

UTRECHT UNIVERSITY

DOCTORAL THESIS

**Temporal Segmentation using Support
Vector Machines in the context of
Human Activity Recognition**

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*A thesis submitted in fulfilment of the requirements
for the degree of Master of Science*

in the

Research Group Name

Department or School Name

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Declaration of Authorship

I, R.Q. VLASVELD, declare that this thesis titled, 'Temporal Segmentation using Support Vector Machines in the context of Human Activity Recognition' and the work presented in it are my own. I confirm that:

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- Where I have consulted the published work of others, this is always clearly attributed.
- Where I have quoted from the work of others, the source is always given. With the exception of such quotations, this thesis is entirely my own work.
- I have acknowledged all main sources of help.
- Where the thesis is based on work done by myself jointly with others, I have made clear exactly what was done by others and what I have contributed myself.

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Date:

“Thanks to my solid academic training, today I can write hundreds of words on virtually any topic without possessing a shred of information, which is how I got a good job in journalism.”

Dave Barry

***** TODO: Find nice quote *****

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Abstract

Faculty Name

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Master of Science

**Temporal Segmentation using Support Vector Machines in the context of
Human Activity Recognition**

by R.Q. VLASVELD

The Thesis Abstract is written here (and usually kept to just this page). The page is kept centered vertically so can expand into the blank space above the title too...

***** *TODO: Write abstract* *****

Acknowledgements

The acknowledgements and the people to thank go here, don't forget to include your project advisor...

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Acronyms

AIC Akaike Information Criterion. [13](#), [82](#)

AR Autoregressive. [40](#), [44](#), [48](#), [49](#)

BIC Bayesian Information Criterion. [13](#), [82](#)

changeFinder is a unifying framework proposed by Takeuchi and Yamanishi [70] which combines outlier detection and change detection. [22](#)

CUSUM Cumulative Sum. [9–12](#), [14–17](#), [44–46](#), [77](#), [82](#)

DR Dimensionality Reduction. [8](#)

FAR False Alarm Rate. [50](#)

GMM Gaussian Mixture Model. [25](#)

HAR Human Activity Recognition. [2–4](#), [6](#), [11](#), [18](#), [19](#), [21](#), [38](#)

HMM Hidden Markov Model. [13](#), [90](#)

ICSS Iterated Cumulative Sums of Squares. [x](#), [14](#), [15](#), [17](#), [76](#)

i.i.d. independently and identically distributed. [22](#), [92](#)

I-SVDD Incremental Support Vector Data Description. [41–44](#), [64](#)

KKT Karush-Kuhn-Tucker. [42](#)

KL Kullback-Leibler. [19](#), [22](#), [24](#)

KLIEP Kullback-Leibler Importance Estimation Procedure. [12](#), [17](#), [18](#), [77](#), [82](#)

MLE Maximum Likelihood Estimates. [15](#)

- MOSUM** Moving Sum. [11](#), [14](#), [16](#)
- OCC** One-Class Classification. [ix](#), [2](#), [3](#), [8](#), [16](#), [21](#), [23–27](#), [43](#), [63](#), [82](#)
- OC-SVM** One-Class Support Vector Machine. [3–6](#), [8](#), [19](#), [20](#), [24](#), [27](#), [32](#), [41–43](#), [48](#), [64](#), [66](#), [82](#), [84](#)
- PCA** Principal Component Analysis. [12](#), [13](#), [26](#)
- PDF** Probability Density Function. [9](#), [24](#)
- PLR** Piecewise Linear Representation. [11](#)
- QP** Quadratic Programming. [29](#), [33](#)
- RBФ** Radial Base Function. [31](#), [34–37](#), [43](#), [51](#), [52](#), [95](#)
- RKHS** Reproducing Kernel Hilbert Space. [31](#)
- ROC** Receiver-Operating Characteristic. [81](#)
- RT** Ratio-Thresholding. [48](#), [51](#)
- SV** Support Vector. [34](#), [35](#)
- SVC** Support Vector Regression. [15](#), [30](#), [91](#)
- SVCPD** Support Vector based Change Point Detection. [x](#), [6](#), [19](#), [22](#), [41](#), [64](#)
- SVDD** Support Vector Data Description. [vi](#), [ix](#), [2](#), [3](#), [5](#), [19](#), [21](#), [22](#), [26](#), [27](#), [32](#), [34](#), [36–38](#), [40–43](#), [63](#), [64](#), [81](#), [82](#), [91](#), [96](#)
- SVM** Support Vector Machine. [ix](#), [2](#), [3](#), [6](#), [8](#), [9](#), [11](#), [18](#), [19](#), [21](#), [24](#), [26–34](#), [36](#), [42](#), [81](#), [84](#), [95](#), [96](#)
- ν -SVM** ν -Support Vector Machine. [vi](#), [ix](#), [15](#), [18](#), [19](#), [21](#), [26](#), [27](#), [32–34](#), [36](#)
- SWAB** Sliding Window And Bottom-up. [10–12](#)
- UCI HAR** Human Activity Recognition Using Smartphones Data Set. [4](#), [54](#)
- WISDM** Wireless Sensor Data Mining. [4](#), [54](#)

Symbols

a distance m
 P power W (Js^{-1})

ω angular frequency rads^{-1}

For/Dedicated to/To my...

– Overall todo's –

- *** *TODO: The term emperical data/distribution is nowhere used in the thesis. or: Empirical cumulative distribution. Especially Chapter 2.* ***
- *** *TODO: Check for “tang-constructions”: saying to much in a single sentence.* ***
- *** *TODO: Overall: meer focus op de waarom vraag/antwoord bij keuzes. Bouwt aan motivatie en context van het geheel.* ***

Chapter 1

Introduction

With the wide availability of smartphones and built-in inertial sensors, more and more applications of Human Activity Recognition (HAR) are introduced [7, 23, 30]. Many approaches to recognize the performed activity rely on classification of recorded data [6, 8, 13, 24, 36, 80, 84], which can be done online or in batches after the performance [25]. Often a time-windowed based approach is used, which feeds short consecutive segments of data through a model construction and recognition phase. The constructed model is used to determine which (earlier learned) activity is performed. Besides the explicit classification of the data, an implicit obtained result is a segmentation of performed activities over time.

In this thesis the goal is to find the temporal segmentation of time series data explicitly, prior to the classification of the activities. This is done under the assumption that it could be beneficial for classification methods to possess this explicit segmentation, since the model construction phase can use more data than the time-windowed approach would allow. To find a temporal segmentation, we rely on change detection in time series data. In the context of this research, this time series data consists of recordings from inertial sensors found in smartphones, such as the accelerometer signal, during the performance of human activities. We are interested in both in- and outdoor activities in an uncontrolled environment and in a continuous manner, which can be regarded as real-world data. Although the number of performed activities will be limited, we assume the temporal segmentation must be more robust than in the case of data from a controlled environment.

For the change detection algorithm we have used a special form of Support Vector Machine (SVM), the One-Class Classification (OCC) based Support Vector Data Description (SVDD) as introduced by Tax [72]. This method models the data under consideration in the shape of a high-dimensional hypersphere. From this hypersphere the

radius is extracted, which can be used as an indication of change and be processed by one-dimensional change detection algorithms. Since a change in data characteristics, resulting from a change in performed activity, alters the data distribution, the model and thus the radius should reflect this change as well.

1.1 Scope

The scope of this thesis is to find a temporal segmentation of time series data from inertial sensors embedded in smartphones, obtained during the performance of human activities. As mentioned above, the segmentation is often obtained as a by-product from direct windowed classification. Other approaches have a very rigid form of segmentation, e.g. by limiting the number of possible segment types [17, 38], or have applied it to different type of time series data [27, 31, 49]. Others have extracted features from windows of data which are used for the segmentation [32]. These activities include sitting, standing, walking, running, and ascending and descending staircases. The problem of finding a temporal segmentation can be seen as a sub-problem to the problem of Activity Classification. This relation is illustrated in Figure 1.1. The figure shows that we can apply classification over windows of the time series data. In many approaches this is constructed with a (partially overlapping) sliding window. In the context of HAR, the window length commonly consists of around 2 seconds of data points. In our setup, we create a temporal segmentation instead of a fixed window length. Each segment should consist of homogeneous data, in the sense that the underlying data generating activity should not change within a segment. Likewise, the previous and next segments (if present) should be generated by a different performed activity.

To find these segments of homogeneous data, we employ a model construction phase. The One-Class Support Vector Machine (OC-SVM) model transforms the data points to a high-dimensional hyperspherical shape from which we extract the radius as characterizing metric. In this phase the data is processed by a fixed window length and a change in data characteristics should reflect in a (significant) change of the hyper-sphere's radius. Such a sudden change in the radius thus indicates a change in the time series data and indicates the end of the current and beginning of a new segment. In Section 2.5 a more detailed overview of temporal segmentation methods is discussed. The information about segments can be used in the classification phase of HAR, which applies classification to windows (or in this case: segments) of data. The final result, which is outside the scope of this thesis, will be a full classification of activities over the time series data.

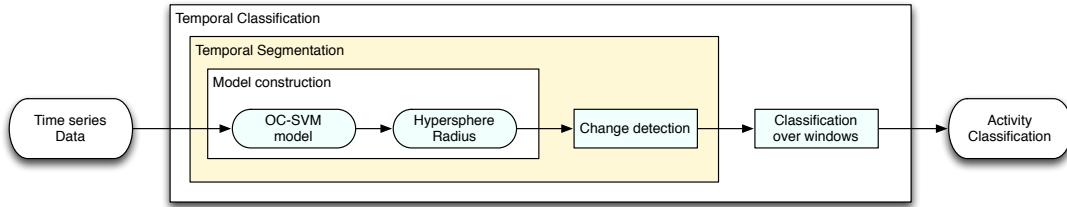


FIGURE 1.1: The goal of this thesis. The scope of this thesis is Temporal Segmentation, which can be useful in the context of Temporal Classification. Given a data set, we construct a OC-SVM high-dimensional spherical model, from which we extract the radius. This metric is then applied to direct change detection algorithms. The detected change points can support the classification of homogeneous segments of data.

1.2 One-Class Support Vector Machines

In the setup, as described in the previous section, we employ a model construction phase. For this model we will use an One-Class Support Vector Machine implementation: the Support Vector Data Description algorithm by Tax [72]. In earlier research multi-class SVMs are used for direct classification of inertial sensor data [6, 36, 58]. Others have used OC-SVM classifiers for novelty, or outlier, detection [15, 50, 54, 66, 73]. However, to our knowledge, OC-SVM methods have not yet been applied to inertial sensor time series data directly. This algorithm transforms the time series data, which can be of any high dimension, to an higher dimensional feature space. When the data is assumed to be of the same class, it can be characterized by an enclosing boundary, in the shape of a hypersphere. Using this OCC method, we are able to test new data points of being a member of this class. When a new data point, after transformation to the feature space, lies within the boundary, it is a member of the class, and otherwise it is regarded as an outlier.

In case the data distribution changes, the data points will have a larger variance which results in a larger hypersphere in the feature space. This means that with continuous model updating, a change in the underlying process of a time series data means the hypersphere will have a larger radius. Thus the OC-SVM method allows us to generate a one-dimensional time series data, reduced from a complex high-dimensional original signal. The final radius time series data can be inspected by simpler change detection methods, in a number of ways. Chapter 3 will discuss the OC-SVM methods in detail and Chapter 4 elaborates on the overall change detection method.

1.3 Data sets

In recent previous research two data sets for the context of HAR have been made public. In order to benchmark our proposed method we tried to employ it to these data sets. However, it turned out the data sets were not appropriate for continuous temporal segmentation. The first set, the Wireless Sensor Data Mining (WISDM) from [47], consists of non-continuous recordings of activities. Obviously, this voids the usefulness of the data set of our research. The second set, the Human Activity Recognition Using Smartphones Data Set (UCI HAR) from [6], also lacks continuous recordings and furthermore exhibits patterns and labeling which seems to be incorrect. Besides these problems, since there are no visual images of the performed activities, there is no ground truth which can be consulted in case of ambiguity. To overcome these problems, we have created our own real-world data sets.

Our own data sets are recorded by placing a smartphone with inertial sensors in the front right pants pocket of a subject. The subject was asked to perform common and simple activities in an uncontrolled environment, both in- and outdoor situated. During the performance the subjects were also recorded with a video camera from the third-person point of view. This allows us to create a ground truth for the temporal segmentation of performed activities.

Besides the recorded data sets we have used artificial data sets to obtain an objective performance measure of the method. These artificial data sets are modeled to the sets used in [15, 70]. In Chapter 5 we discuss the artificial data sets and results in detail. The real-world recordings and results are discussed in Chapter 6.

1.4 Contributions

As a result from our proposed method and application to recorded real-world data sets, this thesis will provide the following contributions:

1. **Continuous recorded human activity data:** the proposed method is applied to our own recorded human activity data. This data set can be grounded by using the video recordings of the subject while performing the activities. The data set, consisting of raw inertial sensor recordings, manual change point and activity labeling, and video recordings, are used for testing the method and are made publicly available [79].
2. **Application of OC-SVM methods to inertial sensor data:** up to our knowledge, this thesis is the first application of OC-SVM methods, especially the SVDD

method, to inertial sensor signals, such as accelerometer time series data. Furthermore, this thesis contributes to the small amount of research that has a temporal segmentation of inertial sensor data as its primary objective.

3. **Adaptation of SVCPD:** we have adopted and slightly adapted the SVCPD method by Camci [15] in order to find change points in time series data. In our simplification we have not encountered noticeably decrease in performance.

1.5 Thesis structure

The structure of this thesis is as follows. In Chapter 2 a literature review is provided. We will look at the different interpretations and implementations for change, novelty, and outlier detection. Previous work in the field of HAR is discussed and we end with existing applications of SVMs to change detection. The next chapter further analyses SVMs and two implementations of OC-SVMs. It relates the properties of the constructed OC-SVM models to change detection in time series data. That relation is applied to our problem formulation in Chapter 4, where we construct our change detection method *******
TODO: add name ***, based on the work of Camci [15]. The two following chapters apply the method to both artificial and real-world data. Chapter 5 show the objective performance of the method to artificial constructed data. In Chapter 6 we apply the method to our self-recorded real-world data. In that chapter we show the ability of detecting change in HAR data, recorded by inertial sensors. This thesis is concluded in Chapter 7, in which we reflect on the performed research and state possibilities for feature research.

Chapter 2

Literature review

2.1 Outline

Not intented for the reader.

- Literature review about Temporal Segmentation (previous draft was more about classification)
- Consider methods for the context of filter-methods for classification
- Take a loot at 3-4 different kind of methods for change detection:
 - Introduction with a lot of techniques
 - Explain why look at a few
 - CUSUM - or other more traditional methods
 - Density-ratio estimation
 - Support Vector Machines (?) - if there are more sources about this
 - (Dimensionality reduction) –*i* probably not
 - *Not to much attention to all techniques, focus is on SVM*
- With each method, shortly look at characteristics, strengths and weaknesses and consider applicability to accelerometer sensor data

2.2 Statistical framework

- Nieuwe indeling Chapter 2 –

Intro/outline Introduction and overview of this chapter. Put in the context of temporal classification.

Temporal segmentation Give overview of used temporal segmentation methods, move towards a split in model building/dimensionality reduction and change detection methods

Dimensionality reduction Explain that Dimensionality Reduction (DR) can be useful in data processing. Name a few techniques, make bridge to OC-SVM.

Change detection Describe methods for *direct* change detection. End with notion

Model fitting

Cusum

Density ratio

2.3 Overview

As described in Chapter 1, the focus of this research is the application of temporal segmentation to accelerometer data. This is with the assumption that explicit temporal segmentation can aid the process of temporal classification.

***** TODO: Give examples of temporal classification techniques *****

In recent years a lot of research is performed in the classification of human activities, recorded by on-body sensors. Especially since smartphones with accelerometer sensors became more available, research has focused on recordings from these devices.

***** TODO: Include highlights from old-classification text *****

In the following of this chapter we will start with an overview of statistical models used in this field of study. That section will act as a starting point to look at the different types, applications and methods of temporal segmentation. The following section, Section 2.5 follows the distinction made and looks at a collection of temporal segmentation and change detection methods. It will also relate the concept of OCC to temporal segmentation and change detection. The final section of this chapter, Section 2.9, will discuss a specific class of algorithms for OCC, namely the methods that use SVMs for the classification task.

2.4 Statistical models

***** TODO: Introduce the different models and thus different approaches *****

Many applications require the detection of time points at which the underlying properties of a system change. This problem has received a lot of attention in the fields of data mining, etc... ***** TODO: list and refs *****. Often this problem is formulated in a statistical framework, by inspecting the underlying data generating Probability Density Function (PDF) of the time series data. A change point is then defined as a significant change in the properties of the PDF, such as the mean and variance.

The widely used Cumulative Sum (CUSUM) method by Basseville *et al.* [11] follows this approach. It originates from control methods for detection from benchmarks. This method and some derivatiges are discussed and analyzed in Section 2.7.

Many methods rely on pre-specified parametric model assumptions and considers the data be independent over time, which makes it less flexible to real-world applications. The methods proposed by Kawahara *et al.* [43] and Lui *et al.* [51] try to overcome these problems by estimating the *ratio* between the PDFs, instead of estimating each PDF. This approach is discussed and analyzed in Section 2.8.

The density-estimation methods rely on the log-likelihood ratio between PDFs. The method of Camci [15] follows an other approach within the statistical framework, by using a SVM. One problem it tries to overcome is the (claimed) weakness of many methods to detect a decrease in variance. The method represents the distribution over the data points as a hyper-sphere in a higher dimension using the kernel trick. A change in the PDF is represented by a change in the radius of this sphere. Section 2.9 discusses the SVM-methods. ***** TODO: Put emphasis that this is the source of inspiration for the chosen method? *****

– NEW –

In the field of temporal segmentation of time series data we can distinguish different approaches and common frameworks in which they perform. The problem is commonly formulated in the statistical framework and regarding the properties of the underlying data generating PDF fo the time series data. In that sense, a change point is then defined as a significant change in the properties of the PDF, such as the mean or variance.

In the search for the change in properties, temporal segmentation and change point detection methods can roughly be categorized in three methods in the way the data is processed, as discussed by Avci *et al.* [7]:

Support Vector Machine based methods **Top-Down** methods iteratively divide the signal in segments by splitting at the best location. The algorithm starts with two segments and completes when a certain condition is met, such as when an error value or number of segments k is reached.

- **Bottom-Up** methods are the natural complement to top-down methods. They start with creating $n/2$ segments and iteratively join adjacent segments while the value of a cost function for that operation is below a certain value.
- **Sliding-window** methods are simple and intuitive for online segmenting purposes. It starts with a small initial subsequence of the time series. New data points are joined in the segment until the fit-error is above a threshold. Since the data is only processed very locally, these methods can yield in poor results [45].
- **Sliding Window And Bottom-up**, as introduced by Keogh *et al.* [45], combines the ability of the sliding window mechanism to process time series online and the bottom-up approach to create superior segments in terms of fit-error. The algorithm processes the data in two stages. The first stage is to join new data points in the current segment created by a sliding window. The second stage processes the data using Bottom-Up and return the first segment as the final result. Since this second stage retains some (semi-)global view of the data, the results are comparative with normal Bottom-Up.

It is clear that for the application of this research sliding-window and preferably Sliding Window And Bottom-up (SWAB)-based algorithms should be considered. In the following we will discuss classes of algorithms grouped by the type of decision function, assuming a SWAB-based data processing order.

A widely used class of methods is based on the CUSUM approach by Basseville *et al.* [11]. This approach originates from control methods for detection and faults and benchmarking. In Section 2.5.2 a further overview of this class of methods is discussed.

- Density
- Outlier based

2.5 Temporal Segmentation

**** TODO: Is there any research of temporal segmentation on accelerometer/inertia signals? Note if there is/isn't ****

Give overview of used temporal segmentation methods. Problem is that it is not really well-defined.

- Given overview of segmentation techniques, for times series data
- Use different “point-of-views”, or terms
- “Segmentation”
- “Change detection”
- “Novelty detection”
- Specific view on SVMs

This section gives an overview of the literature on temporal segmentation in the context of HAR. It takes a look on different implementations and methodologies. A wide range of terms and subtle differences are used in the field, such as ‘segmentation’, ‘change detection’, ‘novelty detection’ and ‘outlier detection’. These will be the categorical terms for which we discuss the literature.

Aspects we will consider when discussing the literature are applicability to HAR, parameter tuning and ... *** ***TODO: What more aspects?*** ***

2.5.1 Segmentation

Methods that apply temporal segmentation on time series data can be roughly categorized in three different methods, as discussed by Avci *et al.* [7]. In that survey the distinction between *Top-Down*, *Bottom-Up*, and *Sliding-Window* approaches is made, based on the way data is processed by the algorithm. Since we are interested in online change detection, the literature discussed in this section will mainly be forms of sliding-window algorithms.

In Keogh *et al.* [45] a comparison of the aforementioned approaches is made. The research also introduces the SWAB method, which combines the simple and intuitive approach of the sliding-window approach with the (semi-)global view over the data from the bottom-up method. This proposed method is dependent on user provided parameters, setting the maximum error when performing the algorithm. Each segment is approximated by using a Piecewise Linear Representation (PLR). The provided error threshold controls the granularity and number of segments.

Other methods have been proposed, such as an adaptive threshold based on the signal energy by Guenterberg *et al.* [31], the adaptive CUSUM-based test by Alippi *et al.* [4] and

the Moving Sum (MOSUM) by Hsu [40] in order to eliminate this user-dependency. The latter of these methods is able to process the accelerometer values directly, although better results are obtained when features of the signal are processed, as done in the former method. Here the signal energy, mean and standard deviation are used to segment activities and by adding all the axial time series together, the Signal-To-Noise ration is increased, resulting in a robuster method.

The method of Guenterberg *et al.* [31] extracts features from the raw sensor signal to base the segmentation on other properties than the pure values. The method of Bernecker *et al.* [13] uses other statistical properties, namely autocorrelation, to distinguish periodic from non-periodic segments. Using the SWAB method the self-similarity of a one-dimensional signal is obtained. The authors claim that only a slight modification is needed to perform the method on multi-dimensional data. After the segmentation phase, the method of Bernecker *et al.* extracts other statistical features which are used in the classification phase.

The proposal of Guo *et al.* [32] dynamically determines which features should be used for the segmentation and simultaneously determines the best model to fit the segment. For each of the three dimensions features such as the mean, variance, covariance, correlation, energy and entropy are calculated. By extending the SWAB method, for every frame a feature set is selected, using an enhanced version of Principal Component Analysis (PCA). The research also considered the (Stepwise) Feasable Space Window as introduced by [52], but since it results in a higher error rate than SWAB the latter was chosen to extend. Whereas the before mentioned algorithms use a linear representation, this methods considers linear, quadratic and cubical representations for each segment. This differs from other methods where the model is fixed for the whole time series, such as [27], which is stated to perform inferior on non-stationary time series such as daily life.

The time series data from a sensor can be considered as being drawn from a certain stochastic process. Probabilistic models can be constructed on that signal, yielding in probabilistic and Bayesian based segmentation methods. The CUSUM-methods follows a statistical approach and relies on the log-likelihood ratio [34] to measure the difference between two distributions. To calculate the ratio, the probability density functions need to be calculated. The method of Kawahara *et al.* [43] proposes to estimate the ratio of probability densities (known as the *importance*), based on the log likelihood of test samples, directly, without explicit estimation of the densities. The method by Liu *et al.* [51] uses a comparable dissimilarity measure using the Kullback-Leibler Importance Estimation Procedure (KLIEP) algorithm. They claim this results in a robuster approach for real-world scenarios. Although this is a model-based method, no strong assumptions (parameter settings) are made on the models.

The method of Adams and MacKay [1] builds a probabilistic model on the segment run length, given the observed data so far. Instead of modeling the values of the data points as a probabilistic distribution, the length of segments as a function of time is modeled by calculating the posterior probability. It uses a prior estimate for the run length and a predictive distribution for newly-observed data, given the data since the last change point. This method contrasts with the approach of Guralnik and Srivastava [33] in which change points are detected by a change in the (parameters of an) underlying, observed, model. For each new data point, the likelihoods of being a change point and part of the current segment are calculated, without a prior model (and thus is a non-Bayesian approach). It is observed that when no change point is detected for a long period of time, the computational complexity increases significantly.

Another application of PCA is to characterize the data by determining the dimensionality of a sequence of data points. The proposed method of Berbić *et al.* [9] determines the number of dimensions (features) needed to approximate a sequence within a specified error. With the observation that more dimensions are needed to keep the error below the threshold when transitions between actions occur, cut-points can be located and segments will be created. The superior extension of their approach uses a Probabilistic PCA algorithm to incorporate the dimensions outside the selected set as noise.

In the method by Himberg *et al.* [38] a cost function is defined over segments of data which is to be minimized. The cost functions thereby searches for internally homogeneous segments of data, reflecting states in which the devices and the user are. The cost function can be any arbitrary function and in the implementation the sum of variances over the segments is used. Both in a local and global iterative replacement procedure (as an alternative for the computationally hard dynamic programming algorithm) the best breakpoint locations c_i for a pre-defined number of segments $1 \leq i \leq k$ are optimized.

Many methods obtain an implicit segmentation as a result of classification over a sliding window *** ***TODO: add refs*** ***. The method of Yang *et al.* [83] explicitly performs segmentation and classification simultaneously. It argues that the classification of a pre-segmented test-sequences becomes straightforward with many classical algorithms to choose from. The algorithm matches test examples with the *sparsest* linear representation of mixture subspace models of training examples, searching over different temporal resolutions.

The method of Chamroukhi *et al.* [17] is based on a Hidden Markov Model (HMM) and logistic regression. It assumes a K -state hidden process with a (hidden) state sequence, each state providing the parameters (amongst which the order) for a polynomial. The order of the model segment is determined by model selecting, often using the Bayesian

Information Criterion (BIC) or the similar Akaike Information Criterion (AIC) [3], as in [36].

Field of computer vision: [87], [49].

“Segmentation and Recognition of Motion Streams by Similarity Search” [49]. 29, 2007

“Aligned Cluster Analysis for Temporal Segmentation of Human Motion” [87]. 63, 2008

2.5.2 CUSUM

***** TODO: Link this subsection with previous and next *****

Notes: Non-Bayesian change detection algorithm (i.e. no prior distribution believe available for the change time). The CUSUM method is developed by Page [62] for the application of statistical quality control (it is also known as a control chart). Primary for detection of mean shift. The MOSUM of squares test for monitoring variance changes [40]. Use of Cumulative Sums of Squares for Retrospective Detection of Changes of Variance [41]

An often used approach in the statistical framework of change detection is the CUSUM as introduced by Page [62]. Originally used for quality control in production environments, its main function is to detect change in the mean of measurements and has been applied to this problem [11]. It is a non-Bayesian method and thus makes no assumptions, in the form of prior belief distributions, for the change points. Many extensions to this method have been proposed. Some focus on the change in mean, such the method of Alippi and Roveri [4]. Others apply the method to problems in which the change of variance is under consideration. Among others are there the centered version of the cumulative sums, introduced by Brown, Durbin and Evans [14] and the MOSUM of squares by [40].

The method of Inclán and Tiao [41] builds on the centered version of CUSUM [14] to detect changes in variance. Using the batch Iterated Cumulative Sums of Squares (ICSS) algorithm they are able to find multiple change points, offline while post-processing the data. Let $C_k = \sum_{i=1}^k \alpha_t^2$ be the cumulative sum of squares for a series of uncorrelated random variables $\{\alpha_t\}$ of length T . The centered (and normalized) sum of squares is defined as

$$D_k = \frac{C_k}{C_T} - \frac{k}{T}, \quad k = 1, \dots, T, \quad \text{with } D_0 = D_T = 0. \quad (2.1)$$

For a series with homogeneous variance, the value of D_k will oscillate around 0. In case of a sudden change, the value will increase and exceed some predefined boundary with

high probability. By using an iterative algorithm, the method is able to minimize the masking effect of successive change points.

One of the motivations for the ICSS algorithm was the heavy computational burden involved with Bayesian methods, which need to calculate the posterior odds for the log-likelihood ratio testing. The ICSS algorithm avoids applying a function at all possible locations, due to the iterative search. The authors recommend the algorithm for analysis of long sequences.

2.5.3 Change detection

***** TODO: change order of this and temporal segmentation sections? So first change, then segmentation? *****

Whereas the above mentioned researches focus on *segmentation*, many have focused on *change detection*. Although these techniques are closely related, there is a subtle difference. In the case of *change detection* to goal is to find, possibly unrelated, sudden change points in a signal [70]. In contrast, the goal of *temporal segmentation* is to find homogeneous segments of data, which can be the result of multiple detected changes.

The ICSS by Inclán and Tiao [41] is a statistical method which obtains results (when applied to stock data) comparable to Maximum Likelihood Estimates (MLE) and Bayesian ***** TODO: Bayesian What? *****. Whereas CUSUM can be applied to search for a change in mean, the ICSS is adapted to find changes in variance. It obtains a *likelihood ratio* for testing the hypothesis of one change against no change in the variance. Using an iterative approach, all possible change points are considered. The proposal of [19] extends on the CUSUM-based methods to find change points in mean and variance, by creating a more efficient and accurate algorithm.

Section 3.2 discusses the problem of change detection in time series further, and gives a formal problem definition.

***** TODO: move CUSUM based techniques to this subsection *****

2.5.4 Novelty and Outlier detection

In the case of time series data, many approaches rely on the detection of outlier, or novel, data objects. An increase in outlier data objects indicates a higher probability of change, as discussed by Takeuchi and Yamanischi [70]. The concepts of novelty detection and outlier detection are closely related and often used interchangeable.

The algorithm by Ma and Perkins [55] uses Support Vector Regression (SVC) to model a series of past observations. Using the regression, a matching function $V(t_0)$ is constructed which uses the residual value of t_0 to create an outlier (out-of-class) confidence value. The method defines novel *events* as a series of observations for which the outlier confidence is high enough. In an alternative approach by the same authors [54] a classification method, in contrast with regression, is used to detect outlier observations. The latter approach uses the ν -Support Vector Machine (ν -SVM) algorithm by Schölkopf *et al.* [66], which is further discussed in Section 2.9

A extensive overview of novelty detection based on statistical models is given by Markou and Singh [55]. In the second part of their review [56], novelty detection by a variety of neural networks is discussed. The survey by Hodge and Austin [39] distinguishes between three types of outlier detection: 1) unsupervised, 2) supervised, and 3) semi-supervised learning. As we will see in Section 3.3, in this research we are interested in methods from Type 3, from which OCC is a member. More theoretical background and foundation on outliers in statistical data can be found in [10].

2.6 Change Detection methods

Describe methods for *direct* change detection. End with notion that all work on low/single dimensional time series data, so dimensionality reduction is needed.

2.6.1 CUSUM

2.6.2 Model fitting

2.6.3 Density-Ratio

– OLD –

2.7 CUSUM

Notes: Non-Bayesian change detection algorithm (i.e. no prior distribution believe available for the change time). The CUSUM method is developed by Page [62] for the application of statistical quality control (it is also known as a control chart). Primary for detection of mean shift. The MOSUM of squares test for monitoring variance changes

[40]. Use of Cumulative Sums of Squares for Retrospective Detection of Changes of Variance [41]

An often used approach in the statistical framework of change detection is the CUSUM as introduced by Page [62]. Originally used for quality control in production environments, its main function is to detect change in the mean of measurements and has been applied to this problem [11]. It is a non-Bayesian method and thus makes no assumptions, in the form of prior belief distributions, for the change points. Many extensions to this method have been proposed. Some focus on the change in mean, such the method of Alippi and Roveri [4]. Others apply the method to the problems in which the change of variance is under consideration. Among others are there the centered version of the cumulative sums, introduced by Brown, Durbin and Evans [14] and the MOSUM of squares by [40].

The method of Inclán and Tiao [41] builds on the centered version of CUSUM [14] to detect changes in variance. Using the batch ICSS algorithm they are able to find multiple change points, offline while post-processing the data. Let $C_k = \sum_{i=1}^k \alpha_t^2$ be the cumulative sum of squares for a series of uncorrelated random variables $\{\alpha_t\}$ of length T . The centered (and normalized) sum of squares is defined as

$$D_k = \frac{C_k}{C_T} - \frac{k}{T}, \quad k = 1, \dots, T, \quad \text{with } D_0 = D_T = 0. \quad (2.2)$$

For a series with homogeneous variance, the value of D_k will oscillate around 0. In case of a sudden change, the value will increase and exceed some predefined boundary with high probability. By using an iterative algorithm, the method is able to minimize the masking effect of successive change points.

One of the motivations for the ICSS algorithm was the heavy computational burden involved with Bayesian methods, which need to calculate the posterior odds for the log-likelihood ratio testing. The ICSS algorithm avoids applying a function at all possible locations, due to the iterative search. The authors recommend the algorithm for analysis of long sequences.

2.8 Change-detection by Density-Ratio Estimation

Many approaches to detect change points monitor the logarithm of the likelihood ratio between two consecutive intervals. A change point is regarded to be the moment in time when the underlying probabilistic generation function changes. Some methods which rely on this are novelty detection, maximum-likelihood estimation and online learning of autoregressive models [43]. A limitation of these methods is that they rely on pre-specified parametric models. Non-parametric models for density estimation have

been proposed, but it is said to be a hard problem [35, 69]. A solutions to this is to estimate the *ratio* of probabilities instead of the probabilities themselves. One of the recent methods to achieve this is the KLIEP by Sugiyama *et al.* [68].

The method proposed by Kawahara and Sugiyama [43] is composed of an online version of the KLIEP algorithm. The method also considers *sequences* of samples (rather than samples directly) because the time series samples are generally not independent over time. An advantage over other non-parametric approaches, such as sequential one-class support vector machines, is that the model has an natural cross-validation procedure. This makes that the value of tuning parameters, such as the kernel bandwidth, can be objectively obtained.

In their formulation change is detected by monitoring the logarithm of the likelihood ratio between the reference (past) and test (current) time intervals

$$S = \sum_{i=1}^{n_{\text{te}}} \ln \frac{p_{\text{te}}(\mathbf{Y}_{\text{te}}(i))}{p_{\text{rf}}(\mathbf{Y}_{\text{te}}(i))} \quad (2.3)$$

Where $\mathbf{Y}_{\text{te}}(i)$ is a sequence of samples from the test interval. A change is detected when $S > \mu$, for some predetermined threshold μ . The question is then how to calculate the density ratio

$$w(\mathbf{Y}) := \frac{p_{\text{te}}(\mathbf{Y})}{p_{\text{rf}}(\mathbf{Y})} \quad (2.4)$$

because this ratio is unknown and should be estimated. The naive approach is to estimate the ratio by taking the ratio of the estimated densities. Since this is known to be a hard problem and sensitive for errors, the solution would be to estimate the ratio directly.

The procedure of the method proposed by Kawahara and Sugiyama [43] is to first apply the batch KLIEP algorithm with model selection for initial parameter α and kernel width calculation. Then for every new sample the reference and test intervals are shifted and the calculated parameters α are updated. Finally the logarithm of the likelihood ratio is evaluated. If it is above the threshold μ the current time is reported as a change point.

Improvements in this line of research by Liu *et al.* [51] has led the application of improved density-ratio estimation methods to the problem of change detection. Such an improvement is the Unconstrained Least-Squares Importance Fitting (uLSIF) method [42] and an extension which possesses a superior non-parametric convergence property: Relative uLSIF (RuLSIF) [82].

2.9 Support Vector Machines in Change Detection

Many proposals in the field of remote sensing and HAR make use of SVMs as a (supervised) model learning method. An elaborate overview of applications is given in [58]. In this section we review methods of change detection based on the applications of SVMs as model construction method. A number of proposals have been made using this method. Schölkopf *et al.* [66] applies Vapnik's principle, to never solve a problem which is more general than the one that one is actually interested in, to novelty detection. In the case of novelty detection, they argue there is no need for density estimation of the distribution. Simple algorithms estimate the density by considering how many data points fall in a region of interest. The ν -SVM method instead starts with the number of data points that should be within the region and estimates a region with that desired property. It builds on the method of Vapnik and Vladimir [77], which characterizes a set of data by separating it from the origin. The ν -SVM method adds the kernel method, allowing non-linear decision functions, and incorporates 'softness' by the ν -parameter. Whereas the method in [77] focuses on two-class problems, the ν -SVM method introduces the method for one-class problems.

The method introduced by Ma and Perkins [54] creates a *projected phase* of a time series data, which is intuitively equal to applying a high-pass filter to the time series. The projected phase of the time series combines a history or data points to a vector, which are then classified by the ν -SVM method. The method is applied to a simple synthetic sinusoidal signal with small additional noise and a small segment with large additional noise. The algorithm is able to detect that segment, without false alarms.

The algorithms of SVMs has been applied to the problem of HAR, as by Anguita *et al.* [6]. In that research a multi-class classification problem is solved using SVMs and the One-Vs-All method. The method exploits fixed-point arithmetic to create a hardware-friendly algorithm, which can be executed on a smartphone.¹

With the same concepts as ν -SVM, the SVDD method by Tax and Duin [73, 75] uses a separating hypersphere (in contrast with a hyperplane) to characterize the data. The data points that lie outside of the created hypersphere are considered to be outliers, which number is a pre-determined fraction of the total number of data points.

The method by Yin and Yang [85] uses the SVDD method in the first phase of a two-phase algorithm to filter commonly available normal activities. The Support Vector based Change Point Detection (SVCPD) method of Camei [15] uses SVDD applies it to

¹Smartphones have limited resources and thus require energy-efficient algorithms. In [5] a Hardware-Friendly SVM is introduced. It uses less memory, processor time and power consumption, with a loss of precision.

time-series data. By using an OC-SVM the method is able to detect changes in mean variance. Especially the detection of variance *decrease* is an improvement over other methods that rely in the Kullback-Leibler (KL) divergence, since these are unable to detect decreases in variance [70]. This main research subject of this thesis is to apply the method of Camci [15] to sensor data (such as accelerometer time series) obtained by on-body smartphones.

The inner workings of OC-SVMs are discussed in detail in Section 3.4.

***** TODO: Add notion of ‘supervised’ vs ‘unsupervised’ learning. OC-SVM is unsupervised. *****

Chapter 3

Change detection by Support Vector Machines

3.1 Outline

Not intenedt for the reader.

- Content follows blogpost, but more formal
- Explain the connection between change detection and {outlier detection, density estimation, etc. }
- Explain change detection in relation with “M-Estimators”.
- Explain why and how SVM can be used for outlier detection, and thus for change detection in time series
- Explain options when using SVM, such as RBF kernel
- Relate characteristics of (accelerometer) data to the used (RBF?) kernel
- Define some quality metrics – this should be in a different chapter (About experiments)
- Note: try to avoid the perspective of *density estimation*. Instead: *data description* or *boundary description*.

This chapter discusses the concepts and algorithms that will be used as a basis for the proposed method, as discussed in Chapter 4. The first sections formulates the problem of change detection and relates it to outlier and novelty detection. It transforms the

traditional problem to change detection for times series data. In Section 3.3 the problem of One-Class Classification is discussed and shows a number of implementations. Two Support Vector Machine-based methods, ν -SVM and SVDD, are further discussed in Section 3.4. For the application to the problem of Human Activity Recognition, the characteristics of the collected sensor data is discussed in 3.5. Finally a theoretic set of quality metrics is discussed in Section 3.6.

***** TODO: Put somewhere difference and emphasis of online vs. offline/batch/post-processing *****

3.2 Change Detection in Time Series

***** TODO: Write section introduction *****

The section should relate the problem of outlier detection to change detection. It should transform the traditional problem formulation to that of time series data. Build to one-class classification, which can be used for outlier detection

3.2.1 Relation to outlier detection

The problems of outlier and novelty detection, segmentation, and change detection are closely related. The terminology depends on the field of application, but there are subtle differences. The problem of outlier detection is concerned with finding data objects in a data set which have small resemblance with the majority of the data objects. These objects can be regarded as erroneous measurements. In the case of novelty detection these objects are considered to be member of a new class of objects. The unifying framework of Takeuchi and Yamanishi [70], changeFinder, creates a two stage process expressing change detection in terms of outlier detection. The first stage determines the outliers in a time series by giving a score based on the deviation from a learned model, and thereby creates a new time series. The second stage runs on that new created time series and calculates a average over a window of the outlier scores. The problem of change detection is then reduced to outlier detection over that average-scored time series. The implementation by Camci [15], SVCPD, implements outlier detection with the SVDD algorithm to detect changes in mean and variance.

3.2.2 Problem formulation

The problem of change point detection can be formulated using different type of models, as discussed in 2.5.1. The methods by Takeuchi and Yamanishi [70] and Camci [15] use

the following formulation for change detection, which we will also use for our problem formulation. The algorithm searches for sudden changes in the time series data. In other words, slowly changing properties in the data are not considered to be changes. Considered a time series $x_1x_2\dots$, which is drawn from a stochastic process p . Each x_t ($t = 1, 2, \dots$) is a d -dimensional real valued vector and p a probability density function of the sequence $x_1x_2\dots$. Assume p can be decomposed in two different independently and identically distributed (i.i.d.) stationary stochastic processes p^1 and p^2 and are one-dimensional Gaussian density functions. For a time point a data points for which $t < a$ are drawn from $p^1 = N(\mu_1, \sigma_1^2)$ and for $t \geq a$ from $p^2 = N(\mu_2, \sigma_a^2)$. If p^1 and p^2 are different, then the time point $t = a$ is a *change point*. In [70] the similarity between the stochastic processes are expressed by the KL divergence $D(p^2||p^1)$. It is observed that this measure is not able to detect a change by decrease in variance [15, 70]. This problem is the motivation for Camci [15] to create the SVCPD algorithm.

The definition of change point being sudden changes in the time series data is in line with the search of changes in activities. Since we are only interested in different activities (which are represented by sudden changes), slight changes within an activity are not of interest. Section 3.5 discusses the representation of activities and changes between them in the data in more detail.

***** TODO: add more formal definition or analysis of change detection *****

– Literature –

“Online segmentation of time series based on polynomial least-squares approximations”, [27]. 25, 2010

3.3 One-Class Classification

***** TODO: Add ref to [39], which states 3 types of outlier detection. It puts OCC as of Type 3: semi-supervised recognition or detection *****

As discussed in the previous section, change detection in time series can be implemented using outlier, or novelty, detection. To regard a data point as an outlier, there must be a model of the normal time series data and a (dis)similarity measure defined over the model and data objects. When a data point differs enough from the created model, it can be labeled as an outlier. The class of OCC algorithms is especially designed for that purpose. The algorithms build up a model of the data, assuming only normal data objects are available (or a very limited amount of example outlier data objects). This

differs from classical classification algorithms, which commonly rely of both positive and negative examples.

In Section 3.3.1 the problem formulation of OCC methods is explained. In section 3.3.2 an overview of OCC methods is given. The following section will discuss one specific set of methods, the OC-SVM which use SVMs to model the normal training data.

3.3.1 Problem formulation

The problem of OCC is closely related to the (traditional) two-class classification situation¹. In the case of traditional classification algorithms, the problem is to classify an unknown object to one of the pre-defined categories. Every object i is represented as a vector $\mathbf{x}_i = (x_{i,1}, \dots, x_{i,d})$, $x_{i,j} \in \mathbb{R}$ with d real-valued measurements. Using this notation, an object \mathbf{x}_i thus represents one point in a feature space: $\mathbf{x}_i \in \mathcal{X} = \mathbb{R}^d$. The two classes of objects, ω_1 and ω_2 , are labeled -1 and $+1$ respectively. The objects with a label $y_i \in \{-1, +1\}$ attached are in the training set \mathcal{X}^{tr} (note that it can be both positive and negative example objects). This problem is solved by determining a decision boundary in the feature space of the data objects and label the new data object based on the location relative to this boundary. This is expressed by the decision function $y = f(\mathbf{x})$:

$$f : \mathbb{R}^d \rightarrow \{-1, +1\} \quad (3.1)$$

In case of the OCC problem, only one class (often referred as the target class, or positive examples) of training data is used to create a decision boundary. The goal is to determine whether a new data object belongs to the target class or to the unknown class and thus is an outlier. One could argue that this problem is equal to the traditional two-class problem by considering all other classes as negative examples, although there are important differences. In pure OCC problems there are no negative example objects available. This could be because the acquisition of these examples is very expensive, or because there are only examples of the ‘normal’ state of the system and the goal is to detect ‘abnormal’ states. Since the algorithm’s goal is to differentiate between normal and abnormal objects (relative to the training objects), OCC is often called outlier, novelty or anomaly detection, depending on the origin of the problem to which the algorithm is applied². The difference between two and one-class classification and the consequence for outlier objects is illustrated in Figure 3.1. In the two-class classification problem the object **o** will be member of the **-1** class whilst the OCC problem will label it as an outlier. In [72] a more detailed analysis of the OCC is given.

¹Two-class problems are considered as to be the basic problem, since multi-class classification problems can be decomposed into multiple two-class problems [28].

²The term One-Class Classification originates from Moya *et al.* [59].

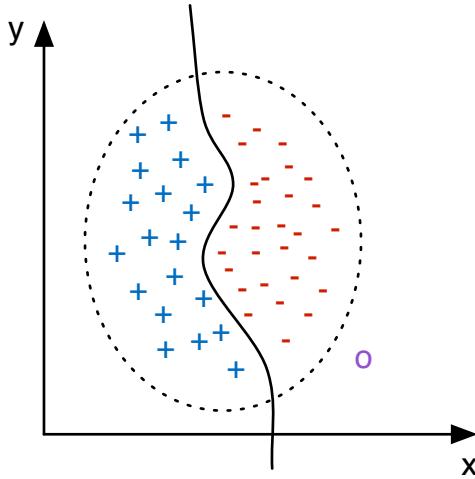


FIGURE 3.1: This plot shows the difference between two and one-class classification. The solid line indicates a possible decision boundary between the +1 and -1 example objects. The dashed circle indicates the closed boundary around all the data objects. In the first type the object o is considered to be member of the -1-class, whilst in the latter (OCC) formulation it is an outlier.

The OCC algorithms have been applied to a wide range of applications. The first is, obviously, outlier detection of objects which do not resemble the bulk of the training data. It can be a goal by itself and can be used as a filtering mechanism for other data processing methods. Often methods that rely on data-characteristics are sensitive for remote regions in the data set. Using OCC these remote regions can be removed from the data set. A second application is for the problem as described above, in which only data from a single target class is available. When this problems originates from e.g. a monitoring process, the OCC is able to recognize abnormal system states, without the need to create (or simulate) faulty states beforehand. The final possible application given by Tax [72] is the comparison of two data sets. By constructing a OCC-classifier using a training data set, one can compare that set to a new data set. This will result in a similarity-measure expressed in the properties of outliers. This measure is related to other similarity measures, such as PDF estimation and the KL divergence as discussed in Section 3.2.2.

3.3.2 One-Class Classification methods

The methods and algorithms used for the OCC-problem can be organized into three categories [61, 72], visually represented in Figure 3.2. The first category consists of methods that estimate the density of the training data and set a threshold on this density. Among those are Gaussian models, Gaussian Mixture Models (GMMs) and Parzen density estimators. In order to get good generalization results with these methods, the

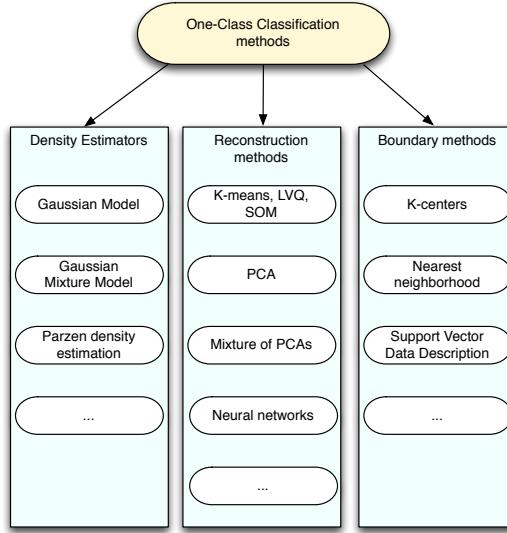


FIGURE 3.2: Overview of OCC methods categorized in Density Estimators, Reconstruction methods and Boundary methods. This categorization follows the definition of Tax in [72].

dimensionality of the data and the complexity of the density need to be restricted. This can cause a large bias on the data. When a good probability model is assumed, these methods work very well, since when one threshold is optimized, a minimum volume is automatically found for the given probability density model [72].

Boundary methods are based on Vapnik's principle³ which imply in this case that estimating the complete data density for a OCC may be too complex, in case one is only interested in the closed boundary. Examples of methods that focus on the boundary (a direct threshold) of the training data distribution are K-centers, Nearest-neighborhood and SVDD or a combination of those methods [37]. Especially the latter has a strong bias towards minimal volume solutions. These type of methods are sensitive to scaling of features, since they rely on a well-defined distance measure. The number of objects that is required is smaller than in the case of density methods. The boundary method SVDD, constructed by Tax and which has shown good performance [46], will be further discussed in Section 3.4.5.

Reconstruction methods take a different approach. Instead of focusing on classification of the data and thus on the discriminating features of data objects, they model the data. This results in a compact representation of the target data and for any object a reconstruction error can be defined. Outliers are data objects with a high reconstruction error, since they are worse represented by the constructed model. Examples of reconstruction methods are K-means, PCA and different kind of neural network implementations.

³With a limited amount of data available, one should avoid solving a more general problem as an intermediate step to solve the original problem [78].

In [46, 61] an overview of applications for OCC-algorithms, and explicitly for SVM-based methods (such as SVDD and ν -SVM), is given. It shows successful applications for, amongst others, problems in the field of Handwritten Digit Recognition, Face Recognition Applications, Spam Detection and Anomaly Detection [50, 63]. As discussed in Section 3.2, this can be used for change detection in time series data.

In this Section we have discussed the problem of OCC and different kind of implementations. An often used implementation is the SVM-based method [61], since it shows good performance in comparative researches. ***** TODO: Add refs for good results of OC-SVM ***** In the following section (3.4) two implementations of OC-SVM will be discussed, the SVDD method of Tax and Duin [73] and the ν -SVM-algorithm by Schölkopf.

3.4 One-Class Support Vector Machine

3.4.1 Support Vector Machine

We will first discuss the traditional two-class SVM before we consider the one-class variant, as introduced by Cortes and Vapnik in [22]. Consider a data set $\Omega = \{(x_1, y_1), (x_2, y_2), \dots, (x_n, y_n)\}$; points $x_i \in \mathbb{R}^d$ in a (for instance two-dimensional) space where x_i is the i -th input data point and $y_i \in \{-1, 1\}$ is the i -th output pattern, indicating the class membership.

A SVM can create a boundary between linear-separable data points, making it a non-probabilistic binary linear classifier. More flexible non-linear boundaries can be obtained by the use of a non-linear function $\phi(x)$, as illustrated in Figure 3.3. This function maps the input data from space \mathcal{I} to a higher dimensional space \mathcal{F} . The SVM can create a linear separating hyperplane in the space \mathcal{F} that separates the data points from the two classes. When the hyperplane is projected to the (lower) original input space \mathcal{I} it creates a non-linear separating curve. This is illustrated in Figure 3.4. The mapping and projection of data points can be efficient (and implicit) performed by using the kernel trick, which is discussed in Section 3.4.2.

The separating hyperplane is represented by

$$w^T x + b = 0, \quad (3.2)$$

with $w \in F$ and $b \in R$. The hyperplane that is created determines the *margin* between the classes; the minimal distance from one of the data points to the hyperplane. In geometric sense, w is the normal vector indicating the direction of the hyperplane and

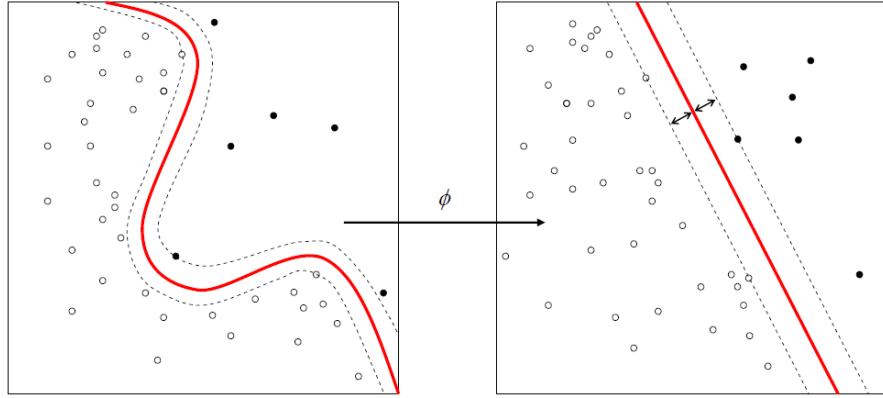


FIGURE 3.3: The non-linear boundary in the input space \mathcal{I} (left) is transformed to a linear boundary in the feature space \mathcal{F} (right) by mapping the data points with the function ϕ . The kernel trick uses a function K which performs an implicit mapping.

Image from Wikipedia.org

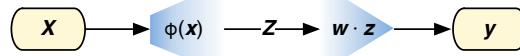


FIGURE 3.4: The input vector x from input space \mathcal{I} is mapped by a non-linear function $\phi(x)$ to a feature vector z in the high dimensional feature space \mathcal{F} . The weights of w create a linear separating hyperplane, which maps the high dimensional vector to the predicted outcome y . *** *TODO: Is this figure obsolete? Figure 3.3 shows almost the same ****

$\frac{b}{\|w\|}$ determines the offset of the hyperplane to the origin. Since the distance between the two margins is equal to $\frac{2}{\|w\|}$, the maximum-margin hyperplane is found by minimizing $\|w\|$. The data points which lie on the margin are the *support vectors*. This geometrical interpretation is illustrated in Footnote 4. All data points for which $y_i = -1$ are on one side of the hyperplane and all other data points (for which $y_i = 1$) are on the other side. The minimal distance from a data point to the hyperplane is for both classes equal. This results in a *maximal margin* between the two classes. Thus, the SVM searches for a maximal separating hyperplane.

With every classification method there is a risk of overfitting. In that case the random error or noise of the data set is described instead of the underlying data. The SVM classifier can use a *soft margin* by allowing some data points to lie within the margin, instead of on the margin or farther away from the hyperplane. For this it introduces *slack variables* ξ_i for each data point and the constant $C > 0$ determines the trade-off between maximizing the margin and the number of data points within that margin (and thus the training errors). The slack variables minimize the *sum of deviations* rather than the *number* of incorrect data points [20]. The objective function for a SVM is the following minimization function:

⁴http://en.wikipedia.org/wiki/File:Svm_max_sep_hyperplane_with_margin.png

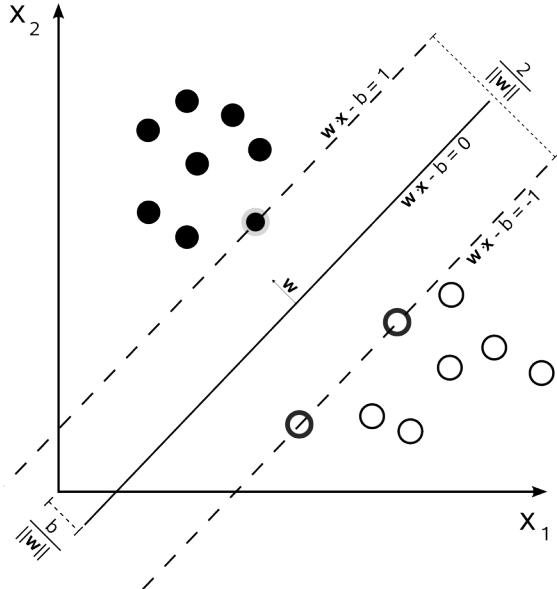


FIGURE 3.5: Illustration of the separating hyperplane of a SVM. Here w is the normal vector for the separating hyperplane and the distance between the two margins is $\frac{2}{\|w\|}$.

Image from Wikipedia.org⁴

$$\min_{w, b, \xi_i} \frac{\|w\|^2}{2} + C \sum_{i=1}^n \xi_i \quad (3.3)$$

subject to:

$$\begin{aligned} y_i(w^T \phi(x_i) + b) &\geq 1 - \xi_i && \text{for all } i = 1, \dots, n \\ \xi_i &\geq 0 && \text{for all } i = 1, \dots, n \end{aligned} \quad (3.4)$$

***** TODO: better format of above formulas. Check with notation and formulas of chapter 9 of [20]. *****

This minimization problem can be solved (using Quadratic Programming (QP)) and transformed to its (Lagrange) dual formulation. In the dual formulation the problem scales with the number of training examples n instead of the dimensionality d of the samples. Solving this problem directly in the high dimensional feature space \mathcal{F} makes it untractable. The linear approximation function corresponds to the kernel function in the dual formulation. Solving this dual formulation is equivalent to solving the primal formulation [20]. In the dual formulation the Lagrange multipliers $a_i \geq 0$ are introduced and the decision function becomes:

$$f(x) = \operatorname{sgn}\left(\sum_{i=1}^n \alpha_i y_i K(x, x_i) + b\right), \quad (3.5)$$

where $K(\mathbf{x}, \mathbf{x}_i) = \phi(\mathbf{x})^T \phi(\mathbf{x}_i)$ is the dot product of data objects in feature space \mathcal{F} (which is further discussed in Section 3.4.2). Here every data point \mathcal{I} for which $a_i > 0$ is weighted in the decision function and thus “supports” the classification machine: hence the name “Support Vector Machine”. Since it is shown that under certain circumstances SVMs show an equality to sparse representations [29, 67], there will often be relatively few Lagrange multipliers with a non-zero value.

Using this formulation two important properties arise [26]:

1. Searching for the maximum margin decision boundary is equivalent to searching for the support vectors; they are the training examples with non-zero Lagrange multipliers.
2. The optimization problem is entirely defined by pairwise dot products between training examples: the entries of the kernel matrix K .

The second property is what enables powerful adaption for support vector machines to learn non-linear decision boundaries. The workings of the kernel matrix K and the non-linear boundaries is discussed in the following section.

***** TODO: Add more on sparsity and good results, because of sparse representations, even in case of data of high dimensionality. e.g. [20]. *****

3.4.2 Kernels

In the previous section, the mapping function $\phi(\mathbf{x})$ and the kernel function K were briefly mentioned. The decision function in Equation (3.5) only relies on the dot products of mapped data points in the feature space \mathcal{F} (i.e. all pairwise distances between the data points in that space). It shows [26] that as long as any function has the same result, without an explicit mapping to the higher dimension \mathcal{F} , the dot products can be substituted by the kernel function K , as introduced by Aizerman *et al.* [2] and applied to Support Vector Classifiers (SVCs) by Vapnik [78]:

$$K(\mathbf{x}, \mathbf{x}') = (\mathbf{z} \cdot \mathbf{z}') = \phi(\mathbf{x}) \cdot \phi(\mathbf{x}') \quad (3.6)$$

where vectors \mathbf{z} and \mathbf{z}' are projections of data objects \mathbf{x} and \mathbf{x}' through $\phi(\mathbf{x})$ on the features space \mathcal{F} and the dot product kernel K is determined by the sum

$$K(\mathbf{x}, \mathbf{x}') = \sum_{j=1}^m g_j(\mathbf{x}) g_j(\mathbf{x}') \quad (3.7)$$

of basis functions $g_j(\mathbf{x})$. Note that the evaluation of dot products in the feature space \mathcal{F} between vectors is performed indirectly via the evaluation of the kernel K between (support) vectors in the input space \mathcal{I} . This is known as the *kernel trick* and gives the SVM the ability to create non-linear decision function without high computational complexity.

The kernel function K can have different forms, such as linear, polynomial and sigmoidal but the most used (and flexible) form is the Gaussian Radial Base Function (RBF). The basis functions have the form

$$g(x) = \text{sign} \left(\sum_{i=1}^n \alpha_i \exp \left\{ \frac{\|\mathbf{x} - \mathbf{x}_i\|^2}{\sigma^2} \right\} \right), \quad (3.8)$$

where σ defines the width and $\|\mathbf{x} - \mathbf{x}'\|^2$ is the dissimilarity measure expressed as Euclidian distance. The inner product kernel K then becomes

$$K(\mathbf{x}, \mathbf{x}') = \exp \left\{ -\frac{\|\mathbf{x} - \mathbf{x}'\|^2}{\sigma^2} \right\}. \quad (3.9)$$

The kernel K maps input space \mathcal{I} to the feature space \mathcal{F} which is a Reproducing Kernel Hilbert Space (RKHS) of (theoretically) infinite dimensions. As Smola *et al.* [67] state, this Gaussian kernel yields good performance, especially when no assumptions can be made about the data. As an explanation, they show a correspondence between learning SVMs with RBF kernels and good regularization operators. This may give insights in why SVMs have been found to exhibit high generalization ability (by learning with few training objects).

The number of basis functions, the center parameters that correspond with support vectors, and the weights in the ouput layer are all automatically determined via the optimal hyperplane in features space \mathcal{F} [20]. The width parameter σ is equal for all basis functions and is set a priori and determines the flexibility and complexity of the boundary. In Section 3.4.6 this (hyper)parameter for a SVM is further discussed.

The mapping from input space \mathcal{I} to \mathcal{F} via $\phi(x)$ is subject to the continuity assumptions. This general assumption in pattern recognition state that two near objects in feature space should also resemble each other in real life [72]. Thus, objects which are close in feature space should be close in the original input space. When this assumption would not hold, the example objects would be scatter through the feature space and finding a decision function becomes very complex.

– Quotes and refs to use –x

sparsity, RKHS: [29]

Use Chapter 2 from “Learning with kernels”, [64].

3.4.3 One-Class Support Vector Machines

The classical implementation of a SVM is to classify a dataset in two distinct classes. This is a common usecase, although sometimes there is no training data for both classes available. Still, one would like to classify new data points as regular, or in-class, or out-of-class, e.g. in the case of a novelty detection. With that problem only data from one class is available and the objective is to recognize new data points that are not part of that class. This unsupervised learning problem is closely related to density estimation. In that context, the problem can be the following. Given an underlying probability distribution P the goal is to find a subset S for which the probability that a data point from P lies outside S equals some predetermined value ν between 0 and 1 [66].

We will discuss two implementations of OC-SVMs. The first is the ν -SVM by Schölkopf *et al.* [66] and closely follows the above problem statement regarding density estimation. The second, on which we will base our change detection method, is the SVDD by Tax and Duin [73].

***** TODO:** Add something about robustness, discusses in section 9.2 from [18, 20] ***

3.4.4 ν -Support Vector Machine

***** TODO:** Check notations with book of Schölkopf [64], chapter 8, page 227. ***

The first of the OC-SVM methods we will discuss is often referred to as ν -SVM and introduced by Schölkopf *et al.* [66]. Instead of estimating the density function of an distribution P , it focuses on an easier problem: the algorithm find regions in the input where the “probability density lives”. This results in a function such that most of the data is in the region where the function is nonzero.

The constructed decision function \mathcal{F} resembles the function discussed in Section 3.4.1. It returns the value +1 in a (possibly small) region capturing most of the data points, and -1 elsewhere. The method maps the data points from input space \mathcal{I} to a feature space \mathcal{F} (following classical SVMs). In that space \mathcal{F} it separates the data points with maximal margin from the origin, with a hyperplane. For a new data points x , the function value

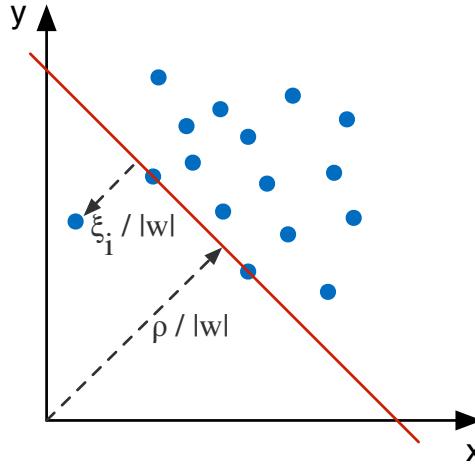


FIGURE 3.6: Graphical representation of ν -SVM. The separating hyperplane $w \cdot \phi(x_i) + \rho = 0$ creates a maximal margin, in the feature space, between the data points and the origin. Slack variables ξ_i are used to create a soft margin.

$f(x)$ determines whether the data point is part of the distribution (i.e. the value is +1) or a novelty (i.e. the value is -1). The hyperplane is represented by $g(x) = w \cdot \phi(x) + \rho = 0$ and the decision function is $f(x) = \text{sgn}(g(x))$. This hyperplane and the separation from the origin is illustrated in Figure 3.6.

The objective function to find the separating hyperplane is the following minimization function, which can be solved using QP:

$$\min_{w, \xi_i, \rho} \frac{\|w\|^2}{2} + \frac{1}{\nu n} \sum_{i=1}^n \xi_i - \rho \quad (3.10)$$

subject to:

$$\begin{aligned} (w \cdot \phi(x_i)) &\geq \rho - \xi_i && \text{for all } i = 1, \dots, n \\ \xi_i &\geq 0 && \text{for all } i = 1, \dots, n \end{aligned} \quad (3.11)$$

The decision function in the dual formulation with Lagrange multipliers is denoted as:

$$f(x) = \text{sgn}((w \cdot \phi(x_i)) - \rho) = \text{sgn}\left(\sum_{i=1}^n \alpha_i K(x, x_i) - \rho\right) \quad (3.12)$$

In the classical SVM objective function, as denoted in Equation (3.3), the parameter C decided the smoothness of the boundary, with respect to the slack variables ξ_i . In the formulation of ν -SVM the equivalent parameter is $\nu \in (0, 1)$ (hence the name). It characterizes the solution in two ways:

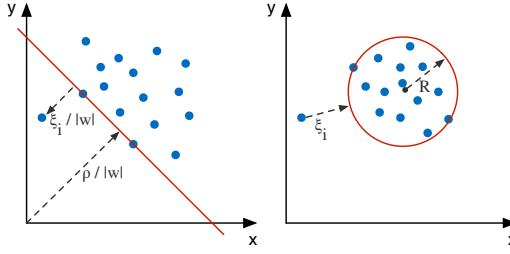


FIGURE 3.7: Graphical representation of the difference between ν -SVM (left) and SVDD (right). Note that for the sake of simplicity the kernel functions are not applied.

1. ν is an upper bound on the fraction of outliers, i.e. training examples regarded as out-of-class.
2. ν is a lower bound on the fraction of Support Vectors (SVs), i.e. training examples with a nonzero Lagrange multiplier α_i .

When ν approaches 0, the penalty factor for nonzero Lagrange multipliers ($\frac{1}{\nu n}$) becomes infinite, and thus the solution resembles a *hard margin* boundary.

This method creates a *hyperplane*, characterized by w and ρ , that separates the data with maximal margin from the origin in the feature space \mathcal{F} . In the following section we will discuss an alternative method, which uses an circumscribing *hypersphere* to characterize the data (and the region of distribution P where the density (or: support) lives).

3.4.5 Support Vector Data Description

The method introduced by Tax and Duin [73], known as Support Vector Data Description, follows a spherical instead of planar approach. The boundary, created in feature space \mathcal{F} , forms a hypersphere around the (high density region of the) data. The volume of this hypersphere is minimized to get the smallest enclosing boundary. The chance of accepting outlier objects is thereby also minimized [76]. By allowing outliers using slacks variables, in the same manner as classical SVM and ν -SVM, a soft margin is constructed.

The constructed hypersphere is characterized by a center \mathbf{a} and a radius $R > 0$ as distance from the center to (any data point that is a SV on) the boundary, for which the volume, and thus the radius R , will be minimized. The center \mathbf{a} is a linear combination of the support vectors. Like the classical SVM and SVDD it can be required that all the distances from the data points x_i to the center \mathbf{a} are strict less than R (or equivalent measure, to create a hard margin) or soft margins are allowed by using slack variables ξ_i .

In the case of a soft margin, the penalty is determined by C and the minimization is expressed as Equation (3.13). This principle is illustrated in the right image or Figure 3.7. Instead of a separating hyperplane, constructed by ν -SVM and illustrated on the left of the Figure, the SVDD creates a hypersphere (in the illustration a circle) around the data points. By using kernel functions (e.g. the RBF) the hyperspheres in the high dimensional feature space \mathcal{F} corresponds to a flexible and tight enclosing boundary in input space \mathcal{I} . Possible resulting closed boundaries are illustrated in Figure 3.8. This enclosing boundary is obtained by minimizing the following error function L which contains the volume of the hypersphere and the distance from the boundary to the outlier objects:

$$L(R, \mathbf{a}, \boldsymbol{\xi}) = R^2 + C \sum_{i=1}^n \xi_i \quad (3.13)$$

subject to:

$$\begin{aligned} \|x_i - \mathbf{a}\|^2 &\leq R^2 + \xi_i \quad \text{for all } i = 1, \dots, n \\ \xi_i &\geq 0 \quad \text{for all } i = 1, \dots, n \end{aligned} \quad (3.14)$$

In the dual Lagrangian formulation of this error function L the multipliers $\boldsymbol{\alpha}$ are maximized:

$$L = \sum_i \alpha_i (x_i \cdot x_i) - \sum_{i,j} \alpha_i \alpha_j (x_i \cdot x_j) \quad (3.15)$$

subject to:

$$0 \leq \alpha_i \leq C, \sum_i \alpha_i = 1 \quad (3.16)$$

In the maximization of Equation (3.15) a large fraction of the multipliers α_i become zero and for a small fraction $\alpha_i > 0$. This small fraction, for which α_i is non-zero, are called the SVs and these objects lie on the boundary of the description. The center of the hypersphere only depends on this small number of SVs and the objects for which $\alpha_i = 0$ can be disregarded from the solution. Testing the membership of a (new) object \mathbf{z} is done by determining if the distance to the center \mathbf{a} of the sphere is equal or smaller to the radius R :

$$\|\mathbf{z} - \mathbf{a}\|^2 = (\mathbf{z} \cdot \mathbf{z}) - 2 \sum_i \alpha_i (\mathbf{z} \cdot \mathbf{x}_i) + \sum_{i,j} (\mathbf{x}_i \cdot \mathbf{x}_j) \leq R^2 \quad (3.17)$$

***** TODO: Note of inner products and that it can be replaced by kernel functions. Good ref: page 4/158 from [74] and [73]. *****

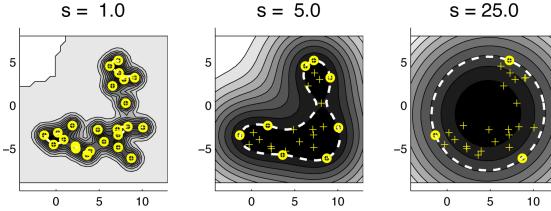


FIGURE 3.8: The SVDD method trained on a banana-shaped data set with different sigma-values for the RBF kernel. Solid circles are support vectors, the dashed line is the boundary. Image by Tax [72].

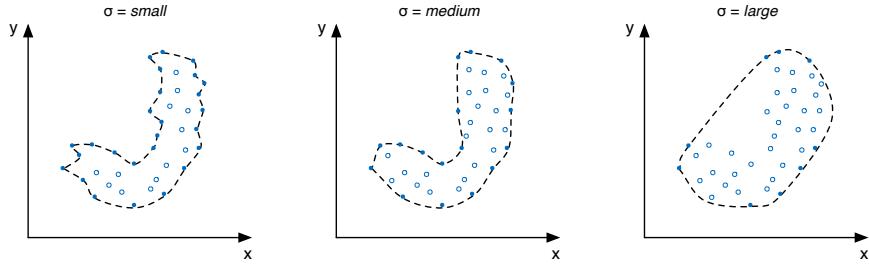


FIGURE 3.9: The SVDD method trained on a banana-shaped data set with different σ -values for the RBF kernel. Solid circles are support vectors, the dashed line is the boundary.

Because the Gaussian RBF often yields good (i.e. tight) boundaries, this set of kernels is commonly used:

$$(\mathbf{x} \cdot \mathbf{y}) \rightarrow K(\mathbf{x}, \mathbf{y}) = \exp\left(-\frac{\|\mathbf{x} - \mathbf{y}\|^2}{\sigma^2}\right) \quad (3.18)$$

Using this kernel function, the Lagrangian error function L of Equation (3.15) changes to:

$$L = 1 - \sum_i \alpha_i^2 - \sum_{i \neq j} \alpha_i \alpha_j K(x_i, x_j) \quad (3.19)$$

Using Equation (3.17), the following kernel formulation needs to hold for a new object \mathbf{z} to lie within the hypersphere:

$$\sum_i \alpha_i K(\mathbf{z}, x_i) \leq \frac{1}{2} \left(1 - R + \sum_{i,j} \alpha_i \alpha_j K(x_i, x_j) \right) \quad (3.20)$$

*** *TODO: Use Figure 3.8 or 3.9?* ***

*** *TODO: Note that SVDD and ν -SVM have identical solutions when data is preprocessed to have unit form (in the case of ν -SVM) [74]. and the RBF kernel is used. Page 234 of [64].* ***

3.4.6 SVM model parameters

SVM-model selectiong and tuning depends on two type of parameters [20]:

1. Parameters controlling the ‘margin’ size,
2. Model parameterization, e.g. the kernel type and complexity parameters. For the RBF kernel the width parameter determines the model complexity.

In case of a RBF kernel, the width parameter σ determines the flexibility and complexity of the boundary. The value of this parameter greatly determines the outcomes of the algorithm (e.g. SVDD) as illustrated in Figure 3.8. With a small value for the kernel width σ , each data point will tend to be used as a support vector (for almost all $\alpha_i > 0$) and the SVDD solution resembles a Parzen density estimation. For large values of σ , the solution will resemble the original hypersphere solution is obtained (in contrast with a tight boundary around the data). With a large value for the width σ , the boudary approximates the spherical boundary.

***** TODO: More on SVM parameters, [20], section 9.8, page 446 *****

***** TODO: Analysis of C/ν -parameter, which sets a lower bound for the fraction of support vectors and an uppor bound for samples that will be outliers. [26] section 9.8 and [64] and other Schölkopf material. *****

***** TODO: Maybe add section about “Change indication” rather than “detection”? *****

– Notes –

- Low target rejection rate f_{T-} and low outlier acceptance rate f_{O+} . When only target examples are present, the first one can be estimated by the number of support vectors that we obtain as a solution of Lagrangian 3.19.

– Literature –

***** TODO: These papers need to be referenced and included *****

“A geometric approach to support vector machine (SVM) classification” [57]. 136, 2006

“Least squares one-class support vector machine” [21]. 27, 2009

“On simple one-class classification methods” [61]. 2012 – ζ decouples radius and center optimization, gives fast approximations instead of precise results.

“Choosing a small width of the kernels leads to high generalization error as it effectively decouples the separate basis functions of the kernel expansion into very localized functions which is equivalent to memorizing the data, whereas a wide kernel tends to oversmooth.” [67].

“For small values of σ almost all $\alpha_i > 0$ and the SVDD resembles a Parzen density estimation.” [74] page 4, [73] page 4.

3.5 Sensor data characteristics

***** TODO: Other title? More in Human Activity Recognition in general?**

– Literature – “Sensor-based abnormal human-activity detection” [85]. 74, 2008 (builds one-class SVM of all normal traces)

3.6 Quality metrics

***** TODO: This section should be in the chapter about experiments *****

Chapter 4

Proposed method

4.1 Outline

Not intented for the reader.

- Based on the problem statement with current research as stated in Chapter 3
- Adjust method to needs
- Explain using graphs, pseudo-algorithms. Make clear distinction in origin of ideas and why to apply

4.1.1 Experiment notes

- ICSS/CUSUM is goed in het vinden van variance changes. Niet goed in mean veranderingen.
- Problemen met SVM methode: ook na de verandering blijft de threshold nog stijgen;
- geprobeerd direct model-reset te doen na change point, maar dan kan je achteraf niet meer verder analyseren.
- Veranderingen in mean geven “extra” change point wanneer alle data weer in het window zit. Zie Figure 5.1 op de 50-tallen.

Data gathering Explain data gathering methods. Refer to chapter 5 and 6 for artificial and real-world details.

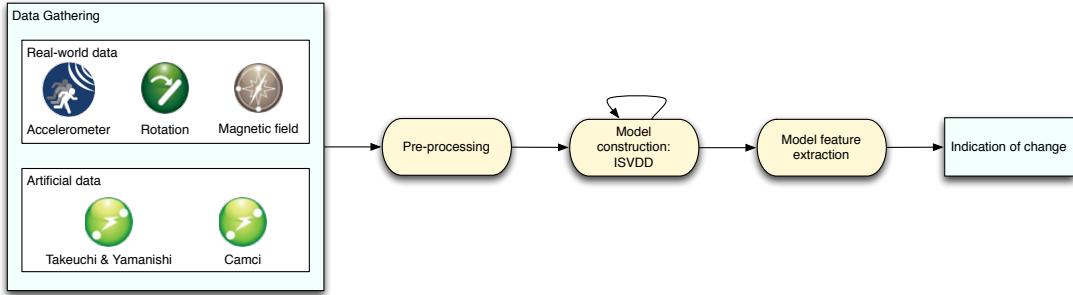


FIGURE 4.1: Schematic overview of the change detection method. The first step is the data gathering, described in Section 4.2. After the pre-processing, the data is used to construct a SVDD model, as described in Section 4.3. Section 4.4 describes which features of the model are used for the final change indication algorithm, discussed in Section 4.5.

Model construction Explain SVDD model construction and updating.

Model properties Explain the SVDD properties that are used to calculate the change indication.

Change detection Explain the interpretation of the properties, the possible (modular) methods to give change indication

**** TODO: Write chapter introduction/outline. Give overview of method approach and refer to each section for details of that stage. ****

**** TODO: Puts emphasis on two-stage framework by Takeuchi and Yamanishi [70]. ***.*

4.2 Data Gathering

In this section we briefly discuss the different data gathering methods used for the change detection algorithms and experiments. Section 4.2.1 reviews the artificial data sets we will use. In Section 4.2.2 an overview of the real-world data sets used is provided. Both sections refer to Chapters 5 and 6 for more details, respectively.

4.2.1 Artificial data

In order to provide an objective comparison to other methods, we will use artificial data sets which are also used in the researches on which our method is based. These are the data sets used by Takeuchi and Yamanishi [70] and Camci [15]. Both construct a

collection of one-dimensional time series data according to a second order Autoregressive (AR) model:

$$x_t = a_1 x_{t-1} + a_2 x_{t-2} + \epsilon_t. \quad (4.1)$$

In the different data series the mean and variance of the Gaussian random variable ϵ_t differs and changes at pre-determined change points. Using this data set an objective quality measure over the change detection methods can be obtained and compared. All the used data sets are listed and analyzed in Chapter 5.

4.2.2 Real-world data

In the second type of data sets we apply our method of change detection and temporal segmentation to real-world data sets. For our setup we record the activities of humans performed both in- and outdoor in an uncontrolled environment. Activities performed include sitting, standing, walking, running in a straight and curved line, and walking up- and downstairs. Our method uses the signals from the accelerometer, gravity, and rotation sensors. These time series data are used to detect change points. A video recording from the performed activity is used to annotate the time series with real change points. The discovered change point are compared with these annotated change points to give a subjective quality measure. In Chapter 6 we give a detailed analysis of the performed activities and the recorded data sets.

For the experiments we used a HTC Sensation XE smartphone as recording device. The activities were recorded using a free Android application [48]. This application was chosen for its convenient data format of the sensor recording and its regularity of the sampling interval. Table 4.1 lists the recorded metrics. For our experiments we used the data for the accelerometer, magnetif field and rotation.

*** *TODO: Complete Table 4.1 ****

4.3 Model Construction: Incremental SVDD

After the data is collected and pre-processed (or in the case of the artificial data sets: generated), we construct an online incremental sliding window algorithm. We follow the SVCVD method by Camci [15] and the Incremental Support Vector Data Description (I-SVDD) implementation by Tax and Laskov [76]. The latter algorithm combines the

| Metric | Description | Units of measure | Typical range |
|---------------------|---|------------------|---------------|
| Accelerometer | Acceleration force along each axis. | m/s^2 | -20 – 20 |
| Gravity | Force of gravity along each axis. | m/s^2 | -10 – 10 |
| Gyroscope | | rad/s | -15 – 15 |
| Light | Light sensitive sensor at the front of the phone. | | 0 – 10000 |
| Linear acceleration | | m/s^2 | -20 – 20 |
| Magnetic field | Geomagnetic field strength along each axis. | μT | -60 – 60 |
| Orientation | | | -100 – 360 |
| Rotation | | | -1 – 1 |

TABLE 4.1: Measured metrics. The set of axis is always the triple (x, y, z) direction.

techniques of online, unsupervised, and incremental learning methods with the earlier introduced OC-SVM algorithm SVDD. The method is initialized with a fixed window length and then in every step a new data object is added to and the oldest data object is removed from the working set.

Using the following abstract form of the SVM optimization problem, the extension of the incremental SVM to the SVDD can be carried out:

$$\max_{\mu} \min_{\substack{0 \leq x \leq C \\ \mathbf{a}^T \mathbf{x} + b = 0}} : W = -\mathbf{c}^T \mathbf{x} + \frac{1}{2} \mathbf{x}^T K \mathbf{x} + \mu(\mathbf{a}^T \mathbf{x} + b), \quad (4.2)$$

where \mathbf{c} and \mathbf{a} are $n \times 1$ vectors, K is a $n \times n$ matrix and b is a scalar. The SVDD implementation of this abstract form is set by the parameters $\mathbf{c} = \text{diag}(K)$, $\mathbf{a} = \mathbf{y}$ and $b = 1$. The procedure for the incremental version has two operations for a data object k : add to and remove from the working set. When a data object k added, its weight x_k is initially set to 0. In case of an object removal, the weight is forced to be $x_k = 0$. Both the operations conclude with the recalculation of μ and the weights \mathbf{x} for all the objects, in order to obtain the optimal solution for the enlarged or reduced data set. These two operations are the basis for I-SVDD. With respect to the timed index, new data objects are added to and old data objects are removed from the working set.

The size of the initial window of data objects has a lower bound determined by the hyperparameter C (Equation (3.13)). Because of the equality constraint $\sum_{i=1}^n a_i x_i = 1$ and the box constraint $0 \leq x_i \leq C$, the number of objects in the working set must be at least $\lceil \frac{1}{C} \rceil$. Thus the algorithm is initialized by selection the first $\lceil \frac{1}{C} \rceil$ objects for the working set. In every loop of the algorithm the number of elements added are at least equal to the number of elements removed. The optimality of the algorithm is proved by analysis of the Karush-Kuhn-Tucker (KKT) conditions [76].

From experiments it shows that the (online) I-SVDD method results in less false alarms than the static SVDD. An explanation for this is that I-SVDD follows the changing data distribution, i.e. small changes over time. Such changes are a drift in mean or increase in frequency. The I-SVDD algorithm continuously re-models the SVM representation. This re-modeling of the SVM representation is beneficial for our purpose, since we are only interested in sudden changes between activities. The following section will discuss the features extracted from the constructed OC-SVM model at every loop-step of the algorithm, before Section 4.5 describes how these features are used to detect change.

4.4 Model Features

In the previous section we have discussed the I-SVDD method, which creates a OC-SVM representation of a working set of data objects at every step of the algorithms loop. This section shows how we interpret the constructed model and extract features to obtain a measure which can be used for a indication of change points. The following section discusses how this obtained measure is used to indicate change.

The I-SVDD algorithm creates a spherical OC-SVM representation of the working set at every step of the algorithm. This model is obtained by the minimization of Equation (3.13), which incorporates the radius R of the sphere and the distances ξ from the outliers to the boundary. We will use the the radius R of the hypersphere as an indication of change.

In [74] Tax and Duin provide an analysis of the error of the SVDD algorithm. This error is based on 1) the fraction f_{T-} of target objects that is rejected, and 2) the fraction f_{O+} of outliers that is accepted. Since in OCC situation typically there are (almost) no examples of outlier objects, Tax and Duin construct a method to generate outliers based on the assumption that the outliers are uniformly distributed around the target set. To minimize the error, calculated by the fractions f_{T-} and f_{O+} , we should minimize the volume of the target data description (i.e. the boundary of SVDD). This is because the fraction of accepted outliers f_{O+} is an estimate of the volume of the target data description, with respect to the volume of the outlier distribution. Tax and Duin provide a method to optimize the parameters of the SVDD method, i.e. the trade-off parameter C and the RBF kernel width σ . This optimization will result in the modification of the radius R of Equation (3.13) and affects the Lagrangian inequality (3.20).

Since in our method the parameters C and σ are kept constant, and thereby also the fraction of target objects being rejected, the only free parameter is the radius R . During the I-SVDD algorithm the volume of the hypersphere is being minimized. This means

that only the radius of the sphere will change during the algorithm. We will interpret changes in the radius R with the same continuity assumptions as mentioned in Section 3.4.2. This means that when two objects (in this case radius sizes) are close to each other, their original objects are also close. In other words, when the underlying distribution of time series is changed, and thus the characteristics of the data objects changes, the corresponding radius R will also change. Since in that case the data objects in the working set become more heterogeneous, the radius of the hypersphere will increase. When, instead, the data objects change from a heterogeneous set to a more homogeneous, we expect the radius to decrease in value, since the data objects are closer to each other in the feature space.

With the I-SVDD algorithm we have effectively implemented a form of dimensionality reduction by feature extraction, using the radius R . The following section discusses the algorithms which can be applied to the extracted radius R as a volume estimate. We thereby follow the setup of the unifying framework by Takeuchi and Yamanishi [70], of which this section described the first stage.

**** TODO: Put the SVM method more in the light of dimensionality reduction. Applies to text in whole thesis... ****

4.5 Change Detection

In the following sections we have discussed what data is used for the model construction how the model is interpreted in the context of change detection. In this section we discuss the methods applicable to the extracted radius R of the hypersphere, in order to indicate a change in the underlying distribution properties. This employs the second stage of our algorithm, analogue to the second stage of the unifying framework by Takeuchi and Yamanishi [70].

In the previous sections we have discussed how a multi-dimensional signal can be reduced to a single dimension time series data based on the radius R . We have argued that in the case of a change in the underlying data, where it becomes more heterogeneous, we expect an increase in the radius R . In the same manner we expect that when the change is in the oldest data objects of the working set the radius R will decrease, since the data becomes more homogeneous. An abstract representation of these expectations is illustrated in Figure 4.2.

The problem of change detection in complex multi-dimensional time series is now reduced to finding change in a one-dimensional time series. Besides the dimensionality reduction, the form of the signal is also simplified. Whereas the original signal was represented as

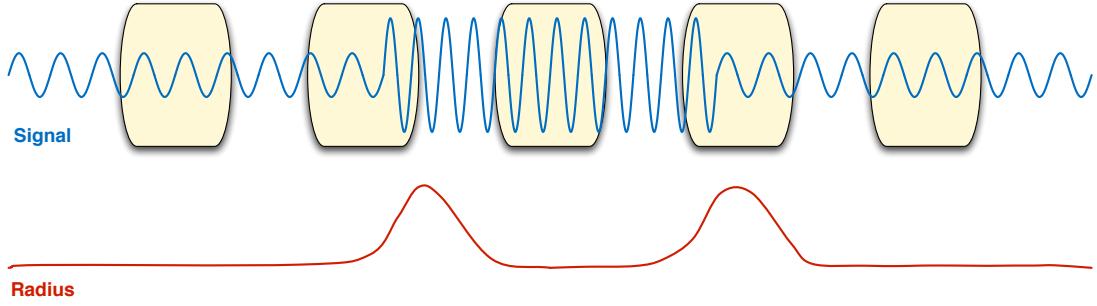


FIGURE 4.2: Expected behavior of the radius R of the hypersphere. The upper part shows a typical sinusoidal time series signal. The lower graph visualizes an abstract expectation of the values of R . Five possible windows are illustrated. The left, middle, and right windows cover an area of homogeneous signal. The expected value of R is low. The other two windows cover a change entering and leaving the window, respectively. At these locations the radius R is expected to increase temporarily.

a sinusoidal or second order AR model, the new time series is of much simpler form. In our method we leave open the precise method which is used to find change points in the obtained change indication values. Below, we will give two examples of methods which can be applied. The first is a family of methods based on the CUSUM method. The second example is a ratio-based thresholding mechanism used by Camci [15]. We conclude this section by discussing some post-processing techniques we have used, to decrease the number of false positives.

4.5.1 CUSUM based methods

Many of the simple change detection methods are based on CUSUM, originally introduced by Page [62]. Many variations and extensions of the method are proposed and used ([4, 40, 41]). Here we will discuss the simple form, which only detects changes for an increase of the examples, in this case the radius R . The cumulative sum for all the values is calculated:

$$S_n = \sum_{k=1}^n r_k \quad (4.3)$$

and a change is detected when the value of the cumulative sums minus the minimum encountered exceeds a predetermined threshold h :

$$S_n - \min_{0 \leq i < n} S_i \geq h. \quad (4.4)$$

Extensions of the CUSUM method have been proposed. Amongst others, extensions which extend its use to two-threshold methods, and methods appropriate for changes in mean or variance [41]. Whilst adaptive methods have been proposed [4], most methods require manual determination of the threshold parameter h .

*** *TODO: This subsection has double information. Cleanup. Mention iterated cumulative sum of squares of inclan [41]. ****

4.5.2 Ratio-thresholding

The second example of an algorithm that interprets the change indication time series and transforms it to change detection is the radius ratio thresholding method used by Camci [15]. The method shares characteristics with CUSUM, since it relies on summation of historic data and thresholds for change detection. The method calculates the radius ratio \hbar_t by taking the ratio of the current radius r_t at time t to the average radii since the last change point y :

$$\hbar_t = \frac{r_t}{\text{mean}(r_{y:t-1})}, \quad (4.5)$$

where $\text{mean}(r_{y:t-1})$ is the average of the previous approximated radii. By using only historic data, this method can be incorporated in an online change detection method. The ratio \hbar_t is compared with two thresholds: the low threshold th_{low} and the high threshold th_{high} . When the data objects in the working set becomes more homogeneous at time t , the radius R of the hypersphere and thereby the ratio \hbar_t will decrease. When the new value of \hbar_t is lower than the low threshold th_{low} , a change detection is observed for time t . The same holds for a more heterogeneous set of data and an increase of \hbar_t higher than th_{high} .

The appropriate values for the thresholds are highly depended on the characteristics of the data and the trade-off parameter C (as discussed in Section 3.4.5). This trade-off parameters regulates the fraction of data objects that will be rejected from the constructed model. Since a high value of C assigns a high penalty to outliers, data objects are more likely to be incorporated into the hypersphere by increasing the radius. For low values of C the cost of rejecting data objects is, compared to the benefits of a smaller hypersphere, relatively low. This gives a relation between the parameters C , th_{low} , and th_{high} and the sensitivity of the radius ratio based thresholding method. A high value of C , or values close to 1 for th_{low} and th_{high} result in a sensitive change detection procedure. The reverse results in less sensitive methods. The correct values for the intended sensitivity need to be empirically determined.

4.5.3 Post-processing

In our method we use the ratio based thresholding, since it is also used by Camci [15]. From preliminary experiments we observed that a single change in the data can cause many detected change points, using the ratio based method. This phenomenon can

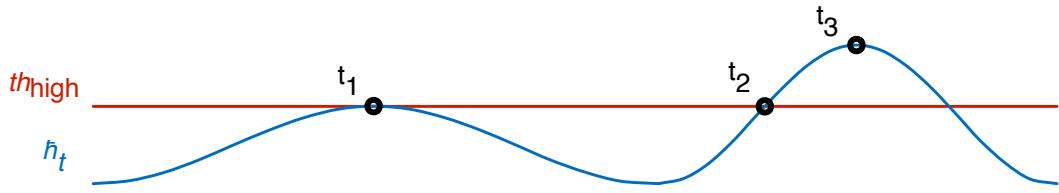


FIGURE 4.3: Abstract illustration of the radius ratio thresholding. The peak at t_1 generates a single change point. The region between t_2 and t_3 generates multiple change points, since the value of h_t keeps increasing.

| Step | Action |
|------|---|
| 1 | Start with n data objects as working set and construct hypersphere |
| 2 | Add next data object x_t and drop first one |
| 3 | Identify new hyper-sphere and its <i>approximate radius</i> |
| 4 | calculate radius average of hyperspheres since last change point |
| 5 | calculate radius ratio \bar{h} . If lower than th_{low} or greater than th_{high} then mark t as change point |
| 6 | continue from step 2, until no more data objects available |
| 7 | Apply post-processing: merge close change points |

TABLE 4.2: Algorithm of the proposed change detection method, using the Ratio-Thresholding method of 4.5.2 for change detection.

be explained by the nature of the thresholding method. Since a single (high or low) threshold is set for ratio of the radii, high values are considered to be a change point before the highest point of the peak. As illustrated in Figure 4.3, the peak at t_1 represents a single change point. The region from t_2 to t_3 is strictly increasing. At t_2 a change point is detected, since \bar{h}_t exceeds the threshold. But since it is increasing up to t_3 , all values of \bar{h}_t in that period will trigger the ratio based method to indicate a change point.

To overcome this problem, we apply a post-processing method on the generated change points. All the change points that are within a time period δ of each other are merged together. ***** TODO: Merged to the front, or to the back, depending on high/low threshold exceeding? *****

***** TODO: Add reference to Table 4.2. *****

Chapter 5

Artificial data results

5.1 Outline

Not intented for the reader.

- Compare proposed method with methods of Chapter 2
- Provide KL-analysis (as Takeuchi does)
- Provide plots, tables, graphs, error rates, precision, etc.
- Apply to a multiple of data, to compare to previous research - use that data
- Give theoretical analysis about performance. Big-O, memory, run-time, precision.
- This sections needs programmed implementations of own method and the ones compared

In this chapter we will apply the proposed algorithm to artificial data sets. For comparison, we use some of the data sets that are used by Camci [15] and Takeuchi *et al.* [70]. These data sets are generated by Gaussian noise distributions. In Section 5.2 the precise generation method and characteristics of the data sets are discussed. For our final change detection mechanism we use the Ratio-Thresholding (RT)-method, also applied by Camci [15]. This is a simple and fast method and allows us to mainly focus on the OC-SVM model properties that should reflect changes in the data. The results of these two methods are discussed in Section 5.3.

5.2 Artificial data generation

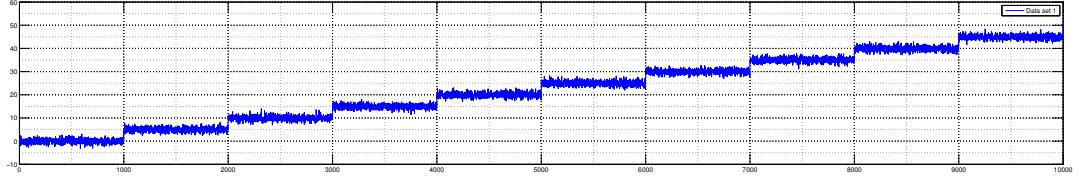
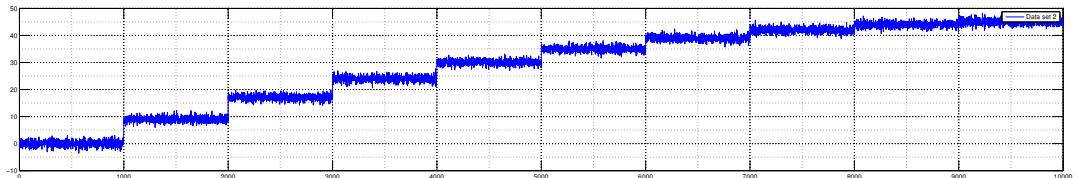
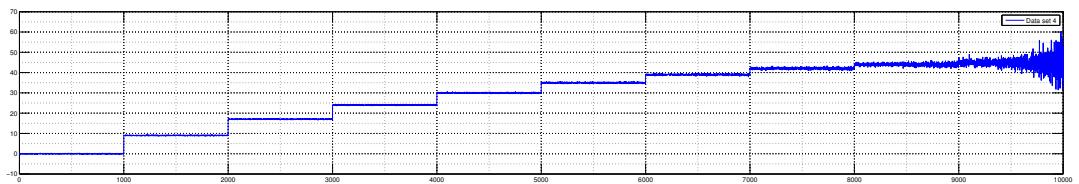
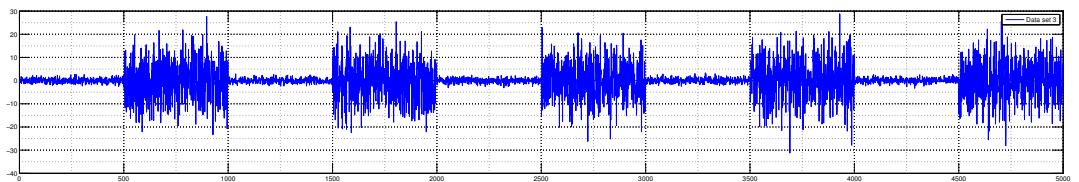
In this section we present four data sets as used by [15, 70] to provide for a objective performance comparison. All the data sets are modeled by a second-order AR-model as in Equation (5.1), where ϵ_t is a Gaussian distribution modeling the noise with mean 0 and variance $\sigma^2 = 1$, $a_1 = 0.6$ and $a_2 = -0.5$.

$$x_t = a_1 x_{t-1} + a_2 x_{t-2} + \epsilon_t, \quad (5.1)$$

The length of x_t is 10000 and change points are generated at each $y \times 10000^{\text{th}}$ data point, with $y = (1, 2, 3, \dots, 9)$.

Using this general AR-model, we create four different data sets. Each data set is characterized by a change in mean, variance, or both of the Gaussian term ϵ_t :

1. **Fixed increasing mean:** at each change point y the mean is increased with $\Delta(y) = 5$. This set origins as the first data set of Camci [15]. The main characteristic is that the difference between the means of the Gaussian term ϵ_t is fixed and thus the relative distance becomes smaller. The data is plotted in Figure 5.1.
2. **Reduced increasing mean:** at each change point y the mean is increased with $\Delta(y) = 10 - y$. This set origins as the first data set of Takeuchi *et al.* [70]. In contrast with the previous set, in this set the absolute difference in mean is reduced over time. The data is plotted in Figure 5.2.
3. **Reduced increasing mean, increasing variance:** at each change point y the mean is increased with $\Delta(y) = 10 - y$ and the standard deviation is of ϵ_t is $0.1/(0.01 + (10000 - x)/1000)$. This set origins as the second set of Camci [15]. This set combines the reduced increasing mean property of the previous set with an increasing variance, causing the change points to become more vague over time. The data is plotted in Figure 5.3.
4. **Alternating variance:** at each change point y the variance σ^2 is set to 9.0 when y is odd, and to 1.0 otherwise. This set origins as the thirds sets from Camci [15] and Takeuchi *et al.* [70]. This data set is used to measure the ability of detecting changes in decrease of variance, as Camci [15] claims is not trivial. The data is plotted in Figure 5.4.

FIGURE 5.1: Data set 1, *Fixed increasing mean*.FIGURE 5.2: Data set 2, *Reduced increasing mean*.FIGURE 5.3: Data set 3, *Reduced increasing mean, increasing variance*.FIGURE 5.4: Data set 4, *Alternating variance*.

5.3 Results

For an objective measure of quality of the proposed method applied to the four aforementioned data sets, we employ two metrics, as defined by Takeuchi *et al.* [70]. The first metric is the average_benefit, for which we first need to define the notion of benefit for each change:

$$\text{benefit}(y) = 1 - |t_y - t_y^*|/10 \quad (\text{when } |t_y - t_y^*| < 10), \quad (5.2)$$

where t_y is the time of the discovered change point and t_y^* is the true change time. We can then define the average_benefit over all the discovered change points Y as:

$$\text{average_benefit}(Y) = \frac{\sum_{y=1}^Y \text{benefit}(y)}{Y}. \quad (5.3)$$

Besides the benefit, which rewards discovered change points close to the actual change points, we need to penalize discovered change points which do not relate to a true change

point. For this we use the False Alarm Rate, expressed as

$$\text{far}(Y) = \frac{Y_{\text{false}}}{Y}. \quad (5.4)$$

For a high quality method the average_benefit should be high and the far should be low.

***** TODO: Above metrics are not used, remove it and replace with own metric (offset, accuracy) *****

The results of all the data sets are provided in Table 5.1, together with the used parameters. For each data set it shows the high and low thresholds used in the RT based change detection method. During the post-processing all detected change points within a certain *closeness* range are merged, for which the value differs per data set. The difference between the actual and final detected change points are expressed as an offset. The data sets were processed with different window lengths and σ value for the RBF kernel.

To give a better impression of the spread of the accuracy of the detected change points, a box plot for each data set is displayed in Figure 5.5. With each data set embodying different characteristics, different observations can be drawn from the data sets. In the references figures, the blue lines represent the radius of the constructed hypersphere. The vertical red lines are the discovered change points. For each data set the following is observed:

1. **Fixed increasing mean:** In Figure 5.6 we see that each change point is almost equally fast and accurate detected. This implies that the relative difference between the means of the Gaussian distribution has no effect on the detectability of the algorithm.
2. **Reduced increasing mean:** Figure 5.7 shows that the absolute difference between the means of the Gaussian distribution is a certain influence to the detectability. Although all change points are correctly detected (at the beginning of the series are two outliers), the change in radius becomes less significant at every change point.
3. **Reduced increasing mean, increasing variance:** In Figure 5.9 we see the same effect, in regard to the mean, as with the previous data set. Furthermore, the increasing variance makes change detection harder. This is visible around the 9000th data point and after, where the radius keeps increasing.
4. **Alternating variance:** The ability to detect decreases in variance of the Gaussian distribution is displayed in Figure 5.8. Although some change points are discovered

| | Set 1 | Set 2 | Set 3 | Set 4 |
|----------------------------------|-------|-------|-------|-------|
| High threshold | 1.6 | 1.6 | 1.5 | 2.2 |
| Low threshold | 0.1 | 0.1 | 0.5 | 0.1 |
| Closeness merging | 10 | 10 | 10 | 50 |
| Number of change points detected | 10 | 11 | 11 | 11 |
| Mean offset | 2.27 | 6.18 | 0.64 | 15.36 |
| Standard deviation offset | 1.19 | 7.94 | 0.92 | 17.70 |
| Window length | 50 | 100 | 50 | 50 |
| Sigma of RBF | 13 | 13 | 15 | 13 |

TABLE 5.1: Results of the artificial data sets.

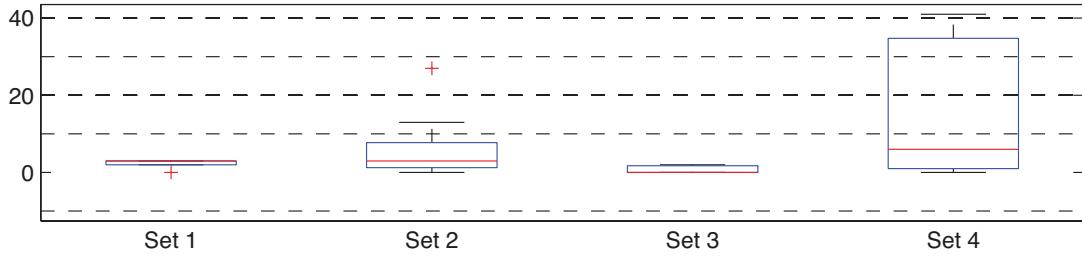
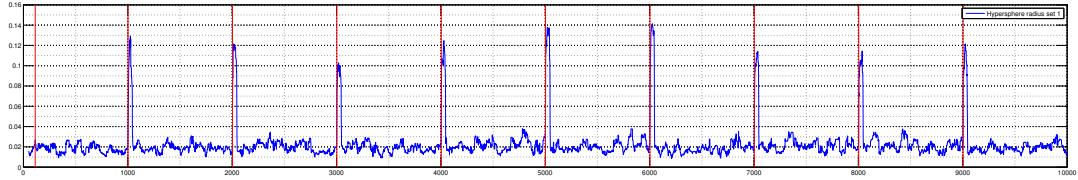
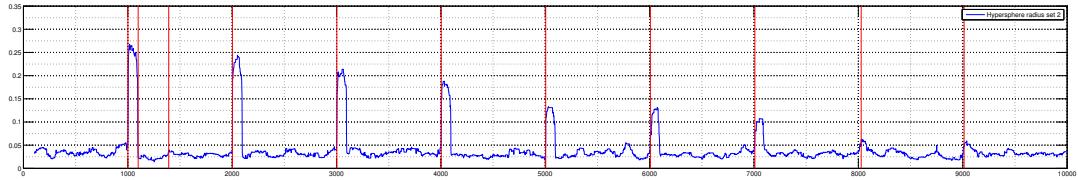


FIGURE 5.5: Box plot of the results for the artificial data sets, indicating the number of data points difference between the actual and detected change points.

FIGURE 5.6: Hypersphere radius sizes for the *Fixed increasing mean* data set with detected change points as red vertical bars.FIGURE 5.7: Hypersphere radius sizes for the *Reduced increasing mean* data set with detected change points as red vertical bars.

with a delay almost up to the length of the window processing the data, the decreases are all detected. The box plot of this set, number 4 in Figure 5.5, shows a wider spread for the results.

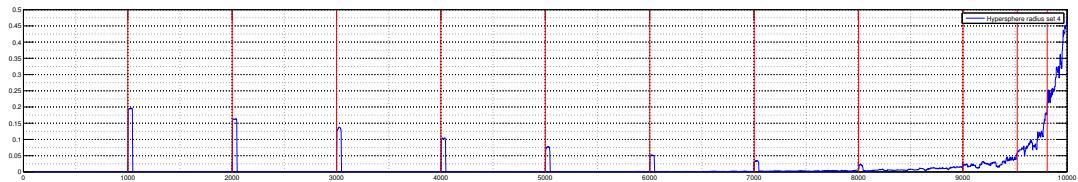


FIGURE 5.8: Hypersphere radius sizes for the *Reduced increasing mean, increasing variance* data set with detected change points as red vertical bars.

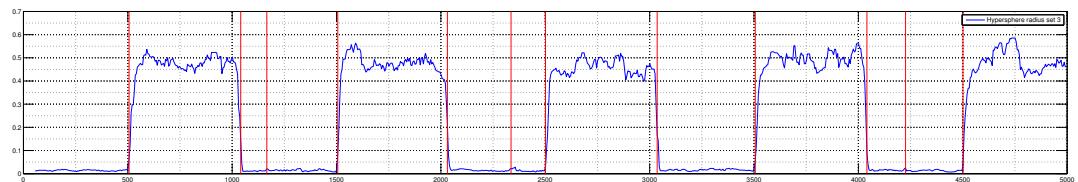


FIGURE 5.9: Hypersphere radius sizes for the *Alternating variance* data set with detected change points as red vertical bars.

Chapter 6

Real-world results

6.1 Outline

Not intented for the reader.

- Apply proposed method to real-world applications, such as
 - Daily life activity recognition (as the original context of this thesis is)
 - PowerHouse sensor data
 - Stock data?
- Relate back to filter vs. wrapper methods - give results with different methods?

This chapter discusses the real-world data sets used for this research. In Section 6.2 we discuss earlier used data sets and argue that these are inappropriate for our research. It is followed by an overview of the setup we have created to record continuous data sets from an uncontrolled environment, both in- and outdoor. The activities performed are discussed in Section 6.3. As discussed in Chapter 4, the algorithm is subject to user parameters. In Section 6.4 the effect and ranges of the parameters on the real world data sets are discussed. Finally, the performance of the algorithm is discussed in Section 6.5.

6.2 Data Sets

In the previous chapter we have applied our method to the artificial data sets from [15, 70]. In this chapter we apply the method to real-world data sets. The data sets are inertial sensor data recorded during human activities, such as walking, running,

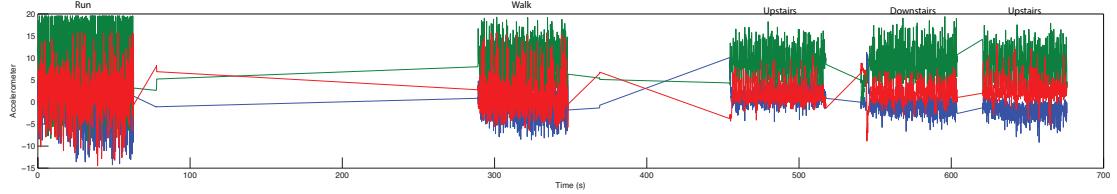


FIGURE 6.1: Excerpt from the WISDM data set [47]. First five activities for subject 33 are displayed. Due to the discontinuous nature of the recordings, this data set can not be used for change detection.

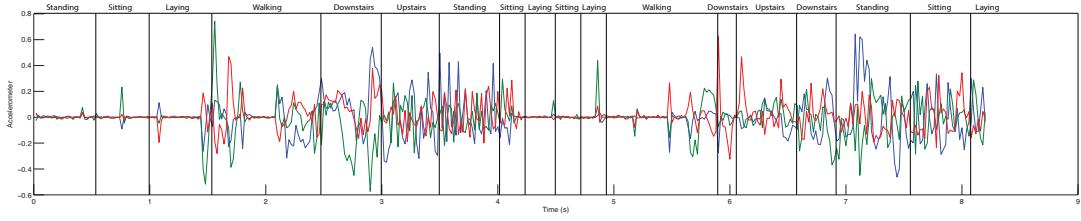


FIGURE 6.2: Excerpt from the UCI HAR data set [6]. The recorded training activities for subject 25 are displayed. Due to the imprecise (and possibly incorrect) labeling and the short duration of activities, the data set can not be used for the change detection method as described in this thesis.

ascending and descending stairs, and standing still. To compare our results with other research, we have tried to apply our method to two commonly used data sets. The first is the data from the WISDM lab [47]. As an excerpt from the data in Figure 6.1 shows, the activities are recorded non-continuous. Whilst this data set is convenient for activity classification, it does not allow for detection of change points. The other commonly used data set is the UCI HAR from the Machine Learning Repository and originates from [6]. As shown in an excerpt in Figure 6.2, the labeling to the data segments seems to be incorrect. Furthermore, it is not clear how the data is recorded and whether all activities are performed continuously.

Because of the above described shortcomings of commonly used data sets, we have decided to record activities by ourselves. The following characterizations were set for our data sets:

1. The activities need to be performed and recorded in a continuous matter,
2. The environment should be natural and uncontrolled, both in- and outdoor,
3. There should be a clear annotation possible, as objective as possible,
4. The hardware and software should be widely available.

With these requirements in mind, we created the following setup. All activities were recorded by one smartphone in the right front pants pocket of the subject. The phones

that were used are the HTC SENSATION XE and HTC DESIRE, running the ANDROID smartphone operating system. During the activities the inertial sensor data is recorded using a free application, SENSOR LOGGER [48]. This application records the sensor data to CSV files, which are then transformed to MATLAB compatible files. The constructed algorithm processes the data in an online matter (using only current and historic data). During the activities, the subject is recorded with a video recorder to enable manual labeling and determining the change points.

Using the video recordings, the data sets are manually annotated, as shown in Figure 6.3. The graph displays from a single recording the rotational-axis values (see Table 4.1 for explanation of the metrics), with manually annotated activities above the data. The manually determined change points are used to draw quality conclusion over the algorithms performance, by comparing it to the discovered change points. All used data recordings, including the video material and manual labeling, are made available [79].

***** TODO: Create web page with data sets ***** The following section discusses the performed activities during the recordings.

6.3 Data Gathering

For our data sets of real world activities we have sampled both in- and outdoor activities. The subjects performing the activities are three males, in an age around 25. We have used two series of recordings. The first series are various outdoor recordings with segments of walking, running and standing. Some movement activities are performed in a straight line, whilst others are performed around corners or in a wide circular direction. The second series consist of mainly walking up and down the stairs, with small vertical parts between the segments. The stairs are all in a circular shape.

6.3.1 Outdoor straight lines

The first series of outdoor performed activities consist of walking and running segments in a straight line. Halfway the recording is a 180° turn. The activities consist of standing still, walking and running (both jogging and sprinting). The plots of Figures 6.3 to 6.5 shows the recordings of Subject 1. For Subject 2 the plots are visible in Figures 6.6 to 6.8. The recorded metrics are from the accelerometer, rotational and magnetometer sensors. The solid black lines indicate manually annotated change points, the dashed lines indicate the closest discovered change point. A still from the video recording, showing Subject 2 performing a (sprinting) run segment, is in ??.

***** TODO: Add found change points to plots *****

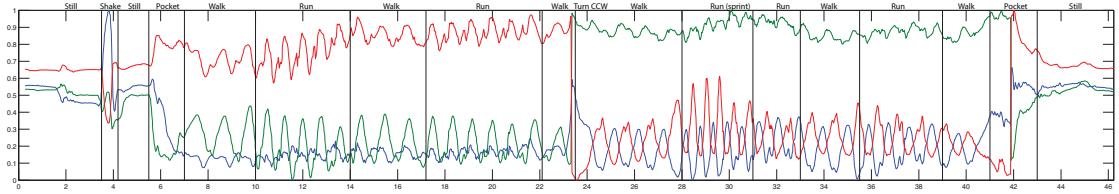


FIGURE 6.3: Run 1: Walk-run-roemer, rotation

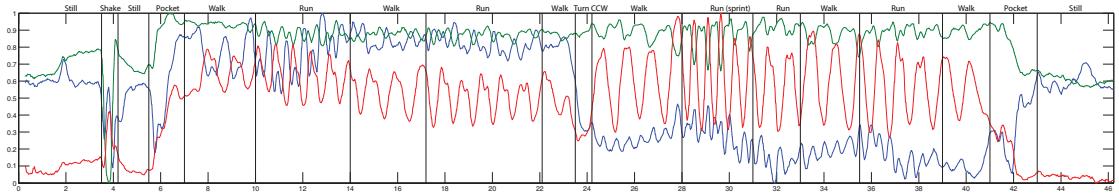


FIGURE 6.4: Run 1: Walk-run-roemer, Mag

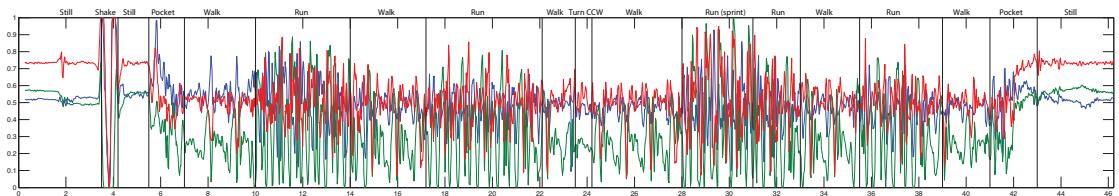


FIGURE 6.5: Run 1: Walk-run-roemer, accelerometer

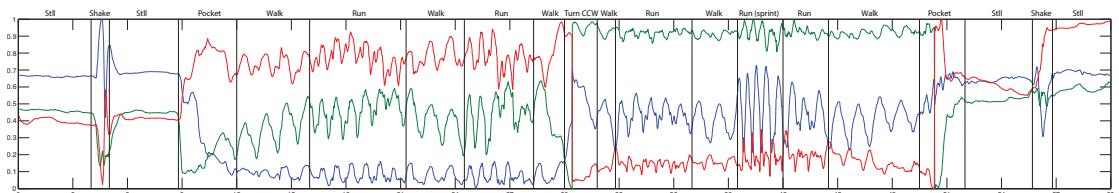


FIGURE 6.6: Run 2: Walk-run-jos, rotation

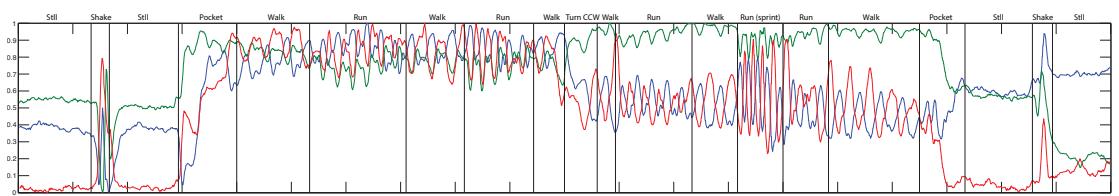


FIGURE 6.7: Run 2: Walk-run-jos, Mag

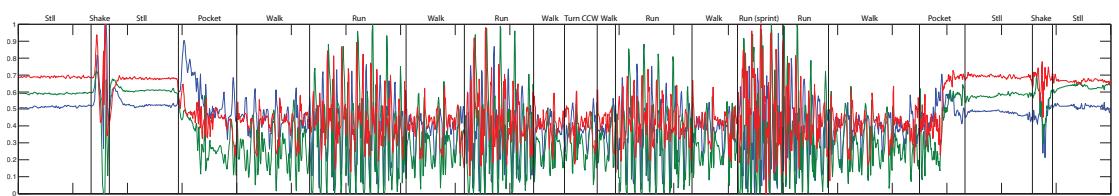


FIGURE 6.8: Run 2: Walk-run-jos, accelerometer

| Subj 1, run 1 | | |
|--------------------|--------|--------|
| Act. | Ann. | Disc. |
| Still | 0 | *0* |
| Shake | 3.5 | *3.5* |
| Still | 4.2 | *4.2* |
| In pocket | 5.5 | *5.5* |
| Walk | 7 | *7* |
| Run | 10 | *10* |
| Walk | 14 | *14* |
| Run | 17.2 | *17.2* |
| Walk | 22.1 | *22.1* |
| Turn CCW | 23.5 | *23.5* |
| Walk | 24.2 | *24.2* |
| Run (sprint) | 28 | *28* |
| Run | 31 | *31* |
| Walk | 33 | *33* |
| Run | 35.5 | *35.5* |
| Walk | 39 | *39* |
| Out pocket | 41 | *41* |
| Still | 43 | *43* |
| Ratio Total CPs | 3.2 | |
| Sum of differences | 12.341 | |

TABLE 6.1: The outdoor series performed activities by subject 1, run 1.

6.3.2 Outdoor straight lines results

***** TODO:** For each data set: discovered timepoint with acc, mag, rot, and all combined. Use closest change point ***

***** TODO:** Replace all times in the stars with the closest discovered change point ***

6.3.3 Outdoor free

The second series of outdoor recordings consist of more free-form activities. The performed activities consist, as with the first set, of standing, walking, and running. Furthermore, the segments are performed in a circular manner. e.g. the running activities are performed around a fountain with an estimated diameter of 10 meters. The plots of the recordings of Subject, for the accelerometer, rotation, and magnetometer are shown in... ***** TODO: Add plots ***** For Subject 2 the still of the video recordings are in ??????????. The stills for Subject 1 are in ????.



FIGURE 6.9: Stills of video recordings during performing of the outdoor activities of walking and running. Figure 6.9b shows the change point between the two activities. Figure 6.9d shows the running in clockwise motion.

6.3.4 Indoor stairs

The final series of activities recorded consist of walking up and down the stairs, indoor. The stairs are shaped in an semi-circular form, with a small vertical segment on each floor. The still of ?? illustrates the circular shape of the stairs. In ?? the small flat segment is visible. Between the stairs the subject walked in a hallway with a 180° counter-clockwise turn, as shown in ???. The recorded sensor data of the performed activities are visible in the plots of Figures 6.11 to 6.13.

6.4 Parameters

***** TODO:** *Describe how all the parameters are set, for the SVM methods and change-indication methods. Kernel type, width, /C values etc. ****



(A) Downstairs

(B) Walking

(C) Upstairs

FIGURE 6.10: Stills of video recordings during performing of the indoor activities of walking, ascending and descending the stairs.

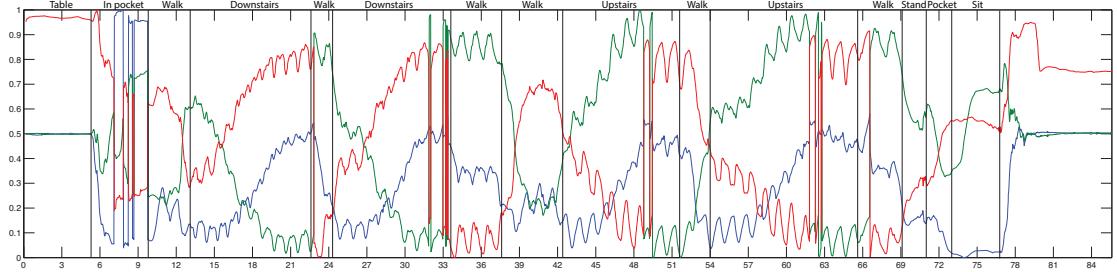


FIGURE 6.11: Run 3: Indoor stairs Marc, rotation

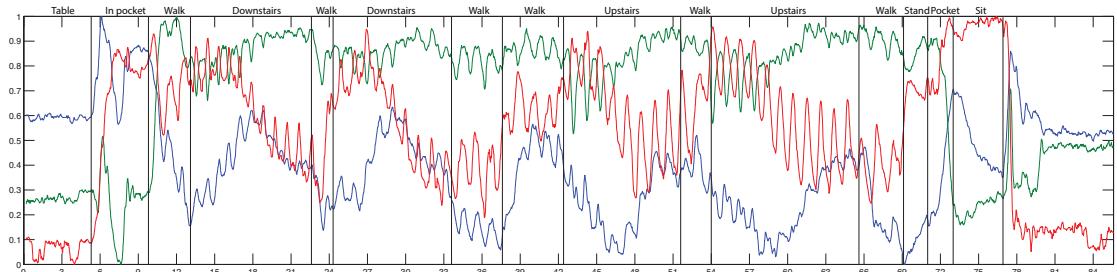


FIGURE 6.12: Run 3: Indoor stairs Marc, Mag

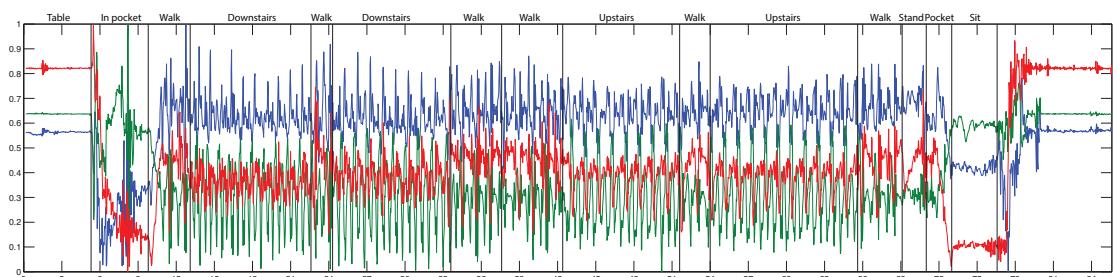


FIGURE 6.13: Run 3: Indoor stairs Marc, accelerometer

6.5 Performance

Chapter 7

Conclusion

7.1 Outline

Not intended for the reader.

- Tie together, integrate, synthesize all the issues from the chapters, reflecting on introductory thesis statements.
- Provide answers to research questions
- Highlight study limitations
- Directions for further research.
- Content: Summarize
 - What have I researched
 - Main arguments
 - How researched
 - What discovered
 - What pre-existing views were challenged (?)
- Overview of
 - New knowledge
 - Significance of research
 - Limitations (data, concepts)
 - Speculations on implications of research

- Further research and development, or: links with different fields, other methods applied to same data.
- Must: make clear statement of my original contribution
- Ideally:
 - Shows links across key ideas spread in chapters
 - Show commitment and enthusiasm for research
 - Positive impression
- Avoid:
 - claim findings that have not been proven
 - introducing new data/concepts
 - Be self-critical, but dont put weaknesses or limitation in research
 - Too long/too short

Paragraph: into on conclusion; what have I researched and what is my contribution.
Break into sections further down.

====

In this research we have applied OCC methods to accelerometer data, recorded during the performance of various human activities, in order to create a temporal segmentation of those recordings. The goal was to find the change points between activities, assuming that it will aid better understanding of the sensor values. To do so, we used the SVDD algorithm by Tax [73], following the method of applying it to a sliding window of data, as done by Camci [15]. Instead of using both the information whether a new data point is an outlier and the radius of the hypersphere to indicate change, we only used on the latter model properties. The increase of the radius of the constructed hypersphere, which encloses the data objects and increases with heterogeneous segments of data, is extracted and used for indication of change.

****** TODO: Write overview of this chapter. In the following section we will... ******

7.2 What is done

The scope of this research was the temporal segmentation of recordings, obtained from human activities. This was performed in the wider context of activity classification. Currently, many algorithms obtain an implicit segmentation as a side-effect of direct activity

classification. In this research the primary goal was finding a temporal segmentation, which is assumed to be able to aid the classification step.

We have considered a range of segmentation methods, from which the method by Camci [15] showed potential. It is based on the detection of outliers in a time series data, assuming that an increase of outliers indicates a change in the underlying generating model. For the detection of outliers it uses the SVDD method by Tax [73]. It tests every new data point with the constructed model; whether the data point is in or outside the model, and whether the model increases or decreases in radius size. The constructed sliding-window algorithm, SVCPD, is applied to artificial Gaussian noise data.

In this research we have applied the method by Camci [15] to inertial signals, recorded by smartphones. We have used the accelerometer data for measurement of speed, the gyroscope data for measurement of rotation, and the magnetometer to measure the direction and orientation of the performed activities. The constructed method reduces this 9-dimensional signal to a single property, obtained from the constructed model, which can be interpreted to indicate change.

The constructed model follows the implementation of Tax and Laskov [76] for an incremental version of SVDD, I-SVDD. This algorithm constructs a OC-SVM model by processing the data over a sliding window. The model represents a hypersphere from which the radius size is abstracted. That property is of interest since the assumption is that a heterogeneous window of data will show an increase of radius, in relation to a homogeneous segment of data. The homogeneous segment of data will have a relatively small radius since the data points will be close together, resulting from the continuity assumptions.

To test our approach, we have used the same data as used in the experiments from Camci [15] and Takeuchi and Yamanishi [70]. Furthermore, since this research is focused around human activities, we have recorded and manually annotated in- and outdoor activities. The discovered change points were compared to the annotated change points, obtained from video recordings. In this research we found that other public available and wide used common data sets, such as the WISDM [47] and UCI HAR [6], were not useful for our purpose, since the activities are non-continuously recorded.

***** TODO:** *In the above, refer to the corresponding chapters/sections. ****

7.3 Main findings

What we have found, show links across chapters.

For each finding a different paragraph. How did we arrive at this finding, and it challenges/improves on previous research. Not just a summary, but the effects and implications.

While temporal segmentation of time series data is not uncommon, the application to inertial signals is currently not under much research attention. It is applied in other contexts, such as motion tracking and first person vision sensing, the segmentation obtained from inertial signals is often the implicit result of classification.

7.4 Contributions

7.5 Other research

Relate the finding with earlier research. Provide similarities and differences. Better/-worse results?

7.6 Limitations

Show what limitations were encountered or decided (data collection, scope). Note the focus of the limitations and how they worked together (to get positive note). This can create bridge to "future research".

7.7 Future research

The motivation for this research was, amongst others, the assumption that an explicit temporal segmentation of inertial signals can be used to obtain a better classification of the performed activities. There are two reasons for that. First, since the segmentation adds information about sequential data points (whether they belong to the same class), the a priori knowledge about the distribution changes. Second, the window of data used for model construction can be much larger (than the often used length of 1-3 seconds). This enables a better mathematical model to be constructed. A future research in this line of assumptions is to compare the performance of classification methods using this obtained temporal segmentation and those that do not.

Since the temporal segmentation of inertial signal is not yet a very active field of study, more studies can be performed to obtain it. In our approach we have used the raw data directly. In the field of activity recognition many methods make use of pre-processing steps, from which one step often is feature extraction from the raw data. That, and other pre-processing steps, could be incorporated in the explicit temporal segmentation of inertial signals. Future research could focus on extracted features that aid the detection of change points.

****** TODO: Add future research on OC-SVM applications. ******

What has not been covered? What is worthwhile. Show that I am thinking ahead and know the field of study.

7.8 Final section

Reminding of original contribution and significance. This section is the overall conclusion and thus should be very concise and precise.

****** TODO: Formulate the research questions in the introduction of thesis, and in the chapters. ******

Appendix A

Summaries

Please ignore this Appendix. This appendix is for my own personal use. It contains summaries of articles I have read.

A.1 Support Vector Machines

A.1.1 Machine learning: the art and science of algorithms that make sense of data

Book by Peter Flach: [26]. Mainly about chapter 7, “Linear Models”. Most important: section 7.3 - 7.5, about support vector machines and non-linearity. **Some parts are direct text; do not use this text directly!**

A.1.1.1 Linear models

Models can be represented by their geometry of d real-values features. Data points are represented in the d -dimensional Cartesian coordinate system/space $\mathcal{X} = \mathbb{R}^d$. Geometric concepts such as lines and planes can be used for *classification* and *regression*. An alternative approach is to use the distance between data points as a similarity measure, resulting from the geometrical representation. Linear methods do not use that property, but rely on understanding of models in terms of lines and planes.

Linear models are of great interest in machine learning because of their simplicity. A few manifestations of this simplicity are:

- Linear models are *parametric*, thus fixed small number of parameters that need to be learned from the data.

- Linear models are *stable*, thus small variations in training data have small impact on the learned model. In logical models they can have large impact, because “splitting rules” in root have great impact.
- Due to relative few parameters, less likely to *overfit* the training data.

The last two are summarized by saying that *linear models have low variance but high bias*. This is preferred with limited data and overfitting is to be avoided.

Linear models are well studied, in particular for the problem of linear regression. This can be solved by the *least-squares* method and classification as discussed in Appendix A.1.1.2, the *perceptron* as explained in Appendix A.1.1.3. Linear regression with the *support vector machine* is handled in Appendix A.1.1.4 and used for probability density estimation in Appendix A.1.1.5. The kernel trick used for learning non-linear models is explained in Appendix A.1.1.6.

A.1.1.2 Least-squares method

The regression problem is to learn a function estimator $\hat{f} : \mathcal{X} \rightarrow \mathbb{R}$ from the examples $(x_i, f(x_i))$ where we assume $\mathcal{X} = \mathbb{R}^d$. The difference between the actual and estimated function values are called *residuals* $\epsilon_i = f(x_i) - \hat{f}(x_i)$. The *least-squares method* finds the estimation \hat{f} by minimizing $\sum_{i=1}^n \epsilon_i^2$. Univariate regression assumes a linear equation $y = a + bx$, with parameters a and b chosen such that the sum of squared residuals $\sum_{i=1}^n (y_i - (a + bx_i))^2$ is minimized. Here the estimated parameter \hat{a} is called the *intercept* such that it goes through the (estimated) point (\hat{x}, \hat{y}) and \hat{b} is the *slope* which can be expressed by the (co)variances: $\hat{b} = \frac{\sigma_{xy}}{\sigma_{xx}}$. In order to find the parameters, take the partial derivatives, set them to 0 and solve for a and b .

Although least-squares is sensitive to outliers, it works very well for such a simple method. This can be explained as follows. We can assume the underlying function is indeed linear but contaminated with random noise. That means that our examples are actually $(x_i, f(x_i) + \epsilon_i)$ and $f(x) = ax + b$. If we know a and b we can calculate what the residuals are, and by knowing σ^2 we can estimate *the probability of observing the residuals*. But since we don't know a and b we have to estimate them, by estimating the values for a and b that maximizes the probability of the residuals. This is the *maximum-likelihood estimate* (chapter 9 in the book).

The least-squares method can be used for a (binary) classifier, by encoding the target variable y as classes by real numbers -1 (negative) and 1 (positive). It follows that $\mathbf{X}^T(y) = P\boldsymbol{\mu}^+ - N\boldsymbol{\mu}^-$, where $P, N, \boldsymbol{\mu}^+$ and $\boldsymbol{\mu}^-$ are the number of positive and negative

examples, and the d -vectors containing each feature's mean values, resp. The regression equation $y = \bar{y} + \hat{b}(x - \bar{x})$ can be used to obtain a decision boundary. We need to determine the point (x_0, y_0) such that y_0 is half-way between y^+ and y^- (the positive and negative examples, i.e. $y_0 = 0$).

A.1.1.3 Perceptron

Labeled data is *linearly separable* if there exists a linear boundary separating the classes. The least-squares may find one, but it is not guaranteed. Imagine a perfect linearly separable data set. Move all the positive points away from the negative, but one. At one point the new boundary will exclude (mis qualify) the one original positive outlier, due to the mean-statistics it relies on. The *perceptron* will guaranteed perform perfect separation when the data allows it to be. It was originally proposed as a *simple neural network*. It works by iterating over the training set and modifying the weight vector for every misclassified example ($\mathbf{w} \cdot \mathbf{x}_i < t$ for positive examples \mathbf{x}_i). It uses a learning rate η , for a misclassified $y_i = \{-1, +1\}$: $\mathbf{w}' = \mathbf{w} + \eta y_i \mathbf{x}_i$. The algorithm can be made *online* by processing a stream of data points and updating the weight vector only when a new data point is misclassified.

When the algorithm is completed, every $y_i \mathbf{x}_i$ is added α_i times to the weight vector (every time it was misclassified). Thus, the weight vector can be expressed as: $\mathbf{w} = \sum_{i=1}^n \alpha_i y_i \mathbf{x}_i$. In other words: the weight vector is a linear combination of the training instances. The dual form of the algorithm learns the instance weights α_i rather than the features weights \mathbf{w}_i . An instance \mathbf{x} is then classified as $\hat{y} = \text{sign}(\sum_{i=1}^n \alpha_i y_i \mathbf{x}_i \cdot \mathbf{x})$. This means that during the training only the pairwise dot products of the data is needed; this results in the n -by- n Gram matrix $\mathbf{G} = \mathbf{X} \mathbf{X}^T$. This instance-based perspective will be further discussed in Appendix A.1.1.4 about the support vector machine.

A.1.1.4 Support Vector Machine

A training example can be expressed by its *margin*: $c(x)\hat{s}(x)$, where $c(x)$ is $+1$ for positive and -1 for negative examples and $\hat{s}(x)$ is the score. The score can be expressed as $\hat{s}(x) = \mathbf{w} \cdot \mathbf{x} - t$. A true positive example \mathbf{x}_i has a margin $\mathbf{w} \cdot \mathbf{x}_i > 0$ and a true negative \mathbf{x}_j has $\mathbf{w} \cdot \mathbf{x}_j < 0$. If m^+ and m^- are the smallest positive and negative examples, then we want the sum of these to be as large as possible. *The training examples with these minimal values are closest to the decision boundary t and are called the support vectors.* The decision boundary is defined as a linear combination of the support vectors. The margin is thus defined as $\frac{m}{\|\mathbf{w}\|}$. Minimizing the margin (which is often set to 1 and rescaling is allowed) yields to minimizing $\|\mathbf{w}\|$, or: $\frac{1}{2}\|\mathbf{w}\|^2$, restricted that none of the

training points fall inside the margin. This gives the following quadratic, constrained optimization problem:

$$\mathbf{w}^*, t^* \in \operatorname{argmin}_{\mathbf{w}, t} = \frac{1}{2} \|\mathbf{w}\|^2 \quad \text{subject to } y_i(\mathbf{w} \cdot \mathbf{x}_i - t) \geq 1, 1 \leq i \leq n \quad (\text{A.1})$$

This equation can be transformed with the Lagrange multipliers by adding the constraints to the minimization part with multipliers α_i . Taking the partial derivative with respect to t and setting it to 0, we find that for the optimal solution (threshold) t we have $\sum_{i=1}^n \alpha_i y_i = 0$. When we take the partial derivative with respect to \mathbf{w} we see that the Lagrange multipliers define the weight vector as a linear combination of the training examples. This partial derivative is 0 for an optimal weight we get that $\mathbf{w} = \sum_{i=1}^n \alpha_i y_i \mathbf{x}_i$, which is the same expression as for the perceptron derived in Appendix A.1.1.3. By plugging \mathbf{w} and t back into the Lagrange equation, we can eliminate these and get the dual optimization problem entirely formulated in terms of the Lagrange multipliers:

$$L(\alpha_1, \dots, \alpha_n) = -\frac{1}{2} \sum_{i=1}^n \sum_{j=1}^n \alpha_i \alpha_j y_i y_j \mathbf{x}_i \cdot \mathbf{x}_j + \sum_{i=1}^n \alpha_i \quad (\text{A.2})$$

The dual problem maximizes this function under positivity constraints and one equality constraint: *** ***TODO: fix equation (now commented)*** ***

$$\text{subject to } \alpha_i \geq 0, 1 \leq i \leq n \text{ and } \sum_{i=1}^n \alpha_i y_i = 0 \quad (\text{A.3})$$

This shows two important properties:

1. Searching for the maximum-margin decision boundary is equivalent to searching for the support vectors; they are the training examples with non-zero Lagrange multipliers.
2. The optimization problem is entirely defined by pairwise dot products between training instances: the entries of the Gram matrix.

The second property enables powerful adaption for support vector machines to learn non-linear decision boundaries, as discussed in Appendix A.1.1.6.

An other solution to non-linear separable data, that is when the constraints $\mathbf{w} \cdot \mathbf{x}_i - t \geq 1$ are not jointly satisfiable, is to add *slack variables* ξ_i , one for each example. This allows them to be in the margin, or even at the wrong side of the boundary – known as boundary errors. Thus, the constraints become $\mathbf{w} \cdot \mathbf{x}_i - t \geq 1 - \xi_i$.

“In summary, support vector machines are linear classifiers that construct the unique decision boundary that maximizes the distance to the nearest training examples (the support vectors). Training an SVM involves solving a large quadratic optimization problem and is usually best left to a dedicated numerical solver.”

A.1.1.5 Density Functions from linear classifiers

The score of an data point can be used to obtain the signed distance of \mathbf{x}_i to the decision boundary:

$$d(\mathbf{x}_i) = \frac{\hat{s}(\mathbf{x}_i)}{\|\mathbf{w}\|} = \frac{\mathbf{w} \cdot \mathbf{x}_i - t}{\|\mathbf{w}\|} = \mathbf{w}' \cdot \mathbf{x}_i - t' \quad (\text{A.4})$$

where $\mathbf{w}' = \mathbf{w}/\|\mathbf{w}\|$ rescaled to unit length and $t' = t/\|\mathbf{w}\|$ corresponds to the rescaled intercept. this geometric interpretation of the scores enables them to turn into probabilities. Let $\bar{d}^+ = \mathbf{w} \cdot \boldsymbol{\mu}^+ - t$ denote the mean distance of the positive examples to the boundary, where $\boldsymbol{\mu}^+$ is the mean of positive examples (in the grid) and \mathbf{w} is unit length. We can assume that the distance of the examples is normally distributed around the mean (which give a bell curve when plotted).

If we obtain a new point \mathbf{x} we can get the class by $\text{sign}(d(\mathbf{x}))$. We would like, instead, to get the probability (using Bayes’ rule)

$$\hat{p}(\mathbf{x}) = P(+|d(\mathbf{x})) = \frac{P(d(\mathbf{x})|+)P(+)}{P(d(\mathbf{x})|+)P(+) + P(d(\mathbf{x})|-)P(-)} = \frac{LR}{LR + 1/\text{clr}} \quad (\text{A.5})$$

where LR is the likelihood ratio obtained from the normal score distributions, and clr is the class ratio. With some rewriting we can convert d into a probability by means of the mapping $d \mapsto \frac{\exp(d)}{\exp(d)+1}$, which is the *logistic function*. The logarithm of the likelihood ratio is linear in \mathbf{x} and such models are called *log-linear models*. This logistic calibration procedure can change the location of the decision boundary but not its direction. There may be an alternative weight vector with a different direction that assign a higher likelihood to the data. Finding that maximum-likelihood linear classifier using the logistic model is called *logistic regression*.

A.1.1.6 Non-linear models

Linear methods such as least-squares for regression can be used for binary classification, yielding in the basic linear classifier. The (heuristic) perceptron guarantees to classify correctly linear separable data points. Support vector machines find the unique decision boundary with maximum margin and can be adapted to non-linear separable data. These methods can be adjusted to learn non-linear boundaries. The main idea is to

transform the data from the *input space* non-linearly to a *feature space* (which can, but does need to be in a higher dimension) in which linear classification can be applied. The mapping back from the feature space to the input space is often non-trivial (e.g. mapping (x, y) to feature space by (x^2, y^2) , yields in four coordinates when transformed back to the input space).

The remarkable thing is that often the feature space does not have to be explicitly constructed, as we can perform all necessary operations in input space. For instance; the perceptron algorithm mainly depends on the dot product of $\mathbf{x}_i \cdot \mathbf{x}_j$. Assuming $\mathbf{x}_i = (x_i, y_i)$ and $\mathbf{x}_j = (x_j, y_j)$, the dot product can be written as $\mathbf{x}_i \cdot \mathbf{x}_j = x_i x_j + y_i y_j$. The instances in quadratic feature space are (x_i^2, y_i^2) and (x_j^2, y_j^2) and their dot product is $(x_i^2, y_i^2) \cdot (x_j^2, y_j^2) = x_i^2 x_j^2 + y_i^2 y_j^2$. This is almost equal to $(\mathbf{x}_i \cdot \mathbf{x}_j)^2 = (x_i x_j)^2 + (y_i y_j)^2 + 2x_i x_j y_i y_j$, but not quite because of the third term. We can make the equations equal by *extending the feature space* (to a higher dimension) with a third feature $\sqrt{2xy}$, so the feature space is $\phi(\mathbf{x}_i) = (x_i^2, y_i^2, \sqrt{2x_i y_i})$.

If we define $\kappa(\mathbf{x}_i, \mathbf{x}_j) = (\mathbf{x}_i \cdot \mathbf{x}_j)^2$ and replace $\mathbf{x}_i \cdot \mathbf{x}_j$ with $\kappa(\mathbf{x}_i, \mathbf{x}_j)$ in the (perceptron) algorithm, we obtain the *kernel perceptron* with the degree $p = 2$. We are not restricted to polynomial kernels; an often used kernel is the *Gaussian kernel*, defined as:

$$\kappa(\mathbf{x}_i, \mathbf{x}_j) = \exp\left(-\frac{\|\mathbf{x}_i - \mathbf{x}_j\|^2}{2\sigma^2}\right) \quad (\text{A.6})$$

where σ is known as the *bandwidth* parameter. We can think of the Gaussian kernel as imposing a Gaussian (i.e., multivariate normal) surface on each support vector in instance space, so that the boundary is defined in terms of those Gaussian surfaces. Kernel methods are best known in combination with support vector machines. Notice that the soft margin optimization problem is defined in terms of dot product between training examples, and thus the ‘kernel trick’ can be applied. Note that the decision boundary learned with a non-linear kernel cannot be represented by a simple weight vector in input space. Thus, to classify a new example \mathbf{x} we need to evaluate $y_i \sum_{j=1}^n \alpha_j y_j \kappa((x), \mathbf{x}_j)$ (the Gram matrix?) involving all training examples, or at least all with non-zero multipliers α_j (the support vectors).

A.1.2 Change Point Detection In Time Series Data Using Support Vectors

Paper by Fatih Camci [15] About segmentation with SVMs. Will be main material for Section 2.9 about SVMs.

A.1.2.1 Introduction

Interprets change detection as finding the transition points from one underlying time series generation model to another. The change point is mostly represented in a sudden change in mean or variance. Existing models detect changes in mean and increase in variance, *but fail to recognize decrease in variance*. Many methods require some model (like Auto-Regressive [AR]) to fit the time series in order to eliminate the noise. Thus, the effectiveness of the method is tied to the fitness degree of the model to the time series data. These two problems (lack of variance decrease detection and model-bound fitness degree) leads to this work; Support Vector based Change Point Detection targeting changes in variance and/or mean without any assumption of model fitting of data distribution. This method *does not use a time series model* for fitting and targets *both increase and decrease* in mean and variance.

A.1.2.2 Related work

Change Point Detection (CPD) can be categorized in posterior (off-line) and sequential (on-line). Sequential receive data sequentially and analyze previously obtained data to detect the possible change in current time. This method is based on sequential analysis and focuses on change on mean and variance in time domain. Other methods generally suffer from:

- Inability / inefficiency in detecting variance decrease.
- Assumptions about the statistical distribution of the data, obtained as error of fitting the (AR) model.
- Necessity of training the model with possible changes.

A.1.2.3 Support vector based one-class classification

Although SVM was originally designed for two-class classification, it has been successfully applied to multi-class and one-class classification. SVM-based one-class classification gives the minimum volume closed spherical boundary around the data, represented by center c and radius r . It minimizes r^2 (representing structural error), and uses a penalty coefficient C for each outlier with distance ξ_i from the hyper-sphere boundary:

$$\begin{aligned} \text{Min } & r^2 + C \sum_i \xi_i \\ \text{Subject to : } & \|x_i - c\|^2 \leq r^2 + \xi_i \quad \xi_i \geq 0, \quad \forall i, x_i : i\text{th data point} \end{aligned} \tag{A.7}$$

This quadratic optimization problem can be transformed to its dual form by introduction Lagrange multipliers α_i . If, for a data point, the multiplier $\alpha_i = 0$, then that point is inside the sphere. When it is $0 < \alpha_i < C$, then it is on the boundary. Data points for which the multiplier is $\alpha_i = C$ are located outside the sphere (and are penalized). The dual form is:

$$\begin{aligned} \text{Max } & \sum_i \alpha_i (\mathbf{x}_i \cdot \mathbf{x}_i) - \sum_{i,j} \alpha_i \alpha_j (\mathbf{x}_i \cdot \mathbf{x}_j) \\ \text{Subject to : } & 0 \leq \alpha_i \leq C \quad \forall i, \quad \sum_i \alpha_i = 1 \end{aligned} \tag{A.8}$$

Note that only dot products of the data points \mathbf{x} appear. In order to transform the data points to a higher dimension, to create a good representational hyper-sphere, kernels replace the dot products without compromising computational complexity. The problem then becomes:

$$\text{Max } \sum_i \alpha_i K(\mathbf{x}_i, \mathbf{x}_i) - \sum_{i,j} \alpha_i \alpha_j K(\mathbf{x}_i, \mathbf{x}_j) \tag{A.9}$$

It has been shown that Gaussian kernels offer better performance for one-class classification the others. The optimization of the *scale parameter* has led to several implementations. As can be seen, there are no assumptions about the data distribution or independency made.

A.1.2.4 Problem formulation

[Not summarized here, useful for e.g. Section 2.2]

A.1.2.5 SVCPD: The algorithm

Instead of using statistical properties of the data, for each window of size w a hyper-sphere is constructed without increasing computational complexity due to the *kernel trick*. The window size is related to the sensitivity of the method to change; small windows are sensitive with high false alarm rate whilst large windows are slow to detect change and have low alarm rates. The algorithm is listed in table A.1. Note that SVCPD can be applied directly to multidimensional data, whilst many other methods can only be applied to one-dimensional data.

| Step | Action |
|------|---|
| 1 | Start with n observations and construct hyper-sphere |
| 2 | Add next observation x_t and drop first one |
| 3 | Identify new hyper-sphere and its <i>approximate radius</i> |
| 4 | if x_t is outside hyper-sphere, mark t as change points and continue from step 2 |
| 5 | calculate radius average of last w hyper-planes |
| 6 | calculate radius ratio \bar{h} . If lower than th_{low} or greater than th_{high} then mark t as change point |
| 7 | continue from step 2 |

TABLE A.1: Support Vector machine based Change Point Detection algorithm

A.2 CUSUM for variance

A.2.1 Use of Cumulative Sums of Squares for Retrospective Detection of Changes of Variance

Carla Inclan and George C. Tiao [41], 1944, 162 refs.

A.2.1.1 Introduction

This paper is about reflective detection of multiple changes of variance in a sequence of independent observations. This is a statistical method, which differs from others (in that field) such as Bayesian method (Bayes ratio, posterior odds), maximum likelihood methods and (autoregressive) models. This approach uses the centered version of cumulative sums of squares to search for change points systematically and iteratively (and reflective).

A.2.1.2 Centered Cumulative Sum of Squares

The cumulative sum of squares is often used for change detection in the mean. It is defined as $C_k = \sum_{i=1}^k \alpha_i^2$ for a series of uncorrelated random variables $\{\alpha_t\}$ with mean 0 and variance $\sigma_t^2, t = 1, 2, \dots, T$. The centered (and normalized) cumulative sum of squares is:

$$D_k = \frac{C_k}{C_T} - \frac{k}{T}, \quad k = 1, \dots, T, \quad \text{with } D_0 = D_T = 0 \quad (\text{A.10})$$

For homogeneous variance the plot of D_k against k (the first k elements of the series) will oscillate around 0. When a sudden change in variance occurs, the pattern of the plot of D_k will break out some specified boundaries with high probability. For C_k it holds that, under homogeneous variance, the plot will be a straight line with slope σ^2 .

With one or more change points the plot appears as a line of several straight pieces. The plot of D_k creates a peak for a smaller and a trough for a larger variance, is visually more clear and breaks out a predefined value. The search for a change point is variance is than to find $k^* = \max_k |D_k|$. If the value of D_k at k^* exceeds a predefined value (e.g. $D_{0.5}^* = 1.358$, for $\sqrt{T/2D_k}$ because of the Brownian bridge property), that value of k^* will be an estimate for a change point.

There is a relation between D_k and the F statistic, which is used for testing equality of variances between two independent samples. For a fixed k , $D_k(F)$ is a monotone function of F (it depends only on k through k/T). An important distinction: the F statistic is *used with known k* , whereas we are looking for $\max_k |D_k|$ to determine the location of the change point.

When we assume that $\{\alpha_t\}$ is normally distributed with mean 0 and variances σ_t^2 , then we can obtain the *likelihood ratio* for testing the hypothesis of one change against the hypothesis of no change in the variance. When maximizing the likelihood estimator for a location κ , we can find the log-likelihood ratio $LR_{0,1}$. Although $LR_{0,1}$ and $\max_k |D_k|$ are related, they are not the same. The latter puts more weight near the middle of the series is thus biased toward $T/2$.

The (expected) value of D_k given a change in variance differs in the context. If a smaller variance corresponds to the smaller portion of the series, then it will be harder to find the change point using D_k . There is a masking effect when there are multiple change points in the series; the order of small, medium and large variances result in the value of D_k . The iterative algorithm presented in this paper in Appendix A.2.1.3 is designed to lessen the masking effect.

A.2.1.3 Multiple changes: Iterated cumulative sums of squares

In case of a single change point the D_k method would succeed. But we are interested in multiple change points of variance, and thus the usefulness of the D_k reduces due to the masking effect. A solution is to iteratively applying the method and dividing the series at each possible change point. The algorithm is presented in table A.2. It is the third steps which reduces the masking effect and helps to “fine tune” the algorithm by (re)moving the potential change points by checking each location given the adjacent ones.

| Step | Action |
|------|--|
| 0 | Let $t_1 = 1$ |
| 1 | Calculate $D_k(\alpha[t_1 : T])$. Let $k^*(\alpha[t_1 : T])$ be the point at which $\max_k D_k(\alpha[t_1 : T]) $. Let D^* be the asymptotically critical value and M the max value in the series segment (?). If $M > D^*$ then consider k^* to be a change point. Else, there is no change point and the algorithm stops. |
| 2a | Repeat for the first part (up to the change point), until no more change points are found. |
| 2b | Repeat for the second part (from the change point forward), until no more change points are found. |
| 3 | When two or more change points are found; check for each $\alpha[j-1 : j+1]$ if there is indeed a change point (j). Repeat until the number of change points does not change and each new found change point is “close” enough to previous. |

TABLE A.2: Iterated Cumulative Sums of Squares Algorithm

A.2.1.4 Results

When the ICSS algorithm was applied to stock data, it resulted in comparable results as the maximum likelihood estimates and Bayesian analysis. The performance (CPU-time and correct observations with artificial data) of ICSS outperforms the other two. The heavy computational burden of posterior odds can be partially alleviated by the maximum log-likelihood method. The ICSS algorithm avoids calculating a function at all possible locations of change points due the iterative manner.

A.3 Density Ratio Estimation

A.3.1 Change-Point Detection in Time-Series Data by Direct Density-Ratio Estimation

Kawahara and Sugiyama [43], 2009, 45 refs.

“This paper provides a change-point detection algorithm based on direct density-ratio estimation that can be computed very efficiently in an online manner”.

A.3.1.1 Introduction

The problem of change-point detection is well studied over the last decades in the field of statistics. A common statistical formulation of change-point detection is to consider the probability distributions over past and present data intervals, and regard the target time

as a change-point if the two distributions are significantly different. Some approaches (such as CUSUM and GLR) make use of the *log-likelihood ratio*, and are extensively explored in the data mining community. Many approaches (novelty detection, maximum-likelihood ratio, learning of autoregressive models, subspace identification) rely on pre-specified parametric models (probability density models, autoregressive models, state-space models). That makes it less applicable to real-life problems. There have been some non-parametric density estimation approaches proposed, but that is known to be a hard problem. The key idea of this paper to directly estimate the *ratio* of the probability densities (also known as *importance*). The KLIEP is an example, but it is a batch algorithm. This paper introduces an online version of the KLIEP algorithm and develops a flexible and computationally efficient change-point detection method. This method is equipped with a natural cross validation procedure and thus the value of tuning parameters can be objectively determined.

A.3.1.2 Problem formulation and Basic Approach

Let $\mathbf{y}(t)(\in \mathbb{R}^d)$ be a d -dimensional time series sample at time t . The task is to detect whether there exists a change point between two consecutive time intervals, called the *reference* and *test* intervals. The conventional algorithms consider the likelihood ratio over samples from the two intervals. Since time-series samples generally are not independent over time it is hard to deal with them directly. To overcome this difficulty, we consider *sequences* of samples in the intervals: $\mathbf{Y}(t)(\in \mathbb{R}^{dk})$ is the forward subsequence of length k at time t . This is a common practice in subspace identification since it takes implicitly time correlation into consideration. The algorithm in the paper is based on the logarithm of the likelihood ration of the *sequence sample* \mathbf{Y} :

$$s(\mathbf{Y}) = \ln \frac{p_{\text{te}}(\mathbf{Y})}{p_{\text{rf}}(\mathbf{Y})} \quad (\text{A.11})$$

where $p_{\text{te}}(\mathbf{Y})$ and $p_{\text{rf}}(\mathbf{Y})$ are the probability density functions of the reference and test sequence samples. Let t_{rf} and t_{te} be the starting points of the reference and test intervals. Decide if there is a change-point between the reference and test interval by monitoring the logarithm of the likelihood ratio:

$$S = \sum_{i=1}^{n_{\text{te}}} \ln \frac{p_{\text{te}}(\mathbf{Y}_{\text{te}}(i))}{p_{\text{rf}}(\mathbf{Y}_{\text{te}}(i))} \quad (\text{A.12})$$

If, for a predefined $\mu > 0$, it holds that $S > \mu$ then a change occurs. The remaining question is how to calculate the density ratio, because it is unknown and we need to estimate it from examples. The naive approach would be to first estimate the densities for the reference and test interval separately and then take the ratio. This approach

via non-parametric density estimation may not be effective — directly estimating the density ratio without estimating the densities would be more promising.

The direct estimation of the density ratio is based on the Kullback-Leibler Importance Estimation Procedure. Let us model the density ratio $w(\mathbf{Y})$ by a non-parametric Gaussian kernel model:

$$\hat{w}(\mathbf{Y}) = \sum_{l=1}^{n_{\text{te}}} \alpha_l K_\sigma(\mathbf{Y}, \mathbf{Y}_{\text{te}}(l)), \quad (\text{A.13})$$

where $\{\alpha_l\}_{l=1}^{n_{\text{te}}}$ are parameters to be learned from the data samples and $K_\sigma(\mathbf{Y}, \mathbf{Y}')$ is the Gaussian kernel function with mean \mathbf{Y}' and standard deviation σ .

A.3.1.3 Online Algorithm

...

A.4 Outlier Detection methods

A.4.1 A Survey of Outlier Detection Methodologies

Hodge and Austin, [39], 2004, 734 refs.

A.4.2 Summary

This survey takes a look at different methodologies that perform outlier detection. It gives two definitions of outliers, one of which relates to the problem statement in this thesis (taken from [10]):

An observation (or subset of observations) which appears to be inconsistent with the remainder of that set of data.

The survey introduces three fundamental approaches to the problem of outlier detection:

Type 1 - no prior knowledge about the data; analogous to *unsupervised clustering*.

Flags the remote points as outliers; mainly batch-processing systems.

Type 2 - model (and requires) both normal and abnormal data; analogous to *supervised classification*. Is able to process new data online.

Type 3 - Model only normal data (and in very few cases abnormal). Generally referred to as *novelty detection*, analogous to *semi-supervised recognition or detection*. It only requires pre-classified normal data. It aims to define a boundary of normality.

The type of approaches of interest in this research is of **type 3**. It is characterized by the ability to recognize new data as normal when it lies within the constructed boundary and as a novelty otherwise. This ability removes the need of sample-abnormality data, which may be hard (or costly) to produce. The method of Tax *et al.* [71] is stated to be of **type 2**, and one can argue that other methods of Tax *et al.* [72, 75] are by their one-class classification instances of **type 3** methods.

The survey states that density-based methods estimate the density distribution of the training data. Outliers are identified as data points lying in a low-density region.

Appendix B

Session with Anne 24-06-2013 - Paper Camci analysis

Please ignore this Appendix. This appendix is for my own personal use. This chapter will look at the paper of Camci [15] (“Change point detection in time series using support vectors”) and will answer many question that the paper leaves open. The goal is to make a better justification for the used techniques and made assumptions.

B.1 Density estimation / Data description / Vapnik’s principle

Following Vapnik’s principle, one should “When solving a problem of interest, do not solve a more general problem as an intermediate step” [78] when a limited amount of data is available. For the problem of change detection we are only interested in some characteristics of the data. Solving the complete density estimation might require more data than actually needed when the requested characteristic is a closed boundary around the data.

In [51] it is stated that the SVM by Cortes and Vapnik [22] is a representative example of this principle. Instead of estimating the more general data generating probability distributions, it only learns a decision boundary to differentiate between the two distributions.

The proposed method SVDD of Tax and Duin [73, 75] models the boundary of data under consideration. Thereby it characterizes a data set and can be used to detect novel data or outliers. The performance is compared to methods which model the distribution’s density instead, using Receiver-Operating Characteristic (ROC) curves and false

negative rates. The compared methods are: (1) normal density which estimates the mean and covariance matrix; (2) the Parzen density where the width of the Parzen kernel is estimated; (3) a Gaussian Mixture Model optimized using EM; and (4) the Nearest-Neighbor Method which compares the local density of an object with the density of the nearest neighbor in the target set (and is thus, just as SVDD, a boundary-based method). The results show that when the problem formulation is to characterize an area in a feature space (and not the complete density distribution) SVDD gives a good data description.

The study of Tax on OCCs [72] further compares density methods, boundary methods (amongst which SVDD) and reconstruction methods. One promising result for SVDD is that it performs well on real-world data, for which generalization is needed.

The method of Camci [15] uses a Support Vector based method to find change points in the data. It does not explicitly create a density estimation, but instead relies on the spherical boundary and uses its ability to detect novel data or outliers to detect change points in time series data.

***** TODO: Thus methods of data descriptions should be compared (which are more general) and not only density estimation? *****

The paper of Yin *et al.* [85] makes a distinction between similarity based (using a defined distance measure) and model based (which characterize the data using predictive models) approach. The OC-SVM is used in the model-approach to filter out normal activities in order to detect abnormality behavior.

B.2 Change point definition

The method of Camci [15] regards a change point as the moment in time that the underlying stochastic process has changed, say from p^1 to p^2 . It assumes that each of these stochastic processes is modeled following a Gaussian distribution, such that a change can occur in the value of the mean and/or the variance; $p^1 \sim N(\mu_1, \sigma_1^2)$. The CUSUM-based method of [41] also regards each segment as a Gaussian distribution.

The method of Kawahara *et al.* [43] is based on the log likelihood ratio of test samples, and the method by Liu *et al.* [51] uses a comparable dissimilarity measure using the KLIEP algorithm.

The method of Chamroukhi *et al.* [17] is based on a Hidden Markov Model and logistic regression. It assumes a K -state hidden process with a (hidden) state sequence, each state providing the parameters (amongst which the order) for a polynomial. The order of

the model segment is determined by model selecting, often using the BIC or the similair AIC [3], as in [36].

***** TODO: REVIEW zoeken: change points in time series *****

Periodicity/consecutive data vs unique/irregular data?

Change in model parameters (mean/variance, of linear/non-linear)? – i Model selection?

Definition of continuity – i windows the domain and problem. Will result in definition of dis-continuity – i this is the goal to find Relation with double differentiation.

B.3 Data and model

Why assume (model of) data is Gaussian/normal distribution? Thus, piecewise linear with mean and variance as changing properties. Why not set of polynomial models, as for example in [17]?

What is the best model for accelerometer data of human activities? – i Look to result of model-selecting papers.

Should we build a model of the data? (Gaussian distribution is also the model). And be able to reconstruct?

Why is it better (as Camci states) that a method makes no assumptions about the form of data/distribution of data? Is it that there are less parameters to estimate?

Many methods describe and compare methods to construct classifier models for the classification of accelerometer data, such as [47] and [86] (often using extracted features from the raw data signal). In contrast, we could not find a clear characterization of accelerometer data obtained from human activities. When the problem of temporal segmentation is regarded in this context, a formalization of the data under consideration is needed. Some assume the data follows a piecewise linear set of segments with a mean and noise/variance modeled by a normal (Gaussian) distribution (such as [15]). Other approaches regard the data as a set of polynomials, which can be estimated by regression (such as [17]) and apply a form of model selection to each segment.

***** TODO: make a clear distinction between model types; similarity (distance based) or model based, as in [85] *****

B.4 Segmentation (SVM) method

Overview of segmentation methods. Collection of papers use relative and direct density-ratio estimation [43, 51].

Why use SVM for density estimation? Look for justification, perhaps a review paper which compares/mentions SVM for temporal segmentation of (human activity type of) data?

Why use RBF/Gaussian kernel? Is it because of OC-SVM or because of form the data?
Why not polynomial/linear?

- “Use RBF when relation between class and data is non-linear”
- “RBF uses less parameters (C for penalty/soft margin and gamma for kernel width) than non-linear polynomial kernels”
- (arguments from [86] “Optimal model selection for posture recognition in home-based healthcare”)
- Survey [39] states RBF is similar to Gaussian Mixture model (page 25).

***** TODO: read [57] and [12] on geometry of SVMs *****

Re-evaluation [32], uses (amongst others) a pca-based dimension-detection method (?).
Also uses model-selection as an intermediate step.

B.4.1 Higher dimension mapping (including kernel)

What does the mapping from the data-space to higher dimension looks like?

What is a RBF kernel?

What form has the higher dimensional space?

How do relations over data, such as distance, volume and noise, act in the higher dimensional space?

What is the kernel trick to not explicitly do the mapping to the higher space?

***** TODO: Note: in [57] it is explained why the inner-product between two vectors is a logical choice for the distance/similarity measure. *****

B.5 Relation to other methods

B.5.1 Novelty/outlier detection

**** TODO: Read [39] “A survey of outlier detection methodologies” to compare with other methodologies. ****

- One-class classification is referred to as “Type 3”, with *semi-supervised recognition or detection*.
- It explains why one-class can be beneficial over type-2 where negative examples needs to be provided.
- We are interested in type-3, so compare SVM with the others stated in this survey regarding type-3.
- Often refers to the convex hull of the data set. Link with geometric approach as in [12, 57]?
- It states that PCA and regression techniques are linear models and thus often are too simple for practical applications. SVMs try to find a hyperplane in higher dimensional space; linear models to implement complex class boundaries. It refers to [73].

B.5.2 Scale parameter

B.5.3 Robust statistics / ”M-Estimators”

Is the method robust, in the sense that outliers have restricted impact on the quality.

What is the relation to M-Estimators (Wikipedia: “M-estimators are a broad class of estimators, which are obtained as the minima of sums of functions of the data”, <http://en.wikipedia.org/wiki/M-estimator>)

B.6 Quality metrics

As used in Camci: benefit, false alarm rate

Asymmetric test: feed data from front-to-back and back-to-front; how far are matched datapoint apart.

Model reconstruction error: try to reconstruct the simulated models, test similarity (BIC?). Is that a good measure? (If we are only interested in finding change points...)

Appendix C

Summary of papers and principle formulas

C.1 Change point detection in time series data using support vectors, by Camci

Paper: [15]. The main concept of this paper is to construct a hypersphere around the data and thereby generating a boundary. A change point is detected when the radius of the hypersphere grows or shrinks significantly, or when a data point falls outside the boundary.

The main cost function being minimized:

$$\begin{aligned} & \underset{r}{\text{minimize}} \quad r^2 + C \sum_i \xi_i \|x\| \\ & \text{subject to} \quad \|x_i - c\|^2 \leq r^2 + \xi_i, \quad \xi_i \geq 0 \quad \forall i, x_i : i\text{th data point} \end{aligned} \tag{C.1}$$

Where r is the radius of a (hyper)circle with center c , C is the penalty coefficient for every outlier and ξ_i is the distance from the i th data point to hypersphere (also known as the slack variable).

The dual form by introducing the Lagrange multipliers ($\alpha_i, \alpha_i \geq 0$) and eliminating the slack variables ξ is:

$$\begin{aligned} & \underset{\alpha}{\text{maximize}} \quad \sum_i \alpha_i (x_i \cdot x_i) - \sum_{i,j} \alpha_i \alpha_j (x_i \cdot x_j) \\ & \text{subject to} \quad 0 \leq \alpha_i \leq C \quad \forall i, \quad \sum_i \alpha_i = 1 \end{aligned} \tag{C.2}$$

To allow for a non-linear relation between the data points and the data boundary, the inner product can be replaced by a (e.g. Gaussian) kernel function: $K(\mathbf{x}_i, \mathbf{x}_j)$.

C.2 Change-Point detection in time-series data by Direct Density-Ratio Estimation

Paper: [43].

The density ratio $w(\mathbf{Y})$ is modeled by a Gaussian kernel over sequences \mathbf{Y} of samples (sequence $\mathbf{Y}_{te}(l)$ is the test sequence from the l th position on):

$$\hat{w}(\mathbf{Y}) = \sum_{l=1}^{n_{te}} \alpha_l K_\sigma(\mathbf{Y}, \mathbf{Y}_{te}(l)), \quad (\text{C.3})$$

where $\{\alpha_l\}_{l=1}^{n_{te}}$ are parameters to be learned from the data samples and $K_\sigma(\mathbf{Y}, \mathbf{Y}')$ is the Gaussian kernel function with mean \mathbf{Y}' and standard deviation σ . The learned parameters minimize the Kullback-Leibler divergence from the sequence to the test sequence. The maximization problem then becomes:

$$\begin{aligned} & \underset{\{\alpha_l\}_{l=1}^{n_{te}}}{\text{maximize}} \quad \sum_{i=1}^{n_{te}} \log \left(\sum_{l=1}^{n_{te}} \alpha_l K_\sigma(\mathbf{Y}_{te}(i), \mathbf{Y}_{te}(l)) \right) \\ & \text{subject to} \quad \frac{1}{n_{rf}} \sum_{i=1}^{n_{rf}} \sum_{l=1}^{n_{te}} \alpha_l K_\sigma(\mathbf{Y}_{rf}(i), \mathbf{Y}_{te}(l)) = 1, \text{ and } \alpha_1, \dots, \alpha_{n_{te}} \geq 1 \end{aligned} \quad (\text{C.4})$$

With the estimated parameters the logarithm of the likelihood ratio between the test and reference interval can be calculated, which signals a change point if it is beyond a certain threshold μ :

$$S = \sum_{i=1}^{n_{te}} \ln \frac{p_{te}(\mathbf{Y}_{te}(i))}{p_{rf}(\mathbf{Y}_{te}(i))} \quad (\text{C.5})$$

C.3 Joint segmentation of multivariate time series with hidden process regression for human activity recognition, by Chamroukhi

Paper: [17]. This approach models the time series data by a parameterized regression, filtered with a HMM to smooth out high frequency activity transitions. With each observation i , generated by a K -state hidden process, an activity label z_i (and thus sequence) is associated. Observations follow a regression model:

$$y_i = \beta_{z_i}^T \mathbf{t}_i + \sigma_{z_i} \epsilon_i; \quad \epsilon_i \sim \mathcal{N}(0, 1), \quad (i = 1, \dots, n) \quad (\text{C.6})$$

The observations get a label assigned by maximizing the logistic probability (π_k):

$$\hat{z}_i = \underset{1 \leq k \leq K}{\operatorname{argmax}} \pi_k(t_i; \hat{\mathbf{w}}), \quad (i = 1, \dots, n) \quad (\text{C.7})$$

C.4 Support Vector Data Description, by Tax and Duin

Paper: [75]. The paper proposes the SVDD method, analogous to the SVC of Vapnik [78], based on the separating hyper-plane of Schölkopf *et al.* [65]. Where SVC is able to distinguish data between two classes, SVDD obtains a closed boundary around the target class and can detect outliers.

Method and formulas very similar to description in Appendix C.1.

C.5 Support Vector Density Estimation, by Weston et al.

Paper: [81]. Using the notation of [81], the distribution function of a density function $p(x)$ is represented as:

$$F(x) = P(X \leq x) = \int_{-\infty}^x p(t) dt \quad (\text{C.8})$$

To find the density the following linear equation need to be solved:

$$\int_{-\infty}^{\infty} \theta(x-t)p(t) dt = F(x) \quad (\text{C.9})$$

where

$$\theta(x) = \begin{cases} 1, & x > 0 \\ 0, & \text{otherwise} \end{cases}$$

In this problem the distribution function $F(x)$ is unknown and instead we are given the i.i.d. data x_1, \dots, x_l generated by F .

The empirical distribution function can now be constructed as:

$$F_l(x) = \frac{1}{l} \sum_{i=1}^l \theta(x - x_i) \quad (\text{C.10})$$

C.6 An online algorithm for segmenting time series, by Keogh et al.

Paper: [45]. This method approximates the signal with piecewise linear representation. Change points are encountered at the time at which a new segment is used to represent the signal. The method uses linear regression by taking the best fitting line in the least squares sense, since that minimizes the Euclidian distance which is used as a quality metric. Linear interpolation is considered but since that always has a greater sum of squares error it is disregarded.

Linear regression assumes a relation from n observations \mathbf{X} to the dependend variable \mathbf{y} using the parameter vector $\boldsymbol{\beta}$:

$$\mathbf{y} = \mathbf{X}\boldsymbol{\beta} + \epsilon \quad (\text{C.11})$$

The error function, the sum of squared residuals, being minimized by searching for the best estimation of $\boldsymbol{\beta}$ is:

$$b^* \in \underset{b}{\operatorname{argmin}} = \sum_{i=1}^n (y_i - x'_i b)^2 = (\mathbf{y} - \mathbf{X}b)^T (\mathbf{y} - \mathbf{X}b) \quad (\text{C.12})$$

C.7 Online novelty detection on temporal sequences, by Ma and Perkins

Paper: [53]. This method uses support vectors for regression (in contrast with classification). The regression function, using a kernel function $K(x_i, x_j)$ can be written as:

$$f(\mathbf{x}) = \sum_{i=1}^l \theta_i K(\mathbf{x}_i, \mathbf{x}) + b, \quad (\text{C.13})$$

where θ_i is a coefficient resulting from the Lagrange multipliers of the original minimization problem. A small fraction these of coefficients are non-zero, and the corresponding samples \mathbf{x}_i are the *support vectors*. The regression function $f(\mathbf{x})$ is non-linear when a non-linear kernel is chosen.

The regression function is used to created a model of past observations. A matching function is constructed which determines the matching value $V(t_0)$ of a new observations with the constructed model. This matching value is the residual of the regression function at t_0 .

The algorithm determines (*novel*) events, occurrences and surprises. *Novel events* are defined as a series of observations for which the confidence value over the number of surprises (out-of-model observations) is high enough. Events thus have a length; they are constructed of a sub-series of observations.

The papers presents an alternative implementation in order to handle fixed-resource environments and thus induce an online algorithm. After W observations have been observed and used for the trained model, the oldest observation is disregarded before the newly obtained observation is incorporated.

Note: the Support Vector approach in this paper is used to select the observations to use in the regression model. This differs from one-class applications of support vector machines. The same authors have also presented a paper which does use one-class construction using support vector machines: [54].

C.8 Time-series novelty detection using one-class support vector machines, by Ma and Perkins

Paper: [54] This approach is very similar to the other paper of this author discussed in the previous section [53]. The difference is that this method does create a SVM-classifier to detect in and out of class examples, whilst the other uses the support vectors to construct a regression function.

The method constructs a hyper-plane which separates as many as possible data points in the feature space with the largest margin from the origin. This is a different from (and more like the original SVM-proposal by Schölkopf [66]) the one-class methodology by Tax which creates a boundary around the data [75].

The hyper-plane in feature space is represented as:

$$f(\mathbf{x}) = \mathbf{W}^T \Phi(\mathbf{x}) - \rho, \quad (\text{C.14})$$

where $\Phi(\mathbf{x})$ maps a vector \mathbf{x} from the input space I to the (potentially infinite dimensional) feature space F . \mathbf{W} and ρ are determined by solving a quadratic optimization problem. The dual formulation (using Lagrange multipliers α_i) is:

$$\mathbf{W} = \sum_{i=1}^l \alpha_i \Phi(\mathbf{x}_i), \quad (\text{C.15})$$

where $0 \leq \alpha_i \leq \frac{1}{\nu l}$. The parameter $\nu \in (0, 1)$ is set to trade-off the smoothness of $f(\mathbf{x})$ and acts as an upper bound on the fraction of outliers over all the data examples in \mathbf{x} [66].

Using the *kernel trick* the inner product of two vectors in feature space F can be replaced by a kernel function K , which is often the RBF. The equation of the hyper-plane (C.14) then becomes the following (non-linear) function:

$$f(\mathbf{x}) = \sum_{i=1}^l \alpha_i K(\mathbf{x}_i, \mathbf{x}) - \rho \quad (\text{C.16})$$

The form of the input vector \mathbf{x} is considered to be the (*projected*) *phase space* representation of the original time series. Just like [44] which constructs *sequences* of samples and in contrast with [15], each element of \mathbf{x} is a vector with the size of the *embedding dimension* E of the time series. Thus, a time series $x(t)$ is converted to a set of vectors $T_E(N)$:

$$T_E(N) = \{\mathbf{x}_E(t), t = E \cdots N\}, \quad (\text{C.17})$$

where

$$\mathbf{x}_E(t) = [x(t-E+1) \ x(t-E+2) \ \cdots \ x(t)] \quad (\text{C.18})$$

If a point of this vector $\mathbf{x}_E(t)$ is regarded (in the feature space F) as an outlier, all corresponding values in the original time series are also regarded as such.

C.9 Least squares one-class support vector machine, by Choi

Paper: [21]. The proposed method uses a SVM for a similarity/distance comparison for testing examples to training examples. Instead of other methods, such as the standard one-class SVM by Schölkopf [66] or the SVDD of Tax and Duin [75], it does not create a boundary for the training data. Instead it uses a least-squared approach to construct a hyperplane to which most of the training examples lie close to.

The objective function to be minimized of the standard one-class method by Schölkopf is formulated as:

$$\begin{aligned} & \underset{\mathbf{w}}{\text{minimize}} \quad \frac{1}{2} \|\mathbf{w}\|^2 - \rho + C \sum_j \xi_j \\ & \text{subject to} \quad \mathbf{w} \cdot \phi(\mathbf{x}_j) \geq \rho - \xi_j \quad \text{and} \quad \xi_j \geq 0 \end{aligned} \quad (\text{C.19})$$

where ϕ is a mapping to the feature space.

The least-squares one-class support vector machine has a small variation on the above formula, which results in the following minimization problem:

$$\begin{aligned} & \underset{\mathbf{w}}{\text{minimize}} \quad \frac{1}{2} \|\mathbf{w}\|^2 - \rho + \frac{1}{2} C \sum_j \xi_j^2 \\ & \text{subject to} \quad \mathbf{w} \cdot \phi(\mathbf{x}_j) = \rho - \xi_j \end{aligned} \quad (\text{C.20})$$

The slack variable (for which in the original formulation $\xi_j \geq 0$ should hold) now represents an error caused by a training example \mathbf{x}_j with relation to the hyperplane, i.e. $\xi_j = \rho - \mathbf{w} \cdot \phi(\mathbf{x}_j)$.

In other words, the minimization problem (C.20)) results in a hyperplane with maximal distance from the origin and for which the sum of the squares of errors ξ_j^2 are minimized.

Appendix D

Planning

| Chapter | Title | Extra | Deadline |
|---------|--|---|------------|
| 1 | Introduction, abstract | Write at last | 15/10/2013 |
| 2 | Literature review | Partially writting. Maybe focus more on SVM and quick look at other segmentation techniques | 15/9/2013 |
| 3 | (Change detection By) One-Class Support Vector Machines | Mix of current chapter and blog post | 1/10/2013 |
| 4 | Proposed method | Propose new method, or just setup of testing the OC-SVMs with accelerometer data | Date |
| 5 | Results | Test with known and public databases of accelerometer data. For this, two implementations (in Matlab?) are needed | 15/8/2013 |
| 6 | Real-world applications | Test with own labeled accelerometer data | 1/9/2013 |
| 7 | Conclusion | Write last, together with introduction | 15/10/2013 |

Appendix E

Data structure quotes

[60], “Predicting Time Series with Support Vector Machines”, p.6.

“Our experiments show that SVR methods work particularly well if the data is sparse (i.e. we have little data in a high dimensional space). This is due to their good inherent regularization properties.”

[58], “Support vector machines in remote sensing: A review”, p.10.

“Most of the findings show that there is empirical evidence to support the theoretical formulation and motivation behind SVMs. The most important characteristic is SVMs ability to generalize well from a limited amount and/or quality of training data. Compared to alternative methods such as backpropagation neural networks, SVMs can yield comparable accuracy using a much smaller training sample size. This is in line with the “support vector” concept that relies only on a few data points to define the classifier’s hyperplane. This property has been exploited and has proved to be very useful in many of the applications we have seen thus far, mainly because acquisition of ground truth for remote sensing data is generally an expensive process.”

(And more)

[16], “Kernel-based framework for multitemporal and multisource remote sensing data classification and change detection”, p.30.

“As core learners, the binary SVC and the one-class SVDD classifier were used, and they were also benchmarked with neural networks in real scenarios. In general, neural networks show inferior results compared to non-linear kernel classifiers, which is a direct consequence of their difficulties when working with very high dimensional input samples particularly important when stacking together other information sources such as contextual or multi-temporal”

Appendix F

Afronden

- Typo's checken en fixen
- Chapter 2: Literature review
 - Prima hoeveelheid, niet meer veel bij doen
 - TODO's: alleen aan elkaar lijmen, geen nieuwe info of details
 - Onderwerpen schrappen: "statistical model/background": mag korter en kleiner
 - Indeling finalizen. Is niet zo belangrijk.
- Chapter 3: inhoud is prima
 - fig 3.4: laten staan. Relateren aan andere figuur, zelfde symbolen gebruiken
 - TODO: alleen aan elkaar lijmen, geen nieuwe inhoud. Eventueel kort refereren naar bron voor meer duiding (parameters C etc)
 - 3.5 en 3.6: overslaan, komt in 5 en 6.
- Chapter 4:
 - In begin aangeven wat mijn contributie is: * continue data met changes erin (gelabeled), en * toepassen van oc-svm op HAR data.
 - Aangeven wat contributie in "proposed method" is: aangeven wat hetzelfde en verschilt van Camci/Takeuchi. O.a.: toepassing op real-world data.
 - Aangeven geen aparte "membership" check zoals Camci doet –*i* argumenteer robustheid (outliers e.d.).
 - Naam van hoofdstuk: "Application to real-world HAR data" o.i.d. (past beter met pre-post processing sections). Meer focus op hele systeem, niet de algoritmes.

- Naam bedenken voor toepassing, om makkelijk te kunnen refereren.
- Chapter 6:
 - Foto's van recordings (veel) kleiner en minder. Alleen om setting te duiden.
 - Een enkele plot van hele run. Verder kleine stukjes uit plots om interessante stukken te duiden (overgang lopen/rennen).
 - Stukjes van plots gebruiken om verschillen te duiden.
 - Echte resultaten in (box)plots en tabellen zetten. "Benefit" en FAR.
 - Performance: vooral aangeven dat het nieuwe (subjectieve) data is. Voor echte vergelijkingen wijzen naar 5.
 - Bijzondere mis-detecties (of extra detecties) aan het einde duiden ("remarks").
 - Overall: het moet wat "cleaner"
- Chapter 7: prima, aanvullen op de open plekken

Tussendoor:

- Verantwoording SVM: generieke methode die op veel types data is gebruikt. "Hypothesese" van onderzoek is: OC-SVM werkt op HAR data. Terug laten komen in 1 introduction en 7 conclusie.

F.0.1 Prioriteiten

1. Hoofdstuk 1, introduction
2. Abstract
 - Vraagstelling
 - Antwoord
 - Aanleiding tot onderzoek
 - Samenvatting van onderzoek
 - Wat gedaan is: Praktische toepassen en uitwerking OC-SVM
 - Wat bijzonder is: applicatie in domein
3. Lijstje hierboven afwerken
4. TODO's eruit filteren
5. Resultaten chapter 6
6. Conclusie afmaken

F.0.2 Planning

- Deadline: 10 januari, geprint op bureau Anne. Final versie geen todo's meer.

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