$$|\Psi\rangle = \sum_n c_n |n\rangle$$

$$c_n = \langle n|\Psi\rangle$$

$$\langle A\rangle = \sum_n |c_n|^2 \lambda_n$$