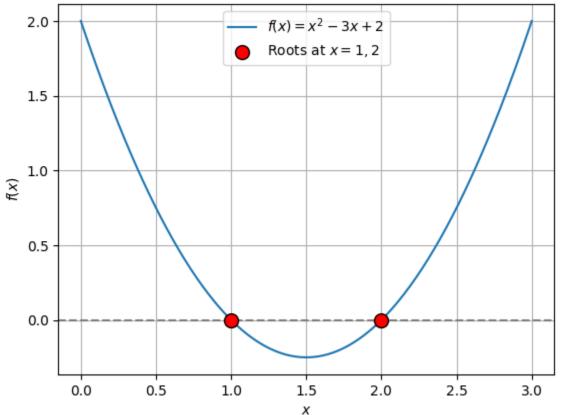
lecture-04 about:srcdoc

```
In [14]:
         import matplotlib.pyplot as plt
         import numpy as np
         # Define the quadratic function
         def quadratic_equation(x):
             return x ** 2 - 3 * x + 2
         # Generate x values
         x \text{ values} = \text{np.linspace}(0, 3, 301)
         # Plot the function
         plt.plot(x_values, quadratic_equation(x_values), label=r"f(x) = x^2 - 3x + 1
         plt.axhline(0, color='gray', linestyle='--') # x-axis
         # # Highlight the roots with circles
         roots = [1, 2]
         plt.scatter(roots, [0, 0], color='red', edgecolor='black', s=100, zorder=5,
         # # Format and display the plot
         plt.xlabel("$x$")
         plt.ylabel("$f(x)$")
         plt.title("Visualization of the Quadratic Function and Its Roots")
         plt.legend()
         plt.grid(True)
         plt.show()
```





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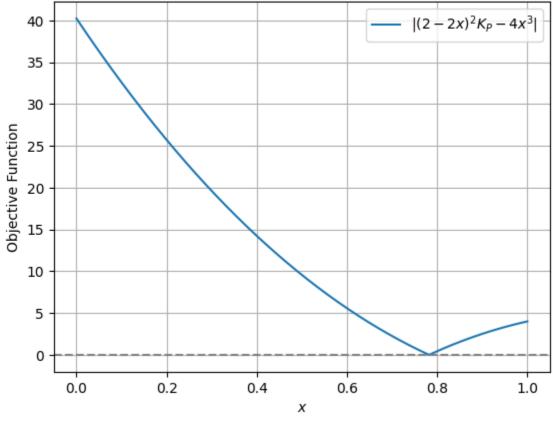
```
In [15]: from scipy.optimize import minimize
         # Define the objective function, which is the absolute value of the quadrati
         def objective_function(x):
             return abs(x ** 2 - 3 * x + 2)
         # Perform the minimization starting from an initial guess of x = 0
         result = minimize(
             fun=objective_function, # Objective function to minimize
                                     # Initial guess
             method="Nelder-Mead", # Optimization method
             tol=1e-6
                                    # Tolerance for convergence
         print(result)
               message: Optimization terminated successfully.
               success: True
                status: 0
                   fun: 8.881784197001252e-16
                     x: [ 1.000e+00]
                   nit: 31
                  nfev: 62
         final_simplex: (array([[ 1.000e+00],
                               [ 1.000e+00]]), array([ 8.882e-16, 9.766e-07]))
In [16]: # Perform the minimization starting from an initial guess of x = 0
         result = minimize(
             fun=objective_function, # Objective function to minimize
                                      # Initial guess
             x0=2.1
             method="Nelder-Mead", # Optimization method
             tol=1e-6
                                    # Tolerance for convergence
         print(result)
               message: Optimization terminated successfully.
               success: True
                status: 0
                   fun: 3.814698725790322e-07
                     x: [ 2.000e+00]
                   nit: 19
                  nfev: 38
         final_simplex: (array([[ 2.000e+00],
                               [ 2.000e+00]]), array([ 3.815e-07, 4.196e-07]))
In [17]: def objective_function(x, K_P):
             equilibrium_equation = (2 - 2 * x) ** 2 * K_P - 4 * x ** 3
             return abs(equilibrium_equation)
In [18]: # Generate x values
         x values = np.linspace(0, 1, 400)
         # Plot the function
         plt.plot(x_values, objective_function(x_values, 10.060), label=r"$|(2 - 2x)^
         plt.axhline(0, color='gray', linestyle='--') # x-axis
```

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lecture-04 about:srcdoc

```
# Format and display the plot
plt.xlabel("$x$")
plt.ylabel("Objective Function")
plt.title("Visualization of the Objective Function")
plt.legend()
plt.grid(True)
plt.show()
```

Visualization of the Objective Function



```
In [19]: # Perform the minimization with an initial guess of x = 0
    result = minimize(
        fun=objective_function,
        x0=0,
        args=(10.060,),
        method="Nelder-Mead",
        tol=1e-6
)

print("{:.0f}%".format(result["x"][0] * 100)) # Convert the result to perce
78%
In []:
```

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