are very “different”.
- ▶ It requires large size training set to avoid overfitting (preliminary results were not presented here)

- Joint components:

- ▶ Many times objects are detected but classes are confused.
- ▶ Does not scale well (Training is too slow)
- ▶ More weak classifiers are selected in the later layers of the cascade (slow).

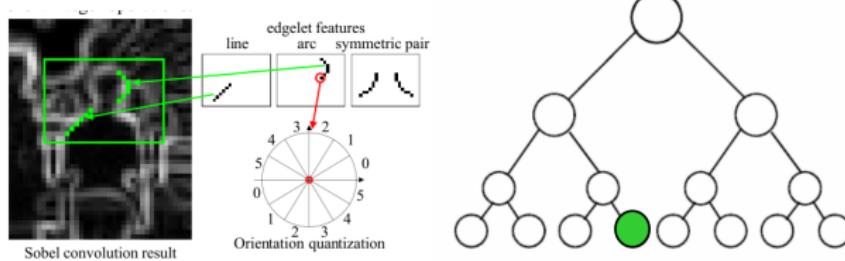
- Coupled components:

- ▶ Best results for 1,2 and 4 classes.
- ▶ They work quite well when the classes are “similar” .
- ▶ Scalable training (fast training).

# Future Work

## Some options of new features to implement

- Edged based
- Rotated Rectangular features:
- Gaussian features and transformations of it: rotation, bending, etc
- “Correlation” with parts of images
- SIFT
- ERCF



## Future work

- Use different training algorithms for training the multiclass weak classifier at different layers of the cascade

# Future work

Build a tree by split the nodes of the cascade as needed

Questions:

- When to split a node?
  - Split at every node of the cascade?
  - How to split the node? (how to group the classes?)
- 
- Which feature to use at each layer?
  - Which criteria to use in the selection of the features?
    - ▶ Trade off between processing speed/ accuracy and training time

[Geman et al.]

# Future work

## Speeding up the detection

- Sequential testing techniques to determine the optimal thresholds.
- Adjacent windows can be skipped depending on the output of the current window.

[Werman et al.]

# Thanks for your attention

Any questions?