

Physics Formula Sheet

402-0023-01L Physics

2023/ 2024

Constants

Constant	Symbol	Value
Speed of light	c	3.00×10^8 m/s
Gravitational constant	G	6.674×10^{-11} N(m/kg) ²
Planck's constant	h	6.626×10^{-34} J.s
Mass of the electron	m_e	9.10939×10^{-31} kg
Mass of the proton	m_p	1.67262×10^{-27} kg
Charge of the electron	$-e$	-1.60218×10^{-19} C
Permittivity of free space	ϵ_0	8.85419×10^{-12} C ² /J m
Permeability of free space	μ_0	$4\pi \times 10^{-7}$ T m / A
Boltzmann constant	k_B	1.38066×10^{-23} J/ K
Avogadro's constant	N_A	6.022×10^{23} 1/mol

Oscillations

- **Natural Frequency:** $\sqrt{\frac{k}{m}}$
- **Damping Ratio (ζ):**

$$\zeta = \frac{b}{b_c}$$

where $b_c = 2\sqrt{mk}$

Quality Factor (Q factor)

The Q factor is a dimensionless parameter that describes the damping of an oscillator. It represents the energy stored to energy dissipated ratio.

$$Q = \frac{1}{2\zeta} = \frac{\omega_0}{\Delta\omega} = 2\pi f \times \frac{\text{energy stored}}{\text{power loss}}$$

where $\Delta\omega$ is the bandwidth over which the energy is stored.

Types of Oscillations

- **Critically Damped** ($\zeta = 1$): The system returns to equilibrium as quickly as possible without oscillating.
- **Overdamped** ($\zeta > 1$): The system returns to equilibrium without oscillating but slower than the critically damped case.
- **Underdamped** ($\zeta < 1$): The system oscillates about the equilibrium position with a frequency ω_d given by:

$$\omega_d = \omega_0 \sqrt{1 - \zeta^2}$$

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1st law: For any process concerning a given system, the change in internal energy ΔU of that system is equal to the sum of the heat Q transferred to that system and the work W performed on that system.

2nd law:

- **Carnot:** Wherever there exists a difference in temperature, motive power can be produced.
- **Kelvin:** It is impossible for a self-acting machine to convey heat from a colder body to a hotter one.
- **Clausius:** Heat cannot flow from a colder to a hotter body without another process occurring, connected therewith, simultaneously.

$$T = \left(\frac{\partial U}{\partial S} \right)_{V,N}$$

Energy per mode: $\langle E_{\text{mode}} \rangle = \frac{3}{2} k_B T$

$$Q = C\Delta T, \quad Q = \int_{T_1}^{T_2} C(T) dT$$

$$L = \frac{Q_{\text{latent}}}{m}, \quad \gamma = \frac{C_P}{C_V}, \quad dS = \frac{\delta Q_{\text{rev}}}{T}$$

Electrostatics and dynamics

$$\mathbf{F} = \sum_{i=1}^N \frac{q_0 q_i (\mathbf{r} - \mathbf{r}_i)}{4\pi\epsilon_0 |\mathbf{r} - \mathbf{r}_i|^3}$$

Torque: $\tau = \mathbf{p} \times \mathbf{E}$

Energy of a dipole: $U(\theta) = -\mathbf{p} \cdot \mathbf{E}$

Gauss' law: $\phi = \oint_{\mathcal{S}} \mathbf{E} \cdot d\mathbf{A}$

Potential: $\Delta V \equiv \frac{\Delta U}{q} = -\int_C \mathbf{E} \cdot d\mathbf{l}$

Energy of a capacitor: $U = \frac{q^2}{2C}$

Current: $I = \dot{Q}$

Potential: $V_b - V_a = -\int_a^b \mathbf{E} \cdot d\mathbf{l}$

Kirchhoff's rules: 1. $\sum_{j,\text{loop}} \Delta V_j = 0$ 2. $\sum_j I_{j,\text{into node}} = 0$

Magnetic force: $\mathbf{F} = q\mathbf{v} \times \mathbf{B}$

Cyclotron radius: $r = \frac{mv}{qB}$

Biot-Savart: $\mathbf{B} = \frac{\mu_0}{4\pi} \frac{q\mathbf{v} \times \mathbf{r}}{r^3}$

Faraday's Law: $\mathcal{E} = -\frac{d\phi_m}{dt}$

Self-inductance of a solenoid: $L = \mu_0 n^2 Al$

Mutual inductance: $\frac{\phi_{m1}}{N_1} = \frac{\phi_{m2}}{N_2}$

Impedance: $Z_R = R$, $Z_C = \frac{1}{i\omega C}$, $Z_L = i\omega L$












General Solution

For a driven damped harmonic oscillator, the general solution can be expressed as:

$$x(t) = e^{-\zeta\omega_0 t} (A \cos(\omega_d t) + B \sin(\omega_d t))$$

where A and B are constants determined by initial conditions.

Moments of Inertia

Object	Axis	Moment of Inertia (I)	
Thin cylindrical shell	Diameter through centre	$\frac{1}{2}mr^2 + \frac{1}{12}ml^2$	
Thin cylindrical shell	Axis	mr^2	
Thin rod	End	$\frac{1}{2}ml^2$	
Thin rod	Centre	$\frac{1}{12}ml^2$	
Spherical shell	Centre	$\frac{2}{3}mr^2$	
Solid sphere	Centre	$\frac{2}{5}mr^2$	
Solid cylinder	Axis	$\frac{1}{2}mr^2$	
Solid cylinder	Diameter through the centre	$\frac{1}{4}mr^2 + \frac{1}{12}ml^2$	
Hollow cylinder	Axis	$\frac{1}{2}m(r_1^2 + r_2^2)$	
Hollow cylinder	Diameter through centre	$\frac{1}{4}m(r_1^2 + r_2^2) + \frac{1}{12}ml^2$	
Rectangular parallelepiped	Through centre, perpendicular to sides	$\frac{1}{12}m(h^2 + w^2)$	

Thermodynamics

0th law: If two objects are in thermal equilibrium with a third object, then all three objects are in thermal equilibrium with each other.

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Waves

$$\oint_S \mathbf{E} \cdot d\mathbf{A} = \frac{Q_{\text{enc}}}{\epsilon_0} \quad \text{(Gauss's Law for Electricity)} \quad (1)$$

$$\oint_S \mathbf{B} \cdot d\mathbf{A} = 0 \quad \text{(Gauss's Law for Magnetism)} \quad (2)$$

$$\oint_C \mathbf{E} \cdot d\mathbf{l} = -\frac{d\Phi_B}{dt} \quad \text{(Faraday's Law)} \quad (3)$$

$$\oint_C \mathbf{B} \cdot d\mathbf{l} = \mu_0 I_{\text{enc}} + \mu_0 \epsilon_0 \frac{d\Phi_E}{dt} \quad \text{(Ampère's Law with Maxwell's addition)} \quad (4)$$

In electromagnetic waves, the ratio $B_0 = \frac{E_0}{c}$ holds.

Wavenumber: $\omega = vk$

Compton wavelength: $\lambda_c = \frac{h}{m_e c}$

De Broglie wavelength: $\lambda_{\text{dB}} = \frac{h}{p}$

Heisenberg uncertainty relation: $\Delta x \Delta p \geq \frac{h}{4\pi}$

Energy of a particle in a 1D box: $E_n = \frac{h^2 n^2}{8L^2 m}$

Quantum Mechanics

$$\text{Time-dependent Schrodinger's Equation : } i\hbar \frac{\partial}{\partial t} \Psi(\mathbf{r}, t) = \left[-\frac{\hbar^2}{2m} \left(\frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} + \frac{\partial^2}{\partial z^2} \right) + V(x) \right]$$

Special relativity

Postulates of relativity and inertial reference frames:

- 1: Absolute uniform motion cannot be detected.
- 2: The speed of light in a vacuum is independent of the motion of the source.

Doppler Shift

Non-relativistic Doppler Shift:

$$f' = f \left(\frac{c \pm v_{\text{observer}}}{c \pm v_{\text{source}}} \right) \quad \text{(for sound or slow-moving sources)} \quad (5)$$

Relativistic Doppler Shift:

$$f' = f \sqrt{\frac{1 + \beta}{1 - \beta}} \quad \text{(for motion towards the observer)} \quad (6)$$

$$f' = f \sqrt{\frac{1 - \beta}{1 + \beta}} \quad \text{(for motion away from the observer)} \quad (7)$$

where $\beta = \frac{v_{\text{source}}}{c}$.

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Velocity Transformations in Special Relativity

For two observers in relative motion with velocity v along the x-axis:

u'_x = (u_x + v) / (1 + (vu_x/c^2))

u'_y = (u_y / gamma(1 + (vu_x/c^2)))

u'_z = (u_z / gamma(1 + (vu_x/c^2)))

where gamma = 1/sqrt(1-v^2/c^2) is the Lorentz factor.

Energy

E_total = gamma mc^2 = sqrt(p^2 c^2 + m^2 c^4), E_rest = mc^2

Mathematical equations

Trigonometric functions:

int sin^n ax dx = -1/a cos ax 2F1[1/2, 1-n, 3/2, cos^2 ax]
int sin^2 ax dx = x/2 - 1/4a sin 2ax + C

int x sin^2 ax dx = x^2/4 - x/4a sin 2ax - 1/8a^2 cos 2ax + C

int x^2 sin^2 xax dx = x^3/6 - (x^2/4a - 1/8a^3) sin 2ax - x/4a^2 cos 2ax + C

int tan ax dx = -1/a ln |cos ax| + C = 1/a ln |sec ax| + C

int cos ax / x dx = ln |ax| + sum_1^inf (-1)^k (ax)^(2k) / (2k(2k)!) + C

int cos^2 ax dx = x/2 + 1/4a sin 2ax + C

int sin^3 ax dx = cos 3ax / 12a - 3 cos ax / 4a + C

int tan^2 x dx = tan x - x + C

int sin ax cos ax dx = -cos^2 ax / 2a + C

int x cos ax dx = cos ax / a^2 + x sin ax / a + C

int cos ax dx = 1/a sin ax + C

int x sin ax dx = sin ax / a^2 - x cos ax / a + C

int (sin ax)(cos^n ax) dx = -1/(a(n+1)) cos^(n+1) ax + C

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Exponential functions:

int from -inf to inf e^-ax^2 dx = sqrt(pi/a) (a > 0)

int from -inf to inf xe^-ax^2+bx dx = sqrt(pi b) e^(b^2/a) (Re(a) > 0)

int from -inf to inf x^n e^-ax dx = { Gamma(n+1)/a^(n+1) (n > -1, a > 0)
n! / a^(n+1) (n = 0, 1, 2, ..., a > 0)

int from -inf to inf x^2 e^-ax^2 dx = 1/2 sqrt(pi/a^3) (a > 0)

int xe^cx dx = (x/c - 1/c^2) e^cx

int x^2 e^cx dx = (x^2/c - 2x/c^2 + 2/c^3) e^cx

int x^k e^-ax^2 dx = sqrt(pi/a) 3/4a^2

Spherical coordinates

x = r sin theta cos phi
y = r sin theta sin phi
z = r cos phi

Volume fraction:

dV = r^2 sin theta dr dtheta dphi

Solid angle:

dOmega = dSr / r^2 = sin theta dtheta dphi

Surface element:

dSr = r^2 sin theta dtheta dphi

nabla f = df/dr + 1/r * 1/sin theta * df/dphi

div F = nabla . F = 1/r^2 * d/dr (r^2 Fr) + 1/r sin theta * d/dtheta (sin theta F_theta) + 1/r sin theta * d/dphi (F_phi)

nabla x F = 1/r sin theta * (d/dtheta (A_phi sin theta) - dA_theta/dphi) r_hat + 1/r * (1/sin theta * dA_z/dphi - d(rA_phi)/dr) theta_hat + 1/r * d/dr (rA_phi) - dA_r/dtheta phi_hat

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nabla^2 f = 1/r^2 * d/dr (r^2 df/dr) + 1/r^2 sin theta * d/dtheta (sin theta df/dtheta) + 1/r^2 sin^2 theta * d^2 f / dphi^2 = (d^2/dr^2 + 2/r * d/dr) f + 1/r^2 sin theta * d/dtheta (sin theta df/dtheta) f + 1/r^2 sin^2 theta * d^2 f / dphi^2

Inner product and expectation

Expectation value (discrete)

<f_i> = sum_i P_i f_i

Expectation value (continuous)

<f(x)> = int from -inf to inf f(x) P(x) dx

<O> = int psi*(r) O psi(r) d^3r

Inner product

<psi|phi> = int psi*(x) phi(x) dx

Variance

sigma_f^2 = <f^2> - <f>^2

Periodic Table of Elements

1 IA																	
1 1.0079																	
1 H																	
2 IIA																	
2 6.044 4 0.032																	
2 Li Be																	
2 3.097 4 0.0075																	
2 Na Mg																	
3 22.990 23 24.305																	
3 Sc Ti V Cr Mn Fe Co Ni Cu Zn Ga Ge As Se Br Kr																	
3 40.078 44.956 47.88 50.94 54.938 58.933 63.546 68.94 72.64 78.96 83.80 88.91 95.94 101.07 118.71 132.91 158.93 178.48 197.04																	
3 3 IIA 4 IVB 5 VB 6 VIB 7 VIIB 8 VIIIB 9 VIIIB 10 VIIIB 11 IB 12 IIB																	
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