

Enclosed Charge

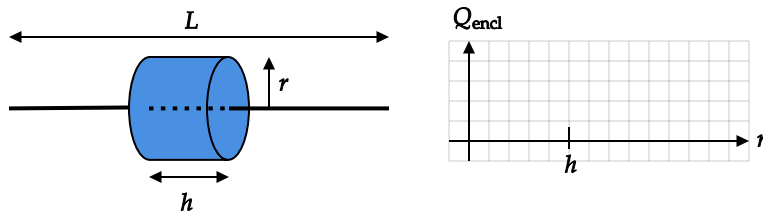
1 Overview

When using Gauss's law, one must draw an imaginary volume in space and compute how much charge is inside the volume.

In general, an imaginary volume is chosen is one for which computation of the electric flux is easy. That is, the imaginary volume will be such that the electric field is either parallel or perpendicular to all parts of the surface. In this activity, you are given the Gaussian volume. However, you should understand the reason for the choice of each Gaussian volume given.

2 Line of Charge

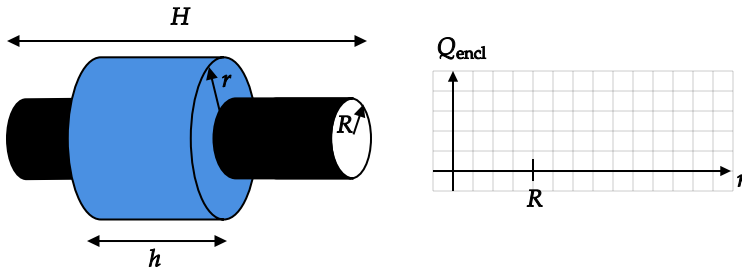
A total of $+3Q$ is uniformly distributed a non-conducting line of length L . The Gaussian cylinder shown has a length h , radius r , and the same center line as the charged line.



1. Find the linear charge density, λ , on the line.
2. Find an equation for Q_{encl} in terms of λ and one or more of r , h , and L .
3. Use your equation from 2. to find the amount of charge enclosed by the Gaussian cylinder when it has radii of $r = h/100$, $r = h/2$, $r = h$, and $r = 2h$.
4. Plot the four values of enclosed charge calculated above versus the radius of the Gaussian cylinder. Then plot the equation found in part 2. as a smooth line.

3 Cylindrical Shell

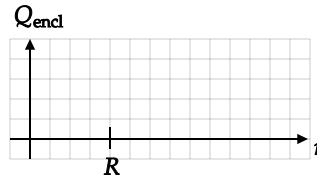
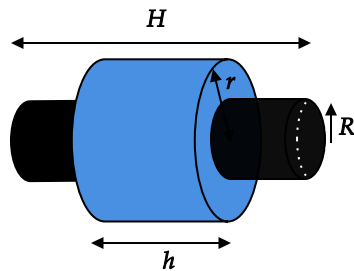
A non-conducting hollow cylinder of radius R and length H has a charge of $+3Q$ uniformly distributed *on its curved surface*. The Gaussian cylinder shown has a length h , radius r , and the same center line as the charged cylinder.



1. Find the linear charge density, λ , of the charged cylinder.
2. Find an equation for Q_{encl} for $r < R$.
3. Find an equation for Q_{encl} for $r > R$. Your equation should involve λ and one or more of h , r , and R .
4. Find the amount of charge enclosed by the Gaussian cylinder when it has radii of $r = 0$, $r = R/2$, $r = 2R$, and $r = 3R$.
5. Plot the four values of enclosed charge calculated above versus the radius of the Gaussian cylinder. Then plot the equations found in parts 2. and 3 as a smooth line.

4 Solid Cylinder

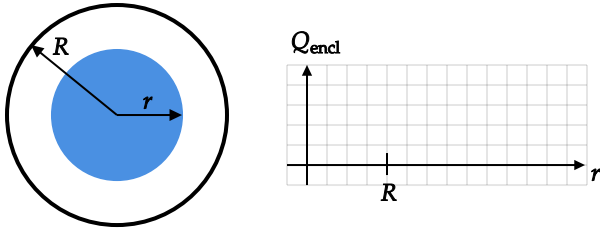
A non-conducting solid cylinder of radius, R and length, L has a charge of $+3Q$ uniformly distributed *throughout it*. The Gaussian cylinder has length h , radius r , and the same center line as the charged cylinder.



1. Find the volume charge density, ρ , of the charged cylinder.
2. Find an equation for Q_{encl} for $r \leq R$. Your equation should involve ρ and one or more of h , r , and R .
3. Find an equation for Q_{encl} for $r \geq R$. Your equation should involve ρ and one or more of h , r , and R .
4. Find the amount of charge enclosed in a Gaussian cylinder of radius $r = 0$, $r = R/2$, $r = R$, and $r = 2R$.
5. Plot the four values of enclosed charge calculated above versus the radius of the Gaussian cylinder. Then plot the equations found in parts 2. and 3 as a smooth line.

5 Spherical Shell

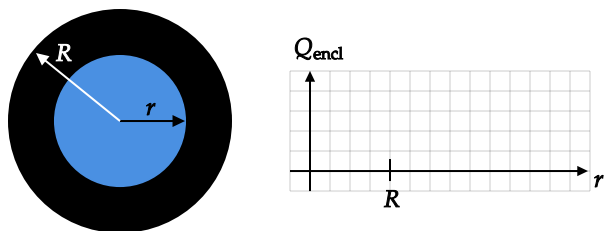
A non-conducting spherical shell of radius R has a charge of $+3Q$ uniformly distributed *on its surface*. Its cross-section is shown along with that of a Gaussian sphere with the same center and a radius r .



1. Find the surface charge density on the sphere.
2. Find an equation for Q_{encl} for $r < R$.
3. Find an equation for Q_{encl} for $r > R$. Your equation should involve σ and one or more of R and r .
4. Find the amount of charge enclosed in Gaussian sphere of radii $r = 0$, $r = R/2$, $r = 2R$, and $r = 3R$.
5. Plot the four values of enclosed charge calculated above versus the radius of the Gaussian sphere. Then plot the equations found in parts 2. and 3 as a smooth line.

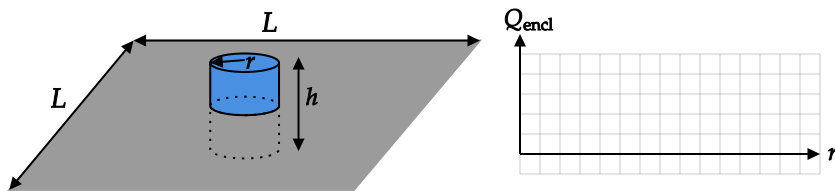
6 Solid Sphere

A non-conducting sphere of radius R has a charge of $+3Q$ distributed uniformly *throughout* it. The cross-section of the sphere is shown along with a dashed line representing the surface of a Gaussian sphere, which has the same center as the charged sphere and a radius r .



1. Find the charged sphere's volume charge density, ρ .
2. Find an equation for Q_{encl} for $r < R$. Your answer should involve ρ and one or more of r and R .
3. Find an equation for Q_{encl} for $r > R$. Your answer should involve ρ and one or more of r and R .
4. Find the amount of charge enclosed in Gaussian sphere of radii $r = 0$, $r = R/2$, $r = R$, and $r = 2R$.
5. Plot the four values of enclosed charge calculated above versus the radius of the Gaussian sphere. Then plot the equations found in parts 2. and 3 as a smooth line.

7 Large Sheet



A non-conducting square sheet with side length L has a charge of $+3Q$ distributed uniformly on it. The Gaussian cylinder has a height h and radius r , and half of it is above the sheet.

1. Find the surface charge density, σ , on the sheet.
2. Find an equation for Q_{encl} for $r < L$. Your answer should involve σ and one or more of r , h , and L .
(In Gauss's law problems, L is much larger than r , so we do not need to consider $r > L$.)
3. Plot the enclosed charge calculated above versus the radius of the Gaussian cylinder.