# 04-630 Data Structures and Algorithms for Engineers

Lecture 8: Constrainers and Dictionaries II

## Agenda

#### **Containers and Dictionaries**

- Containers
- Dictionaries
- List ADT
  - Array implementation
  - Linked list implementation

# Preliminaries: Linked Lists Using Pointers

#### Why Pointer-Based Implementation?

- Linked lists are used to avoid excessive data movement with insertions and deletions
- Elements are not necessarily stored in contiguous memory locations
- Makes efficient use of memory space
  - Allocate space when needed
  - Deallocate space when finished & return it to the free store
- Failure to deallocate space will cause memory leakage

#### Why Pointer-Based Implementation?

Some guidelines when writing programs that dynamically allocate memory

- Use malloc or new to create data-structures of the appropriate size
- Remember to avoid memory leakage by always using free and delete to deallocate dynamically-created data-structures
- Check every call to malloc or new to see if it returned NULL (i.e., check if the allocation was unsuccessful)

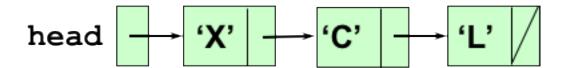
### Why Pointer-Based Implementation?

Some guidelines when writing programs that dynamically allocate memory

- You must expect free or delete to alter the contents of the memory that was freed or deleted
- Never access a data structure after it has been freed or deleted
- If malloc fails in a non-interactive program, make that a fatal error
- In an interactive program, it is better to abort the current command and return to the command reader loop

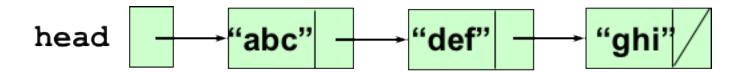
#### A Linked List

- A linked list is a list in which the order of the components is determined by an explicit link member in each node
- The nodes are structs
  - each node contains a component member and also a link member that gives the location of the next node in the list



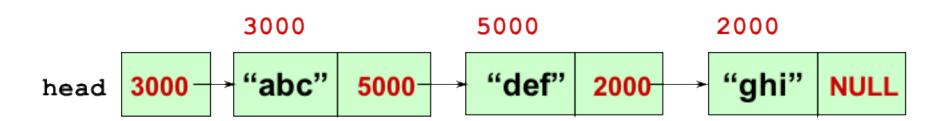
### Pointer-Based (Dynamic) Linked List

A pointer-based linked list is a dynamic linked list where nodes are linked together by pointers, and an external pointer (or head pointer) points to the first node in the list



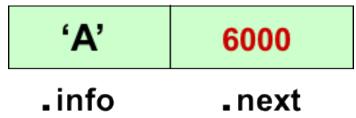
#### Nodes can be located anywhere in memory

The link member holds the memory address of (or a reference to) of the next node in the list

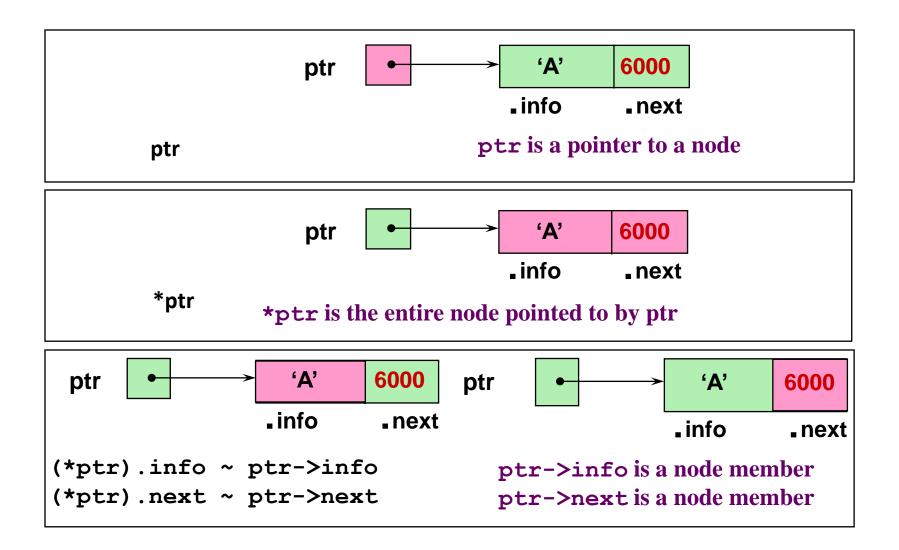


### **Declarations for a Dynamic Linked List**

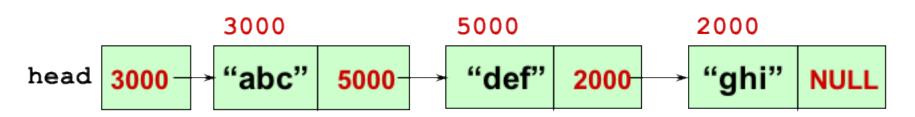
```
// Type DECLARATIONS
struct NodeType
  char info;
  NodeType* next;
typedef NodeType* NodePtr;
// Variable DECLARATIONS
NodePtr head;
NodePtr ptr;
```



#### **Pointer Dereferencing and Member Selection**

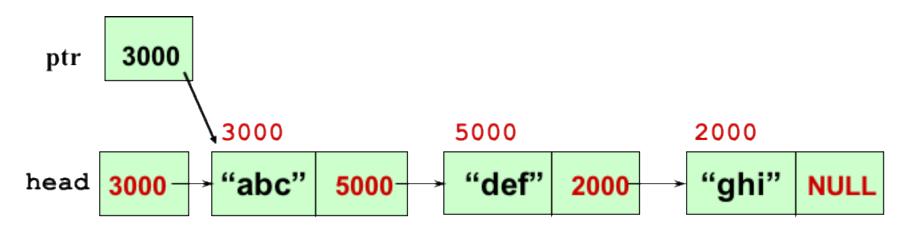






```
//PRE: head points to a dynamic linked list

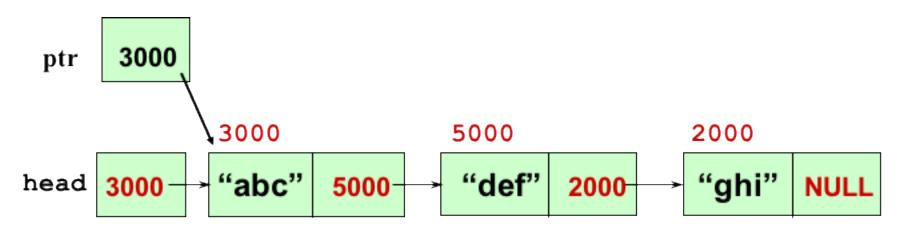
ptr = head;
while (ptr != NULL) {
   cout << ptr->info;
        // Or, do something else with node *ptr
   ptr = ptr->next;
}
```



```
//PRE: head points to a dynamic linked list

ptr = head;

while (ptr != NULL) {
    cout << ptr->info;
        // Or, do something else with node *ptr
    ptr = ptr->next;
}
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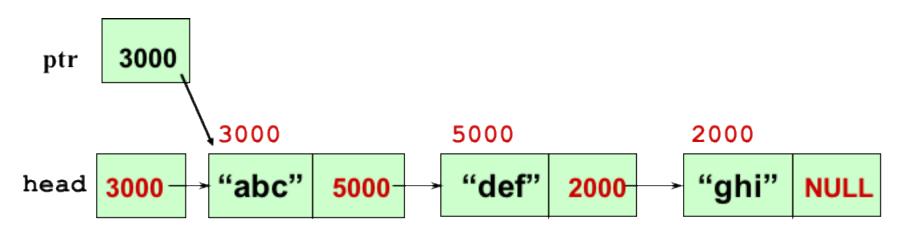
ptr = head;

while (ptr != NULL) {

   cout << ptr->info;

        // Or, do something else with node *ptr

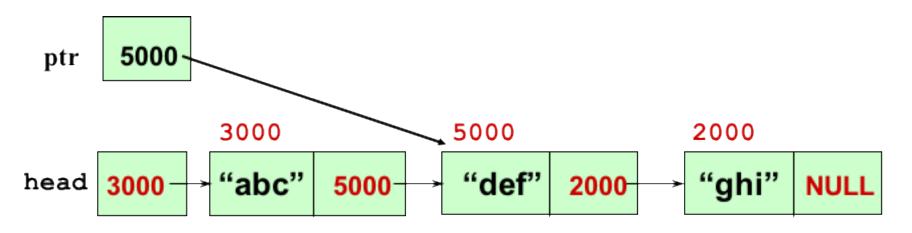
   ptr = ptr->next;
}
```



```
//PRE: head points to a dynamic linked list

ptr = head;
while (ptr != NULL) {
    cout << ptr->info;

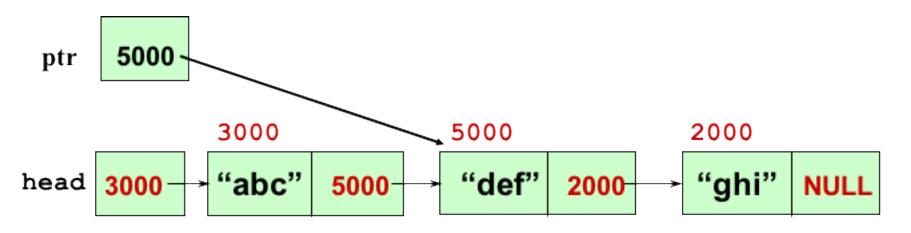
    // Or, do something else with node *ptr
    ptr = ptr->next;
}
```



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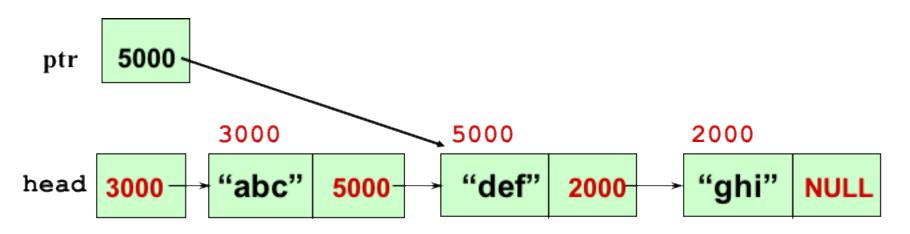
ptr = head;

while (ptr != NULL) {

   cout << ptr->info;

       // Or, do something else with node *ptr

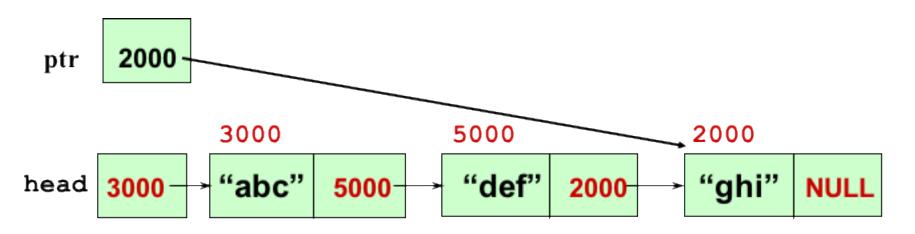
ptr = ptr->next;
}
```



```
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ptr = head;
while (ptr != NULL) {
    cout << ptr->info;

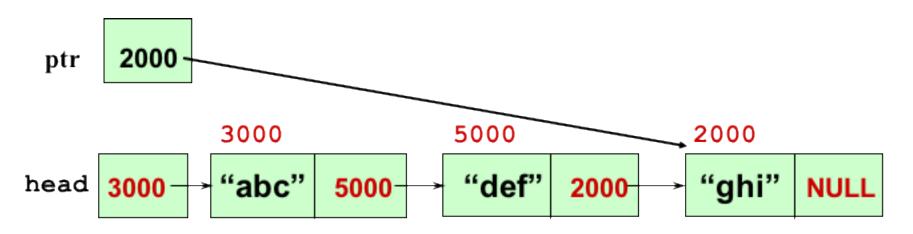
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}
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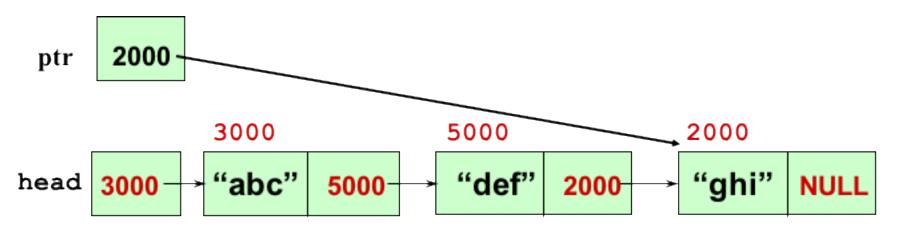
ptr = head;

while (ptr != NULL) {

   cout << ptr->info;

        // Or, do something else with node *ptr

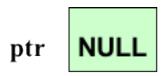
   ptr = ptr->next;
}
```

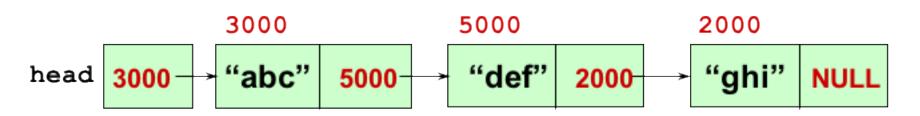


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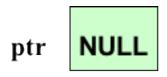


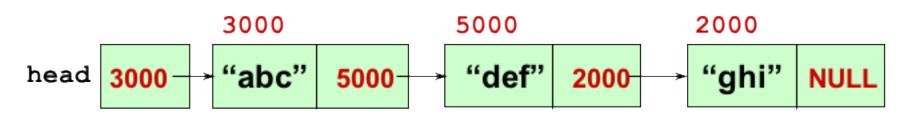


```
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ptr = ptr->next;
}
```





```
//PRE: head points to a dynamic linked list

ptr = head;

while (ptr != NULL) {

   cout << ptr->info;

        // Or, do something else with node *ptr

   ptr = ptr->next;
}
```

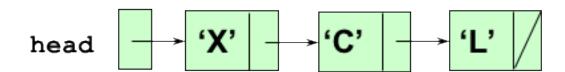
#### Using Operator new

- If memory is available in an area called the free store (or heap), operator new allocates the requested object, and returns a pointer to the memory allocated.
- The dynamically allocated object exists until the delete operator destroys it.

item 'B'

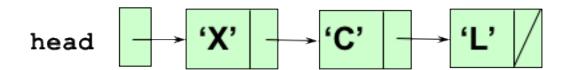
```
char item = 'B';

NodePtr location;
location = new NodeType;
location->info = item;
location->next = head;
head = location;
```



```
item 'B'
```

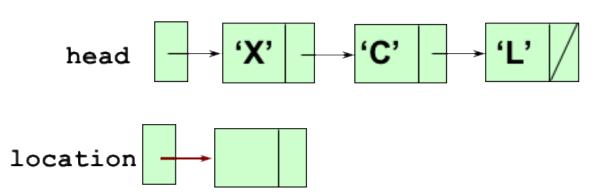
```
char item = 'B';
NodePtr location;
location = new NodeType;
location->info = item;
location->next = head;
head = location;
```





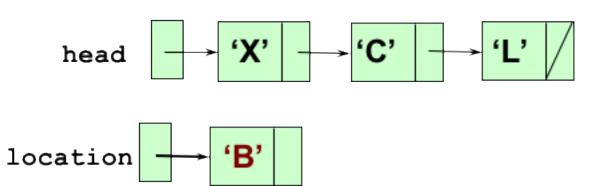
```
item 'B'
```

```
char item = 'B';
NodePtr location;
location = new NodeType;
location->info = item;
location->next= head;
head = location;
```



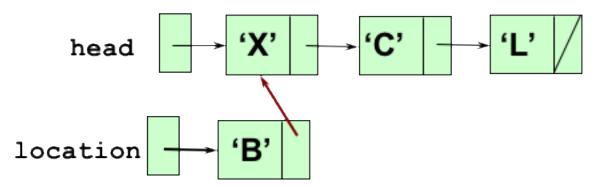
```
item 'B'
```

```
char item = 'B';
NodePtr location;
location = new NodeType;
location->info = item;
location->next= head;
head = location;
```



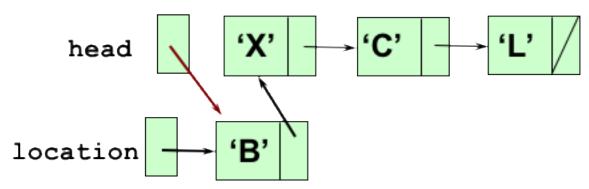
```
item 'B'
```

```
char item = 'B';
NodePtr location;
location = new NodeType;
location->info = item;
location->next= head;
head = location;
```



```
item 'B'
```

```
char item = 'B';
NodePtr location;
location = new NodeType;
location->info = item;
location->next= head;
head = location;
```



#### Using Operator delete

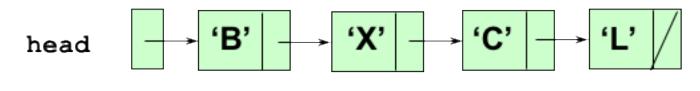
The object currently pointed to by the pointer is deallocated, and the pointer is considered undefined.

The object's memory is returned to the free store.



```
NodePtr tempPtr;

item = head->info;
tempPtr = head;
head = head-> next
delete tempPtr;
```



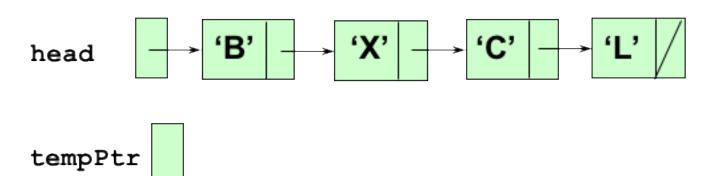




```
NodeType * tempPtr;

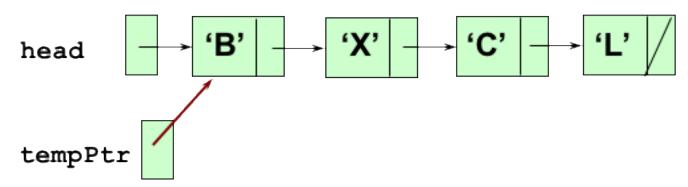
item = head->info;

tempPtr = head;
head = head-> next
delete tempPtr;
```



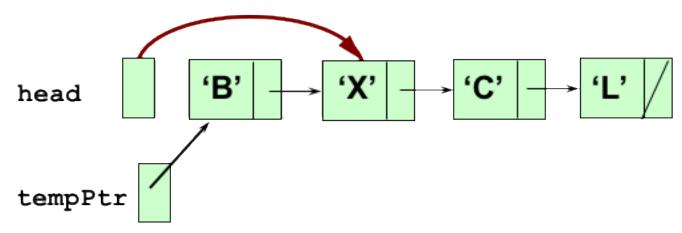
```
item 'B'
```

```
NodeType * tempPtr;
item = head->info;
tempPtr = head;
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delete tempPtr;
```



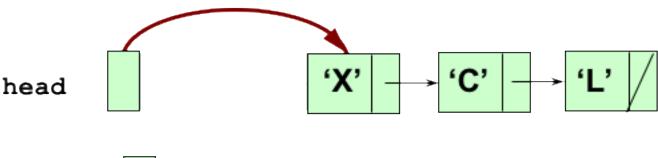
```
item 'B'
```

```
NodeType * tempPtr;
item = head->info;
tempPtr = head;
head = head-> next
delete tempPtr;
```



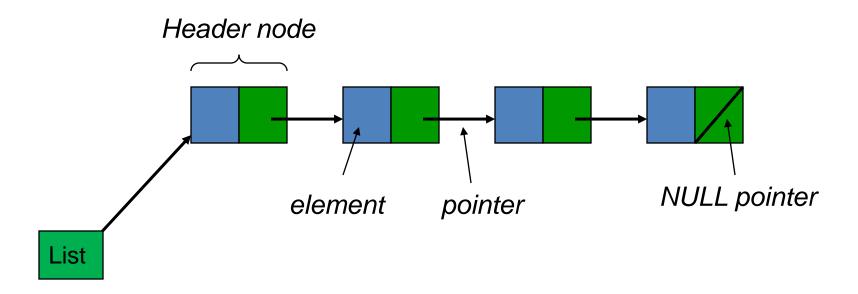
```
item 'B'
```

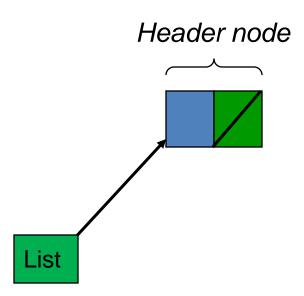
```
NodeType * tempPtr;
item = head->info;
tempPtr = head;
head = head-> next
delete tempPtr;
```



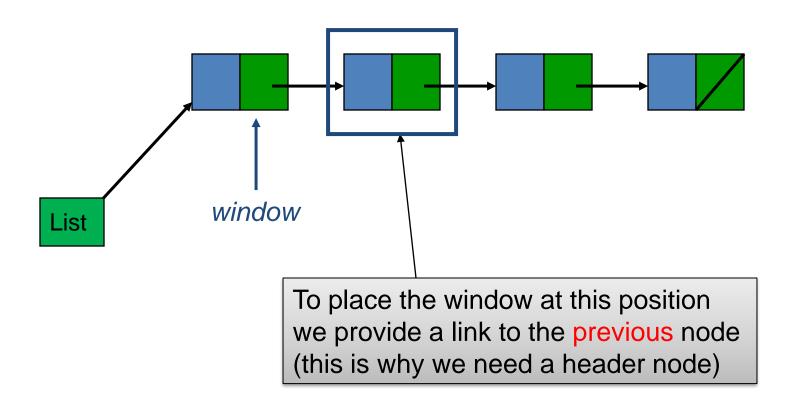
End of Preliminaries:

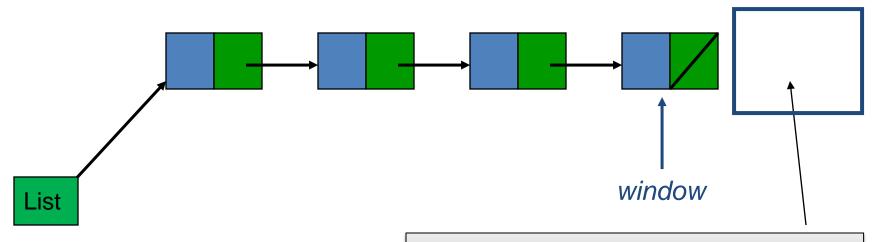
Linked Lists Using Pointers



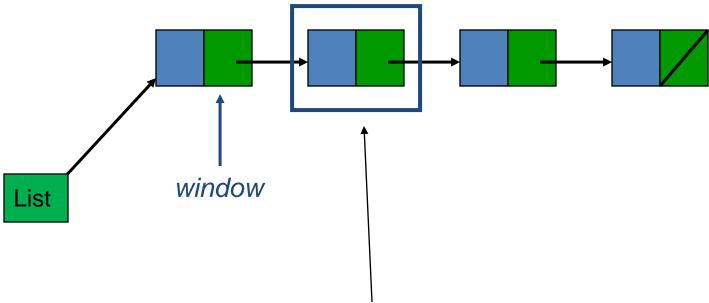


An empty list!!!

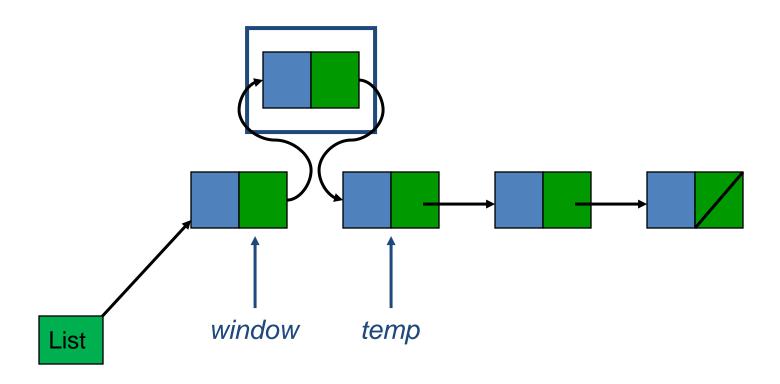




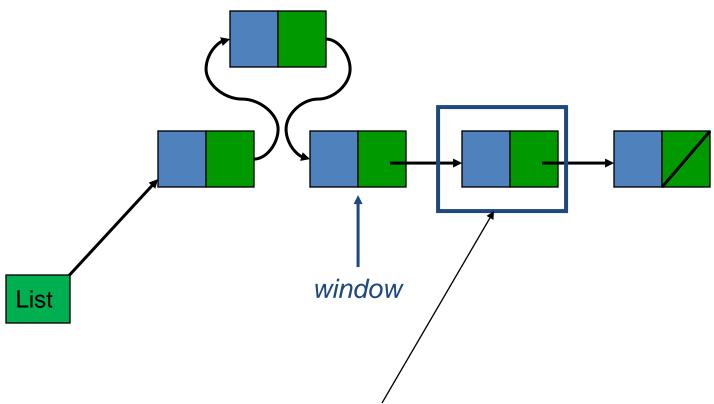
To place the window at end of the list we provide a link to the last node



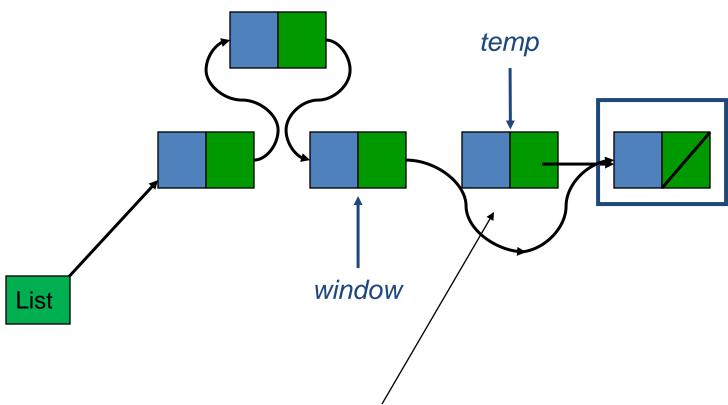
To insert a node at this window position we create the node and re-arrange the links



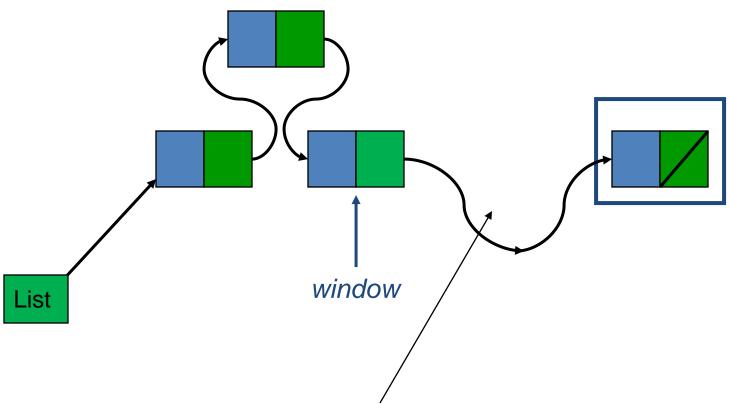
To insert a node at this window position we create the node and re-arrange the links



To delete a node at this window position we re-arrange the links and free the node



To delete a node at this window position we re-arrange the links and free the node



To delete a node at this window position we re-arrange the links and free the node

- type elementtype
- type LIST
- type Boolean
- type windowtype

```
/* linked-list implementation of LIST ADT */
#include <stdio.h>
#include <math.h>
#include <string.h>
#define FALSE 0
#define TRUE 1
typedef struct {
           int number;
                                    number
           char *string;
                                    string
          ELEMENT TYPE;
```

```
typedef struct node *NODE TYPE;
/* alternative approach ...
                                                     * /
/* but need to use sizeof(struct node) in malloc()*/
struct node {
           ELEMENT TYPE element;
                                      number
           NODE TYPE next;
                                       string
       };
typedef NODE TYPE LIST TYPE;
typedef NODE TYPE WINDOW TYPE;
```

```
/*** position following last element in a list ***/
WINDOW TYPE end(LIST TYPE *list) {
   WINDOW TYPE q;
   q = *list;
   if (q == NULL) {
      error("non-existent list");
   else {
      while (q->next != NULL) {
          q = q - next;
                              number
                                             number
                                                            number
                              string
                                             string
   return(q);
                   *list
```

```
/*** position following last element in a list ***/
WINDOW TYPE end(LIST TYPE *list) {
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          q = q - \text{next};
                               number
                                              number
                                                              number
                               string
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                              number
                                              number
                                                             number
                               string
                                              string
                                                             string
   return (q);
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```

```
/*** empty a list ***/
WINDOW TYPE empty(LIST TYPE *list) {
   WINDOW TYPE p, q;
   if (*list != NULL) {
      /* list exists: delete all nodes including header */
      q = *list;
      while (q->next != NULL) {
          p = q;
          q = q-next;
          free(p);
                              number
                                             number
                                                            number
      free (q)
                              strina
                                             string
                   *list
```

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/*** empty a list ***/
WINDOW TYPE empty(LIST TYPE *list) {
   WINDOW TYPE p, q;
   if (*list != NULL) {
      /* list exists: delete all nodes including header */
      q = *list;
      while (q->next != NULL) {
         p = q;//temporary hold before deletion
         q = q->next; //advance to next item before deleting
         free(p);
                             number
                                           number
                                                          number
      free(q);
                             strina
                                           string
```

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                              number
                                             number
                                                            number
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                              string
                                             string
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                                                          number
                                           number
      free (q)
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          free(p);
                                                           number
                                            number
      free (q)
                                             string
                                                            string
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```

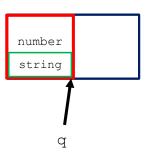
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         q = q-next;
         free(p);
                                                         number
      free (q)
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   WINDOW TYPE p, q;
   if (*list != NULL) {
      /* list exists: delete all nodes including header */
      q = *list;
      while (q->next != NULL) {
         p = q;
         q = q-next;
         free(p);
      free (q)
                  *list
```

```
/* now, create a new empty one with a header node */
if ((q = (NODE_TYPE) malloc(sizeof(NODE))) == NULL)
    error("function empty: unable to allocate memory");
else {
    q->next = NULL;
    *list = q;
}
return(end(list));
```



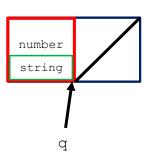




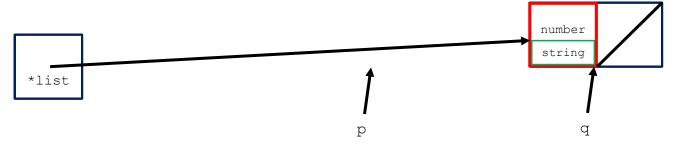
```
/* now, create a new empty one with a header node */
if ((q = (NODE_TYPE) malloc(sizeof(NODE))) == NULL)
    error("function empty: unable to allocate memory");
else {
    q->next = NULL;
    *list = q;
}
return(end(list));
```





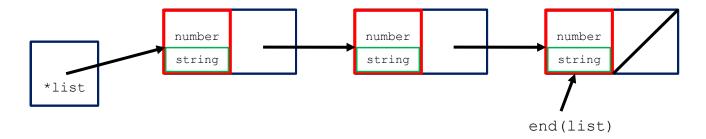


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    error("function empty: unable to allocate memory");
else {
    q->next = NULL;
    *list = q;
}
return(end(list));
```



```
/*** test to see if a list is empty ***/
int is empty(LIST TYPE *list) {
    WINDOW TYPE q;
    q = *list;
    if (q == NULL) {
        error("non-existent list");
    else {
                                                                          number
        if (q->next == NULL) {
                                                                          strina
            return (TRUE);
                                                             *list
        else
            return (FALSE);
                                     number
                                                       number
                                                                          number
                                     strina
                                                        string
                        *list
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```

```
/*** position at first element in a list ***/
WINDOW_TYPE first(LIST_TYPE *list) {
   if (is_empty(list) == FALSE) {
     return(*list);
   else
     return(end(list));
}
```



```
/*** position at next element in a list ***/
WINDOW TYPE next (WINDOW TYPE w, LIST TYPE *list) {
   if (w == last(list)) {
      return(end(list));
   else if (w == end(list)) {
      error("can't find next after end of list");
   else {
      return (w->next);
                              number
                                              number
                                                             number
                              string
                                              string
                                                             string
                    *list
                                                           end(list)
                                            W->next
```

```
/*** position at previous element in a list ***/
WINDOW TYPE previous (WINDOW TYPE w, LIST TYPE *list) {
   WINDOW TYPE p, q;
   if (w != first(list)) {
       p = first(list);
       while (p->next != w) {
          p = p->next;
          if (p == NULL) break; /* trap this to ensure */
                                      /* we don't dereference */
       if (p != NULL)
                                   /* a null pointer in the */
                                  /* while condition
                                                                    * /
           return(p);
               number
                               number
                                               number
                                                                number
               strina
                               strina
                                               string
   *list
          P
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                                                           Carnegie Mellon University Africa
```

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WINDOW TYPE previous (WINDOW TYPE w, LIST TYPE *list) {
   WINDOW TYPE p, q;
   if (w != first(list)) {
       p = first(list);
       while (p->next != w) {
          p = p->next;
          if (p == NULL) break; /* trap this to ensure */
                                      /* we don't dereference */
                                  /* a null pointer in the */
       if (p != NULL)
                                  /* while condition
                                                                    * /
           return(p);
               number
                               number
                                               number
                                                                number
                               strina
                                                string
               string
                                                                string
   *list
          Data Structures and Algorithms for Engineers
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```

```
else {
    error("can't find previous to a non-existent node");
}
else {
    error("can't find previous before first element of list");
    return(w);
}
```

```
/*** position at last element in a list ***/
WINDOW_TYPE last(LIST_TYPE *list) {
    WINDOW_TYPE p, q;
    if (*list == NULL) {
        error("non-existent list");
    }
    else {
        /* list exists: find last node */
```

```
/* list exists: find last node */
if (is_empty(list)) {
   p = end(list);
else {
   p = *list;
   q = p->next;
   while (q->next != NULL) {
       p = q;
       q = q - \text{next};
                           number
                                            number
                                                            number
                                            string
                           string
                                                            string
return(p);
                *list
```

```
/* list exists: find last node */
if (is_empty(list)) {
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else {
   p = *list;
   q = p->next;
   while (q->next != NULL) {
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       q = q - \text{next};
                           number
                                            number
                                                            number
                                            string
                            string
                                                            string
return(p);
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```

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       q = q - \text{next};
                           number
                                            number
                                                            number
                                            string
                                                            string
                           string
return(p);
                *list
```

```
else {
   /* insert it after w */
   temp = w->next;
   if ((w->next = (NODE TYPE) malloc(sizeof(NODE))) == NULL)
      error ("function insert: unable to allocate memory");
   else {
      w-next->element = e;
      w->next->next = temp;
   return(list);
                          number
                                          number
                                                         number
                           string
                                          string
                *list
                                        temp
```

```
else {
   /* insert it after w */
   temp = w->next;
   if ((w->next = (NODE TYPE) malloc(sizeof(NODE))) = NULL)
       error ("function insert: unable to allocate memory");
   else {
      w->next->element = e;
      w-next->next = temp;
                                  number
                                  string
   return(list);
                           number
                                                          number
                                           number
                           string
                                           string
                 *list
                                         temp
```

```
else {
   /* insert it after w */
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       error ("function insert: unable to allocate memory");
   else {
       w->next->element = e:
       w-next->next = temp;
                                  e.number
                                   e.string
   return(list);
                            number
                                                           number
                                           number
                            string
                                           string
                 *list
                                          temp
```

```
/*** delete an element from a list ***/
LIST TYPE *delete(WINDOW TYPE w, LIST TYPE *list) {
   WINDOW TYPE p;
   if (*list == NULL) {
      error ("cannot delete from a non-existent list");
   else {
      p = w - next; /* node to be deleted */
      w->next = w->next->next; /* rearrange the links */
      free(p); /* delete the node */
      return(list);
                            number
                                           number
                                                         number
                            strina
                                           string
                  *list
```

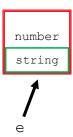
```
/*** delete an element from a list ***/
LIST TYPE *delete(WINDOW TYPE w, LIST TYPE *list) {
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   if (*list == NULL) {
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   else {
       p = w- next; /* node to be deleted */
       w- next = w- next->next; /* rearrange the links */
       free(p); /* delete the node */
       return(list);
                                number
                                                 number
                                                                 number
                                 strina
                                                 strina
                     *list
         Data Structures and Algorithms for Engineers
                                                           Carnegie Mellon University Africa
```

```
/*** delete an element from a list ***/
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       return(list);
                                number
                                                                number
                                strina
                     *list
         Data Structures and Algorithms for Engineers
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```

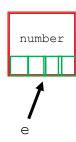
```
/*** retrieve an element from a list ***/
ELEMENT TYPE retrieve (WINDOW TYPE w, LIST TYPE *list) {
   WINDOW TYPE p;
   if (*list == NULL) {
      error ("cannot retrieve from a non-existent list");
   else {
      return (w->next->element);
                              number
                                             number
                                                            number
                              string
                                             string
                   *list
```

```
/*** print all elements in a list ***/
int print(LIST TYPE *list) {
  WINDOW TYPE w;
  ELEMENT TYPE e;
  printf("Contents of list: \n");
  w = first(list);
  while (w != end(list)) {
      e = retrieve(w, *list);
      printf("%d %s\n", e.number, e.string);
     w = next(w, list);
  printf("---\n");
   return(0);
```

```
/*** assign values to an element ***/
int assign_element_values(ELEMENT_TYPE *e, int number, char s[])
{
  e->string = (char *) malloc(sizeof(char) * (strlen(s)+1));
  strcpy(e->string, s);
  e->number = number;
}
```



```
/*** assign values to an element ***/
int assign_element_values(ELEMENT_TYPE *e, int number, char s[])
{
   e->string = (char *) malloc(sizeof(char) * (strlen(s)+1));
   strcpy(e->string, s);
   e->number = number;
}
```





```
/*** main driver routine ***/
   WINDOW TYPE w;
   ELEMENT TYPE e;
   LIST TYPE list;
   int i;
   initialize list(&list);
   empty(&list);
   print(&list);
   assign element values (&e, 1, "String A");
   w = first(\&list);
   insert(e, w, &list);
   print(&list);
```

```
assign element values (&e, 2, "String B");
insert(e, w, &list);
print(&list);
assign element values (&e, 3, "String C");
insert(e, last(&list), &list);
print(&list);
assign element values (&e, 4, "String D");
w = next(last(\&list), \&list);
insert(e, w, &list);
print(&list);
```

```
w = previous(w, &list);
delete(w, &list);
print(&list);
```

#### Key points:

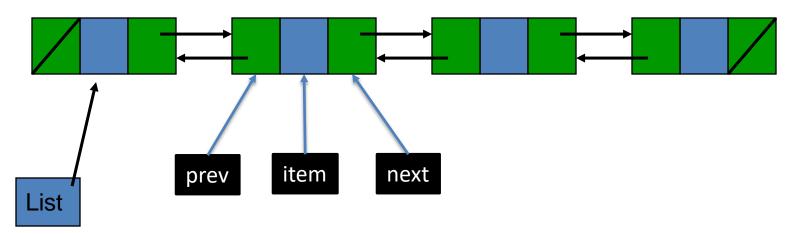
- All we changed was the implementation of the data-structure and the access routines
- But by keeping the interface to the access routines the same as before, these changes are transparent to the user
- And we didn't have to make any changes in the main function which was actually manipulating the list

#### Key points:

- In a real software system where perhaps hundreds (or thousands) of people are using these list primitives, this transparency is critical
- We couldn't have achieved it if we manipulated the data-structure directly

- Possible problems with the implementation:
  - we have to run the length of the list in order to find the end
     (i.e. end(L) is O(n))
  - there is a (small) overhead in using the pointers
- On the other hand, the list can now grow as large as necessary, without having to predefine the maximum size

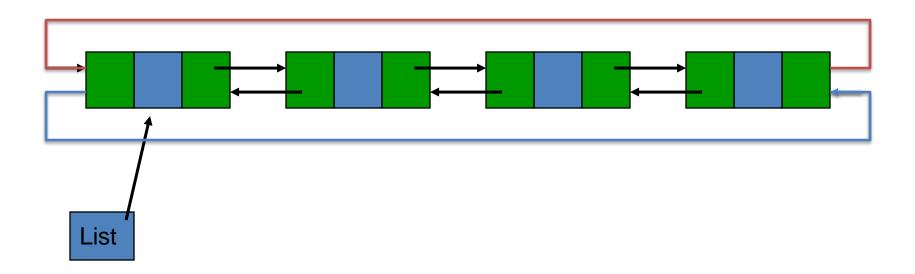
Each node contains the list item and two pointers- next and previous.



We can also have a doubly-linked list; this removes the need to have a header node and make finding the previous node more efficient.

However, we could maintain the Head node as a means of list traversal.

Lists can also be circular



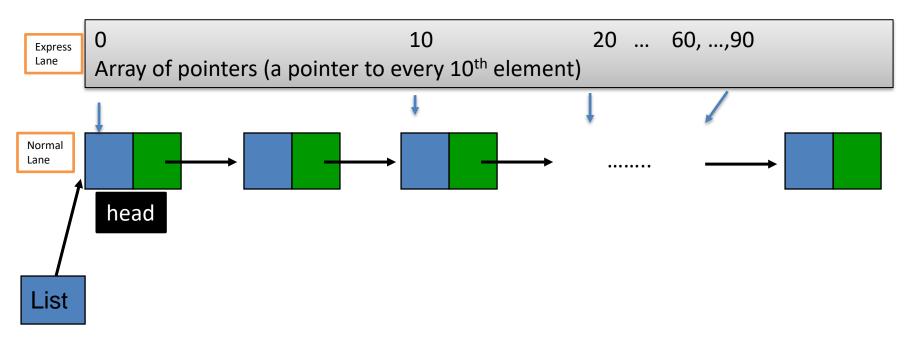
First element points at last element and last element points at first element.

Both singly- and doubly-linked lists can be made circular lists.

Linked lists can be *slow for sort or search operations*, because they rely on linear access.

Skip-linked lists maintain pointers to some or all elements.

- Designed to speed up sort or search operations.
- Consider a list of 100 items



Lists can also be skip-linked lists

#### **Review Exercises**

- Implementation of:
  - Doubly-linked lists
  - Circular linked lists
  - Skip linked lists
- Complexity analysis of:
  - Insert, retrieve, and delete operations under different circumstances, e.g. after some node, before some node, at the head, at the back, etc.

# Comparison: Linked Lists vs. Arrays

- Relative advantages of linked lists
  - Overflow on linked structures can never occur unless memory is actually full
  - Insertions and deletions are simpler than for contiguous (array) lists
  - With large records, moving pointers is easier and faster than moving the items themselves

# Comparison: Linked Lists vs. Arrays

- Relative advantages of arrays
  - Linked structures require extra space for storing pointer fields
  - Linked lists do not allow efficient random access to items(due to linear access)
  - Arrays allow better memory locality and cache performance than random pointer jumping
- Dynamic memory allocation provides us with flexibility on how and where to use limited storage resources

# Comparison: Linked Lists vs. Arrays

- Both lists and arrays can be thought of a recursive objects:
  - Lists: chopping off the first element of a linked list leaves a smaller linked list
  - Lists are recursive objects
  - Splitting the first k elements off an n element array give two smaller arrays, of size k and n-k, respectively
  - Arrays are recursive objects
  - This shows us that lists are amenable to efficient (recursive) divide-andconquer algorithms, such as binary search and quicksort

#### **Practical Application**

Linked lists are great for implementing queues and stacks.

#### **Acknowledgement**

- Adopted and Adapted from Material by:
- David Vernon: <a href="mailto:vernon@cmu.edu">vernon@cmu.edu</a> ; <a href="mailto:www.vernon.eu">www.vernon.eu</a>