5)

```
#!/usr/bin/env python3
import numpy as np
import pandas as pd
\mathbf{def} \operatorname{trap\_int}(f,a,b,n):
    h = (b-a)/float(n)
    X = np. linspace(a,b,n+1)
    Y = f(X)
    result = 0.0
    for i in range(n):
         result += h/2.0 * (Y[i] + Y[i+1])
    return result \#h/2.0 * (Y[0] + 2*np.sum(Y[1:-1]) + Y[-1])
\mathbf{def} \ \mathbf{simp_int}(f,a,b,n):
    h = (b-a)/float(n)
    X = np. linspace(a,b,n+1)
    Y = f(X)
    result = 0.0
    for i in range (int (n/2)):
         1 = 2 * i
         result += h/3.0 * (Y[1] + 4.0*Y[1+1] + Y[1+2])
    return result
def ratio(errors):
    num = errors[:-1]
    den = errors[1:]
    return num/den
def order (ratios):
    return np.log2(ratios)
def get_results(approx):
    errors = abs(1.0 - approx)
    ratios = ratio (errors)
    orders = order(ratios)
    return errors, ratios, orders
if = name = '= main = ':
    f = np.sin
    a = 0.0; b=np.pi/2.0
    exact = 1.0
    results = \{\}
    results[r'$n$'] = ['%d'%2**i for i in range(6)]
    N = [1, 2, 4, 8, 16, 32]
    trap = np.array([trap_int(f,a,b, ]) for _ in N])
    simp = np.array([simp_int(f,a,b, ]) for _ in N[1:]])
    trap_res = get_results(trap)
    simp_res = get_results(simp)
```

Table 1: Results for trapezoidal and simpson rule integrations schemes for different subdivisions on the interval $[0, \pi/2]$.

| \overline{n} | $T_n(f)$ | T error(n) | T ratio(n) | T order(n) | $S_n(f)$ | S error(n) | S ratio(n) | S order(n) |
|----------------|----------|------------|------------|------------|----------|------------|------------|------------|
| 1 | 0.78540 | 0.21460 | - | - | - | - | - | - |
| 2 | 0.94806 | 0.05194 | 4.13168 | 2.04673 | 1.00228 | 0.00228 | - | - |
| 4 | 0.98712 | 0.01288 | 4.03134 | 2.01126 | 1.00013 | 0.00013 | 16.94006 | 4.08237 |
| 8 | 0.99679 | 0.00321 | 4.00774 | 2.00279 | 1.00001 | 0.00001 | 16.22381 | 4.02004 |
| 16 | 0.99920 | 0.00080 | 4.00193 | 2.00070 | 1.00000 | 0.00000 | 16.05529 | 4.00498 |
| 32 | 0.99980 | 0.00020 | 4.00048 | 2.00017 | 1.00000 | 0.00000 | 16.01378 | 4.00124 |