

Due: Thursday December 8, 2022

MATH 6800: Problem Set 9

1. (10 pts) Let $A \in \mathbb{R}^{m \times m}$ be a real symmetric matrix with eigenvalues λ_i and orthonormal eigenvectors $q_i, i = 1, 2, \dots, m$.
 - (a) Prove that for any vector $x \in \mathbb{R}^m$, the Rayleigh quotient $r(x)$, lies in the interval $[\lambda_{\min}, \lambda_{\max}]$, where λ_{\min} is the smallest eigenvalue and λ_{\max} the largest eigenvalue of A .

The Rayleigh quotient is given as:

$$r(x) = \frac{x^T A x}{x^T x}$$

Since, A has orthonormal eigenvectors q_i , they should span the space \mathbb{R}^m . Hence, $x = \sum_{i=1}^m c_i q_i$

$$\begin{aligned} r(x) &= \frac{(\sum_{i=1}^m c_i q_i)^T A (\sum_{i=1}^m c_i q_i)}{(\sum_{i=1}^m c_i q_i)^T (\sum_{i=1}^m c_i q_i)} \\ &= \frac{(\sum_{i=1}^m c_i q_i)^T \sum_{i=1}^m c_i \lambda_i q_i}{\sum_{i=1}^m c_i^2} \\ &= \frac{\sum_{i=1}^m c_i^2 \lambda_i}{\sum_{i=1}^m c_i^2} \end{aligned}$$

Since, all $c_i^2 \geq 0$, $r(x) \in [\lambda_{\min}, \lambda_{\max}]$.

- (b) Suppose that the eigenvalues of A satisfy,

$$|\lambda_1| > |\lambda_2| > |\lambda_3| > \dots > |\lambda_{m-1}| > |\lambda_m| \quad (1)$$

Given an initial guess $v^{(0)}$, how fast would the power method converge (in exact arithmetic) if

$$q_1^T v^{(0)} = 0, \quad q_i^T v^{(0)} \neq 0, \quad i = 2, 3, \dots, m \quad (2)$$

Explain your result. What would likely happen using floating point arithmetic with finite precision ?

We can write $v^{(0)} = c_1 q_1 + c_2 q_2 + \dots + c_m q_m$. Multiplying by q_1^T gives us $c_1 = 0 \implies v^{(0)} = c_2 q_2 + \dots + c_m q_m$.

$$\begin{aligned} v^{(k)} &= h_k A^k v^{(0)} \\ &= h_k A^k (c_2 q_2 + \dots + c_m q_m) \\ &= h_k (c_2 \lambda_2^k q_2 + \dots + c_m \lambda_m^k q_m) \end{aligned}$$

This means, we can't find the largest eigenvalue λ_1 even if $k \rightarrow \infty$.
In floating point arithmetic, $c_1 = \mathcal{O}(\varepsilon)$.

$$\begin{aligned} v^{(k)} &= h_k A^k v^{(0)} \\ &= h_k \left(\mathcal{O}(\varepsilon) \lambda_1^k q_1 + c_2 \lambda_2^k q_2 + \dots + c_m \lambda_m^k q_m \right) \\ &= h_k \lambda_1^k \left(\mathcal{O}(\varepsilon) q_1 + c_2 q_2 \frac{\lambda_2^k}{\lambda_1^k} + \dots + c_m q_m \frac{\lambda_m^k}{\lambda_1^k} \right) \end{aligned}$$

This means,

$$\begin{aligned} \left\| v^{(k)} - \pm q_1 \right\| &= \left\| q_1 (h_k \lambda_1^k \mathcal{O}(\varepsilon) - \pm 1) + h_k \lambda_1^k \left(c_2 q_2 \frac{\lambda_2^k}{\lambda_1^k} + \dots + c_m q_m \frac{\lambda_m^k}{\lambda_1^k} \right) \right\| \\ &\leq \left\| q_1 (h_k \varepsilon \lambda_1^k \pm 1) \right\| + \left\| h_k \lambda_1^k \left(c_2 q_2 \frac{\lambda_2^k}{\lambda_1^k} + \dots + c_m q_m \frac{\lambda_m^k}{\lambda_1^k} \right) \right\| \\ &\Rightarrow = \mathcal{O}(\varepsilon |\lambda_1|^k) + \mathcal{O} \left(\left| \frac{\lambda_2}{\lambda_1} \right|^k \right) \end{aligned}$$

2. (20 pts) Let A be the $m \times m$ tridiagonal matrix with entries

$$\begin{aligned} a_{i,i-1} &= -1, \\ a_{ii} &= 4 + i, \\ a_{i,i+1} &= -1. \end{aligned}$$

- (a) Write a Matlab code to use the power method to find the largest eigenvalue (denoted by λ) and corresponding eigenvector (denoted by v). Take $m = 10$ and use an initial guess of

$$v^{(0)} = [1, 1, 1, \dots, 1]^T. \quad (3)$$

Use the Matlab function **eig** to compute the exact answer for comparison. Perform **maxit** = 25 iterations, and at each iteration k , print the current estimate $\lambda^{(k)}$, the 2-norm of the error in $v^{(k)}$ and the ratio of the 2-norm error in $v^{(k)}$ at step k to the previous step $k - 1$. Use the following statement to output the result:

```
1 fprintf('k=%4d, lambda=%18.14f, error=%8.2e, v-err=%8.2f, ...
2      ratio=%8.5f', k, lambda, abs(lambda - lambda1), vErr, ratio);
```

The convergence rate indicated by **ratio** should approach a certain value. Explain where this value comes from.

Matlab function **powerIteration**($A, v0, maxit, l_ex, q_ex$) is written to find out λ_{max} . It is included in Listing 1. The convergence rate indicated by **ratio** approaches the ratio of $\left| \frac{\lambda_2}{\lambda_1} \right|$, where $|\lambda_1| > |\lambda_2|$. Using **eig**, $|\lambda_2| = 13.2107$, $|\lambda_1| = 14.75462$ and **ratio** = 0.8959. Fig 1 shows the command window for the problem under consideration.

```
1 function lambda_f = powerIteration(A, v0, maxit, l_ex, q_ex)
2
3 [m, ~] = size(A);
4 v = zeros(m, maxit+1);
```

```

5 lambda = zeros(maxit,1);
6 v(:,1) = v0;
7 for k=2:maxit+1
8     w = A*v(:,k-1);
9     v(:,k) = w/norm(w,2);
10    lambda(k-1) = v(:,k)'*A*v(:,k);
11    error = abs(lambda(k-1)-l_ex);
12    vErr = norm(v(:,k)-q_ex,2);
13    ratio = vErr/norm(v(:,k-1)-q_ex,2);
14    fprintf('k=%4d, lambda=%18.14f, error=%8.2e, vErr=%8.2e, ratio=%8.5f\n',k-1,...
15           lambda(k-1), error, vErr, ratio);
16 end
17
18 lambda_f = lambda(end);
19
20 end

```

Listing 1: `powerIteration(A,v0,maxit,l_ex,q_ex)`

```

k= 1, lambda= 9.73707533234860, error=5.01e+00, vErr=1.25e+00, ratio= 0.94465
k= 2, lambda= 11.05988335914097, error=3.69e+00, vErr=1.17e+00, ratio= 0.93520
k= 3, lambda= 11.89831252031907, error=2.85e+00, vErr=1.09e+00, ratio= 0.92760
k= 4, lambda= 12.50570116419184, error=2.24e+00, vErr=1.00e+00, ratio= 0.91975
k= 5, lambda= 12.98000433803850, error=1.77e+00, vErr=9.13e-01, ratio= 0.91246
k= 6, lambda= 13.35850150944157, error=1.39e+00, vErr=8.27e-01, ratio= 0.90632
k= 7, lambda= 13.66027653534852, error=1.09e+00, vErr=7.46e-01, ratio= 0.90152
k= 8, lambda= 13.89894732993262, error=8.47e-01, vErr=6.70e-01, ratio= 0.89801
k= 9, lambda= 14.08609281596197, error=6.60e-01, vErr=6.00e-01, ratio= 0.89560
k= 10, lambda= 14.23187724497717, error=5.14e-01, vErr=5.36e-01, ratio= 0.89406
k= 11, lambda= 14.34499977932975, error=4.01e-01, vErr=4.79e-01, ratio= 0.89315
k= 12, lambda= 14.43264659258538, error=3.14e-01, vErr=4.27e-01, ratio= 0.89270
k= 13, lambda= 14.50057846347998, error=2.46e-01, vErr=3.82e-01, ratio= 0.89256
k= 14, lambda= 14.55331497121092, error=1.93e-01, vErr=3.41e-01, ratio= 0.89261
k= 15, lambda= 14.59435296089282, error=1.52e-01, vErr=3.04e-01, ratio= 0.89278
k= 16, lambda= 14.62637667282058, error=1.20e-01, vErr=2.72e-01, ratio= 0.89302
k= 17, lambda= 14.65143932001440, error=9.48e-02, vErr=2.43e-01, ratio= 0.89328
k= 18, lambda= 14.67111067046611, error=7.51e-02, vErr=2.17e-01, ratio= 0.89356
k= 19, lambda= 14.68659271450290, error=5.96e-02, vErr=1.94e-01, ratio= 0.89382
k= 20, lambda= 14.69880839615397, error=4.74e-02, vErr=1.73e-01, ratio= 0.89407
k= 21, lambda= 14.70846887241110, error=3.77e-02, vErr=1.55e-01, ratio= 0.89430
k= 22, lambda= 14.71612420461681, error=3.01e-02, vErr=1.39e-01, ratio= 0.89450
k= 23, lambda= 14.72220150134279, error=2.40e-02, vErr=1.24e-01, ratio= 0.89469
k= 24, lambda= 14.72703365081295, error=1.92e-02, vErr=1.11e-01, ratio= 0.89485
k= 25, lambda= 14.73088102660057, error=1.53e-02, vErr=9.93e-02, ratio= 0.89500
|| v^k - ((+--q_ex)|| = 6.40e-02 = 0(|lambda_2/lambda_1|^k)
|lambda^k -lambda| = 4.10e-03 = 0(|lambda_2/lambda_1|^(2k))

```

Figure 1: command window of Q2.a

- (b) Write a Matlab code to use the Rayleigh quotient iteration to find a eigenvalue/eigen-vector pair of A . Take $m = 10$ and choose the initial guess

$$v^{(0)} = [1, 1, 1, \dots, 1]^T, \lambda^{(0)} = 10.5 \quad (4)$$

Perform **maxit** = 5 iterations, and at each iteration k print the current estimate $\lambda^{(k)}$, the error in $\lambda^{(k)}$, the 2-norm of the error in the eigenvector $v^{(k)}$ and the ratio of the error in $v^{(k)}$ at step k to *cube of the error* at the previous step $k-1$ (e.g. **ratio** = **vErr**/(**vErrOld**³)). Use the following statement to output the result:

```
1 fprintf('k=%4d lambda=%18.14f, error=%8.2e, v-err=%8.2e,...
2         ratio=%8.5f\n',k,lambda,abs(lambda-lambda1),vErr,ratio);
```

Matlab function **rayleighQuotient**($A, v0, l0, maxit, l_{ex}, q_{ex}$) is written in order to observe cubic convergence. The command window of convergence is shown in Fig 2.

```
1 function [lambda_f,v] = rayleighQuotient(A,v0,l0,maxit,l_ex,q_ex)
2
3 [m,~] = size(A);
4 lambda = zeros(maxit+1,1);
5 v = zeros(m,maxit+1);
6 v(:,1) = v0;
7 % lambda(1) = v(:,1)'*A*(v(:,1));
8 lambda(1)= l0;
9 I = eye(m);
10 vErrOld = norm(v(:,1)-q_ex,2);
11
12 for k=2:maxit+1
13     w = (A-lambda(k-1)*I)\v(:,k-1);
14     v(:,k) = w/norm(w,2);
15     lambda(k) = v(:,k)'*A*v(:,k);
16
17     error = abs(lambda(k)-l_ex);
18     if (mod(k,2)==0)
19         vErr = norm(v(:,k)+q_ex,2);
20     else
21         vErr = norm(v(:,k)-q_ex,2);
22     end
23
24     ratio = vErr/vErrOld^3;
25     fprintf('k=%4d, lambda=%18.14f, error=%8.2e, vErr=%8.2e, ratio=%8.5f
26     \n',...
27         k-1,lambda(k),error,vErr,ratio );
28     fprintf(' | lambda(k+1) - lambda | = %8.2e = 0( | lambda(k) - lambda
29     |^3) \n',...
30         (abs(lambda(k-1)-l_ex))^3 );
31     vErrOld = vErr;
32 end
33 lambda_f = lambda(end);
34 end
```

Listing 2: **rayleighQuotient**($A, v0, l0, maxit, l_{ex}, q_{ex}$)

The script written to generate matrix A and call these functions are in Listing 3.

```
1 clc
2 clear
3 %% Q2.a
4 m = 10;
5 A = zeros(m);
6
7 for i=1:m
8     if i~=1 && i~=m
9         A(i,i-1) = -1;
10        A(i,i) = 4+i;
```

```

k= 1, lambda= 10.30565571901764, error=3.05e-01, vErr=8.05e-01, ratio= 0.49953
| lambda(k+1) - lambda | = 1.25e-01 = 0(| lambda(k) - lambda |^3)
k= 2, lambda= 10.14294003846173, error=1.43e-01, vErr=4.00e-01, ratio= 0.76525
| lambda(k+1) - lambda | = 2.85e-02 = 0(| lambda(k) - lambda |^3)
k= 3, lambda= 10.00485453039090, error=4.64e-03, vErr=6.94e-02, ratio= 1.08508
| lambda(k+1) - lambda | = 2.91e-03 = 0(| lambda(k) - lambda |^3)
k= 4, lambda= 10.00021762235017, error=1.00e-07, vErr=3.22e-04, ratio= 0.96383
| lambda(k+1) - lambda | = 9.97e-08 = 0(| lambda(k) - lambda |^3)
k= 5, lambda= 10.00021752225710, error=1.78e-15, vErr=3.21e-11, ratio= 0.95997
| lambda(k+1) - lambda | = 1.00e-21 = 0(| lambda(k) - lambda |^3)

```

Figure 2: command window of Q2.b

```

11     A(i,i+1) = -1;
12     else
13         A(i,i) = 4+i;
14         if i==1
15             A(i,i+1) = -1;
16         else
17             A(i,i-1) = -1;
18         end
19     end
20 end
21
22 v0 = ones(m,1);
23 v0 = v0/norm(v0,2);
24 maxit = 25;
25 [q_m,l_m] = eig(A);
26 for i=1:m
27     l_m_vec(i) = l_m(i,i);
28 end
29 [l_ex,col] = max(l_m_vec);
30 q_ex = q_m(:,col);
31
32 lambda_p = powerIteration(A,v0,maxit,l_ex,q_ex);
33 fprintf('|| v^k - ((+/-)q_ex)|| = %8.2e = 0(|lambda_2/lambda_1|^k) \n',...
34         abs(l_m_vec(9)/l_ex)^maxit);
35 fprintf('|lambda^k -lambda| = %8.2e = 0(|lambda_2/lambda_1|^(2k))\n',...
36         abs(l_m_vec(9)/l_ex)^(2*maxit));
37 %% Q2.b
38 clc
39 maxit = 5;
40 l0 = 10.5;
41 [lambda_r,v_r] = rayleighQuotient(A,v0,l0,maxit,l_m_vec(6),q_m(:,6));

```

Listing 3: Q2 script

3. (20 pts) QR program. Let $A \in \mathbb{R}^{m \times m}$ be the real symmetric tridiagonal matrix with 2 on the diagonal and -1 on the subdiagonal and superdiagonal.

$$A = \begin{bmatrix} 2 & -1 & & & \\ -1 & 2 & -1 & & \\ & -1 & 2 & -1 & \\ & & \ddots & \ddots & \ddots \\ & & & -1 & 2 \end{bmatrix}$$

Let $\delta(k)$ denote the maximum of the absolute values of the off-diagonal entries of the QR matrix $A^{(k)}$.

Write a program that computes the eigenvalues of A using the UNSHIFTED QR eigenvalue algorithm using the Matlab **qr** function. After each 10 iterations, $k = 10, 20, 30, \dots$, print $k, \delta(k)$ and the convergence ratio $r(k) = \delta(k)/\delta(k-1)$. For example, you could use a statement such as

```
1 fprintf('QR: k=%d : delta%8.2e, ratio=%5.3f\n',k,delta,delta/deltaOld);
```

Continue iterating until $\delta(k) < \text{tol} = 10^{-5}$.

- Show results for $m = 11$. (Hint: you may want to test your code using a smaller value of m).
Included in Figure 3.
- After convergence print the eigenvalues found.
Included in Figure 3.
- Also print the maximum error in the eigenvalues compared to those obtained from the Matlab routine **eig** (Hint: you may want to use the Matlab **sort** function to sort the eigenvalues before comparing).
Included in Figure 3.
- What is the numerically observed asymptotic convergence ratio $r(k)$? Is the convergence linear? Can you relate the convergence rate to the eigenvalues of A ?
The numerically converged ratio at the final iteration is $r(203) = 0.949184032947667$. The convergence was linear. Here (for values of $\delta(203), C$ refer Figure 3),

$$C = \max_{1 \leq k \leq m} \left| \frac{\lambda_k}{\lambda_{k-1}} \right|,$$

$$|\lambda_1| > |\lambda_2| > \dots > |\lambda_m|,$$

$$\delta(k) = \mathcal{O}(C^k)$$

As, $\delta(203) = 9.74e - 06$ and $C^{203} = 2.5243e - 05$, you can see they are almost of the same order.

Matlab function **pureQR**(A, maxit) is shown in Listing 4 and the script written to generate matrix A and compute its eigenvalues are in Listing 5. The command window displaying all the solutions are shown in Figure 3.

```
1 function [L,del,kc] = pureQR(A,maxit)
2
3 L = A;
4 deltaOld = maxAbsOffDiag(L);
5 tol = 1e-5;
6 for k=1:maxit
7     [Qk,Rk] = qr(L);
8     L = Rk*Qk;
9     delta = maxAbsOffDiag(L);
10    ratio = delta/deltaOld;
11    del(k) = ratio;
12    if (mod(k,10)==0)
13        fprintf('QR: k = %d, delta = %8.2e, ratio = %5.3f \n',...
14            k, delta, ratio);
15    end
```

```

16     if (delta < tol)
17         fprintf('Converged with tolerance delta = %8.2e at iteration = %d\n',
delta,k);
18         kc = k;
19         break;
20     end
21     deltaOld = delta;
22 end
23
24 end

```

Listing 4: `pureQR(A,maxit)`

```

1 %% Q3
2 clc
3 clear
4 m = 11;
5 maxit = 1000;
6 A = zeros(m);
7
8 for i=1:m
9     if i~=1 && i~=m
10         A(i,i-1) = -1;
11         A(i,i) = 2;
12         A(i,i+1) = -1;
13     else
14         A(i,i) = 2;
15         if i==1
16             A(i,i+1) = -1;
17         else
18             A(i,i-1) = -1;
19         end
20     end
21 end
22
23 [L,del,kc] = pureQR(A,maxit);
24 l_m = eig(A);
25 for i=1:m
26     l_qr(i,1) = L(i,i);
27 end
28
29 l_qr = sort(l_qr);
30 disp("Eigenvalues sorted : ");
31 disp(l_qr);
32
33 maxErr = max(abs(l_qr-l_m));
34 fprintf('maxErr =%8.2e \n', maxErr);
35
36 al_qr = sort(abs(l_qr));
37 max = al_qr(1)/al_qr(2);
38 for i=1:m-1
39     t = al_qr(i)/al_qr(i+1);
40     if t > max
41         max = t;
42     end
43 end
44 fprintf('C = %5.3f = ratio(kc)\n', max);

```

Listing 5: Q3 script

```
QR: k = 10, delta = 4.83e-01, ratio = 0.920
QR: k = 20, delta = 1.77e-01, ratio = 0.937
QR: k = 30, delta = 8.19e-02, ratio = 0.918
QR: k = 40, delta = 4.56e-02, ratio = 0.954
QR: k = 50, delta = 2.79e-02, ratio = 0.951
QR: k = 60, delta = 1.68e-02, ratio = 0.950
QR: k = 70, delta = 1.00e-02, ratio = 0.949
QR: k = 80, delta = 5.95e-03, ratio = 0.949
QR: k = 90, delta = 3.53e-03, ratio = 0.949
QR: k = 100, delta = 2.10e-03, ratio = 0.949
QR: k = 110, delta = 1.24e-03, ratio = 0.949
QR: k = 120, delta = 7.39e-04, ratio = 0.949
QR: k = 130, delta = 4.39e-04, ratio = 0.949
QR: k = 140, delta = 2.60e-04, ratio = 0.949
QR: k = 150, delta = 1.55e-04, ratio = 0.949
QR: k = 160, delta = 9.18e-05, ratio = 0.949
QR: k = 170, delta = 5.45e-05, ratio = 0.949
QR: k = 180, delta = 3.23e-05, ratio = 0.949
QR: k = 190, delta = 1.92e-05, ratio = 0.949
QR: k = 200, delta = 1.14e-05, ratio = 0.949
Converged with tolerance delta = 9.74e-06 at iteration = 203
Eigenvalues sorted :
    0.0681
    0.2679
    0.5858
    1.0000
    1.4824
    2.0000
    2.5176
    3.0000
    3.4142
    3.7321
    3.9319

maxErr =4.75e-10
C = 0.949 = ratio(kc)
>>
```

Figure 3: command window for Q3

4. (20 pts) Shifted QR program. Repeat question (3) but with writing a code using the SHIFTED QR eigenvalue algorithm with deflation (you may write a new code or write one code that can use a shift or not). Choose the shift based on the Wilkinson shift. The eigenvalues should converge from the *bottom* right corner. When the off-diagonal entry next to the bottom corner has a magnitude less than $\text{tol} = 10^{-5}$, declare the eigenvalue to be converged and deflate the matrix to be one dimension less by eliminating the last row and last column. Continue the shifted QR with deflation on the remaining smaller matrix.

- Show results for $m = 11$.

Included in (pages 1-14) Figure 4.

- After *each* QR iteration, $k = 1, 2, 3, \dots$, print k , the shift $\mu(k)$, the current dimension of the matrix $m(k)$, the value of $\delta(k)$ and the convergence ratio $r(k) = \delta(k)/\delta(k-1)$, $k = 1, 2, \dots$. Continue iterating until all eigenvalues have been found.

Included in (page 1-14) Figure 4.

- After convergence print the eigenvalues found.

Included in (page 14) Figure 4.

- Also print the maximum error in the eigenvalues compared to those obtained from the Matlab routine `eig`.

Included in (page 14) Figure 4.

- How does the convergence of the shifted QR algorithm compare to the unshifted. Does the convergence rate look linear?

Here, the error for each deflated matrix starting from $m = 11$ to $m = 2$ are independently showing linear convergence. But overall, it doesn't show linear convergence.

Matlab function `shiftedQR(A, maxit)` is in Listing 6 and the script to generate the matrix and run this problem is in Listing 7. The solutions are attached in Figure 4.

```

1 function [lambda,d,kc] = shiftedQR(A,maxit)
2
3 [~,H] = hessenberg(A);
4 L = H;
5 [m,~] = size(A);
6 tol = 1e-5;
7 lambda = zeros(m,1);
8
9 deltaOld = maxAbsOffDiag(L);
10 numEig = 0;
11
12 for k=1:maxit
13     if m==1
14         kc = k;
15         numEig = numEig+1;
16         lambda(numEig) = L(1,1);
17         disp('converged');
18         break;
19     end
20     I = eye(m);
21     L = L(1:m,1:m);
22     mk = wilkinsonShift(L);
23     [Qk,Rk] = qr(L-mk*I);
24     L = Rk*Qk + mk*I;
25     delta = maxAbsOffDiag(L);
26     ratio = delta/deltaOld;

```

```

27     d(k) = ratio;
28     fprintf('k=%d,shift(k)=%18.14f,m(k)=%d,delta(k)=%8.2e,ratio(k)=%8.5f\n',
    ,...
29         k,mk,m,delta,ratio);
30     deltaOld = delta;
31
32     if (abs(L(m,m-1))< tol || abs(L(m-1,m))<tol)
33         fprintf('Eigenvalue found, lambda=%18.14f \n', L(m,m));
34         numEig = numEig + 1;
35         lambda(numEig) = L(m,m);
36         m = m - 1;
37     end
38
39 end
40
41 end

```

Listing 6: **shiftedQR**($A, maxit$)

```

1  clc
2  clear
3  m = 11;
4  maxit = 1000;
5  A = zeros(m);
6
7  for i=1:m
8      if i~=1 && i~=m
9          A(i,i-1) = -1;
10         A(i,i) = 2;
11         A(i,i+1) = -1;
12     else
13         A(i,i) = 2;
14         if i==1
15             A(i,i+1) = -1;
16         else
17             A(i,i-1) = -1;
18         end
19     end
20 end
21 l_m = eig(A);
22 [l_sqr,del,kc] = shiftedQR(A,maxit);
23 disp('Sorted Eigenvalues are: ');
24 disp(sort(l_sqr));
25 maxErr = max(abs(sort(l_sqr)-l_m));
26 fprintf('maxErr = %8.2e \n', maxErr);

```

Listing 7: Q4 script

```
k=1,shift(k)= 1.00000000000000,m(k)=11,delta(k)=1.22e+00, ratio(k)= 1.22474
Eigenvalue found, lambda= 1.00000000000000
k=2,shift(k)= 2.73214285714286,m(k)=10,delta(k)=1.43e+00, ratio(k)= 1.16988
k=3,shift(k)= 4.66612016350531,m(k)=10,delta(k)=1.21e+00, ratio(k)= 0.84356
k=4,shift(k)= 6.41910616617420,m(k)=10,delta(k)=1.08e+00, ratio(k)= 0.89334
k=5,shift(k)= 5.71589521598939,m(k)=10,delta(k)=1.17e+00, ratio(k)= 1.08291
k=6,shift(k)= 5.67053736498980,m(k)=10,delta(k)=1.22e+00, ratio(k)= 1.04209
k=7,shift(k)= 7.38259394802086,m(k)=10,delta(k)=1.07e+00, ratio(k)= 0.88131
k=8,shift(k)= 6.85556363298719,m(k)=10,delta(k)=1.01e+00, ratio(k)= 0.93792
k=9,shift(k)= 6.36787782476205,m(k)=10,delta(k)=1.14e+00, ratio(k)= 1.13182
k=10,shift(k)= 6.00083910737372,m(k)=10,delta(k)=1.10e+00, ratio(k)= 0.96085
k=11,shift(k)= 5.84981060762899,m(k)=10,delta(k)=9.24e-01, ratio(k)= 0.84371
k=12,shift(k)= 5.99015356171707,m(k)=10,delta(k)=7.96e-01, ratio(k)= 0.86101
k=13,shift(k)= 6.40699909882951,m(k)=10,delta(k)=6.36e-01, ratio(k)= 0.79941
k=14,shift(k)= 6.99469080305070,m(k)=10,delta(k)=5.85e-01, ratio(k)= 0.91950
k=15,shift(k)= 7.65084236842359,m(k)=10,delta(k)=5.95e-01, ratio(k)= 1.01802
k=16,shift(k)= 8.31788033682743,m(k)=10,delta(k)=5.96e-01, ratio(k)= 1.00074
k=17,shift(k)= 8.96909275569967,m(k)=10,delta(k)=5.87e-01, ratio(k)= 0.98570
k=18,shift(k)= 9.59284991844250,m(k)=10,delta(k)=5.72e-01, ratio(k)= 0.97345
k=19,shift(k)= 10.18454289169625,m(k)=10,delta(k)=5.51e-01, ratio(k)= 0.96382
k=20,shift(k)= 10.74291434109595,m(k)=10,delta(k)=5.27e-01, ratio(k)= 0.95641
k=21,shift(k)= 11.26835184365611,m(k)=10,delta(k)=5.01e-01, ratio(k)= 0.95081
k=22,shift(k)= 11.76205318400997,m(k)=10,delta(k)=4.74e-01, ratio(k)= 0.94663
k=23,shift(k)= 12.22559811094811,m(k)=10,delta(k)=4.48e-01, ratio(k)= 0.94358
k=24,shift(k)= 12.66072050361658,m(k)=10,delta(k)=4.21e-01, ratio(k)= 0.94140
k=25,shift(k)= 13.06918455416562,m(k)=10,delta(k)=3.96e-01, ratio(k)= 0.93989
k=26,shift(k)= 13.45271729516567,m(k)=10,delta(k)=3.72e-01, ratio(k)= 0.93889
k=27,shift(k)= 13.81297268438531,m(k)=10,delta(k)=3.49e-01, ratio(k)= 0.93828
k=28,shift(k)= 14.15151379071763,m(k)=10,delta(k)=3.27e-01, ratio(k)= 0.93798
k=29,shift(k)= 14.46980550832058,m(k)=10,delta(k)=3.07e-01, ratio(k)= 0.93790
k=30,shift(k)= 14.76921341036566,m(k)=10,delta(k)=2.88e-01, ratio(k)= 0.93799
k=31,shift(k)= 15.05100614024986,m(k)=10,delta(k)=2.70e-01, ratio(k)= 0.93820
k=32,shift(k)= 15.31635977144913,m(k)=10,delta(k)=2.53e-01, ratio(k)= 0.93851
k=33,shift(k)= 15.56636318042552,m(k)=10,delta(k)=2.47e-01, ratio(k)= 0.97415
k=34,shift(k)= 15.80202384869601,m(k)=10,delta(k)=2.43e-01, ratio(k)= 0.98353
k=35,shift(k)= 16.02427373929420,m(k)=10,delta(k)=2.39e-01, ratio(k)= 0.98337
k=36,shift(k)= 16.23397503587894,m(k)=10,delta(k)=2.35e-01, ratio(k)= 0.98318
k=37,shift(k)= 16.43192562278312,m(k)=10,delta(k)=2.31e-01, ratio(k)= 0.98298
k=38,shift(k)= 16.61886424116918,m(k)=10,delta(k)=2.27e-01, ratio(k)= 0.98277
k=39,shift(k)= 16.79547529232702,m(k)=10,delta(k)=2.23e-01, ratio(k)= 0.98255
k=40,shift(k)= 16.96239328154072,m(k)=10,delta(k)=2.19e-01, ratio(k)= 0.98233
k=41,shift(k)= 17.12020690968819,m(k)=10,delta(k)=2.15e-01, ratio(k)= 0.98210
k=42,shift(k)= 17.26946282782602,m(k)=10,delta(k)=2.11e-01, ratio(k)= 0.98188
k=43,shift(k)= 17.41066907447954,m(k)=10,delta(k)=2.07e-01, ratio(k)= 0.98165
k=44,shift(k)= 17.54429821747490,m(k)=10,delta(k)=2.03e-01, ratio(k)= 0.98143
k=45,shift(k)= 17.67079022276138,m(k)=10,delta(k)=2.00e-01, ratio(k)= 0.98120
k=46,shift(k)= 17.79055507235704,m(k)=10,delta(k)=1.96e-01, ratio(k)= 0.98099
k=47,shift(k)= 17.90397515267340,m(k)=10,delta(k)=1.92e-01, ratio(k)= 0.98077
k=48,shift(k)= 18.01140743326012,m(k)=10,delta(k)=1.88e-01, ratio(k)= 0.98057
k=49,shift(k)= 18.11318545465202,m(k)=10,delta(k)=1.85e-01, ratio(k)= 0.98036
k=50,shift(k)= 18.20962114257717,m(k)=10,delta(k)=1.81e-01, ratio(k)= 0.98017
k=51,shift(k)= 18.30100646437012,m(k)=10,delta(k)=1.77e-01, ratio(k)= 0.97997
k=52,shift(k)= 18.38761494207120,m(k)=10,delta(k)=1.74e-01, ratio(k)= 0.97979
k=53,shift(k)= 18.46970303539903,m(k)=10,delta(k)=1.70e-01, ratio(k)= 0.97961
k=54,shift(k)= 18.54751140659137,m(k)=10,delta(k)=1.67e-01, ratio(k)= 0.97944
k=55,shift(k)= 18.62126607797589,m(k)=10,delta(k)=1.63e-01, ratio(k)= 0.97927
k=56,shift(k)= 18.69117949213101,m(k)=10,delta(k)=1.60e-01, ratio(k)= 0.97911
k=57,shift(k)= 18.75745148354902,m(k)=10,delta(k)=1.56e-01, ratio(k)= 0.97895
```

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k=58,shift(k)= 18.82027016987720,m(k)=10,delta(k)=1.53e-01, ratio(k)= 0.97880
k=59,shift(k)= 18.87981277003063,m(k)=10,delta(k)=1.50e-01, ratio(k)= 0.97866
k=60,shift(k)= 18.93624635578591,m(k)=10,delta(k)=1.47e-01, ratio(k)= 0.97852
k=61,shift(k)= 18.98972854282464,m(k)=10,delta(k)=1.43e-01, ratio(k)= 0.97838
k=62,shift(k)= 19.04040812663307,m(k)=10,delta(k)=1.40e-01, ratio(k)= 0.97826
k=63,shift(k)= 19.08842566815107,m(k)=10,delta(k)=1.37e-01, ratio(k)= 0.97813
k=64,shift(k)= 19.13391403359641,m(k)=10,delta(k)=1.34e-01, ratio(k)= 0.97801
k=65,shift(k)= 19.17699889247723,m(k)=10,delta(k)=1.31e-01, ratio(k)= 0.97790
k=66,shift(k)= 19.21779917742923,m(k)=10,delta(k)=1.28e-01, ratio(k)= 0.97779
k=67,shift(k)= 19.25642750917056,m(k)=10,delta(k)=1.26e-01, ratio(k)= 0.97769
k=68,shift(k)= 19.29299058956457,m(k)=10,delta(k)=1.23e-01, ratio(k)= 0.97759
k=69,shift(k)= 19.32758956550640,m(k)=10,delta(k)=1.20e-01, ratio(k)= 0.97749
k=70,shift(k)= 19.36032036609266,m(k)=10,delta(k)=1.17e-01, ratio(k)= 0.97740
k=71,shift(k)= 19.39127401531596,m(k)=10,delta(k)=1.15e-01, ratio(k)= 0.97732
k=72,shift(k)= 19.42053692231968,m(k)=10,delta(k)=1.12e-01, ratio(k)= 0.97723
k=73,shift(k)= 19.44819115106095,m(k)=10,delta(k)=1.09e-01, ratio(k)= 0.97715
k=74,shift(k)= 19.47431467106874,m(k)=10,delta(k)=1.07e-01, ratio(k)= 0.97708
k=75,shift(k)= 19.49898159083199,m(k)=10,delta(k)=1.04e-01, ratio(k)= 0.97700
k=76,shift(k)= 19.52226237521399,m(k)=10,delta(k)=1.02e-01, ratio(k)= 0.97693
k=77,shift(k)= 19.54422404816768,m(k)=10,delta(k)=9.97e-02, ratio(k)= 0.97687
k=78,shift(k)= 19.56493038191549,m(k)=10,delta(k)=9.74e-02, ratio(k)= 0.97680
k=79,shift(k)= 19.58444207365317,m(k)=10,delta(k)=9.51e-02, ratio(k)= 0.97674
k=80,shift(k)= 19.60281691075036,m(k)=10,delta(k)=9.29e-02, ratio(k)= 0.97668
k=81,shift(k)= 19.62010992532682,m(k)=10,delta(k)=9.07e-02, ratio(k)= 0.97663
k=82,shift(k)= 19.63637353902027,m(k)=10,delta(k)=8.86e-02, ratio(k)= 0.97657
k=83,shift(k)= 19.65165769868291,m(k)=10,delta(k)=8.65e-02, ratio(k)= 0.97652
k=84,shift(k)= 19.66601000368568,m(k)=10,delta(k)=8.45e-02, ratio(k)= 0.97647
k=85,shift(k)= 19.67947582545286,m(k)=10,delta(k)=8.25e-02, ratio(k)= 0.97642
k=86,shift(k)= 19.69209841979026,m(k)=10,delta(k)=8.05e-02, ratio(k)= 0.97638
k=87,shift(k)= 19.70391903253648,m(k)=10,delta(k)=7.86e-02, ratio(k)= 0.97634
k=88,shift(k)= 19.71497699900956,m(k)=10,delta(k)=7.68e-02, ratio(k)= 0.97629
k=89,shift(k)= 19.72530983769314,m(k)=10,delta(k)=7.49e-02, ratio(k)= 0.97625
k=90,shift(k)= 19.73495333856149,m(k)=10,delta(k)=7.32e-02, ratio(k)= 0.97622
k=91,shift(k)= 19.74394164641949,m(k)=10,delta(k)=7.14e-02, ratio(k)= 0.97618
k=92,shift(k)= 19.75230733959553,m(k)=10,delta(k)=6.97e-02, ratio(k)= 0.97615
k=93,shift(k)= 19.76008150429836,m(k)=10,delta(k)=6.80e-02, ratio(k)= 0.97611
k=94,shift(k)= 19.76729380493835,m(k)=10,delta(k)=6.64e-02, ratio(k)= 0.97608
k=95,shift(k)= 19.77397255066708,m(k)=10,delta(k)=6.48e-02, ratio(k)= 0.97605
k=96,shift(k)= 19.78014475838910,m(k)=10,delta(k)=6.33e-02, ratio(k)= 0.97602
k=97,shift(k)= 19.78583621246924,m(k)=10,delta(k)=6.18e-02, ratio(k)= 0.97599
k=98,shift(k)= 19.79107152134888,m(k)=10,delta(k)=6.11e-02, ratio(k)= 0.98948
k=99,shift(k)= 19.79587417126042,m(k)=10,delta(k)=6.06e-02, ratio(k)= 0.99141
k=100,shift(k)= 19.80026657722198,m(k)=10,delta(k)=6.01e-02, ratio(k)= 0.99139
k=101,shift(k)= 19.80427013147965,m(k)=10,delta(k)=5.95e-02, ratio(k)= 0.99137
k=102,shift(k)= 19.80790524954435,m(k)=10,delta(k)=5.90e-02, ratio(k)= 0.99135
k=103,shift(k)= 19.81119141397460,m(k)=10,delta(k)=5.85e-02, ratio(k)= 0.99133
k=104,shift(k)= 19.81414721603466,m(k)=10,delta(k)=5.80e-02, ratio(k)= 0.99131
k=105,shift(k)= 19.81679039534368,m(k)=10,delta(k)=5.75e-02, ratio(k)= 0.99129
k=106,shift(k)= 19.81913787764357,m(k)=10,delta(k)=5.70e-02, ratio(k)= 0.99127
k=107,shift(k)= 19.82120581077641,m(k)=10,delta(k)=5.65e-02, ratio(k)= 0.99125
k=108,shift(k)= 19.82300959898476,m(k)=10,delta(k)=5.60e-02, ratio(k)= 0.99123
k=109,shift(k)= 19.82456393561607,m(k)=10,delta(k)=5.55e-02, ratio(k)= 0.99121
k=110,shift(k)= 19.82588283432292,m(k)=10,delta(k)=5.50e-02, ratio(k)= 0.99119
k=111,shift(k)= 19.82697965883813,m(k)=10,delta(k)=5.45e-02, ratio(k)= 0.99117
k=112,shift(k)= 19.82786715140033,m(k)=10,delta(k)=5.41e-02, ratio(k)= 0.99116
k=113,shift(k)= 19.82855745989625,m(k)=10,delta(k)=5.36e-02, ratio(k)= 0.99114
k=114,shift(k)= 19.82906216379284,m(k)=10,delta(k)=5.31e-02, ratio(k)= 0.99112
k=115,shift(k)= 19.82939229891026,m(k)=10,delta(k)=5.26e-02, ratio(k)= 0.99110
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k=116,shift(k)= 19.82955838110525,m(k)=10,delta(k)=5.22e-02, ratio(k)= 0.99108
k=117,shift(k)= 19.82957042891046,m(k)=10,delta(k)=5.17e-02, ratio(k)= 0.99106
k=118,shift(k)= 19.82943798518506,m(k)=10,delta(k)=5.12e-02, ratio(k)= 0.99104
k=119,shift(k)= 19.82917013782181,m(k)=10,delta(k)=5.08e-02, ratio(k)= 0.99102
k=120,shift(k)= 19.82877553955445,m(k)=10,delta(k)=5.03e-02, ratio(k)= 0.99101
k=121,shift(k)= 19.82826242691691,m(k)=10,delta(k)=4.99e-02, ratio(k)= 0.99099
k=122,shift(k)= 19.82763863837793,m(k)=10,delta(k)=4.94e-02, ratio(k)= 0.99097
k=123,shift(k)= 19.82691163170821,m(k)=10,delta(k)=4.90e-02, ratio(k)= 0.99095
k=124,shift(k)= 19.82608850060241,m(k)=10,delta(k)=4.85e-02, ratio(k)= 0.99094
k=125,shift(k)= 19.82517599058911,m(k)=10,delta(k)=4.81e-02, ratio(k)= 0.99092
k=126,shift(k)= 19.82418051427010,m(k)=10,delta(k)=4.76e-02, ratio(k)= 0.99090
k=127,shift(k)= 19.82310816591546,m(k)=10,delta(k)=4.72e-02, ratio(k)= 0.99088
k=128,shift(k)= 19.82196473543703,m(k)=10,delta(k)=4.68e-02, ratio(k)= 0.99087
k=129,shift(k)= 19.82075572177522,m(k)=10,delta(k)=4.63e-02, ratio(k)= 0.99085
k=130,shift(k)= 19.81948634571855,m(k)=10,delta(k)=4.59e-02, ratio(k)= 0.99083
k=131,shift(k)= 19.81816156219010,m(k)=10,delta(k)=4.55e-02, ratio(k)= 0.99082
k=132,shift(k)= 19.81678607201196,m(k)=10,delta(k)=4.51e-02, ratio(k)= 0.99080
k=133,shift(k)= 19.81536433317632,m(k)=10,delta(k)=4.47e-02, ratio(k)= 0.99078
k=134,shift(k)= 19.81390057164771,m(k)=10,delta(k)=4.43e-02, ratio(k)= 0.99077
k=135,shift(k)= 19.81239879170684,m(k)=10,delta(k)=4.38e-02, ratio(k)= 0.99075
k=136,shift(k)= 19.81086278586641,m(k)=10,delta(k)=4.34e-02, ratio(k)= 0.99074
k=137,shift(k)= 19.80929614436614,m(k)=10,delta(k)=4.30e-02, ratio(k)= 0.99072
k=138,shift(k)= 19.807770226427252,m(k)=10,delta(k)=4.26e-02, ratio(k)= 0.99071
k=139,shift(k)= 19.80608435819710,m(k)=10,delta(k)=4.22e-02, ratio(k)= 0.99069
k=140,shift(k)= 19.80444546264771,m(k)=10,delta(k)=4.18e-02, ratio(k)= 0.99068
k=141,shift(k)= 19.80278844603085,m(k)=10,delta(k)=4.15e-02, ratio(k)= 0.99066
k=142,shift(k)= 19.80111601631473,m(k)=10,delta(k)=4.11e-02, ratio(k)= 0.99065
k=143,shift(k)= 19.79943072837583,m(k)=10,delta(k)=4.07e-02, ratio(k)= 0.99063
k=144,shift(k)= 19.79773499102979,m(k)=10,delta(k)=4.03e-02, ratio(k)= 0.99062
k=145,shift(k)= 19.79603107377213,m(k)=10,delta(k)=3.99e-02, ratio(k)= 0.99061
k=146,shift(k)= 19.79432111322842,m(k)=10,delta(k)=3.95e-02, ratio(k)= 0.99059
k=147,shift(k)= 19.79260711933733,m(k)=10,delta(k)=3.92e-02, ratio(k)= 0.99058
k=148,shift(k)= 19.79089098126932,m(k)=10,delta(k)=3.88e-02, ratio(k)= 0.99057
k=149,shift(k)= 19.78917447309597,m(k)=10,delta(k)=3.84e-02, ratio(k)= 0.99055
k=150,shift(k)= 19.78745925921553,m(k)=10,delta(k)=3.81e-02, ratio(k)= 0.99054
k=151,shift(k)= 19.78574689955295,m(k)=10,delta(k)=3.77e-02, ratio(k)= 0.99053
k=152,shift(k)= 19.78403885453433,m(k)=10,delta(k)=3.74e-02, ratio(k)= 0.99052
k=153,shift(k)= 19.78233648984738,m(k)=10,delta(k)=3.70e-02, ratio(k)= 0.99050
k=154,shift(k)= 19.78064108100416,m(k)=10,delta(k)=3.66e-02, ratio(k)= 0.99049
k=155,shift(k)= 19.77895381770281,m(k)=10,delta(k)=3.63e-02, ratio(k)= 0.99048
k=156,shift(k)= 19.77727580800372,m(k)=10,delta(k)=3.60e-02, ratio(k)= 0.99047
k=157,shift(k)= 19.77560808232455,m(k)=10,delta(k)=3.56e-02, ratio(k)= 0.99046
k=158,shift(k)= 19.77395159726604,m(k)=10,delta(k)=3.53e-02, ratio(k)= 0.99044
k=159,shift(k)= 19.77230723926731,m(k)=10,delta(k)=3.49e-02, ratio(k)= 0.99043
k=160,shift(k)= 19.77067582810450,m(k)=10,delta(k)=3.46e-02, ratio(k)= 0.99042
k=161,shift(k)= 19.76905812023760,m(k)=10,delta(k)=3.43e-02, ratio(k)= 0.99041
k=162,shift(k)= 19.76745481201073,m(k)=10,delta(k)=3.39e-02, ratio(k)= 0.99040
k=163,shift(k)= 19.76586654271124,m(k)=10,delta(k)=3.36e-02, ratio(k)= 0.99039
k=164,shift(k)= 19.76429389749443,m(k)=10,delta(k)=3.33e-02, ratio(k)= 0.99038
k=165,shift(k)= 19.76273741018185,m(k)=10,delta(k)=3.30e-02, ratio(k)= 0.99037
k=166,shift(k)= 19.76119756593006,m(k)=10,delta(k)=3.26e-02, ratio(k)= 0.99036
k=167,shift(k)= 19.75967480378589,m(k)=10,delta(k)=3.23e-02, ratio(k)= 0.99035
k=168,shift(k)= 19.75816951912932,m(k)=10,delta(k)=3.20e-02, ratio(k)= 0.99034
k=169,shift(k)= 19.75668206599935,m(k)=10,delta(k)=3.17e-02, ratio(k)= 0.99033
k=170,shift(k)= 19.75521275932359,m(k)=10,delta(k)=3.14e-02, ratio(k)= 0.99032
k=171,shift(k)= 19.75376187704106,m(k)=10,delta(k)=3.11e-02, ratio(k)= 0.99031
k=172,shift(k)= 19.75232966213650,m(k)=10,delta(k)=3.08e-02, ratio(k)= 0.99030
k=173,shift(k)= 19.75091632457466,m(k)=10,delta(k)=3.05e-02, ratio(k)= 0.99029
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k=174,shift(k)= 19.74952204314978,m(k)=10,delta(k)=3.02e-02, ratio(k)= 0.99028
k=175,shift(k)= 19.74814696725082,m(k)=10,delta(k)=2.99e-02, ratio(k)= 0.99027
k=176,shift(k)= 19.74679121854614,m(k)=10,delta(k)=2.96e-02, ratio(k)= 0.99027
k=177,shift(k)= 19.74545489258715,m(k)=10,delta(k)=2.93e-02, ratio(k)= 0.99026
k=178,shift(k)= 19.74413806034203,m(k)=10,delta(k)=2.90e-02, ratio(k)= 0.99025
k=179,shift(k)= 19.74284076965363,m(k)=10,delta(k)=2.88e-02, ratio(k)= 0.99024
k=180,shift(k)= 19.74156304663308,m(k)=10,delta(k)=2.85e-02, ratio(k)= 0.99023
k=181,shift(k)= 19.74030489698395,m(k)=10,delta(k)=2.82e-02, ratio(k)= 0.99022
k=182,shift(k)= 19.73906630726874,m(k)=10,delta(k)=2.79e-02, ratio(k)= 0.99022
k=183,shift(k)= 19.73784724611095,m(k)=10,delta(k)=2.77e-02, ratio(k)= 0.99021
k=184,shift(k)= 19.73664766533979,m(k)=10,delta(k)=2.74e-02, ratio(k)= 0.99020
k=185,shift(k)= 19.73546750108471,m(k)=10,delta(k)=2.71e-02, ratio(k)= 0.99019
k=186,shift(k)= 19.73430667480948,m(k)=10,delta(k)=2.68e-02, ratio(k)= 0.99019
k=187,shift(k)= 19.73316509430570,m(k)=10,delta(k)=2.66e-02, ratio(k)= 0.99018
k=188,shift(k)= 19.73204265462975,m(k)=10,delta(k)=2.63e-02, ratio(k)= 0.99017
k=189,shift(k)= 19.73093923899518,m(k)=10,delta(k)=2.61e-02, ratio(k)= 0.99017
k=190,shift(k)= 19.72985471962499,m(k)=10,delta(k)=2.58e-02, ratio(k)= 0.99016
k=191,shift(k)= 19.72878895855807,m(k)=10,delta(k)=2.56e-02, ratio(k)= 0.99015
k=192,shift(k)= 19.72774180841559,m(k)=10,delta(k)=2.53e-02, ratio(k)= 0.99015
k=193,shift(k)= 19.72671311313087,m(k)=10,delta(k)=2.51e-02, ratio(k)= 0.99014
k=194,shift(k)= 19.72570270863882,m(k)=10,delta(k)=2.48e-02, ratio(k)= 0.99013
k=195,shift(k)= 19.72471042353366,m(k)=10,delta(k)=2.46e-02, ratio(k)= 0.99013
k=196,shift(k)= 19.72373607969137,m(k)=10,delta(k)=2.43e-02, ratio(k)= 0.99012
k=197,shift(k)= 19.72277949285930,m(k)=10,delta(k)=2.41e-02, ratio(k)= 0.99012
k=198,shift(k)= 19.72184047321442,m(k)=10,delta(k)=2.38e-02, ratio(k)= 0.99011
k=199,shift(k)= 19.72091882589495,m(k)=10,delta(k)=2.36e-02, ratio(k)= 0.99010
k=200,shift(k)= 19.72001435150124,m(k)=10,delta(k)=2.34e-02, ratio(k)= 0.99010
k=201,shift(k)= 19.71912684657135,m(k)=10,delta(k)=2.31e-02, ratio(k)= 0.99009
k=202,shift(k)= 19.71825610402945,m(k)=10,delta(k)=2.29e-02, ratio(k)= 0.99009
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k=730,shift(k)= 19.67885405288434,m(k)=10,delta(k)=1.04e-04, ratio(k)= 0.98981
k=731,shift(k)= 19.67885405088992,m(k)=10,delta(k)=1.03e-04, ratio(k)= 0.98981
k=732,shift(k)= 19.67885404894519,m(k)=10,delta(k)=1.02e-04, ratio(k)= 0.98981
k=733,shift(k)= 19.67885404704887,m(k)=10,delta(k)=1.01e-04, ratio(k)= 0.98981
k=734,shift(k)= 19.67885404519999,m(k)=10,delta(k)=1.00e-04, ratio(k)= 0.98981
k=735,shift(k)= 19.67885404339704,m(k)=10,delta(k)=9.90e-05, ratio(k)= 0.98981
k=736,shift(k)= 19.67885404163864,m(k)=10,delta(k)=9.80e-05, ratio(k)= 0.98981
k=737,shift(k)= 19.67885403992407,m(k)=10,delta(k)=9.70e-05, ratio(k)= 0.98981
k=738,shift(k)= 19.67885403825258,m(k)=10,delta(k)=9.60e-05, ratio(k)= 0.98981
k=739,shift(k)= 19.67885403662256,m(k)=10,delta(k)=9.50e-05, ratio(k)= 0.98981
k=740,shift(k)= 19.67885403503334,m(k)=10,delta(k)=9.40e-05, ratio(k)= 0.98981
k=741,shift(k)= 19.67885403348343,m(k)=10,delta(k)=9.31e-05, ratio(k)= 0.98981
k=742,shift(k)= 19.67885403197212,m(k)=10,delta(k)=9.21e-05, ratio(k)= 0.98981
k=743,shift(k)= 19.67885403049906,m(k)=10,delta(k)=9.12e-05, ratio(k)= 0.98981
k=744,shift(k)= 19.67885402906213,m(k)=10,delta(k)=9.03e-05, ratio(k)= 0.98981
k=745,shift(k)= 19.67885402766057,m(k)=10,delta(k)=8.93e-05, ratio(k)= 0.98981
k=746,shift(k)= 19.67885402629394,m(k)=10,delta(k)=8.84e-05, ratio(k)= 0.98981
k=747,shift(k)= 19.67885402496178,m(k)=10,delta(k)=8.75e-05, ratio(k)= 0.98981
k=748,shift(k)= 19.67885402366290,m(k)=10,delta(k)=8.66e-05, ratio(k)= 0.98981
k=749,shift(k)= 19.67885402239613,m(k)=10,delta(k)=8.57e-05, ratio(k)= 0.98981
k=750,shift(k)= 19.67885402116092,m(k)=10,delta(k)=8.49e-05, ratio(k)= 0.98981
Eigenvalue found, lambda= 3.93185165207897
k=751,shift(k)= 11.74201846579245,m(k)=9,delta(k)=8.34e-05, ratio(k)= 0.98288
Eigenvalue found, lambda= 3.73205080806804
```

```
k=752,shift(k)= 8.24264068711937,m(k)=8,delta(k)=8.14e-05,ratio(k)= 0.97556
Eigenvalue found, lambda= 3.41421356237301
k=753,shift(k)= 6.21939655491338,m(k)=7,delta(k)=7.87e-05,ratio(k)= 0.96752
Eigenvalue found, lambda= 2.999999999999993
k=754,shift(k)= 4.86370330515670,m(k)=6,delta(k)=7.55e-05,ratio(k)= 0.95834
Eigenvalue found, lambda= 2.51763809020501
k=755,shift(k)= 3.86370330515726,m(k)=5,delta(k)=7.15e-05,ratio(k)= 0.94736
Eigenvalue found, lambda= 2.000000000000002
k=756,shift(k)= 1.65335987410644,m(k)=4,delta(k)=6.25e-05,ratio(k)= 0.87396
Eigenvalue found, lambda= 1.48236190979511
k=757,shift(k)= 1.84303888382545,m(k)=3,delta(k)=5.54e-05,ratio(k)= 0.88743
Eigenvalue found, lambda= 0.58578643762593
k=758,shift(k)= 1.34108141904978,m(k)=2,delta(k)=4.67e-05,ratio(k)= 0.84304
k=759,shift(k)= 1.34108140700144,m(k)=2,delta(k)=3.94e-05,ratio(k)= 0.84304
k=760,shift(k)= 1.34108139843852,m(k)=2,delta(k)=3.32e-05,ratio(k)= 0.84304
k=761,shift(k)= 1.34108139235272,m(k)=2,delta(k)=2.80e-05,ratio(k)= 0.84304
k=762,shift(k)= 1.34108138802745,m(k)=2,delta(k)=2.36e-05,ratio(k)= 0.84304
k=763,shift(k)= 1.34108138495342,m(k)=2,delta(k)=1.99e-05,ratio(k)= 0.84304
k=764,shift(k)= 1.34108138276866,m(k)=2,delta(k)=1.68e-05,ratio(k)= 0.84304
k=765,shift(k)= 1.34108138121592,m(k)=2,delta(k)=1.41e-05,ratio(k)= 0.84304
k=766,shift(k)= 1.34108138011236,m(k)=2,delta(k)=1.19e-05,ratio(k)= 0.84304
k=767,shift(k)= 1.34108137932805,m(k)=2,delta(k)=1.01e-05,ratio(k)= 0.84304
k=768,shift(k)= 1.34108137877063,m(k)=2,delta(k)=8.48e-06,ratio(k)= 0.84304
Eigenvalue found, lambda= 0.26794919207258
converged
Sorted Eigenvalues are:
    0.0681
    0.2679
    0.5858
    1.0000
    1.4824
    2.0000
    2.5176
    3.0000
    3.4142
    3.7321
    3.9319

maxErr = 4.99e-10
>>
```



```
k=752,shift(k)= 8.24264068711937,m(k)=8,delta(k)=8.14e-05,ratio(k)= 0.97556
Eigenvalue found, lambda= 3.41421356237301
k=753,shift(k)= 6.21939655491338,m(k)=7,delta(k)=7.87e-05,ratio(k)= 0.96752
Eigenvalue found, lambda= 2.999999999999993
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Eigenvalue found, lambda= 2.51763809020501
k=755,shift(k)= 3.86370330515726,m(k)=5,delta(k)=7.15e-05,ratio(k)= 0.94736
Eigenvalue found, lambda= 2.000000000000002
k=756,shift(k)= 1.65335987410644,m(k)=4,delta(k)=6.25e-05,ratio(k)= 0.87396
Eigenvalue found, lambda= 1.48236190979511
k=757,shift(k)= 1.84303888382545,m(k)=3,delta(k)=5.54e-05,ratio(k)= 0.88743
Eigenvalue found, lambda= 0.58578643762593
k=758,shift(k)= 1.34108141904978,m(k)=2,delta(k)=4.67e-05,ratio(k)= 0.84304
k=759,shift(k)= 1.34108140700144,m(k)=2,delta(k)=3.94e-05,ratio(k)= 0.84304
k=760,shift(k)= 1.34108139843852,m(k)=2,delta(k)=3.32e-05,ratio(k)= 0.84304
k=761,shift(k)= 1.34108139235272,m(k)=2,delta(k)=2.80e-05,ratio(k)= 0.84304
k=762,shift(k)= 1.34108138802745,m(k)=2,delta(k)=2.36e-05,ratio(k)= 0.84304
k=763,shift(k)= 1.34108138495342,m(k)=2,delta(k)=1.99e-05,ratio(k)= 0.84304
k=764,shift(k)= 1.34108138276866,m(k)=2,delta(k)=1.68e-05,ratio(k)= 0.84304
k=765,shift(k)= 1.34108138121592,m(k)=2,delta(k)=1.41e-05,ratio(k)= 0.84304
k=766,shift(k)= 1.34108138011236,m(k)=2,delta(k)=1.19e-05,ratio(k)= 0.84304
k=767,shift(k)= 1.34108137932805,m(k)=2,delta(k)=1.01e-05,ratio(k)= 0.84304
k=768,shift(k)= 1.34108137877063,m(k)=2,delta(k)=8.48e-06,ratio(k)= 0.84304
Eigenvalue found, lambda= 0.26794919207258
converged
Sorted Eigenvalues are:
    0.0681
    0.2679
    0.5858
    1.0000
    1.4824
    2.0000
    2.5176
    3.0000
    3.4142
    3.7321
    3.9319

maxErr = 4.99e-10
>>
```