Vectors

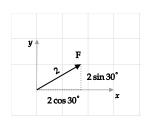
1 Problem I

A vector $\vec{\mathbf{F}}$ has a magnitude of 2 and makes an angle of 30° with the x-axis (with positive rotation counterclockwise).

- 1. Draw $\vec{\mathbf{F}}$.
- 2. Write $\vec{\mathbf{F}}$ in the form $F_x \hat{\boldsymbol{\imath}} + F_y \hat{\boldsymbol{\jmath}}$.

Solution

1.



2. $\vec{\mathbf{F}} = 2\cos(30^\circ)\hat{\imath} + 2\sin(30^\circ)\hat{\jmath} = \sqrt{3}\hat{\imath} + \hat{\jmath}$, where $\cos(30^\circ) = \sqrt{3}/2$ and $\sin(30^\circ) = 1/2$ was used in the last step.

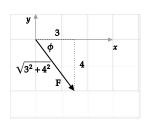
2 Problem II

Given $\vec{\mathbf{F}} = 3\hat{\imath} - 4\hat{\jmath}$, find

- 1. Draw $\vec{\mathbf{F}}$.
- 2. Compute F.
- 3. The angle $\vec{\mathbf{F}}$ makes with respect to the x-axis (with positive rotation counterclockwise).

Solution

1.



2.
$$F = \sqrt{3^2 + 4^2} = 5$$

$$3.~ heta = 360^\circ - \phi = 360^\circ - rac{180}{\pi} an^{-1} (4/3) \simeq 307^\circ$$