Coordinate Systems and Transforms in Space Physics: Terms, Definitions, Implementations, and Recommendations for Reproducibility

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Key Points:

- Reproducing coordinate system transforms is difficult due to inconsistencies in definitions and implementations in software.
- Ephemerides from different providers can differ significantly, as do Z-axis orientations from surveyed software libraries.
- We present recommendations to improve the precision and reproducibility of these calculations and reduce effort duplication by missions.

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Abstract

In space physics, acronyms for coordinate systems (e.g., `GEI`, `GSM`) are commonly used; however, differences in their definitions and implementations can prevent reproducibility. In this work, we compare definitions in online resources, software packages, and frequently cited journal articles and show that implementation differences can lead to transformations between same-named coordinate systems and ephemerides values from different data providers to differ significantly. Based on these comparisons and results, and to enable reproducibility, we recommend that (a) a standard for acronyms and definitions for coordinate systems is developed; (b) a standards body develops a citable database of reference data needed for these transforms; (c) a central authority maintains the SPICE (Spacecraft, Planet, Instrument, C-matrix, Events) kernels used by space physics spacecraft missions to generate data products in different coordinate systems; and (d) software developers provide explicit comparisons of their implementations with the results of (b) and documentation on implementation choices. Additionally, we provide recommendations for scientists and metadata developers to ensure that sufficient information is provided to enable reproducibility if these recommendations are not implemented.

1 Introduction

In space physics, journal articles, software, and online resources, the definition of a coordinate system is typically given by citing a reference that describes it. This work stems from a project to develop a standard for terms and descriptions for coordinate system acronyms such as `GEI`, `GSE`, `GSM`, and their commonly used variations, e.g., `GEI_J2000`, `GEI_MOD`; see Appendix A for definitions and Russell (1971), Hapgood (1992), Fränz and Harper (2002), and Laundal and Richmond (2016) for additional details. The objective is that, given a statement such as "the vector measurements in `ABC` were transformed into `XYZ`," a scientist with measurements in `ABC` would be able to reproduce the transformation with the only uncertainty being due to rounding errors associated with floating point precision.

As documented in this work, comparing data transformed with different software is complicated by the fact that transform implementations are not unique, introducing unknown uncertainty. In the early era of space physics, uncertainty due to implementation differences was much smaller than measurement uncertainty. Here, we argue that, in some applications, these differences matter and that implementation uncertainty poses an unnecessary impediment to reproducibility and intercomparison of data. In addition, as a matter of scientific practice, terms and definitions should be precise.

Our background research revealed additional issues that must be addressed to meet the objective of reproducibility in the sense defined above. First, implementing a given coordinate system given a general description requires making implementation choices. Therefore, terms and definitions for reference implementations are also needed. In sections 2, we note that in astronomy and the earth sciences, this has been recognized and addressed, and we describe their terminology and conventions.

Second, the standard for terms and descriptions must address their existing ambiguity. Examples of ambiguity are given for the `GEI` coordinate system in section 3. The general conclusion is that in space physics, there is no agreed-upon standard for coordinate system acronyms, and descriptions generally lack key implementation details.

To quantify the impact of ambiguity in definitions and implementations, we give examples that demonstrate the reported ephemerides for spacecraft in the same-named reference systems can significantly differ depending on the data source in section 4.1. In section 4.2 we demonstrate that software that transforms a vector between two coordinate systems exhibits smaller, but possibly significant, differences.

Having summarized the problems arising from ambiguity in definitions and implementations, we next consider how spacecraft missions compute transforms. To meet the objective of reproducibility, we must understand how calculations are performed in practice and account for this in our recommendations. In section 5, we describe how missions develop data products in different coordinate systems, which may explain the differences observed in the ephemeris results in section 4.1.

In section 6, we provide a set of recommendations that address definition issues described in section 3, the results in section 4, and the description in section 5. These recommendations address ambiguity in terminology and definitions, how software for transforms is created and tested, and how missions compute transformed data products.

2 Coordinate Systems, Reference Systems, and Reference Frames

Thus far, we have used the term "coordinate system" consistent with common usage in space physics as described in section 2.1. In section 2.2, we note that "ideal reference system", "reference system", or "reference frame" is more consistent with literature outside of space physics and will use these terms in the remainder of this article.

2.1 Coordinate Systems

In geometry, introductory physics, and mathematics textbooks, coordinate values in a "coordinate system" uniquely identify spatial positions relative to an *arbitrary* set of three orthogonal vectors and an origin. Common coordinate systems are Cartesian, cylindrical, and spherical. In the space physics literature, a coordinate system is generally meant as a *specific* set of three orthogonal vectors and an origin, with coordinate values expressed in a coordinate system such as Cartesian, cylindrical, or spherical.

This usage, which "coordinate system" has two meanings, dates back to at least early documentation of the NASA shuttle program (Davis, 1974) and has been consistently used in frequently cited literature related to space physics reference frames (Russell (1971); Hapgood (1992); Hapgood (1995); Laundal and Richmond (2016)). (However, an earlier work involving analysis of data from the OGO (Orbiting Geophysical Observatory; NASA (1970)) satellite used only "system" for the central noun, e.g., `GCI` system, instead of `GCI` coordinate system.)

2.2 Reference Systems and Frames

In astronomy, the terms "reference system" and "reference frame" are used; from US Naval Observatory (2025):

"A reference system is the complete specification of how a celestial coordinate system is to be formed. It defines the origin and fundamental planes (or axes) of the coordinate system. It also specifies all of the constants, models, and algorithms used to transform between observable quantities and reference data that conform to the system. A reference frame consists of a set of identifiable fiducial points on the sky (specific astronomical objects), along with their coordinates, that serves as the practical realization of a reference system."

The terms "reference system" and "reference frame" are also used in the same sense in terrestrial geodesy (Seitz et al., 2014).

A fundamental reference system in astronomy is the International Celestial Reference System (ICRS) (Petit & Luzum, 2010). No unique reference frame is associated with this reference system because creating (or, equivalently, "realizing" or "implementing") one requires measurements for computing reference system model parameters. The International Celestial Reference Frame (ICRF) is the general name for realizations of

the ICRS that are agreed upon by a standards body and are updated as new measurements and model versions become available. There are three versions of the ICRF (Charlot et al., 2020).

Kovalevsky and Mueller (1981) and Mueller (1985) use the term "ideal reference system" to refer to reference frames with definitions that are incomplete in the sense that only fundamental planes, axes, and an origin are specified: "The term 'ideal' indicates the conceptual definition only and that no means are proposed to actually construct the system". Note that the term "ideal" in this quote should be interpreted not as meaning "preferred" but rather means ideal in the sense of "idealized model", or a model that has practical or important attributes omitted to simplify its description.

Thus, what space physicists call a "coordinate system" (e.g., GEI, GSM) is analogous to an "ideal reference system" because it only has a general definition for their axes orientation and origin. There are no standards for the constants, models, or algorithms required to transform between observable quantities, which are necessary to define a reference system, nor for the model parameters needed to define a reference frame. For example, the GSE reference frame requires a vector from the center of Earth to the center of the Sun — Russell (1971) gives a Fortran program provided through private communication; Hapgood (1992) uses equations from Doggett et al. (1990); and Fränz and Harper (2002) uses equations from Seidelmann et al. (1992). All three cases can be regarded as unique GSE reference frames for the GSE reference system.

Terminology related to reference systems and frames also varies in other fields. For example, SPICE (Spacecraft, Planet, Instrument, C-matrix, Events; NAIF (2023)) states "a reference frame (or simply 'frame') is specified by an ordered set of three mutually orthogonal, possibly time-dependent, unit-length direction vectors; this definition does not include an origin. In robotics, the term "coordinate frame" refers to a set of three orthogonal axes and an origin relative to a different coordinate frame (Murray et al., 1994).

3 Examples of Definition Ambiguity

In the previous section, examples were given of general issues with the terminology used to describe reference systems and frames. For specific reference systems or frames in space physics, there are additional ambiguities.

For example, we GEI. The GEI ideal reference frame has $\mathbf{Z}$ aligned with Earth's rotation axis with positive northward, $\mathbf{X}$ as the intersection of Earth's equatorial plane with the plane of Earth's orbit around the Sun (the ecliptic plane), with positive in the direction from the Earth to the Sun at the time of the vernal equinox, and $\mathbf{Y} = \mathbf{Z} \times \mathbf{X}$. The line of intersection of Earth's equatorial plane with the ecliptic, or the time that it is computed, is sometimes referred to as "the equinox," and whether a line or time is meant must be determined from context.

First, there is no consistency in the expansion of the acronym GEI. Russell (1971) and Hapgood (1992) associate GEI with "Geocentric Equatorial Inertial System". Fränz and Harper (2002) and Mumford et al. (2025) associate GEI with "Geocentric Earth Equatorial". Another ambiguity is in GCI; Satellite Situation Center System and Services (2025c) notes "Geocentric Inertial (GCI) and Earth-Centered Inertial (ECI) are the same as GEI.", which implicitly defines GCI as "Geocentric Inertial", in contrast to Russell (1971) and NASA (1970), which use "Geocentric Celestial Inertial".

When reporting positions for GEI, the origin is taken as the center of mass of Earth. To establish this as a reference system as defined in section 2.2, Earth's rotation axis, center, and the ecliptic plane must be specified, along with the models used to compute them. To define a GEI reference frame, the model parameters must be specified.

156   Common variations of `GEI` depend on whether precession and nutation of Earth's
157 rotation axis and precession of the ecliptic plane are accounted for (Davis (1974); Hapgood
158 (1995); Fränz and Harper (2002)). The term "mean epoch–of–date" (or mean–of–date)
159 is used when only precession is accounted for, that is, the nutation variation is estimated
160 and removed. If nutation variation is not removed, the term "true epoch–of–date" or "true–
161 of–date" is used (Hapgood, 1995). If the **X** and **Z** orientations are time independent, an
162 abbreviation for a reference date and time is specified, e.g., J2000.0 (2000-01-01T12:00
163 Terrestrial Time), at which they were determined. The reference date and time is referred
164 to as an "epoch" in the sense of a reference time instant rather than a period of time.

165   Two basic categories of `GEI`-related reference frames and systems are commonly
166 used: inertial and non-inertial. The following acronyms are associated with an inertial
167 reference system: an idealized system that is not rotating with respect to the distant stars,
168 i.e., stars at an effectively infinite distance from its origin, and with an origin that trans-
169 lates with a constant velocity (NAIF, 2023). Note that if the origin is specified as Earth's
170 center (usually its center of mass rather than its centroid is implied but not stated), `GEI`
171 is non-inertial by definition. However, in the following summary of `GEI`–related reference
172 systems and frames below, we have ignored this technicality.

173   The objective of the following summary is to demonstrate the diversity in the terms
174 and definitions used for `GEI`–related reference systems and to motivate the need for the
175 standard recommended in section 6.1. Similar diversity also exists in terminology and
176 definitions in other commonly used reference systems in space physics, further motivat-
177 ing.

178   • `J2000` – Used by Satellite Situation Center System and Services (2025c) to refer
179   to a frame with its origin at Earth's center of mass and by SPICE to refer to a
180   system with origin at the solar system barycenter (Acton (1997); NAIF (2025)).

181   Satellite Situation Center System and Services (2025c) provides the definition:

182   "Geocentric Equatorial Inertial for epoch J2000.0 (`GEI2000`), also known as Mean
183   Equator and Mean Equinox of `J2000.0` (Julian date 2451545.0 TT (Terrestrial
184   Time), or 2000 January 1 noon TT, or 2000 January 1 11:59:27.816 TAI or 2000
185   January 1 11:58:55.816 UTC.) This system has X-axis aligned with the mean equinox
186   for epoch `J2000`; Z-axis is parallel to the rotation axis of the Earth, and Y com-
187   pletes the right-handed orthogonal set."

188   NAIF (2025) notes that `J2000` is "generally used in SPICE to refer to the `ICRF`";
189   "The rotational offset between the `J2000` frame and the `ICRS` has magnitude of
190   under 0.1 arcseconds [$2.\overline{7}\cdot10^{-5}$ degrees]."; "The `ICRF` frame is defined by the adopted
191   locations of 295 extragalactic radio sources."; "The `J2000` (aka `EME2000`) frame
192   definition is based on the earth's equator and equinox, determined from observa-
193   tions of planetary motions, plus other data."; and "The realization of `ICRF` was
194   made to coincide almost exactly with the `J2000` frame."

195   • `GEI2000` – Satellite Situation Center System and Services (2025c) identifies this
196   as equivalent to `J2000` by a parenthetical statement in the definition of `J2000`: "Geo-
197   centric Equatorial Inertial for epoch J2000.0 (`GEI2000`)."

198   • `GeocentricEarthEquatorial` – Used by `SunPy` (Mumford et al., 2025) with sup-
199   porting definition of "A coordinate or frame in the Geocentric Earth Equatorial
200   (`GEI`) system."

201   • `GCRS` – Used in `AstroPy` (Price-Whelan et al., 2022) with supporting definition
202   "A coordinate or frame in the Geocentric Celestial Reference System (`GCRS`). `GCRS`
203   is distinct from `ICRS` mainly in that it is relative to the Earth's center-of-mass rather

than the solar system Barycenter. That means this frame includes the effects of aberration (unlike `ICRS`)."

- `GEI`$_{\text{J2000}}$ – Fränz and Harper (2002) state that `GEI`$_{\text{J2000}}$ is realized through the `ICRF`. This is ambiguous today, because there are now three `ICRF` versions (Charlot et al., 2020).

- `EME2000` – Earth Mean Equator and Equinox J2000.0; defined in NAIF (2025) via "... with those of the `J2000` (aka `EME2000`) reference frame". Satellite Situation Center System and Services (2025c) defines as "Mean Equator and Mean Equinox of `J2000.0`" in its definition of `J2000`.

- `ECI2000` – Earth Centered Inertial for `J2000` epoch; used in `SpacePy` (Niehof et al., 2022).

- `ECI` – Earth Centered Inertial; used in NASA (2024) with the note "`GEI/J2000` – Earth-Centered Inertial (`ECI`). To fully specify the system the equinox must be defined. This system uses the mean equinox at the `J2000` epoch."

  `GCI` – Geocentric Celestial Inertial; used in OGO satellite data analysis (NASA, 1970) and stated in Russell (1971) as equivalent to `GEI`.

4 Comparisons

Space physics researchers and analysts have several options for obtaining data in different coordinate frames or transforming between them.

1. From datasets provided to a data archive, e.g., NASA's Coordinated Data Analysis Web (CDAWeb) and ESA's Cluster Science Archive (CSA), with vector measurements in different reference systems; in this case, a dataset in a needed reference frame is selected, if available.

2. Using data services that provide vector measurements in different reference frames. For example, SSCWeb provides ephemerides for spacecraft in various reference frames as a function of time (Satellite Situation Center System and Services, 2025c) and a calculator that takes an input of a geocentric position in a given reference system at a specific time and outputs the position in other reference systems (Satellite Situation Center System and Services, 2025a).

3. Using software packages that have coordinate transform functions. For example, in Python, `Astropy` (Price-Whelan et al., 2022), `SunPy` (Mumford et al., 2025), `SpacePy` (Morley et al., 2024), and `PySPEDAS` (Angelopoulos et al., 2024a). Other libraries include (Boller & Santiago, 2025) in C, and `Geopack` (Tsyganenko, 2008) and `IRBEM` (Boscher et al., 2022) in Fortran.

It is sometimes argued that, although reference-frame implementations may yield different results, this uncertainty is small relative to measurement uncertainty. For example, Hapgood (1995) notes that "The attitude error that arises from an error in the epoch used to compute `GEI` is 0.036°, which is small compared to the angular resolution of most space plasma measurements ...".

Although this statement was made thirty years ago, based on the results in this section, it appears the convention in space physics is that differences at this level are considered negligible. That is, we find angular differences in the ephemerides from different providers of $\sim$0.3° and coordinate transforms from different software packages of $\sim 0.03°$, and this uncertainty is not discussed in the documentation, suggesting that it is considered small enough to be ignored.

Although the convention for determining which uncertainties are considered negligible may have been appropriate at one time, we suggest revisiting these assumptions. First, spacecraft constellations now have a nearest separation of 7 km (NASA, 2016). This separation was achieved for the MMS constellation when the spacecraft were at a radial distance of ∼8.9 R_E from Earth's center. At this radial distance, the angular separation between two points 7 km apart is 0.007°. Second, having different data providers or software libraries compute transforms in different ways can impede validation, for example,

- In an attempt to develop a 3D visualization program that returns the region of geospace (e.g., plasma sheet, interplanetary medium, plasmasphere) given an arbitrary position, we implemented the models used by SSCWeb (Satellite Situation Center System and Services, 2025c) and attempted to validate our work by comparing our predicted regions at the positions provided by its web service for spacecraft. Although our predictions were generally consistent, we were unable to reproduce the exact time at which a spacecraft crossed from one region to another. After a search for errors in our model implementation failed to explain the differences, we realized that the discrepancies were due to the software that we used for reference-frame transformation differing from that used by SSCWeb.
- Not all global magnetosphere simulation models are executed in the same reference frame. To compare two models, the solar wind input must be transformed to the simulation reference frame, and simulated variables from both models must be transformed into the same reference frame for comparison. The uncertainty associated with this transformation must be known to determine the difference in the model output attributable to the simulation algorithm.

The fact that different software libraries provide different options for reference frames is indirect evidence that differences can matter. For example, `SpacePy` (Morley et al., 2024) provides multiple options for computing the `MAG` system, which have angular differences of ∼0.01°, and `SunPy` (Mumford et al., 2025) has options for how the `GEI` frame is computed. A general finding is that differences in transform results within a single library, with different options for the transform, are on the order of, or smaller than, differences in transform results between two different software libraries. As a result, improvements in how a transform is computed within a single library are lost when comparing data computed with a different library.

Even if the uncertainty associated with how a given reference frame was implemented is small relative to that of the measurements, we suggest that it is illogical for two data providers to report the location of a spacecraft that differs by more than what is expected due to numerical precision unless the reason for differences is clearly documented and ideally evident in the name of the dataset, e.g., by including the word "preliminary". A recommendation for addressing this is given in section 6.4.

4.1 Ephemerides

In this section, we give examples showing how ephemerides values from data providers can differ. We quantify the differences in terms of three quantities:

- $|\Delta\mathbf{r}|/R_E$, the magnitude of the difference in position vectors relative to an Earth radius, with $R_E \equiv 6378.16$ km, which is the value used by SSCWeb;
- $|\Delta\mathbf{r}|/\bar{r}$ the magnitude of the difference in position vectors relative to the average of the magnitudes of the position vectors; and
- $\Delta\theta$, the angular difference between position vectors.

Angular differences can be compared to:

1. The average angular change in Earth's dipole Z axis of $\sim 0.04°$ per year (from 1970–2025, computed using the libraries used in section 4.2).

2. The precession, also referred to as luni–solar precession, of Earth's rotation axis (also the $\mathtt{GEI}_Z$ reference system axis), which drifts by $\simeq 0.006°$ per year (Hapgood, 1995).

3. The one–year change in angle due to nutation of Earth's rotation axis of $\simeq 0.0025°$ per year (Hapgood, 1995).

4. The precession of the ecliptic (planetary precession) of $\Delta\theta \simeq 0.000014°$ per year (Hapgood, 1995).

Figure 1 shows the ephemerides of the Geotail spacecraft from `2021-11-25` through `2021-12-05` from the SSCWeb web service and the `GE_OR_DEF` dataset in CDF (Common Data Format, 2025) files from CDAWeb. SSCWeb provides ephemerides for scientific spacecraft in reference systems that include `GEI`, `J2K`, `GSE`, `GSM`, and `GM` (frequently referred to as `MAG`). The `GE_OR_DEF` dataset has ephemerides values in `GCI`, `GSE`, and `GSM`.

We used the SSCWeb option to return data as a fraction of R_E with 10 fractional digits. The CDAWeb dataset stores values with units of km as IEEE–754 64-bit floats, and the metadata indicates a recommended display precision of 10 fractional digits. The cadence of the SSCWeb Geotail data is 12 minutes while the CDAWeb Geotail dataset is 10-minutes. In the time interval displayed in Figure 1, values from the datasets are only shown when they have the same timestamps in the time interval shown.

Based on the precision of the data, and if both providers use the same definition of `GEI`, we expect $|\Delta r|/R_E \simeq 10^{-10}$ given that the SSCWeb values are reported in R_E to 10 fractional digits and the CDAWeb values are recommended for display with 10 fractional digits. For $\bar{r} = 20 R_E$, this corresponds to an uncertainty due to the precision of the data of $\Delta\theta \simeq 20 \cdot (180/\pi) \cdot 10^{-10}$ degrees $\simeq 10^{-7}$ degrees.

In Figure 1(a), and based on the documentation for Satellite Situation Center System and Services (2025c), which has the statement "Geocentric Inertial (`GCI`) and Earth-Centered Inertial (`ECI`) are the same as `GEI`.", we expect the SSCWeb/`GEI` and CDAWeb/`GCI` ephemerides difference to be near $\simeq 10^{-7}$ degrees, assuming both data sources use the same definition of `GEI`. The average angular difference between position vectors is $\Delta\theta \sim 0.3°$, and the average error relative to an Earth radius, $|\Delta\mathbf{r}|/R_E \sim 0.16$, or 16%. The maximum error relative to the average geocentric distance, $|\Delta\mathbf{r}|/\bar{r}$ is 1/187, or 0.5%.

In Figure 1(b), there is a much closer match between SSCWeb/`J2K` and CDAWeb/`GCI` ephemerides, with an average angular difference in the position vector of $\sim 0.001°$ and an average error relative to an Earth radius of $\sim 0.05\%$.

In summary, Figure 1(a) and (b) show that what is labeled as `GCI` in the CDAWeb ephemerides is much closer to SSCWeb/`J2K` ephemerides than SSCWeb/`GEI`, which is unexpected given the SSCWeb documentation that notes `GCI` and `GEI` are equivalent. Although the CDAWeb/`GCI` ephemerides is a better match to the SSCWeb/`J2K` ephemerides, the differences are not explained by the numerical precision of the reported values. They may be due to whether or how precision and nutation in items 2.–4. listed above were accounted for.

In Figure 1(c), a comparison is made for the `GSE` reference system. To transform a vector from `GEI` to `GSE`, two rotations are required: a rotation around $\mathtt{GEI}_X$ to align Earth's equator with the ecliptic plane and a rotation around the $\mathtt{GEI}_Z$ axis (as it is after the first rotation) to orient $\mathtt{GEI}_X$ to point to center of the Sun. These two angles are the obliquity of the ecliptic and the ecliptic longitude of the Sun, respectively (Hapgood (1992)).

In Figure 1(d), a comparison is made for the `GSM` reference system. A vector in the `GSE` reference system is transformed to `GSM` by an angle that depends on the orientation of the North geomagnetic pole (Russell (1971); Hapgood (1992)). The primary uncertainty is how the orientation of the North geomagnetic pole, which has an average yearly change of ∼0.04°, is computed. If both SSCWeb and CDAWeb computed the `GSM` ephemerides based on a transform from `GSE`, we could conclude that the observed $\Delta\theta$ are due to the use of different locations of the North geomagnetic pole. However, the maximum $\Delta\theta \simeq$ 0.37° is much larger than the average yearly angular change in Earth's dipole Z axis of ∼0.04°.

In Figure 2, a comparison is made between data from SSCWeb, CDAWeb, and the JPL Horizons web service (JPL, 2022), which provides ephemerides for some of the spacecraft available from SSCWeb. The CDAWeb dataset is `MMS2_EPD-EIS_SRVY_L2_ELECTRONENERGY`. The JPL Horizons web service provides ephemerides in the `ICRF` reference frame (the version of `ICRF` is not documented), and `SunPy` is used to transform it to other reference frames.

Figure 2a shows that the $\Delta\mathbf{r}$ between `GSE` locations from CDAWeb and SSCWeb match to within ∼3 km, which is much larger than expected by numerical precision but smaller than the closest separation distance of MMS spacecraft of ∼7 km (NASA, 2016). Figure 2b shows that there are larger differences for `GSM`.

In Figure 2c, much larger differences are shown to exist between SSCWeb and JPL than between SSCWeb and CDAWeb, with the maximum angular difference being up to ∼1° instead of 0.003° found in the comparison of SSCWeb and CDAWeb in Figure 2a. A similar conclusion is made by a comparison of Figure 2b and Figure 2d. A possible explanation for the sharp increase in $\Delta\theta$ near 11:00 is a thruster firing – the raw JPL Horizons web service output notes that "The spacecraft may be maneuvered frequently. Therefore, the JSpOC TLE-based [Joint Space Operations Center Two–Line Element] trajectory provided here may at times depart from the actual trajectory. This can happen because TLEs do not model thruster firings; the TLE trajectory solutions must be reinitialized after each event."
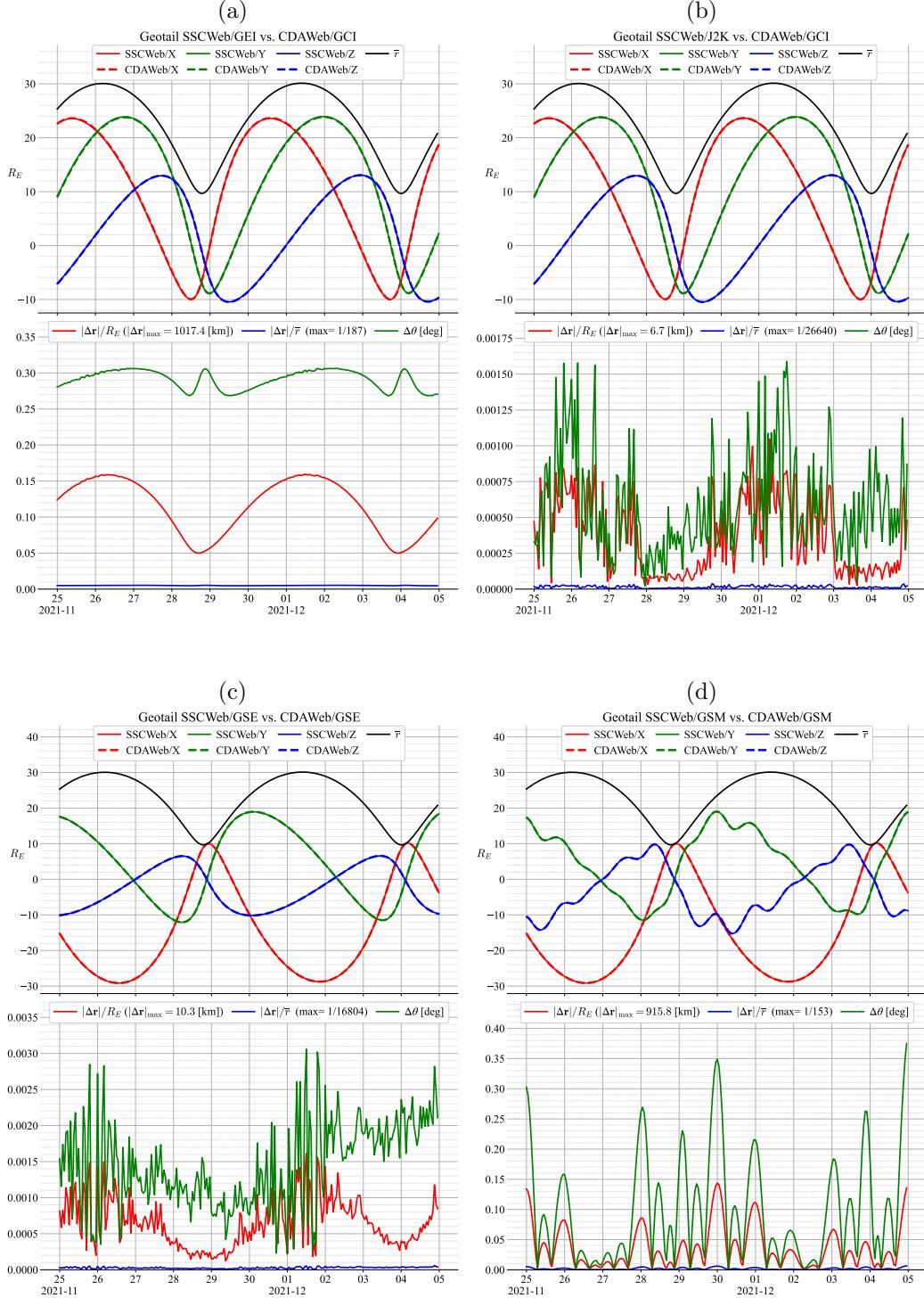
Figure 1: Comparison of ephemerides values for the Geotail spacecraft from SSCWeb and CDAWeb in four different reference systems. The top panel in each subplot displays the X, Y, and Z values from each provider (on this scale, differences are not visible) and the average radial distance, $\overline{r}$, between the two providers. The bottom panel of each subplot shows relative differences in the position vector $\Delta\mathbf{r}$ and the angular difference in the position vectors, $\Delta\theta$.
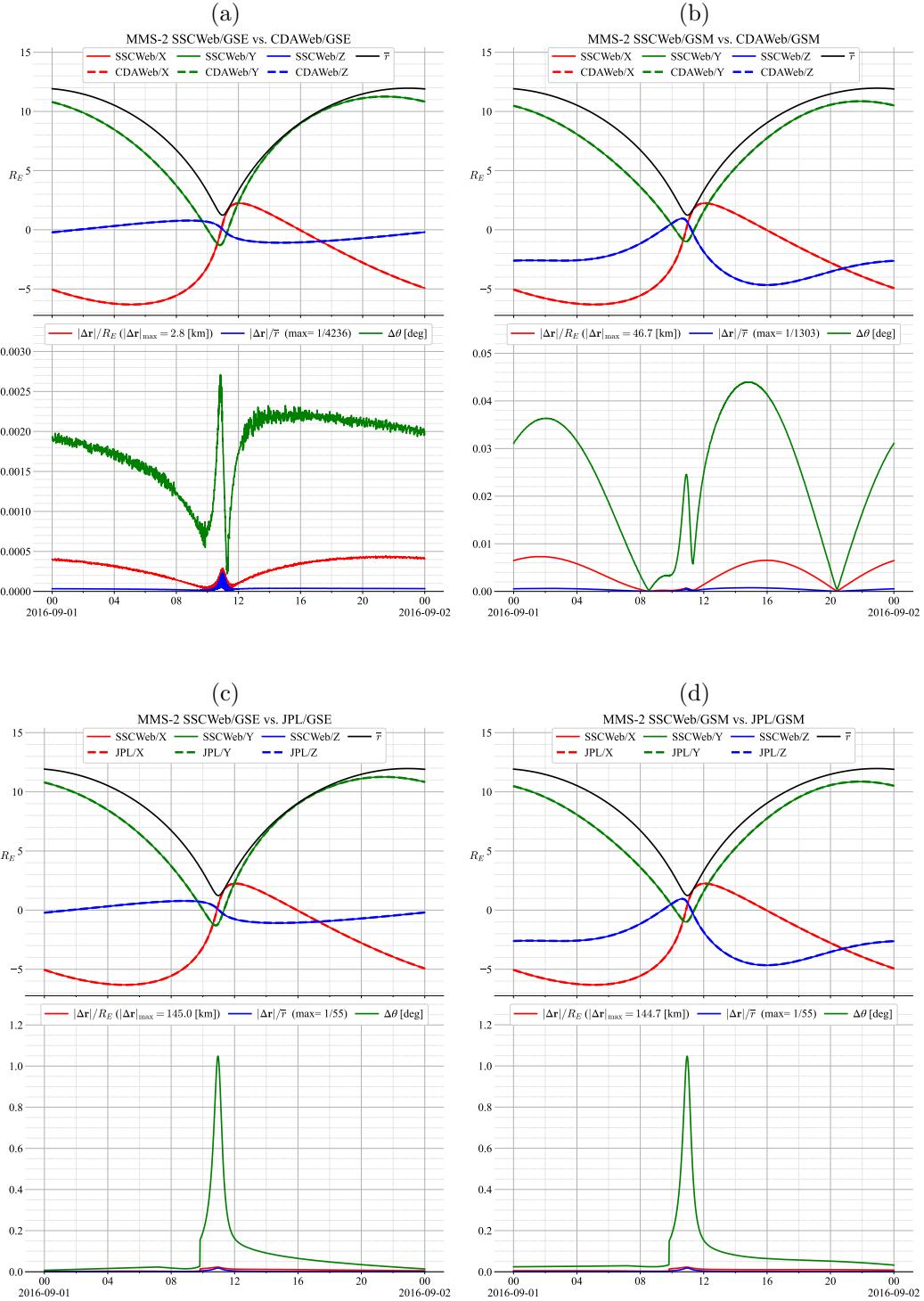
Figure 2: Comparison of ephemerides values for the MMS-2 spacecraft from (a)–(b) SSCWeb and CDAWeb; (c)–(d) SSCWeb and JPL Horizons in two different reference systems.

4.2 Software

In this section, we compare reference frame calculations using the following software packages.

- `Geopack-2008` double precision (Tsyganenko (2008); labeled as `geopack_08_dp` in the figures in this section), a Fortran library that was upgraded from earlier versions to support calculations using 64-bit floating point values.
- `PySPEDAS` 1.7.28, which uses transformation code derived from the IDL version of `PySPEDAS` (Angelopoulos et al., 2024b), which in turn used code from the `ROCOTLIB` Fortran (CDPP/IRAP, 2025) library, which was used for data from the Cluster spacecraft mission (Robert, 1993).
- `SpacePy` 0.0.6, which has an option to use the `IRBEM` Fortran library (Boscher et al. (2022); labeled as `spacepy-irbem`) or an alternative and native Python implementation (`spacepy`) of the transforms.
- `SpiceyPy` 6.0.0 is a Python wrapper for the SPICE toolkit. Two versions of SPICE kernel files were used, indicated by `spicepy1` and `spicepy2`. `spicepy1` was used for reference frame transforms for the Van Allen Probes mission. `spicepy2` had an update to the `MAG` frame, which used a more recent version of the IGRF model (Alken et al., 2021) to determine the Earth's magnetic dipole orientation.
- `SunPy` version 7.0.0, which extends the AstroPy coordinates framework to include space physics reference frames.

The top subplots in Figure 3 show the angles between the Z axis of four coordinate frame pairs. The angle between the Z axis in frame A and the Z axis in frame B, $\angle(Z_A, Z_B)$, was computed by transforming the Z axis in frame A into frame B, and the angle was computed between this transformed axis and the Z axis in frame B.

The middle subplots in Figure 3 show the difference of the angles between the Z axes for each library with respect to that for `geopack_08_dp`. The choice of library to use as the baseline for this comparison is arbitrary; in general, we are interested in the maximum differences among the libraries, which are shown in the lower panel of each subplot. The maximum absolute values range from $4 \cdot 10^{-9}$ degrees for `pyspedas` in Figure 3(a) to $1 \cdot 10^{-2}$ degrees for `spicepy1` in Figure 3(c); the values for each library are given in the legend in the middle panel of each subplot.

The bottom panels of Figure 3 shows that across all libraries, the maximum absolute value of lines in the middel panel are $\sim 0.01°$ for `GEO/GSE`, $\sim 0.03°$ for `GEO/GSM`, $\sim 0.04°$ for `GSE/GSM`, and $\sim 0.03°$ for `GSE/GSM`, all of which are comparable to the average angular change in Earth's dipole Z axis of $\sim 0.04°$ per year.

We have also performed coordinate transforms using the Satellite Situation Center System and Services (2025a) coordinate calculator web service. However, this service outputs values only to two decimal places, leading to angular differences of $0.3°$. These values are not plotted so that the other library differences are clearly visible.

The range of the maximum absolute differences, $0.001°$-$0.04°$, shown in the bottom panels of the subplots in Figure 3 is smaller than the range, $0°$-$1°$, of angular difference in spacecraft position vectors in the same coordinate system from two different data providers found in section 4.1. The position vectors can differ for two reasons: differences in the source of the ephemerides data and differences in the data providers' software libraries, if a transformation is needed. To determine the magnitude of each requires analyzing the source code used to generate the ephemerides, which is not readily available.

In summary, in this section, we have shown that differences in library implementations of reference frames range from $0.001°$ to $0.04°$ for the chosen set of coordinate

frames and comparison axis. This range of differences is comparable to the range of angles identified in section 4.1, which includes the average angular change in Earth's dipole Z–axis over the past 45 years, the precession of Earth's rotation axis, changes in nutation of Earth's rotation axis over one year, and the precession of the ecliptic. The implication is that inter-comparison of measurements transformed with different libraries may require an analysis of the differences in the transform implementations if the differences in the measurements are not significantly larger than these differences. This type of analysis is challenging because it requires access to the transform software, which may not be maintained or available, and because calculations are needed to quantify differences due to transform implementation choices.
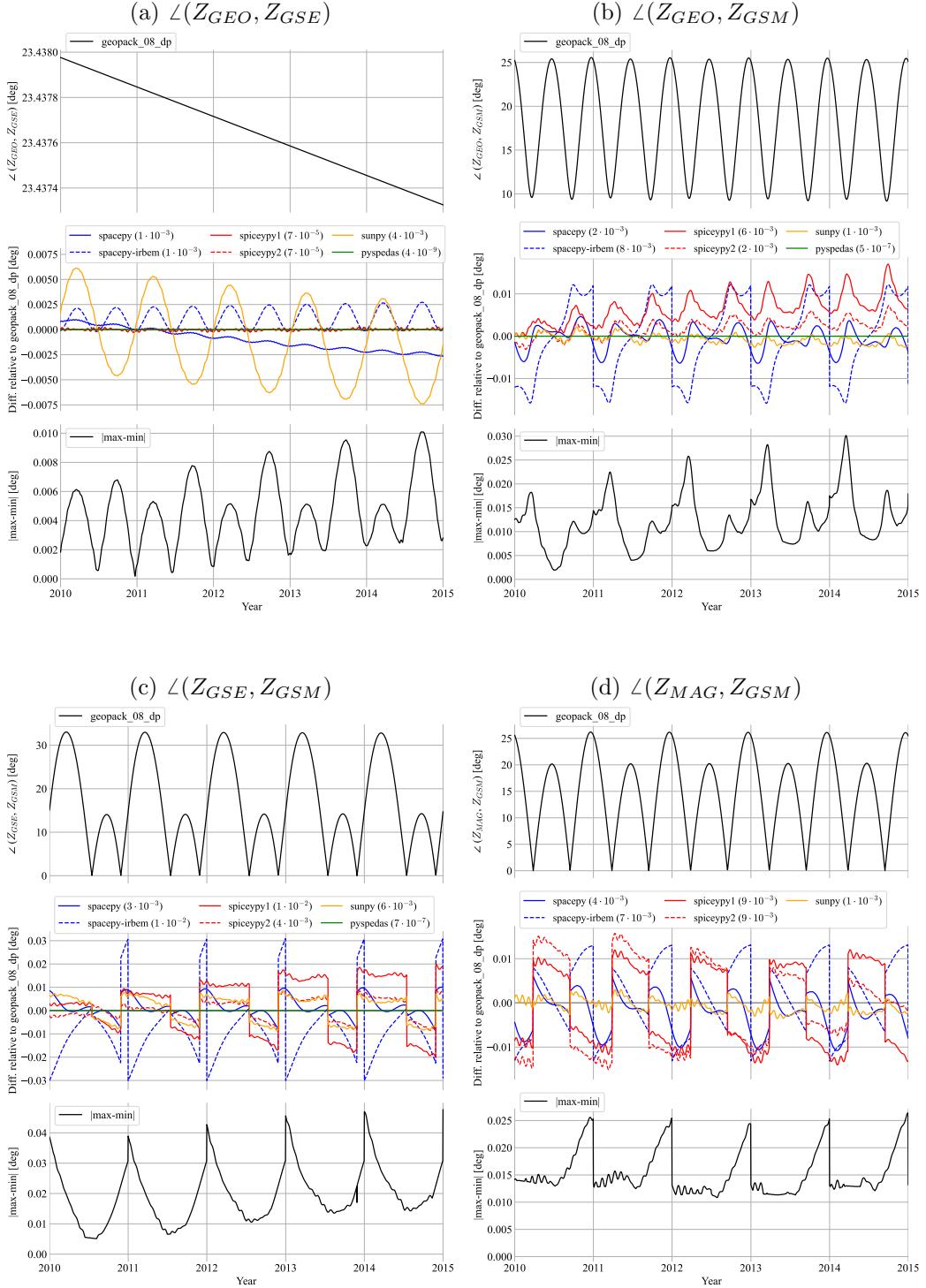
Figure 3: Angles between Z axes in select coordinate frames as computed by different software packages. In the top panels of each subplot, the notation $\angle(Z_A, Z_B)$ means the angle between the Z axis of coordinate frame A and the Z axis of coordinate frame B computed using `geopack_08_dp`. The middle panel of each subplot shows the difference between $\angle(Z_A, Z_B)$ computed using `geopack_08_dp` and that computed using the library indicated in the legend; the maximum of the absolute value of each line is shown in parentheses. The bottom panels show the maximum absolute differences in the middle panel.

5 How transform information is created for spacecraft missions

Archival data for space physics spacecraft missions typically include vector measurements in multiple reference frames. For NASA missions, archival data products are delivered to the Space Physics Data Facility (NASA, 2025). Modern missions typically take one of two approaches for transforms: (a) A mission operations team develops SPICE kernels for select space physics reference frames, and SPICE software is used for the transforms; or (b) A non-SPICE software library is used for the transforms, for example, `ROCOTLIB` and `SpacePy`.

There is significant overlap in effort across missions; typically, a scientist familiar with space physics reference systems but not with their implementation options will use available software or SPICE kernels and develop tests. As noted in the conclusions, this effort to develop and verify transform calculations would not be necessary if either a database of transform matrices or versioned SPICE kernels were available that were accepted as a community standard.

For the SSCWeb data service (Satellite Situation Center System and Services, 2025c), which provides spacecraft ephemerides, three approaches have been taken in order of priority (see Satellite Situation Center System and Services (2025b) for a table indicating which approach was taken and provenance):

1. Mission–developed SPICE kernels for ephemerides are obtained from the mission team periodically and archived. The `GEI` ephemerides–related SPICE kernel information is used to generate the `J2000` ephemerides. Then, International Solar-Terrestrial Physics–era (ISTP; International Solar Terrestrial Physics (2025)) software is used to compute ephemerides in different coordinate frames, including `GEI`, `GEO`, `GM`, `GSE`, `GSM`, and `SM`. The ISTP software uses proprietary information needed for the reference frames, such as the position of the Sun, calculated by GSFC's Flight Dynamics Facility (FDF). This approach is only used on ISTP–era missions, i.e., ACE, Polar, Wind, and Geotail.

2. A `GEI` ephemerides–related variable in archival data files that was computed by the mission is then used to compute orbit and attitude data in different reference frames; only data in the `GEI`–related frame is used. This is a possible source of the differences shown in Figure 1 if the mission computed the ephemerides in the archival data products by transforming `GEI` using different software than SSCWeb. Differences can also occur if the mission uses a different definition of `GEI` than SSCWeb.

3. If SPICE kernels or other mission–computed `GEI` ephemerides-related values are not available, TLE (Two-Line Element) files are obtained from NORAD (North American Aerospace Defense Command), and a translation of the C NORAD library to Pascal (Brodowski, 2002) is used to compute ephemerides in `TEME` (True Equator, Mean Equinox). Often, TLEs are used at the start of the mission, and a switch is made to approaches 1. or 2. as information becomes available. This switching has implications for reproducibility that are discussed in section 6.4 because previous versions of ephemeris are not retained.

6 Summary and Recommendations

In this section, we provide recommendations to address the issues identified in this article.

6.1 Standards for Reference System and Frame Definitions

As defined in section 2, an *ideal reference system* is a general description of a reference frame that lacks key details necessary for its implementation. Examples were provided in which the GEI acronym had different expansions, and different acronyms were identified as equivalent.

The next level of specificity relative to an ideal reference system is a *reference system*, which defines constants, models with free parameters, and algorithms for transforming between observable quantities and reference data.

Finally, a *reference frame* is a realization of a reference system based on measurements used to determine the free parameters in its models.

A community-developed standard should be created for acronyms and definitions. The standard should provide abbreviation/definition pairs for commonly used space physics ideal reference frames. Associated with each ideal reference frame definition, there should be at least one reference system abbreviation/definition pair. If multiple reference systems are in common use, their definitions and referencing conventions should be specified. For each reference system, at least one reference frame should be defined.

6.2 Reference Frame Standard Dataset

For a given transform between reference frames, a transformation matrix at a specific instant in time (or, equivalently, rotation angles or quaternions) relative to a base reference frame is required. We also note that implementing transforms requires technical expertise in software and maintenance, including updating free parameters in reference-frame models, verifying calculations, and documenting changes. Although providing a software version enables reproducibility in principle, in practice, not all users will be familiar with or want to use the cited software, and in the long term, the software may not be maintained or may be difficult to install and use.

Based on this, we recommend that a standards body develop a standard dataset with a long-term plan to keep it up-to-date. Each record in the dataset should consist of a timestamp and a transform matrix that relates a coordinate frame to a reference coordinate frame. The records should be made available in a standard scientific file format and from a web service API (Application Programming Interface). A parsimonious alternative to providing 9 transform matrix values is to define only one or two angles (and associated rotation axes) from which the matrix can be computed.

With such a dataset, if a scientist wants to allow for reproducibility, they could state, for example, "the vector measurements in ABC were transformed into reference frame XYZ," by using ABC to REF and REF to XYZ transformation matrices in the standard dataset and citing both the standard that defines the acronyms and the standard dataset.

Many software libraries do spot checks of transforms. For example, SunPy's unit tests (Mumford et al., 2025) involve a comparison with a table from Fränz and Harper (2002) at several time instants; cxform (Boller & Santiago, 2025) tests its implementation by comparing the ephemeris in GSE of one year of data from three spacecraft from Satellite Situation Center System and Services (2025c); a comparison is also made with a table in Fränz and Harper (2002). With the proposed reference database, a software library developer could make a more comprehensive comparison, allowing users to estimate uncertainties associated with coordinate transforms directly. An additional advantage of this dataset is that software developers can use it for more comprehensive testing of their implementations.

We also suggest that this dataset contains common time representations. Each record should be a UTC timestamp along with values for UT1, TAI, TT, and ET (McCarthy (2011);

see section Appendix A for definitions). Although these time relationships are simple, some require a leap second table, and to perform the computation, one needs to parse (and update if required) the leap second table.

The advantage of the standard dataset over software libraries is that the latter require continual upgrades, and not all users perform their analysis the language in which the library is implemented. Although software that automatically updates IGRF coefficients and leap-second information may work now, it is not guaranteed to be maintained and usable indefinitely. In addition, transform results may change as a given software package evolves. For example, consider a package that utilizes non-definitive IGRF model coefficients for `MAG` and computes a transformation. Five years later, the result will not be the same if the software then uses definitive IGRF coefficients. Although, in principle, the package developers can maintain reproducibility, doing so requires significant effort. The proposed standard dataset could address this by defining two `MAG` reference frames. One uses only definitive IGRF coefficients. The other only uses non-definitive. We also recommend that each release of the IGRF coefficients be given its own DOI and archived in a generalized repository. (At present, it is only possible to cite descriptions of the model, e.g., Alken et al. (2021), but not a specific release.)

Having a dataset of reference frame transform matrices will address another issue. In the development of section 4.2, we encountered significant errors in four of the libraries, despite these libraries passing their tests. (These errors were reported, and a version with the corrections was used in section 4.2). If these libraries had a more comprehensive set of test matrices, these errors would have been noticed.

6.3 Database of SPICE transform kernels

Ideally all mission-specific SPICE kernels would be available from a single repository, kernels related to standard space physics reference frames would be shared across missions, and these standard kernels would either be used to generate the standard dataset described in section 6.2 or an evaluation of the differences between transforms using these SPICE kernels and the standard dataset would be provided as documentation.

We also recommend using modern version control systems for the SPICE kernels. At present, kernels can be found on various websites, and kernel versions are sometimes indicated in the file name, but prior versions are not always provided, thereby inhibiting reproducibility. Storing kernels in a source code repository, which provides versioning and simplifies change tracking, will improve this. Additionally, we recommend assigning unique identifiers, such as DOIs, to kernels to facilitate their citation.

6.4 Versioning and Documenting Ephemerides

In this work, we have been primarily interested in the problem of transforming a vector from one reference frame to another. In the case of ephemerides provided in a given reference frame, there is an uncertainty due to what is meant by that reference frame, which is addressed by the recommendation in section 6.1.

There is an additional source of uncertainty — the source of the ephemerides. Missions have used direct GPS measurements, commercial software such as STK (Systems Tool Kit), and data from facilities such as GSFC Flight Dynamics Facility (FDF), the Deep Space Network (DSN), NAIF, and NORAD to produce the ephemerides for the mission. Section 4.1, we show an example where the ephemerides for two different data providers for the same spacecraft differed in a way that was unlikely to be due to differences in how the data providers implemented the reference frame.

To address this, we suggest that data providers indicate how their ephemerides were obtained. We also suggest that if two data providers provide ephemerides for the same

spacecraft, they document how and why their results may differ, if applicable. We also recommend that the metadata indicate the uncertainty in the locations. Often, data providers will modify the ephemerides values when more accurate calculations become available. This makes reproducibility difficult. Ideally, for reproducibility, old versions of ephemerides would be made available. Often, this is impractical, so an alternative is to include version information in the metadata.

6.5 Documentation

If the above recommendations are followed, the necessary documentation for reproducibility related to coordinate transforms will be simplified. For example, if an author or software package used the standard dataset described in section 6.2 for a transform, only the standard dataset is needed for reproducibility. Similarly, if one or more SPICE kernels are used, each with a unique DOI and stored in a permanent generalized repository, only the DOIs are needed to retrieve the kernels. In this case, these DOIs and the version of the SPICE software library used are sufficient for reproducibility.

In the absence of these options, we recommend the following.

- Software package developers provide documentation on implementation choices (e.g., model used for obliquity). If data from an external resource is used, for example, if the IGRF coefficients are dynamically downloaded, the user should have an option to easily view the data used, so that, if necessary, the values used can be documented in a publication. Software should have a DOI for each version so that the version used can be referenced rather than only a top-level DOI. Additional software citation recommendations are given in Jackson (2012) and Smith et al. (2016).
- Data providers should ensure that metadata associated with ephemerides and variables that are transformed include details about the software version used for the transforms or the data used for the transform, such as SPICE kernels. The metadata description should be validated by having a third party assess whether it contains sufficient information to re-implement the transform.
- Paper authors include the version of software, a DOI for that version if available, and options passed to the transform function. If SPICE kernels are used, they should be provided as supplementary material if they are not otherwise citable and online, or posted to a general repository (e.g., Zenodo).

Appendix A Definitions

- ACE – Advanced Composition Explorer (spacecraft mission)
- CDAWeb – Coordinated Data Analysis Web (NASA data archive)
- CD – Centered Dipole (reference frame). Same as GM and MAG if they use a model dipole with an origin of Earth's center of mass.
- CDF – Common Data Format (file format for scientific data)
- DSN – Deep Space Network (NASA communications network)
- ECI – Earth-Centered Inertial (reference frame)
- EME – Earth Mean Equator (reference frame)
- ET – Ephemeris Time (time standard)
- GEI – Geocentric Equatorial Inertial (reference system)
- GEO – Geographic (reference system)
- GM – Geomagnetic (reference system, often called MAG)
- GSE – Geocentric Solar Ecliptic (reference system)
- GSM – Geocentric Solar Magnetospheric (reference system)
- GCI – Geocentric Celestial Inertial (reference system)

- `GCRS` – Geocentric Celestial Reference System (reference system)
- `GPS` – Global Positioning System
- GSFC – Goddard Space Flight Center (NASA center)
- IGRF – International Geomagnetic Reference Field (geomagnetic model)
- ISTP – International Solar-Terrestrial Physics (NASA program)
- IRBEM – International Radiation Belt Environment Modeling (software library)
- ICRF – International Celestial Reference Frame (reference frame)
- ICRS – International Celestial Reference System (reference system)
- `J2000` – Reference system with reference epoch of 2000 January 1 noon TT.
- J2000.0 – Reference epoch associated with `J2000`
- J2K – Abbreviation of `J2000`
- JPL – Jet Propulsion Laboratory
- `MAG` – Geomagnetic (reference frame). Also referred to as Centered Dipole (CD) and GM.
- MMS – Magnetospheric Multiscale Misson
- NAIF – Navigation and Ancillary Information Facility
- MOD – Mean of Date (reference frame modifier, precession only)
- NORAD – North American Aerospace Defense Command
- `SM` – Solar Magnetic (reference system)
- SPICE – Spacecraft, Planet, Instrument, C-matrix, Events (NAIF toolkit)
- SPEDAS – Space Physics Environment Data Analysis Software (software library)
- SSCWeb – Satellite Situation Center Web (NASA data service)
- STK – Systems Tool Kit (commercial orbit analysis software)
- TAI – International Atomic Time (time standard)
- TT – Terrestrial Time (time standard)
- TLE – Two-Line Element set (satellite orbital elements)
- `TEME` – True Equator, Mean Equinox (reference system)
- UT1 – Universal Time 1 (time standard)

Open Data

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