#### **Radial Basis Functions**

## A Popular GLM For Surrogate Modeling Uses Radial Basis Functions

#### **Definition: Radial Basis Function (RBF)**

A radial basis function is a function  $\phi:\mathbb{R}^{\geq 0}\to\mathbb{R}$ , i.e. it maps non-negative real numbers to the real numbers.

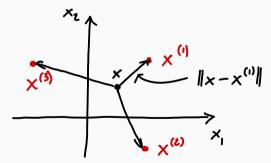


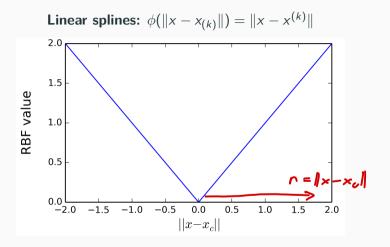
# A Popular GLM For Surrogate Modeling Uses Radial Basis Functions (cont.)

A (GLM) surrogate model using radial basis functions takes the form

$$\hat{f}(x,\alpha) = \sum_{k=1}^{p} \alpha_k \phi(\|x - x^{(k)}\|)$$

where  $\phi: \mathbb{R}^{\geq 0} \to \mathbb{R}$  is an RBF.





Thin-plate splines:  $\phi(\|x - x_{(k)}\|) = \|x - x^{(k)}\|_{p}^{p} \ln \|x - x^{(k)}\|, \qquad p \in [2, 4, 6, ...]$ 

