$$L=rac{1}{2}\mu r^2-V_{
m eff}(r)$$
 where
$$V_{
m eff}=rac{\ell}{2\mu r^2}+U(r)\ell=mr^2\dot{\phi}$$

 $\mu = \frac{m_1 m_2}{m_1 + m_2}$